

Improving Run Length Encoding (RLE) on bit level by preprocessing

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Abstract

Hier steht eine Kurzzusammenfassung (Abstract) der Arbeit. Stellen Sie kurz und präzise Ziel und Gegenstand der Arbeit, die angewendeten Methoden, sowie die Ergebnisse der Arbeit dar. Halten Sie dabei die ersten Punkten eher kurz und fokussieren Sie die Ergebnisse. Bewerten Sie auch die Ergebnissen und ordnen Sie diese in den Kontext ein.

Die Kurzzusammenfassung sollte maximal 1 Seite lang sein.

Contents

1	Introduction	1
1.1	Motivation	1
1.2	Problem statement	1
1.3	Main Objective	2
1.4	Structure of this work	2
2	Principles of compression	3
2.1	Compression and Encoding fundamentals	3
2.1.1	Information Theory and Entropy	3
2.1.2	General Analysis	4
2.1.3	Probabilistic Coding	4
2.1.4	Dictionary Coding	5
2.1.5	Irreversible Compression	5
2.2	Run Length Encoding	5
2.2.1	The History	6
2.2.2	Limitations	6
2.2.3	Run Length Encoding today	7
2.3	Prefix Coding	7
2.3.1	Optimal prefix codes - Huffman Coding	7
2.4	Other methods	8
2.4.1	Burrows-Wheeler-Transformation	8
2.4.2	Inverse Burrows-Wheeler-Transformation	9
2.5	State of the Art	9
2.6	Limits of compression	9
3	Analysis	10
3.1	The Calgary corpus	10
3.2	Initial Findings	10
3.3	Possible Improvements by Preprocessing	13
3.3.1	Burrows-Wheeler-Transformation	13
3.3.2	Vertical byte reading	13
3.3.3	Byte remapping	14
3.3.4	Combined approaches	16
3.3.5	Huffman encoding of the RLE runs	16
3.4	Summary	17
4	Conceptual Design and Implementation	18
4.1	Preprocessing	18
4.1.1	Vertical Byte Reading	18

4.1.1.1	First Ideas	18
4.1.1.2	Other Difficulties	18
4.1.1.3	Compression improvements trough vertical reading	19
4.1.2	Varying maximum run lengths	19
4.1.3	Byte remapping	20
4.1.4	Burrows-Wheeler-Transformation Appliance	22
4.2	Other Processing Options	26
4.3	Implementation Decisions	26
4.4	Implementation Detail	27
4.4.1	Burrows Wheeler Transformation	27
4.4.2	Byte Remapping	27
4.5	Implementation Evaluation	27
4.6	Summary	27
5	Evaluation	28
5.1	Functional Evaluation	28
5.2	Benchmarks	28
5.2.1	Burrows-Wheeler-Transformation	28
5.2.2	Vertical encoding	28
5.3	Conclusion	28
6	Discussion	29
	Bibliography	30

List of Figures

2.1	example Huffman Tree with 3 Leaf Nodes	8
4.1	Byte mapping and varying maximum run lengths	21
4.2	Different run lengths with and without transformations	25

List of Tables

2.1	Entropy in relation to the Probability of Symbols	4
2.2	T4 static Huffman codes	6
2.3	Burrows Wheeler Transformation Matrix (all cyclic rotations)	8
2.4	State of the Art compression ratios	9
3.1	The Calgary Corpus	10
3.2	Binary RLE on the Calgary Corpus	11
3.3	Byte-wise RLE on the Calgary Corpus	12
3.4	The file <i>pic</i> with increasing bits per RLE encoded number	13
4.1	Binary RLE on vertical interpreted data	19
4.2	Calgary Corpus encoded, vertical encoding, using bits per run: 2, 2, 2, 2, 3, 4, 3, 7	20
4.3	Calgary Corpus encoded with vertical reading, byte remapping, using bits per run (2, 2, 3, 3, 3, 4, 5, 8)	22
4.4	Initial BWT implementation on byte wise RLE	22
4.5	Burrows Wheeler Transformation on byte wise RLE	23
4.6	Modified Burrows Wheeler Transformation on byte wise RLE	24
4.7	Calgary Corpus encoded with byte wise RLE after a Burrows-Wheeler- Transformation	24
4.8	Calgary Corpus encoded, all preprocessing steps, using bits per run: 4, 4,4, 4, 5, 7, 8, 10	26

1. Introduction

Die Einleitung besteht aus der Motivation, der Problemstellung, der Zielsetzung und einem ersten Überblick über den Aufbau der Arbeit.

TODO:

- explain compression ratio
- define unit of compression to quantify question and results

1.1 Motivation

In the last decades, digital data transfer became available everywhere and to everyone. This rise of digital data urges the need for data compression techniques or improvements on existing ones. Run-length encoding [14] (abbreviated as RLE) is a simple coding scheme that performs lossless data compression. RLE compression simply represents the consecutive, identical symbols of a string with a run, usually denoted by σ^i , where σ is an alphabet symbol and i is its number of repetitions. To give an example, the string `aaaabbbaabbbba` can be compressed into RLE format as $a^4b^2a^3b^4a^1$. Its simplicity and efficiency make run-length encoding still usable in several areas like fax transmission, where RLE compression is combined with other techniques into Modified Huffman Coding [9]. Most fax documents are typically simple texts on a white background, RLE compression is particularly suitable for fax and often achieves good compression ratios. Another appliance of RLE is optical character recognition, in which the inputs are usually images of large scales of identically valued pixels [1].

1.2 Problem statement

Some strings like `aaaabbbb` achieve a very good compression rate because the string only has two different characters and they repeat more than twice. Therefore it can be compressed to a^4b^4 so from 8 byte down to 4 bytes if you encode it properly. On the other hand, if the input is highly mixed characters with few or no repetitions at all like `abababab`, the run length encoding of the string is $a^1b^1c^1d^1e^1f^1g^1h^1i^1j^1$ which needs up to 16 bytes depending on the implementation.

