Open Policy Analysis: Concepts and Applications

Fernando Hoces de la Guardia

UC Berkeley: Berkeley Initiative for Transparency in the Social Sciences

Evidence Action, Washington DC November 8, 2018

- Why we need Open Policy Analysis (Hoces de la Guardia, Grant & Miguel, 2018)
- Application to policy estimates of the minimum wage.

Policy Analysis And The Evidence-Based Policy Movement

Evidence-Based movement is growing.

- "The golden age of evidence-based policy" (Haskins 2017).
- Credible causal evidence (Angrist & Pischke, 2010)
- Transparency and reproducibility of research (Miguel et al. 2014).

Policy Analysis is a fundamental link.

- As many definitions as textbooks (Dunn, 2015; Weimer & Vining, 2017; Williams, 1971)
- Common denominator: client-oriented empirical analysis meant to inform a specific policy debate
- Aspires at scientific rigor. (Wildavsky 1979),

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Examples of Policy Analysts





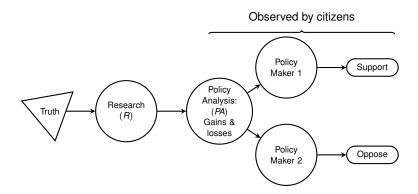








One Ideal Evidence-Based Policy Link



Reproducibility Crisis In Empirical Research

- Large magnitude of publication bias (Franco et al 2014).
- Evidence of extensive p-hacking across social science disciplines (Gerber et al 2008, Brodeur et al 2016).
- Replication rates are low (Collaboration et al, 2015, Camerer et al, 2016, 2018).
- Computational reproducibility is also low (Stodden et al 2016, Chang and Li 2015, Gertler et al 2018).

The Open Science Movement

- Definition of principles of Open Science/Research Transparency (Miguel et al 2014)
- Development of guidelines to operationalize principles of Open Science (Nosek et al 2015)
- Journals and funders: Journals (Science + 5k other journals), Registries (AEA), Funders (NIH, NSF and multiple donors)

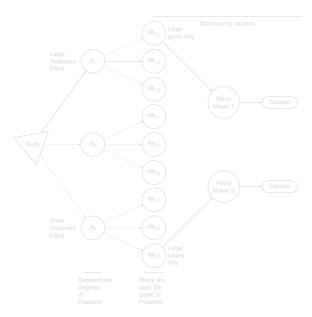
Credibility Crisis Of Policy Analysis

- Incredible Certitudes (Manski, 2013)
- Report wars (Wesselink et al, 2013)
- Alternative facts ("The Death of Expertise" Nichols, 2017; "The Death of Truth", Kakutani 2018; "Truth Decay", Rich & Kavanagh 2018)

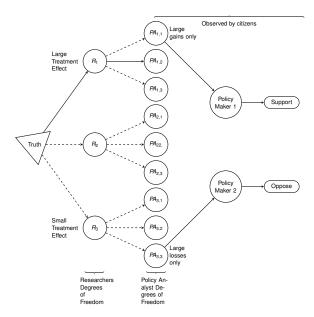
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How This Affects The Evidence Based Policy Link?



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Relevance

Main consequences of policy analysis that lacks openness:

- Cherry picking evidence.
- Challenging to automate and improve systematically recurring reports.
- Oifficulty understanding how research informs policy analysis.

Cherry Picking Evidence

"When I was director of the CBO, I was very frustrated when we would write a policy report [saying] a certain policy would have these two advantages and these two disadvantages, and the advocates would quote only the part about the advantages, and the opponents would quote only the part about the disadvantages. That encourages the view that there are simple answers. There aren't generally simple answers. There are trade-offs."

Douglas Elmendorf (Director of CBO, 2009-2015)
 Harvard Magazine, 2016

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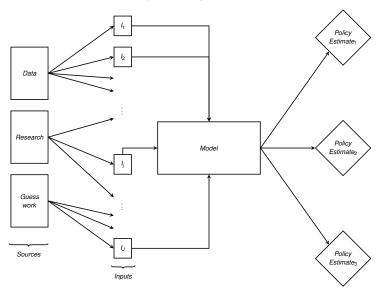
Open Science

	Empirical	Policy
	Research	Analysis
Problems	Reproducibility	Credibility
	Crisis	Crisis
Solutions	Open Science	
	Principles, Guidelines,	
	Applications	

Open Policy Analysis

	Empirical	Policy
	Research	Analysis
Problems	Reproducibility	Credibility
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	Applications	

