

Heidelberg University
Institute of Computer Science
Database Systems Research Group

Lecture: Complex Network Analysis

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Assignment 2
Graph Theory and Networks in Python

https://github.com/nilskre/CNA_assignments

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1 Problem 2-1 Erdos-Renyi Network

Consider an Erdos-Renyi network with $N = 80$ nodes, connected to each other with probability $p = 0.05$.

1. What is (i) the expected number of links in the graph and (ii) the expected degree of a node?

(i) The expected number of links in the graph:

$$\langle L \rangle = p \frac{N(N-1)}{2} = 0.05 \frac{80 \cdot (80-1)}{2} = 158 \quad (1)$$

The expected number of links in the graph is 158.

(ii) The expected degree of a node:

$$\langle k \rangle = p(N-1) = 0.05 \cdot (80-1) = 3.95 \quad (2)$$

The expected degree of a node in the network is 3.95.

2. In which regime is the network?
3. What is the probability to find exactly $L = 200$ links in the graph?

$$p_L = \binom{\frac{N(N-1)}{2}}{L} p^L (1-p)^{(N(N-1)/2)-L} \quad (3)$$

$$p_{200} = \binom{\frac{80(80-1)}{2}}{200} 0.05^{200} (1-0.05)^{(80(80-1)/2)-200} \approx 1.26e^{-4} \quad (4)$$

The probability to find exactly 200 links in the graph is around $1.26e^{-4}$.

4. What is the probability that a node i in the graph has degree $k_i = 5$ (using the binomial distribution)?
5. Use maximum likelihood estimation to estimate the model parameters (N, p) for the shown graph.