So the inherent problem with run length encoding is obviously the possible explosion in size, due to missing repetitions in the input string. Expanding the string to twice the original size is not really a good compression so one has to make sure the input data is fitted for RLE as compression scheme. One goal is to improve the compression ratio on data suited for run length encoding and perform better than the originally proposed RLE. Another goal should be to minimize the increase in size in the worst case scenario.

1.3 Main Objective

The main objectives that derives from the problem statement is to achieve an improved compression ratio compared to regular run length encoding. To unify the measurements, the compression ratio is calculated by encoding all files listed in the Calgary corpus. Since most improvements like permutations on the input, for example a revertable Burros-Wheeler-Transformation to increase the number of consecutive symbols or a different way of reading the byte stream take quite some time, encoding speed will increase.

1.4 Structure of this work

Was enthalten die weiteren Kapitel? Wie ist die Arbeit aufgebaut? Welche Methodik wird verfolgt?

- describe following structure
- use references
- try to keep idea of a recurrent theme

2. Principles of compression

The basic idea of compression is to remove redundancy in data. Compression can be broken down into two broad categories: Lossless and lossy compression. Lossless compression makes it possible to reproduce the original data exactly while lossy compression allows the some degradation in the encoded data to gain even higher compression at the cost of some of the original information. To understand compression, one first has to understand some basic principles of information theory like entropy and different approaches to compress different types of data with different encoding. We will also show the key differences between probability coding and dictionary coding.

2.1 Compression and Encoding fundamentals

TBD

...

2.1.1 Information Theory and Entropy

As Shannon described his analysis about the English language [15], he used the term entropy closely aligned with its definition in classical physics, where it is defined as the disorder of a system. Specifically speaking, it is assumed that a system has a set of states it can be in and it exists a probability distribution over those states. Shannon then defines the entropy as:

$$H(S) = \sum_{s \in S} P(s) i(s)$$

where S describes all possible States, $P(s)$ is the likelihood of the system being in state s . So generally speaking it means that evenly distributed probabilities imply a higher entropy and vice versa. It also implies that, given a source of information S , its average information content per message from S is also described by this formula.

In addition to that, Shannon defined the term self information $i(s)$ as:

$$i(s) = \log_2 \frac{1}{P(s)}$$

indicating that the higher the probability of a state, less information can be contained. As an example, the statement “The criminal is smaller than 2 meters.” is very likely but doesn’t contain much information, whereas the statement “The criminal is larger than 2 meters.” is not very likely but contains more of information. With these definitions in mind, we can analyze some properties for the English language from an information theory perspective of view.

	$P(a)$	$P(b)$	$P(c)$	$P(d)$	$P(e)$	H
1.	0.2	0.2	0.2	0.2	0.2	2.322
2.	0.94	0.01	0.01	0.01	0.01	0.322

Table 2.1: Entropy in relation to the Probability of Symbols

Combining those approaches, you will find that Σ being a finite alphabet, and $P(s_i)$ describing the likelihood of s_i and $i(s_i)$ its self information, $i(s_i)$ also describes the amount of bits needed for this symbol, therefore its \log_2 .

$$H(\Sigma) = \sum_{i=1}^n P(s_i) \cdot \log_2 \frac{1}{P(s_i)}$$

So the entropy also describes the theoretical amount of bits needed to persist a message from Σ , calculated in *bps* as Bits per Symbol.

TODO: describe some relations between probability and entropy of information source

2.1.2 General Analysis

To evaluate the efficiency of a specific compression technique, we have to determine how much information the raw data contains. In this case for textual compression at first, we are talking about the English language. There have been broad analysis of ASCII Entropy, consisting of 96 different printable symbols for the English language, generating approaches for calculating the entropy [12].

If we assume a 96 Symbol alphabet and a uniform probability distribution, we have a quite high entropy of $\log_2(96) = 6.6 \text{ bps}$. In an empirically distribution generated by text analysis, the entropy comes down to 4.5 bps . Using an encoding with separated encoding per Symbol like the Huffman Coding, we can achieve an entropy of 4.7 bps which is only slightly worse than the theoretical entropy. By changing the assumption to blocks of symbols of length 8, we get 96^8 different blocks. With a probability distribution close to the English language we get an entropy as low as 1.3 bps which implies a possible reduction of symbols to 3 printable characters without generating longer texts.

Consulting newer sources we will find that, up to 500 character long symbol based text analysis, with around 20.3 Mio. different symbols, results in an entropy of around $1,58 \text{ bps}$ [8]. This gives a clear limit of how much compression we can theoretically expect from English text. Using a combination of different approaches like Huffman Coding and Run Length Coding, and encoding different bits of a single symbol with different approaches, we do no longer encode every symbol separately, which might result in a better compression.

2.1.3 Probabilistic Coding

The general idea behind Probability Coding is to analyze probabilities for messages and encode them in bit strings according to their probability. This way, messages that are more likely and will repeat more often can be encoded in a smaller bit string representation. The generation of those probability distributions is considered part

of the analyzer module by the algorithm and will be discussed later on in Section 4. Probability coding compression can be discerned into fixed unique coding, which will represent each message with a bit string with the amount of bits being an integer, for example Huffman coding as type of prefix coding. In contrast to Huffman coding there are also arithmetic codes which can represent a message with a floating point number of bits in the corresponding bit string. By doing so they can “fuse” messages together and need less space to represent a set of messages.