The Process of Policy Analysis



Principles for Open Policy Analysis

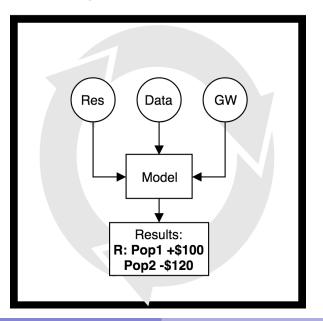
Proposed principles:

- 1 Computational Reproducibility
- 2 Analytic Transparency
- 3 Output Transparency

Principle 1: Stop re-inventing the wheel

Computational Reproducibility

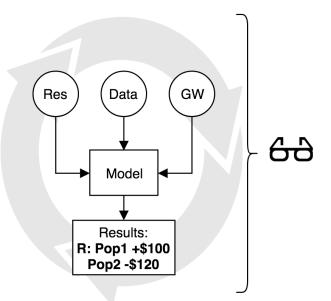
- Literate Programming
- Version control
- File structure
- Label sources



Principle 2: Show your work (readable)

Analytic Transparency

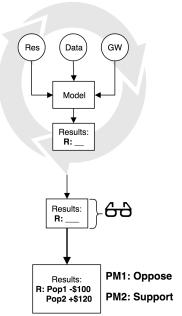
- Open code
- Open data
- Report as Dynamic Document



Principle 3: Let's all agree on one table/viz

Output Transparency

- Pre-committed output display
- Assumptionsoutput link



Suggestions

Suggestions:

- Policy Analysts: Just Post It. Things are moving in this direction. Play a leading role in a credibility revolution for policy analysis.
- Policy Analysis Organizations: Open by Default Boost in credibility, lower costs in the long run. Examples: GiveWell, and AEI.
- Government Agencies and Funders: Support Open Policy Analysis Examples: Require contracted policy analysis to be fully open. Support training and adoption of new tools (VC and DD). Inject resources for the transition.

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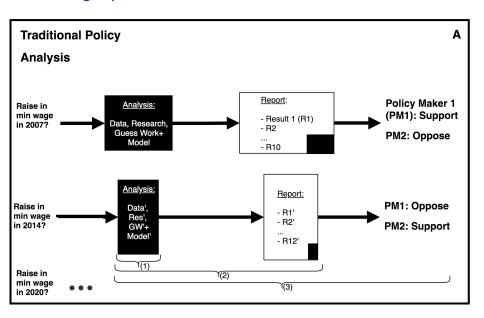
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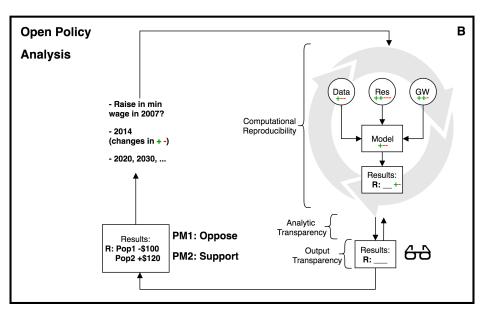
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Summing Up: Where We Are



Summing Up: Where Should We Go



- Why we need Open Policy Analysis (Hoces de la Guardia, Grant & Miguel, 2018)
- 2 Application to policy estimates of the minimum wage.

	Empirical	Policy
	Research	Analysis
Problems	Reproducibility	Credibility
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Solutions	Open Science	Open Policy Analysis
	Principles, Guidelines,	Principles
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Description of Case Study

"The Effects of a Minimum-Wage Increase on Employment and Family Income" Congressional Budget Office (2014)

Description: CBO estimated the effects of a raise in the federal minimum wage from \$7.25/hr to \$10.10/hr.

Main policy estimates:

- 500,000 jobs would be lost.
- 16.5 million workers would receive a salary increase.
- Distributional effects: below poverty line (PL) +\$5billion; between one and three PL +\$12billion; between three and six PL +\$2billion; above six PL -\$17billion

Key research estimate: Elasticity of labor demand for teenagers in the labor force.

