



ITMO UNIVERSITY

Saint Petersburg, Russia

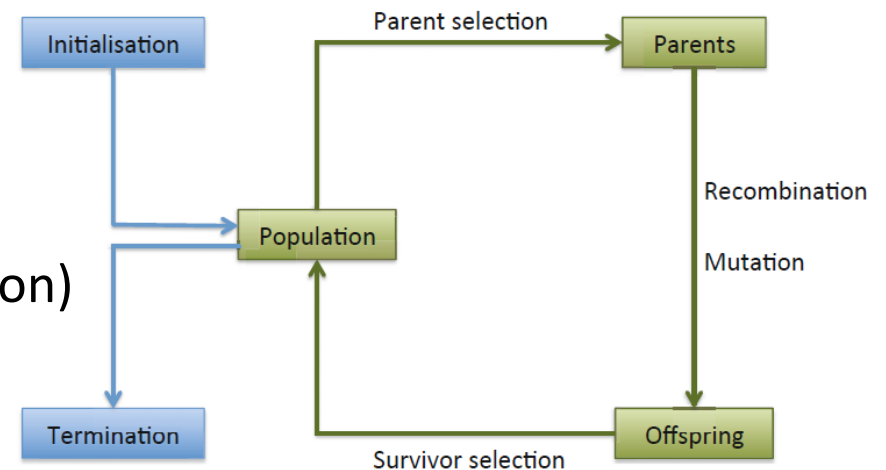
Lecture 3: Selection

Michael Melnik

mihail.melnik.ifmo@gmail.com

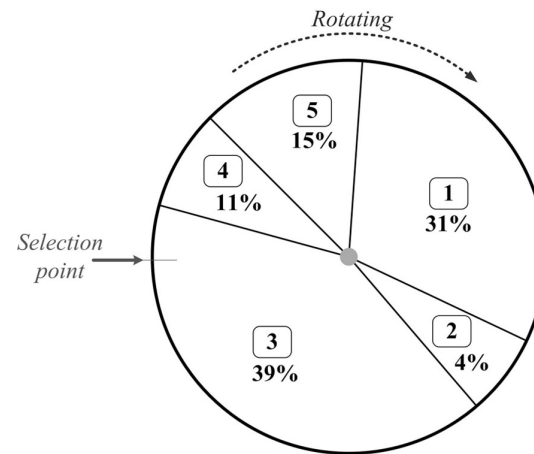
Components

- ✓ Representation of individuals
- ✓ Population of individuals
- ✓ Evaluation function (fitness function)
- ✓ Parent selection mechanism
- ✓ Variation operators (recombination, mutation)
- ✓ **Survivor selection mechanism**
- ✓ Terminate conditions

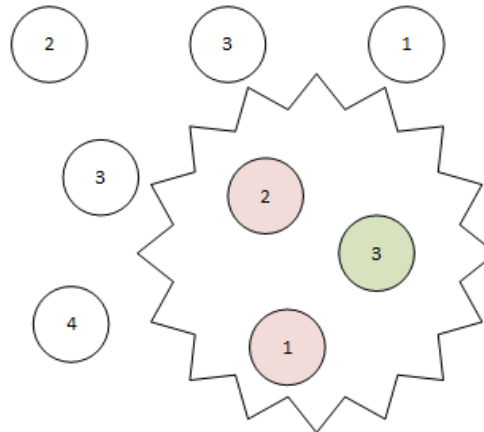


Selection

✓ Roulette wheel



✓ Tournament



Ranking

- ✓ Transform fitness into another values (ranks)
- ✓ Works for roulette wheel
- ✓ Examples:
 - Fitnesses: 101, 102, 103
 - Rank?
 - $(101 - 100), (102 - 100); (103 - 100) \Rightarrow 1, 2, 3$
 - Fitnesses: 100, 5, 4, 6
 - Rank?

$$P_{lin-rank}(i) = \frac{(2 - s)}{\mu} + \frac{2i(s - 1)}{\mu(\mu - 1)}$$

- 0.375, 0.210, 0.125, 0.290

Selection

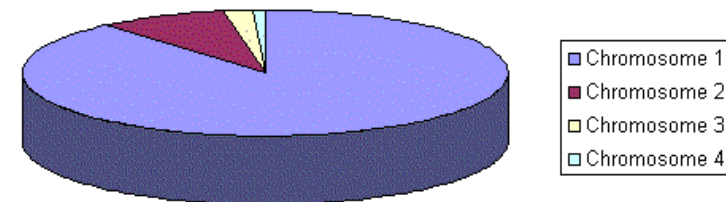
Distinction between

- **selection operators:** define selection probabilities
- **selection algorithms:** define how probabilities are implemented