2.1.4 Dictionary Coding

Dictionary Coding is best suited for data with a small amount of repeating patterns like a text representing specific words. In this case it is very effective to save the patterns just once and refer to them if they are used later on in the text. If we know a lot about the text itself in advance, a static dictionary is sufficient but in general we want to compress an arbitrary text. This requires a more general approach as used by the well known LZ77 and LZ88 algorithms described by Jacob Ziv and Abraham Lempel [17]. They use a so called sliding window principle, a buffer moving across the data to encode in the case of LZ77 or a dynamic dictionary in the implementation of LZ78. Both of them are still used in modified versions in real world applications as described in Section 2.5.

The main difference between probabilistic coding and dictionary coding is, that the so far presented probability based methods like RLE or Huffman Coding are working on single characters or bytes whereas the dictionary based methods encode groups of characters of varying length. This is a clear advantage in terms of compression performance on every day data because of its repeating patterns most textual data has, as shown in Section 3.2.

2.1.5 Irreversible Compression

Irreversible Compression or also called “Lossy Compression” is a type of compression which loses information in the compression process and is therefore not completely reversible, hence the name. There are a lot of use-cases for these type of compression algorithms, mostly used for images, video and audio files. These files typically contain information almost not perceptible for an average human like really small color differences between two pixels of an image or very high frequencies in an audio file. By using approximations to store the information and accept the loss of some information while retaining most of it, lossy image compression algorithms can get twice the compression performance compared to lossless algorithms. Due to the fact that most lossy compression techniques are not suited for text compression which is the main use case for this work, we will not elaborate any further on this topic.

2.2 Run Length Encoding

Run length coding might count as the simplest coding scheme that makes use of context and repeating occurrences as described in the Section 1.1. While the example made earlier was in textual representation, it is best suited and mostly used for pallet based bitmap images [5] such as fax transmissions or computer icons.

run length	white codeword	black codeword
0	00110101	0000110111
1	000111	010
2	0111	11
3	1000	10
4	1011	011
...		
20	0001000	00001101000
...		
64+	11011	0000001111
128+	10010	000011001000

Table 2.2: T4 static Huffman codes

2.2.1 The History

The ITU-T T4 (Group 3) standard for Facsimile (fax) machines [10] is still in force for all devices used over regular phone lines. Each transmission sends a black and white image, where each pixel is called a *pel* and with a horizontal resolution of $8.05 \frac{\text{pels}}{\text{mm}}$ and the vertical resolution depending on the mode. To encode each sequence of black and white pixels, the T4 standard uses RLE to encode each sequence of black and white pixels and since there are only two values, only the run length itself has to be encoded. It is assumed that the first run is always a white run, so there is a dummy white pel at the beginning of each sequence. For example, the sequence *bbbbwwbbbb* can be encoded as 1,4,2,5 with the leading white dummy pixel.

To further reduce the RLE encoded sequence, a probability coding procedure like Huffman coding can be used to code the sequence, since shorter run lengths are generally more common than very long runs, which is also done by the T4 standard. Based on a broad analysis of these run lengths, the T4 defined a set of static Huffman codes, using a different codes for the black and white pixels.

TODO:describe further

A small subset of the static T4 Huffman codes are given in Table 2.2.1 which also shows the most likely runs to occur. Runs of more than 64 have to be encoded in multiple Huffman codes, for example a run of 150 has to be encoded with the Huffman code of 128 followed by the code for 22.

By combining RLE with a probabilistic approach, the ratio of compression rises because we no longer have to encode a run of length 1 or 2 with a fixed size of bits each instead we can write a recognizable Huffman code of varying length, which will be explored in grater detail later on as well as the decoding of the shown Huffman codes.

2.2.2 Limitations

As mentioned in section 1.2, run length encoding is rarely used for regular text or continuous tone images because its potentially increase in size, due to non repetitive characters or bytes. A detailed analysis of this issue is performed in section 3.2. To reduce this problem there are several approaches known, some of them were implemented in this scope, sometimes in more than one variant like the Burrows-Wheeler-Transformation.

2.2.3 Run Length Encoding today

While it is still in use by fax transmission or other highly specific tasks, it is mostly used in combination with other approaches. TODO: give more references [11]

2.3 Prefix Coding

Prefix codes make use of an untypical idea in computer science. Usually we deal with fixed length codes like 7 bit ASCII or 32 bit Integer representations which map each possible value into that fixed amount of bits. For compression it would be a benefit if we could write codes of variable length. The problem with these varying length codes is that as soon as they are part of a sequence, it becomes very hard to tell where one code word starts and finishes, resulting in ambiguous encoding. For example the set of codes $C = \{(a, 1), (b, 01), (c, 101), (d, 011)\}$ and the encoded message is 1011 do not generate distinct decodeable code words because there is no way to tell which message was encoded. From now on a code C for a set of messages S is considered to be in the form of $C = \{(s_1, w_1), (s_2, w_2), \dots, (s_m, w_m)\}$.

One way to address this problem is by adding extra stop symbols or encoding a length before each code but those just add additional data. Another approach is to use so called prefix codes and make no code which is prefix of another code, which makes them distinct and uniquely decodable as show in the next section.

2.3.1 Optimal prefix codes - Huffman Coding

A Huffman coding is one way of generating a prefix code, which is a uniquely decodable. When no code is prefix of another one, it is always decodable and yields a unique result because once a matching code is read, no other longer could also match. Huffman codes have another property, as they are call optimal prefix codes. To understand this property we first have to define the average length l_a of a code C as

$$l_a(C) = \sum_{(s,w) \in C} p(s) l(w)$$

We say that a prefix code is optimal, if $l_a(C)$ is minimized, so there is no other prefix code for a given probability distribution that has a lower average length. The existence of a relation between the average length of a prefix code to the entropy of a set of messages can be shown by making use of the Kraft McMillan Inequality. For a uniquely decodable code C where $l(w)$ is the length of the code word C

$$\sum_{(s,w) \in C} 2^{-l(w)} \leq 1$$

And it is also proven that a Huffman algorithm generates optimal prefix codes[3].