Reasons for Selecting the Case Study

Relatable

Feasible

Recurrent

Relevant:



Figure: Google Search Intensity of "Minimum Wage"

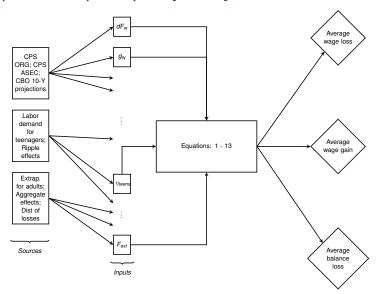
Adapting TOP Guidelines to Policy Analysis

Ø	Dimensions	0	1	2	3
	Computational Reproducibility				
	Follow a common template for file structur	е	Some FS	Standard FS	SFS + sources dir
	Label and document each input sources (data, research, guesswork)		List	+ sources	+detailed links/ref.
	Make code readable.		Scripts in repo/ xls with SOPs	High readability + QA report	One-Click (DD)
	Use a version control strategy.		Some naming	Clear naming	Git
	Analytic Transparency				
	5. Open Code		Final	Final + prep	Human read (DD)
	Open Data (raw & analytic files).		Final	Final+raw	+ repository `+ inst 4 S.I.
	7. Open Report		Final	Final + VC	+ DD
	8. Open notes		List	Final	Final+VC
	Output Transparency.				
	Define results format before publishing/justify changes format output		General	Specific	Specific +

Applying Guidelines to Build an Open Report



Map the complete policy analysis



Easier Methodological Appraisal. Example: dis-employment effects

Steps taken to verify the analysis & employment variation $(\widehat{\Delta E} \times 1000)$ at each line¹

- ① Find an elasticity: -0.1 (page 25): $\widehat{\Delta E} \approx 300$
- igoplus What about adults? $\eta^{adults}=rac{1}{3}\eta^{teens}$ (page 28): $\Delta Epprox$ 100
- What about the adjustment? $\eta_{W \leq MW}^g = \frac{\eta_W^g}{\rho_{W \leq MW}^g} \times \frac{\% \triangle MW}{\% \triangle W^g}$ (page
- The adjustment factors $\frac{1}{\rho_{w \leq MW}^g} \times \frac{\%\Delta MW}{\%\Delta w^g} = F_{adj}^g$ are not computed from the data (3.2 teens, 19.5 adults). Instead: $F^{teen} = F^{adjult} = 4.5$ (page 28) $\Delta F \approx 500$

Steps 2-4 took several days of work!

 $^{^1}$ Assuming target population \approx 22 million, $\overline{\Delta w_{w \leq MW'}} \approx$ 14%, and non-compliance \approx 15%

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All in One Output

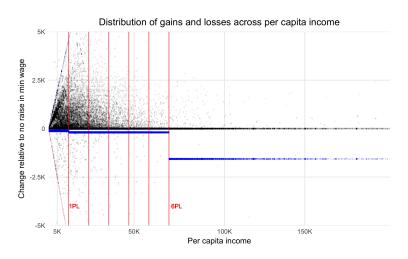


Figure: Gains and losses. Different Units

Sensitivity Analysis: Status Quo

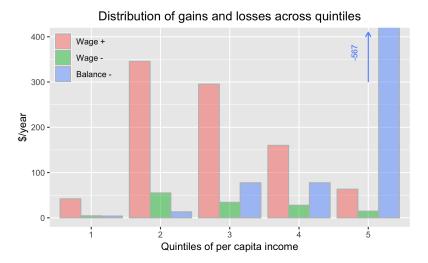


Figure: Default settings

SA: Change in Elasticity of Labor Demand

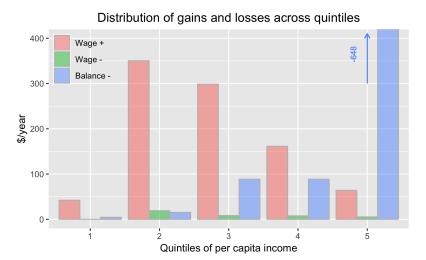


Figure: From
$$\eta_{lit}^{teens} = -0.1$$
 to $\eta_{lit}^{teens} = -0.01(\Delta^-90\%)$

Sensitivity Analysis: Status Quo

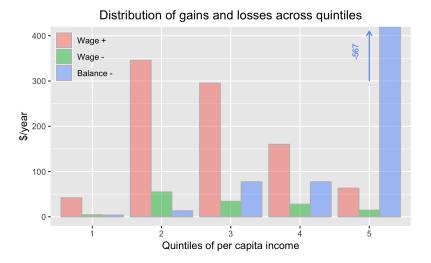


Figure: Default settings

SA: Change in Distribution of Balance Loses

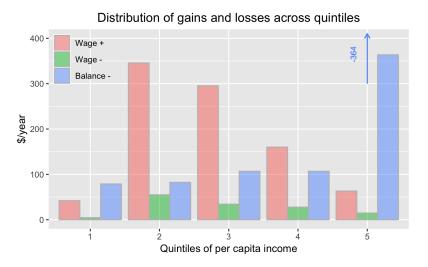


Figure: From $(1PL, 6PL) \sim (1\%, 29\%, 70\%)$ to (20%, 40%, 40%)