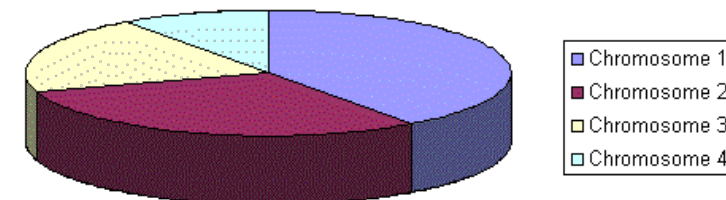
Solving problems:

- premature convergence
- selection pressure

Situation before ranking (graph of fitnesses)



Situation after ranking (graph of order numbers)



Overselection

- ✓ When population is extremely large
- ✓ Population is divided into two groups:
 - Top $x\%$ fittest
 - Other
- ✓ During selection, 80% of parents selected from the 1st group, and 20% from other.

| Population size | Proportion of population in fitter group (x) |
|-----------------|---|
| 1000 | 32% |
| 2000 | 16% |
| 4000 | 8% |
| 8000 | 4% |

Preserving diversity

- ✓ Avoid premature convergence
- ✓ Niching – set of methods to divide population into several subgroups
- ✓ Find several local optimums instead of one global
- ✓ Explicit:
 - Fitness Sharing, Crowding, Speciation
- ✓ Implicit:
 - Island model, Cellular model

Fitness sharing

- ✓ Number of individual within a given niche is controlled by sharing their fitness.
- ✓ Based on distances between individuals (genotype or phenotype)
- ✓ Fitness F of each individual is shared with other individuals within predefined distance σ_{share}

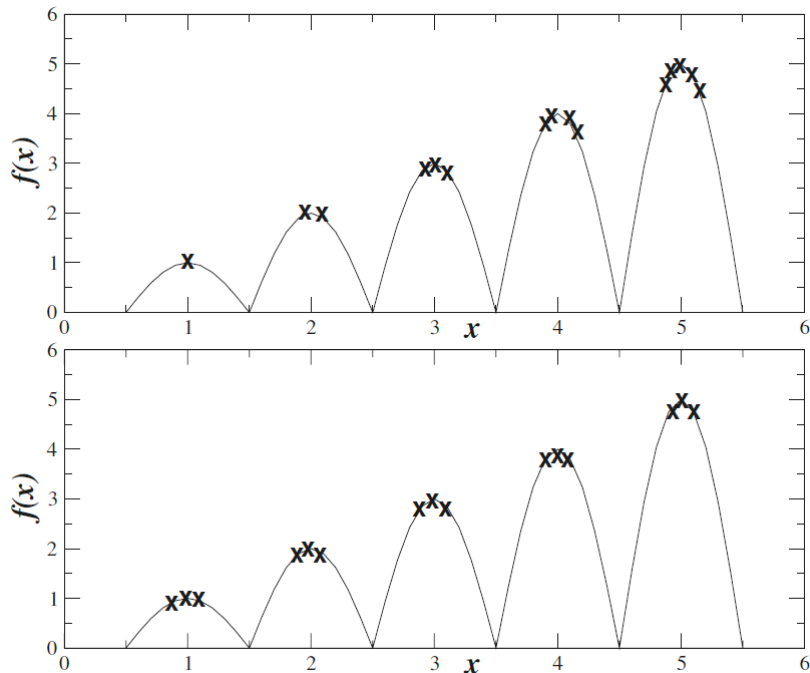
$$F'(i) = \frac{F(i)}{\sum_j sh(d(i,j))}$$

$$sh(d) = \begin{cases} 1 - \left(\frac{d}{\sigma_{share}}\right)^\alpha, & \text{if } d \leq \sigma_{share} \\ 0, & \text{otherwise} \end{cases}$$

Crowding

- ✓ Offspring (children) replace the most similar parents.
 - Parent population is randomly paired
 - Each pair produces two offspring via recombination
 - These offspring are mutated and evaluated
 - Four pairwise distances between offspring and parents are calculated
 - Offspring competes for survival in a tournament with parents