The algorithm in general is rather simple and the generation of the prefix codes will be demonstrated using an example.

TODO: explain stuff ...

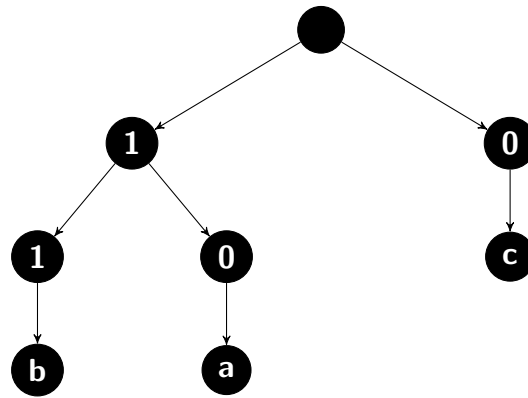


Figure 2.1: example Huffman Tree with 3 Leaf Nodes

2.4 Other methods

There are other well known methods like

- move to front
- arithmetic coding
- real world applications are mostly combinations of those
- ...

2.4.1 Burrows-Wheeler-Transformation

The Burrows-Wheeler-Transformation is not a compression technique but rather a method to prepare text to increase its compression potential, described by M. Burrows and D. J. Wheeler [4]. It is a Transformation of a string S of n characters by forming the n cyclic rotations of S , sorting them lexicographical, and extracting the last character of each of the rotations. The result of this transformation is a string L , consisting of these last characters of each sorted rotation. The algorithm also has to add special termination symbols or compute the index I of the original string S in the sorted list of rotations. Surprisingly, there is an efficient algorithm to invert the transformation back to the original string S given only L and the Index I [13].

As an example of the creation of L , given the input string $S = \text{'abraca'}$, $n = 6$, and the alphabet $X = \{a, b, c, r\}$. Create a $N \times N$ matrix M whose elements are characters, and whose rows are rotations of S . Sort all rotations in lexicographical order.

In this example, the index is $I = 1$ and the matrix M is

row 0	a	a	b	r	a	c
row 1	a	b	r	a	c	a
row 2	a	c	a	a	b	r
row 3	b	r	a	c	a	a
row 4	c	a	a	b	r	a
row 5	r	a	c	a	a	b

Table 2.3: Burrows Wheeler Transformation Matrix (all cyclic rotations)

The resulting string L corresponds to the last column of M , with characters $M[0, n-1]$, \dots , $M[n-1, n-1]$. The output of the transformation is the pair (L, I) , in the

example, $L = \text{'caraab'}$ and $I = 1$. Obviously the string L contains consecutive identical characters, which results in better compressibility as shown in 3.3.1.

2.4.2 Inverse Burrows-Wheeler-Transformation

TODO: explain reversing a bwt

2.5 State of the Art

State of the art compression

- techniques
- use cases
- limits

method	size in bytes	compression	ratio in $\frac{bits}{symbol}$
uncompressed	3,141,622	100.0%	8.00
compress	1,272,772	40.0%	3.24
ZIP v2.32	1,020,781	32.4%	2.59
gzip v1.3.5	1,017,624	32.3%	2.58
bzip2 v9.12b	828,347	26.3%	2.10
ppmd	740,737	23.5%	1.88
ZPAQ v7.15	659,709	20.9%	1.67

Table 2.4: State of the Art compression ratios

2.6 Limits of compression

- existence of not compressable strings
- <https://www.quora.com/Is-there-a-theoretical-limit-to-data-compression-If-so-how-was-it-found>
- unable to compress random data
- Kolmogorow-Komplexität

3. Analysis

The following chapter contains a detailed analysis of the problem and some fundamental requirements for the algorithm. To have a comparison to some extent, the initial performance analysis was performed on the Calgary Corpus but the results of the unmodified run length coding algorithm were very underwhelming as expected.

3.1 The Calgary corpus

The Calgary Corpus [16] is a rather old corpus created by Ian Witten, Tim Bell and John Cleary from the University of Calgary in 1987. It consists of text and some binary data files shown in 3.1 and is still used for comparison between compression algorithms. After some objections were raised [2], it was mostly replaced by the Canterbury Corpus but it is still useful for comparing against other compression algorithms.

file	size	description
bib	111261	ASCII text - 725 bibliographic references
book1	768771	unformatted ASCII text
book2	610856	ASCII text in UNIX “troff” format
geo	102400	32 bit numbers in IBM floating point format
news	377109	ASCII text - USENET batch file on a variety of topics
obj1	21504	VAX executable program
obj2	246814	Macintosh executable program
paper1	53161	UNIX “troff” format
paper2	82199	UNIX “troff” format
pic	513216	1728 x 2376 bitmap image
progC	39611	Source code in C
progl	71646	Source code in Lisp
progp	49379	Source code in Pascal
trans	93695	ASCII and control characters

Table 3.1: The Calgary Corpus

3.2 Initial Findings

The algorithm itself works in a very simple manner. Reading each bit of the input data in a consecutive way, count the consecutive bits and write the count instead of the bits themselves. So the input of “00011100” would resolve to two counts of length 3 and one of length 2 if we also assume a starting zero. Encoding this can be

done by “11 | 11 | 10”. We do not need stop symbols of any kind if we assume a fixed size for the count of each run so we can easily decode this back by making the same assumptions and reading always 2 bit and start with a zero. This implies setting a maximum run length during encoding, limited by the amount of bits used to encode one single count of the input data. If the run is starting with a 1 or a count exceeds this maximum run length, we need to add a pseudo run of length zero, so for example the input of “11000000” would be encoded to “00|10|11|00|11”, corresponding to zero times zero at the beginning, two ones, three zeros, then zero times one then three more zeros. The longer the consecutive runs, the better it can be stored, expecting they do not exceed the maximum run length but on the other hand, a high maximum run length needs more bits per run which implies more overhead if the runs to save are rather short. So in general we assume an improvement when the average run length is close to the maximum run length and not often exceeding it.