Comparing the Trade-offs: A Toy Example

Model for the normative comparison made by a policy maker (welfare function):

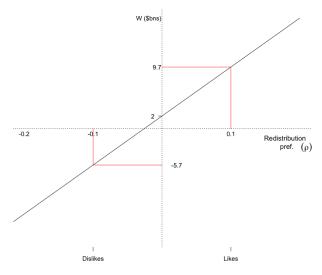
$$W(\rho) = \sum_{i \in N} \left(\omega_{wg} wg_i + \omega_{wl} wl_i + \omega_{bl} bl_i \right) \omega_i^d(Q_i, \rho)$$

with:

$$\omega_i^{\textit{d}}(\textit{Q}_i,\rho) = \frac{(1-\rho(\textit{Q}_i-\textit{Q}_{\textit{median}}))}{\sum_i \omega_i^{\textit{d}}(\textit{Q}_i)} \textit{Q}_{\textit{max}} \quad \text{for } \rho \in \left(-\frac{1}{2},\frac{1}{2}\right)$$

ho>0 represents positive valuation of progressive redistribution. ho<0 represents positive valuation of regressive redistribution.

Redistribiutional Preferences Toy Example ($\omega_{WG} = \omega_{WL} = \omega_{BL} = 1$)



Sensitivity Analysis For Multiple Parameters

Table: $\%\Delta W$ for a $\%\Delta$ in inputs. Two sample policy makers.

		Re-distributional Preferences			
		Dislikes ($\rho = -0.1$)		Likes ($\rho = 0.1$)	
Source	Input	10%Δ+	10%Δ-	10%Δ+	10%Δ-
Data					
	Annual wage growth (g_w)	-3%	2%	-2%	1%
	Annual growth in N	0.8%	-0.9%	0.5%	-0.5%
Research					
	η_{teen}	-4%	4%	-2%	2%
	Ripple Scope (8.7, 11.5)	37%	-24%	21%	-14%
	Ripple Intensity $(50\%\Delta w)$	5%	-5%	3%	-3%
Guess Work					
	Extrapolation factor (F_{ex})	-3%	2%	-1%	1%
	Non compliance (α_1)	-7%	7%	-4%	4%
	Substitution factor (F_{sub})		20%		-8%
	Net benefits	-5%	5%	2%	-2%
	Distribution of balance losses				1
	Current: (1%, 29%, 70%)				
	(1%, 4%, 95%)	22%		13%	
	(5%, 35%, 60%)	-17%		-9%	
	1/ <i>N</i>	-129%		-73%	

Limitations

- There is additional scope for reproducibility.
- Complete case study requires extensive institutional knowledge.
- Guidelines need to be build based on consensus of practitioners.

What lies ahead

Let's assume this becomes the new status quo.

- Costs of producing the next report on effects of minimum wage will be very small.
- Every additional effort will imply improvements on the "state of the art" report (e. g. dBL; η(MW), α₁(MW))
- Learning about one parameter (QALYs, DWL) will update estimates across reports.
- Much easier to have a substantive and normative policy debate.
 Pilot example: Shiny App!.

Your next steps to push OPA forward

- Collaborate with BITSS to open up your PA.
- Fund OPA: directly or conditionally.
- Train students/analysts in OPA.
- Present/showcase your OPA. Pioneers: GiveWell, AEI, CBO.
- Nominate a PA to be open <u>here</u>.

An Aspiration

"Democracy Thrives In Sunlight"

The Work Times

Washington DC

VOL.III... No.14 MARCH 29, 2020 THREE DOLLARS

CBO Publishes Open Report on Minimum Wage

Results Will Be Published Separately in Two Weeks

Lorem ipsum dolor sit amet, consectetuer adipiscing elit. Ut purus elit, vestibulum ut, placerat ac, adipiscing vitae, felis. Curabitur dictum gravida mauris. Nam arcu libero, nonummy eget, connibh mi, congue eu, accumsan eleifend, sagittis quis, diam. Duis eget orci sit amet orci dignissim rutrum.