Fitness sharing and crowding



- ✓ Idealized population distributions for:
- ✓ Fitness sharing
 - Allocate individuals to peaks in proportion to their fitness
- ✓ Crowding
 - Distributed amongst peaks

Speciation

- ✓ Biological analogy, when someone specifically interfering the reproduction of individuals
- ✓ Population may contains several species, and during recombination individuals mate only with same species
- ✓ Species can be defined via distance or special tag

Island based model

- ✓ Population contains several subpopulations
- ✓ Each subpopulations may be evolved by different strategies
- ✓ Some individuals migrate between population every n generations
- ✓ Can be parallelized

Frameworks for EAs

- ✓ JMetal. (Java, 2015).
<http://jmetal.sourceforge.net/index.html>.
- ✓ A full-contained framework containing a huge variety of algorithms (evolutionary, population) for single-criteria and multi-criteria optimization. Provides mechanisms for configuring, monitoring, managing the algorithm.
- ✓ Watchmaker. (Java, 2010).
<https://watchmaker.uncommons.org>.
- ✓ Simple and user-friendly framework. Powerful evolution engine with parallelization and island models. Monitoring and control of the algorithm. Interactive mode.
- ✓ Jenetics. (Java, Live). <https://jenetics.io>.
- ✓ Fresh and modern framework. Uses new Java functionality (stream). Coding solutions through the *Genotype*:
Chromosome: *Gene*.
- ✓ HeuristicLab. (C#, Live).
<https://dev.heuristiclab.com/trac.fcgi/wiki>.
- ✓ Supported platform for developed problems and algorithms. Graphical interface. Less flexible, complex algorithm development for non-standard problems.
- ✓ GeneticSharp. (C#, 2019).
<https://github.com/giacomelli/GeneticSharp>
- ✓ A simple framework with basic functionality and capabilities for developing efficient algorithms.
- ✓ Deap. (Python, ~2019).
<https://deap.readthedocs.io/en/master/>
- ✓ The most popular, simpler Python framework. Convenient implementation of your solutions, parallelization, statistics monitoring.

Lab 1

- ✓ Function optimization
 - Take the template script
 - Change dimension of the problem (dim = 100)
 - Develop your version of algorithm (modify mutation, crossover, selection, ...)
 - The best result for provided function is *10.0*. Try to get at least *9.5*.
 - Prepare a Jupyter Notebook report.
 - Send me to mihail.melnik.ifmo@gmail.com with topic *ec lab1 surname*
 - Deadline is like 2 weeks, but not hard.

Function optimization

✓ In module function_opt presented 3 experiments:

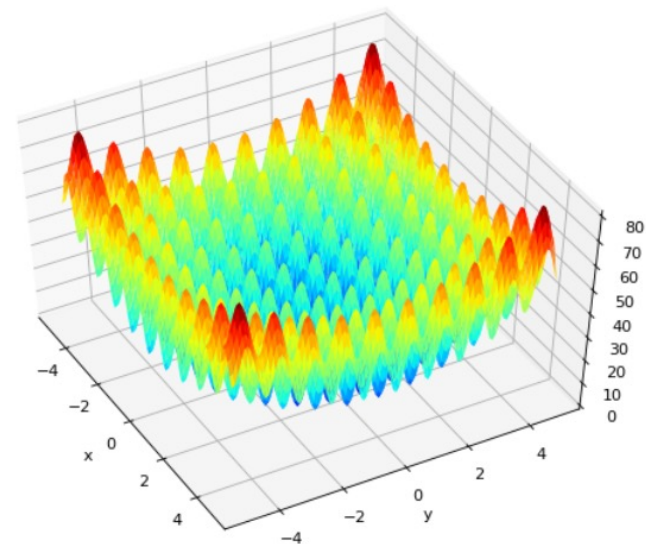
- Genetic algorithm
- Particle swarm optimization
- Together

Benchmark function – Rastrigin function.

<https://www.mathworks.com/help/gads/example-rastrigins-function.html>

Dimension can be modified.

| | |
|---------------|--|
| Type | minimization |
| Range | $x_i \in [-5.12, 5.12]$ |
| Global optima | $x_i = 0, \forall i \in \{1 \dots N\}, f(\mathbf{x}) = 0$ |
| Function | $f(\mathbf{x}) = 10N + \sum_{i=1}^N x_i^2 - 10 \cos(2\pi x_i)$ |





Thank you for your attention!

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