Originally developed and used on black and white pallet images containing only two values often in large repetitions, we want to use it for rather arbitrary data, mostly text. The initial algorithm is not suited for that because continuous text as binary representation does not contain runs of any kind, which could be compressed. The ASCII representation of the letter ‘e’ which is the most common in general English, has the value 130 or ‘01100101’ as 7-bit ASCII or ‘001100101’ as byte value of the UTF-8 representation. As you can see, there are no runs of a considerable size and this is the case for most printable characters as they all have a value between 32 and 127 (or 255 for the extended ASCII). Applied to the Calgary Corpus in this simple implementation, there should be an increase in size expected or *negative compression* as one might say.

With rather low expected average run length in general data it was still unclear which amount of bits per run are most suited for the mix of data residing in the corpus, so between 2 and 8 bits per run were tried and the results are shown in table 3.2. They depict the anticipated, an increase in size regardless of the amount of bits used to encode a run. By using 8 bits to encode a single run, in the worst case scenario a byte which is only alternating values like 01010101, would expand to 8 bytes, all encoding a run of length 1. For this reason, many implementations combine RLE with other encoding schemes like Huffman encoding to be able to encode runs with variable length, which will be discussed later on.

bits per rle number	expansion ratio %	bits per symbol in $\frac{bits}{symbol}$
8	329	26.38
7	288	23.11
6	248	19.87
5	208	16.66
4	168	13.51
3	131	10.50
2	104	8.36

Table 3.2: Binary RLE on the Calgary Corpus

RLE is also applicable on a byte level, because there should be repetitions of any kind like consecutive letters or line endings (EOL). This modified byte level RLE encodes runs of identical byte values, ignoring individual bits and word boundaries.

The most common byte level RLE scheme encodes runs of bytes into 2-byte packets. The first byte contains the run count of 1 to 256, and the second byte contains the value of the byte run. If a run exceeds a count of 256, it has to be encoded twice, one with count 256 and one with any further runs. So for example the word “aaabbbb” will be encoded to “0x02 | 0x61 | 0x03 | 0x62”. We do not need runs of length zero because longer runs just have to be encoded more than once so we can use all 256 possible byte values as a count. Using 8 bit for one run is obviously exaggerated because in arbitrary text it is rather rare that a character repeats more than twice. So different sizes of maximum run lengths were tried and the results are shown below.

bits per rle number	ratio in %	bits per symbol in $\frac{bits}{symbol}$
8	165	13.20
7	154	12.38
6	144	11.57
5	134	10.77
4	125	10.00
3	116	9.29
2	109	8.74

Table 3.3: Byte-wise RLE on the Calgary Corpus

However after some analysis of the corpus data, it was shown that most runs had a value of one and almost no runs larger than 4 occurred, which lead to the conclusion, two bit for the run count should be plenty. But even with a run size of just two bits, there is still a increase in size of about 9% and uses $8.74 \frac{bits}{symbol}$. This is still useful as a kind of a base line. Interestingly the binary implementation performs better on 2 bits per RLE number (4 % increase in size) than the byte implementation (9 % increase in size) but also worse with a higher amount of bits per run, where it expands the data to more than triple in size. It is unclear which kind of implementation will profit most of preprocessing, so both will be further analyzed, but the benefit of byte wise RLE is the better worst case performance of 1.5 up to 2 times the original size compared to binary RLE with up to 4.5 times the original size.

If we take a more detailed look, we can see that while most files expand with larger RLE numbers regardless which implementation of RLE, but some files have their minimum size when encoded with higher RLE numbers of up to 7 bit. With the simple binary based RLE, almost all files of the Calgary Corpus expand linear related to the amount of bits used for the encoding however the file *pic* decreases in size until 7 bits per RLE number used to a sizes of just 19.5% of its original size with only $1.56 \frac{bits}{symbol}$ while the other files just doubled or even tripled in size. Using the byte wise operating RLE we see a similar result with the file *pic*, but not as decent with 27.2% of its original size using $2.17 \frac{bits}{symbol}$ encoding with 6 bits per run. Now it is quite clear why run length encoding is very suited for monochromatic images where it achieves a compression ratio close to the theoretical expected maximum compression because the file mostly consists of long runs of repeating bytes depicting the same color value.

file	size original	$\frac{bits}{RLEnumber}$	size encoded	ratio in %	$\frac{bits}{symbol}$
pic	513216	2	350292	68.25	5.46
		3	235067	45.80	3.66
		4	165745	32.29	2.58
		5	126349	24.61	1.96
		6	106773	20.80	1.66
		7	100098	19.50	1.56
		8	101014	19.68	1.57

Table 3.4: The file *pic* with increasing bits per RLE encoded number

An additional step of the improvement could be the detection of high efficiency with regular binary RLE to simply apply this to files highly suited for this method.

3.3 Possible Improvements by Preprocessing

The broad idea of preprocessing is to manipulate the input data in a way that results in data which can be compressed more efficiently than the original data. This can be done in various ways, some of them will be explored in greater detail to find out if it is implementable or not. One way of doing so is a Burrows-Wheeler-Transformation.

3.3.1 Burrows-Wheeler-Transformation

To understand how a Burrows-Wheeler-Transformation improves the effectiveness of compression, consider the effect in a common word in English text. Examine the letter ‘t’ in the word ‘the’, in an input string holding multiple instances of this word. Sorting all rotations of a string results in all rotations starting with ‘he ’ will be sorted together and most of them are going to end in the letter ‘t’. This implies that the transformed string *L* has a large number of the letter *t*, combined with some other characters, such as space, ‘s’, ‘T’, and ‘S’. This is true for all characters, so any substring of *L* is likely to contain a large number of some distinct characters. “The overall effect is that the probability that given character *c* will occur at a given point in *L* is very high if *c* occurs near that point in *L*, and is low otherwise” [4].