Bipartisan Support for CBO Methodology

Nam dui ligula, fringilla a, euismod sodales, sollicitudin vel, wisi. Morbi auctor lorem non iusto. Nam lacus libero. viverra fermentum felis. Donec nonummy pellentesque ante. Phasellus adipiscing semper elit. Proin fermentum massa ac quam. Sed diam turpis, molestie vitae, placerat a, molestie nec, leo. Maecenas lacinia. Nam ipsum ligula, eleifend at, accumsan nec, suscipit a, ipsum. Morbi blandit ligula feugiat magna. Nunc eleifend consequat lorem. Sed lacinia nulla vitae enim. Pellentesque tincidunt purus vel magna. Integer non enim. Praesent euismod nunc eu purus. Donec bibendum quam in tellus. Nullam cursus pulvinar lectus. Donec et mi. Nam vulputate metus eu enim. Vestibulum pellentesque felis eu massa.

Quisque ullamcorper placerat ipsum.

Thank you.

Pre-prints: Why OPA OPA Case Study

Slides at tinyurl.com/yacz2z78

fhoces@berkeley.edu

Equations from Model in DD

$$\widehat{\Delta E} = N \times \eta \times \% \Delta w + \text{Other factors}$$
 (1)

$$\widehat{N_{\textit{final}}^s} = g_N(\hat{t}'|t) \times \hat{N_t^s} \times P(\hat{w}' \leq MW^{\textit{new}}|s) \times (1 - \hat{\alpha_1^s} - \hat{\alpha_2^s}) \qquad s = \{\textit{teens}\}$$
(2)

The elasticity for adults from the literature is define as the one for teenagers with an extrapolation factor.

$$\eta_{lit}^{adults} = \eta_{lit}^{teens} \times F_{extrapolation}$$
(3)

Adjustments to the elasticity of labor demand

Following Neumark and Wascher (2008), Brown (1999). First:

$$\eta_{lit}^s = p_{w \leq MW}^s \eta_{w \leq MW}^s + (1 - p_{w \leq MW}^s) \eta_{w > MW}^s \qquad s = \{\textit{teens}, \textit{adults}\}$$

Second, assume $\eta_{w \leq MW}^s = 0$:

$$\eta_{w \leq MW}^{s} = \frac{\eta_{lit}^{s}}{p_{w < MW}^{s}} \qquad s = \{teens, adults\}$$

And third, adjust for the effective average wage variation for each group $(\sqrt[8]{\Delta w^s})$:

$$\widetilde{\eta_{w \leq MW}^{s}} = \frac{\eta_{\mathit{lit}}^{s}}{p_{w < MW}^{s}} \times \frac{\% \Delta MW}{\frac{\%}{0} \Delta w^{s}} = \eta_{\mathit{lit}}^{s} \times \mathit{F}_{\mathit{adjs}}^{s} \qquad s = \{\mathit{teens}, \, \mathit{adults}\}$$

(4)

•Final Effect on Employment

$$\widehat{\Delta E} = \sum_{g \in \{A, T\}} \left(\widehat{N_g^{final}} \times \widehat{\eta_{w \le MW}^g} \times \overline{\% \Delta w^g} \right) - \widehat{OF}$$
 (5)

Effect on Wages

w': wages in 2016 under the status quo.

$$w'' = \begin{cases} w' & \text{if} \quad U[0,1] < \alpha_1 \\ w^{\text{new}} & o/w \end{cases}$$
 (6)

$$w^{\text{new}} = \begin{cases} w'/2 & \text{if} \quad w \in U[0,1] < \frac{2\Delta E}{N_{w < MW'}} \\ \widetilde{w^{\text{new}}} & o/w \end{cases}$$
 (7)

Ripple Effects

$$\widetilde{w^{new}} = \begin{cases} MW' & \text{if } w' < R_{lb} \\ MW' + R^{l}(w' - R_{lb}^{s}) & \text{if } w' \in [R_{lb}, MW') \\ w' + R^{l}(R_{ub}^{s} - w') & \text{if } w' \in [MW', R_{ub}) \\ w' & o/w \end{cases}$$
(8)

Computing Income

$$y'_{i,h} = \sum_{i \in N_h} (g_{nw}(t'|t)nw_i + w'_i) / N_h$$

$$y''_{i,h} = \sum_{i \in N_h} (g_{nw}(t'|t)nw_i + w''_i) / N_h$$
(9)