It is obvious that this should always improve the performance of byte level RLE because the transformation is taking place at character level but it should not effect the binary implementations.

3.3.2 Vertical byte reading

Instead of performing compute intense operation on the data, we could also interpret the data in a different way and apply the original run length encoding on binary data. This idea is also know for binary RLE on images, where the encoding in the image follows a specific path.

TODO showcase

By reading the data in chunks of a fixed size, it is possible to read all most significant bits of all bytes, then the second most significant bits of all bytes and so on. This interpretation results in longer runs as shown in the example below.

The binary UTF-8 interpretation of the example string from earlier $S = \text{'abraca'}$ results in 8 runs of length 1, 9 runs of length 2 as well as 3 runs of length 3 and 4.

48 ELEMENTS:

```
00111000001100110000110011110011001110000010111000011100
1110000011
```

Reading the data in a different way, all most significant bits, then all second most significant bits and so forth, results in much longer runs. This becomes clear if we read each row in the example below.

2-D:

001110000011	<Row 1>
001110000100	<Row 2>
001111000100	<Row 3>
001110000011	<Row 4>
001110000111	<Row 5>
001110000011	<Row 6>

Now we have 5 runs of length 6, 2 runs of length 3, 3 runs of length 2 and just 6 runs of length 1 as opposed by the simple interpretation. This is because the binary similarity between the used characters, as the character for a and b only differ in one bit. It is clear that simply a different way of reading the input does not compress the actual data, instead it enables a better application of existing compressions.

3.3.3 Byte remapping

The effect of very long runs in the last example was mainly because the binary representations of the used characters are very similar, so the range of byte values used was very small (between a = 97 and r = 114). Introducing other used symbols like uppercase letters, space or new lines, the used range expands.

The binary representation of a String like $S' = \text{"Lorem ipsum dolor sit amet, consectetur adipiscing elit."}$, results in a worse result as shown below. The usage of other characters expanded the used byte range to between 32 and 117 which results in shorter average runs. Interestingly the most significant bit is always 0, a fragment from the backwards compatibility with standard ASCII encoding.

2-D:

001000111000	<Row 1>
001100111111	<Row 2>
001111000100	<Row 3>
001110001001	<Row 4>
001110011101	<Row 5>
000100000000	<Row 6>
001110010001	<Row 7>
001111000000	<Row 8>
001111000111	<Row 9>
001111001001	<Row 10>
001110011001	<Row 11>

00100000	<Row 12>
0111000100	<Row 13>
0111001111	<Row 14>
0111001100	<Row 15>
0111001111	<Row 16>
0111100010	<Row 17>
0001000000	<Row 18>
0111100011	<Row 19>
0111001000	<Row 20>
0111100100	<Row 21>
0001000000	<Row 22>
0111000000	<Row 23>
0111001100	<Row 24>
0111000100	<Row 25>
0111100100	<Row 26>
0001001110	<Row 27>

One idea to solve the shorter runs might be a dynamic byte remapping, as the input data is read in parts, where the most frequently used bytes are mapped to the lowest value. This way the values are not alternating in the whole range of 0 to 255 but rather in a smaller subset and the most frequent ones will be the smallest values, so in theory our average runs should increase because we should encounter more consecutive zeros. Some sections have more specific characters or bytes than others but this idea can also be applied to the whole file however it is unclear at this point what method outperforms which. A single map for each block of data should result in lower average values used but also creates a kind of overhead because the mapping has to be stored in the encoded file as well. Applying a simple mapping to lower values results in the following horizontally interpreted rows.

2-D:

0000010001	<Row 1>
0000000010	<Row 2>
0000000100	<Row 3>
0000000001	<Row 4>
0000000000	<Row 5>
0000000000	<Row 6>
0000000100	<Row 7>
0000001100	<Row 8>
0000000110	<Row 9>
0000001110	<Row 10>
0000000000	<Row 11>
0000000000	<Row 12>
0000001001	<Row 13>
0000000000	<Row 14>
0000001100	<Row 15>
0000000000	<Row 16>
0000000100	<Row 17>
0000000000	<Row 18>
0000000010	<Row 19>

0000001000	<Row 20>
0000001111	<Row 21>
0000000000	<Row 22>
0000001010	<Row 23>
0000000001	<Row 24>
0000000111	<Row 25>
0000001111	<Row 26>
0000010000	<Row 27>

Using this method, the 4 most significant bits all result in zero columns, even row 5 has long runs while it is worth noting that the mapping itself has to be persisted in the encoded file as well. It is also still unclear if this idea scales well or is applicable to other files.

3.3.4 Combined approaches

The idea of combining different compression methods into a superior method is not new and was also performed on RLE as mentioned in Section 2.2.1. While the idea of encoding the RLE numbers with Huffman codes is already known and analyzed, it is mostly in a static sense and optimized for special purpose applications. However the vertical byte reading enables new approaches, even more in combination with the idea of byte remapping and might become applicable to more than just binary Fax transmissions or DNA sequencing **TODO: reference** with longer runs of any kind in average.

It might be interesting to see how well the appliance performs using the vertical binary encoding, in combination with the byte mapping. We expect the more significant the bit, the longer the runs because alternating values should be mostly on the lower significance bits. Using larger run length numbers for these rows while using smaller RLE numbers or even another encoding scheme like simple Huffman encoding we should improve our initial results.

3.3.5 Huffman encoding of the RLE runs

Another interesting approach is the improvement achieved by the combination of different methods like performing this modified RLE run on arbitrary data and then encode the results with Huffman codes, using shorter codes for more frequent runs. This idea is not new and also used in the current Fax Transmission Protocol but only for the simple binary RLE in combination with modified Huffman Codes. Other papers also mentioned these combined approaches and seemed to achieved good compression ratios, not much worse than the theoretical limit of around $1.5 \frac{\text{bits}}{\text{symbol}}$ shown in Section 2.1. This was for example done by M. Burrows and D.J. Wheeler in 1994 with their Transformation, in combination with a Move-to-Front Coder and a Huffman Coder [4]. Encoding the Calgary Corpus resulted in a decrease in size to just 27% of its original with a mean $\frac{\text{bits}}{\text{symbol}}$ of just 2.43. This approach would no longer be considered preprocessing, but if more compression could be achieved by adding a post-processing step it is still worth trying out. It clearly has some benefits over the encoding of regular RLE numbers with a fixed size because we can encode with varying lengths, which also implies the absence of additional zeros, needed in the initial implementations.

3.4 Summary

TODO

Am Ende sollten ggf. die wichtigsten Ergebnisse nochmal in *einem* kurzen Absatz zusammengefasst werden.

4. Conceptual Design and Implementation

Without further ado, design and implementation of the initial ideas began. As Section 3 showed, there are some potentially promising improvements to be made to run length encoding, but how well they scale and work on a larger input with versatile symbols or bytes has to be determined.

4.1 Preprocessing

4.1.1 Vertical Byte Reading

Implementing the vertical reading of the input shown in Section 3.3.2 was not hard but it should be kept in mind that the size of the input chunks has to be divisible by the size of 8. Otherwise parsing it into an Array of Bytes results in the last Byte having some padding which might cause problems later on. By collecting the bits into a proprietary data structure, we avoid this problem but working with bytes internally should be easier. For larger files it should also be possible to work in space and writing the output on the fly during the reading process. Nonetheless both ways of collecting all bits of identical significance and writing on the fly are implemented.

4.1.1.1 First Ideas

Initially some other ideas have been followed with very poor results. One idea was arranging all input bits in a Matrix or square Matrix in a way it would still be receivable later on. This way other methods from linear algebra would have been applicable to the input data, so that the construction of a triangular matrix or other preprocessing would result in long runs of zeros. Difficulties in the construction and transformation of the Data lead to the abandonment of this approach and the already described vertical interpretation was used further on.

4.1.1.2 Other Difficulties

Other difficulties arose while performing bit operations, because it became slow on larger workloads. This and other issues were solved by using the Kotlin library `IOStreams` for Kotlin. This way most operations can be performed on the stream instead of reading all data to encode and then working in memory.

4.1.1.3 Compression improvements through vertical reading

First results of just plain binary RLE on the vertical interpretation improved its overall performance and achieved a small edge over regular binary RLE with a slightly smaller expansion but it is still not as good as byte wise RLE with a small run value of 2 bits.

bits per rle number	ratio in %	bits per symbol in $\frac{\text{bits}}{\text{symbol}}$
8	255.22	20.41
7	224.45	17.95
6	194.74	15.57
5	167.04	13.36
4	142.58	11.40
3	127.80	10.22
2	139.79	11.18

Table 4.1: Binary RLE on vertical interpreted data

If we take a closer look on each file, we see similar results compared to the original proposed binary RLE, where most files had a compression ratio of above 1 with 3 bits per RLE encoded number, except for the file *pic*. Average sizes are increasing again with more bits per run up to 2.5 times its original size and also the file *pic* has the best compression ratio. This time although it is at its peak using 6 bits per RLE run and only achieves a compression of $3.67 \frac{\text{bits}}{\text{symbol}}$ compared to $1.56 \frac{\text{bits}}{\text{symbol}}$ with simple binary RLE. These results were quite far from the desired outcome which mainly arose because increasing the bits per run improved the result for the most significant bits but also degraded the results for the other bits. So the idea of encoding the bits of different significance with different RLE schemes with varying bits per run arose, to solve this issue.

4.1.2 Varying maximum run lengths

This time the most significant bits have been encoded with more bits per run than the other ones and after bench marking every combination, it turned out, with 2 bits per run and 5 bits per run for the 3 most significant bits, it improved by another 4 percent with most files having a $\frac{\text{bits}}{\text{symbol}}$ ratio of only slightly above 9. More specifically some textual files are close to 8, which relates to the earlier mentioned ASCII fragments in UTF-8 encoding. This time higher possible runs on this position resulted in fewer runs in total, so in a better compression overall. Applying this increase to more than the most significant bit lead to a decrease in performance, which most likely related to the shorter runs on lower order bits, seen in Section 3.3.2. Therefore this idea was applied again but with a much finer granularity and every combination of different run lengths of every bit could be tried out. Also the concept of mapping the input to lower value bytes to artificially increase runs of consecutive zeros on more significant bits should be applied first.

Testing out every reasonable combination of different run lengths would imply running 8^8 combinations because every of the 8 bits could be encoded with 2 to 10 bits per run. Assuming around 10 seconds for each encoding round would still result in somewhat around 46 thousand hours of computing which is clearly too much.