Final Policy Estimates

$$WG_{i} = (y_{i}'' - y_{i}') \mathbf{I} (y_{i}'' > y_{i}')$$
(10)

$$WL_i = \left(y_i' - y_i'' \right) \mathbf{I} \left(y_i'' < y_i' \right) \tag{11}$$

$$BL = \sum_{i} WG_{i} - F_{sub} \sum_{i} WL_{i}; \quad BL_{i} = BL \times dBL$$
 (12)

$$\overline{WG_Q} = \frac{\sum_{i \in Q} WG_i}{N_{pop}/5} \quad \overline{WL_Q} = \frac{\sum_{i \in Q} WL_i}{N_{pop}/5}$$

$$\sum_{i \in Q} RL_i$$

$$\overline{BL_Q} = \frac{\sum_{i \in Q} BL_i}{N_{pop}/5} \tag{13}$$

Clear connection between sources and inputs

Source	Input "		
Data	·		
CPS ORG 2013 (CEPR version)	Number of salary workers in 2013 $(\widehat{N^g_{mal}} \ g \in \{teen, adult\}\}$; Fraction of workers below the new minimum wage $(P_{\widetilde{w} \leq MN^s g})$; Average wage variation for those below the new min wage $(\% \overline{\Delta} w^g)$; Non-compliance rate (α_1^g)		
CPS ASEC 2012 (CEPR version) State level Min. Wage (DOL) 10-year economic forecast (CBO)	Wages and Non-Wage Income distribution (dF_w, dF_{nw}) ; Household size (N_h) ; Hours/weeks worked (\hat{w}, \hat{h}) Trends in state min. wage (MW_i^S) Predicted worker growth by 2016 (in 2013) $(\hat{g_N})$; Wage growth in by 2016 $(\hat{g_w})$; Non-wage growth by 2016 (g_{nw})		
Research			
Elasticity of labor demand for teenagers	$\eta_{teen}^{lit} = -0.1$		
Ripple effects	From $R_{lb} = \$8.7$ to $R_{ub} = \$11.5$ with a "ripple" intensity of $R_{l} = 50\%$		
Guess Work			
Extrapolation factor from teenagers to adults	$F_{ex} = 1/3$		
Net benefits	$\hat{NB} = \$2$ billion		
Adjustment to account for effective wage variation and affected	$F_{adj} = 4.5$		
population	$\hat{OF} = 40.000$ new jobs		
Aggregate consumption effects on employment	OF = 40,000 new jobs		
Distribution of balance loses	$dBL = (1\%, 29\%, 70\%)$ if income $\in [0, 1PL, 6PL, +)$		
Fract. of wage loses used to pay wage gains	$F_{subs} = 1$		
Job killing process: fraction of jobs	Cut wages in half for twice the number of jobs destroyed		

Fully specified model

Model	Policy estimate	
	(per quintile)	
Predicted household income with and without min wage increase. Depends on: $\widehat{N_{final}^g}$, $P_{\hat{w} \leq MW^1 g}$, $\overline{\sqrt[g]{\Delta w^g}}$, α_1^g , dF_w , dF_{nw} , N_h , \hat{w} , \hat{h} , MW_t^s , \hat{g}_N , \hat{g}_w , \hat{g}_{nw} , η_{teen}^{lt} , R_{lb} , R_{ub} , R_l , F_{ex} , F_{adj} , \hat{OF}	Average gain in per capita income due to net wage increase. $(\overline{WG_q})$	
Predicted household income with and without min wage increase.	Average loss in per capita income due	
Depends on: $\widehat{N_{final}^g}$, $P_{\hat{w} \leq MW^1 g}$, $\overline{\%} \Delta w^g$, α_1^g , dF_w , dF_{nw} , N_h , \hat{w} , \hat{h} , MW_t^s , $\hat{g_N}$, $\hat{g_w}$, $\hat{g_{nw}}$, η_{teen}^{lit} , F_{ex} , F_{adj} , \hat{OF}	to net wage decrease. $(\overline{WL_q})$	
Distribution of balance loses	Average loss in per	
Depends on: $\overline{WG_a}(\cdot), \overline{WL_a}(\cdot), \hat{NB}$	capita income to	
F_{subs} , dBL	balance wage	
SUDS, GDL		
	gains. $(\overline{BL_q})$	
Equations; Back		