Even using multi-threading would not resolve this issue so the computation had to be further reduced. By trying only a few specific combinations we assume to be good, we can then selectively small changes to improve further. This way the results were improved and the compression result was lowered around 7 percent points to 112.41% of its original size instead of 127% with a fix length for every bits position as shown in figure 4.2, but this was still far from the desired state. Most files still increased in size except the file *pic*, even though all bits could be encoded differently but the average run length of the lower bits must be very low if 2 bits per RLE number achieved best results. To increase the average run length overall, the already described byte mapping was applied to the input data.

file	size original	size encoded	ratio in %	$\frac{bits}{symbol}$
bib	111261	129424	116.32	9.31
book1	768771	820463	106.72	8.54
book2	610856	659811	108.01	8.64
geo	102400	162274	158.47	12.68
news	377109	400810	106.28	8.50
obj1	21504	31592	146.91	11.75
obj2	246814	379591	153.80	12.30
paper1	53161	57654	108.45	8.68
paper2	82199	88121	107.20	8.58
pic	513216	533254	103.90	8.31
progc	39611	41360	104.42	8.35
progl	71646	74554	104.06	8.32
progp	49379	53403	108.15	8.65
trans	93695	99818	106.54	8.52
all files	3145718	3536225	112.41	8.99

Table 4.2: Calgary Corpus encoded, vertical encoding, using bits per run: 2, 2, 2, 2, 3, 4, 3, 7

4.1.3 Byte remapping

As shown in Section 3.3.3 this effect could become useful if it resulted in higher average runs. To apply the mapping, the individual file has to be analyzed at first to find the occurrence of each byte in the input data. We expect a map with the most occurring byte is assigned the lowest value or 0 as byte, the second most frequently read byte the second most which should be 1 and so on. Then while reading the file during late steps, every byte read will be replaced by its mapped value. If a small mapping is generated, lets say with 62 entries for example we know all bytes to encode will have zeros only on the first and second most significant bit value because the highest value after the mapping took place is 61. This should also be taken into account later on during encoding and finding the optimal maximum run lengths. To reverse the mapping after decoding the runs, the mapping has do be persisted into the encoded file and parsed back during the decoding process. This is simply done by adding the length of the mapping and then just all mapping keys to the header of the output file.

After some analysis it was found that the effect was also seen in the second and third most significant bit, as higher value bytes became unlikely in the input data after

the remapping so the idea of varying maximum run lengths for different significant bits became more appealing again. To determine the best combination of maximum run lengths and how many most significant bits should be encoded with a higher maximum run length, most promising looking combinations of these were tested and the results plotted below.

TODO: fix axis

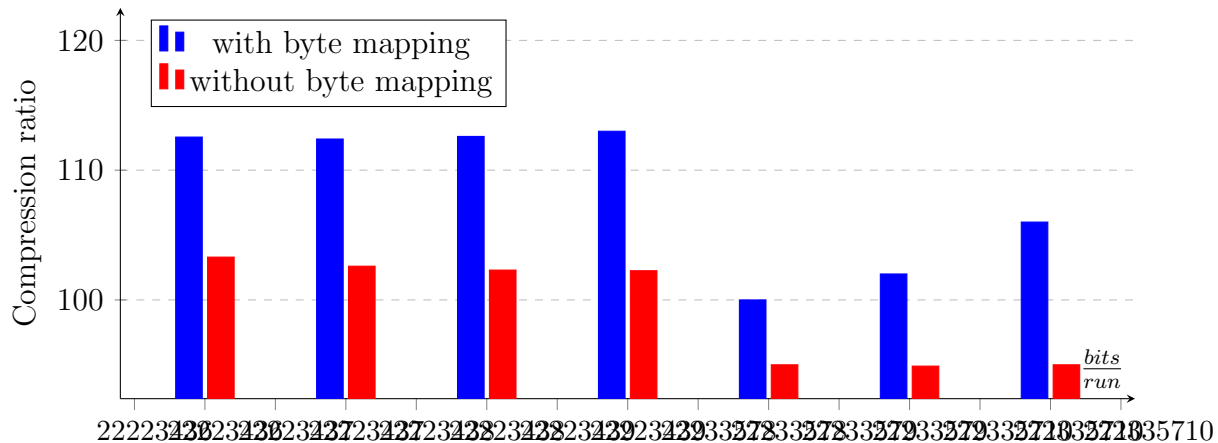


Figure 4.1: Byte mapping and varying maximum run lengths

Using this combined approach the first time a real compression was achieved for the corpus instead of just one very specific file. The combination of 2 bits for the most insignificant bits, 3 for the fourth and fifth most insignificant bit 5 for the sixths most one, 7 bits for the second most significant bit and 9 bits for the most significant one yielded the overall best results with 94.9% of its original size and $7.59 \frac{\text{bits}}{\text{symbol}}$ as shown in Figure 4.1. Some files got a little smaller while other files still expanded which is only somewhat of an enhancement over regular RLE which performs really well on specific files. But on this corpus a slight reduction in size was achieved using preprocessing and a modified RLE.

file	size original	size encoded	ratio in %	$\frac{bits}{symbol}$
bib	111261	111579	100.29	8.02
book1	768771	669578	87.10	6.97
book2	610856	551757	90.33	7.23
geo	102400	144974	141.58	11.33
news	377109	363010	96.26	7.70
obj1	21504	30166	140.28	11.22
obj2	246814	340165	137.82	11.03
paper1	53161	50074	94.19	7.54
paper2	82199	71747	87.28	6.98
pic	513216	408136	79.53	6.36
progc	39611	38490	97.17	7.77
progl	71646	63765	89.00	7.12
progp	49379	46093	93.35	7.47
trans	93695	94729	101.10	8.09
all files	3145718	2988359	94.99	7.59

Table 4.3: Calgary Corpus encoded with vertical reading, byte remapping, using bits per run (2, 2, 3, 3, 3, 4, 5, 8)

4.1.4 Burrows-Wheeler-Transformation Appliance

Another possible preprocessing step which promised an improvement is the mentioned Burrows-Wheeler-Transformation from Section 2.4.1, initially applied to regular binary and byte wise RLE. By mistake a very simple transformation implementation was chosen, working by adding additional start and stop symbols to the input string (0x02 as STX, start of text and 0x03 as ETX, end of text). Some basic testing and playing around worked great but later on it revealed some major issues. For example the Calgary Corpus consists of more than textual data, in fact the files geo, obj1, obj2 and pic contain of some binary data of include the symbols STX or ETX so we wont be able to apply the transformation to these. Another shortcoming was the very poor time complexity of almost $O(n^2)$ because under the hood, it uses a dual pivot Quick-sort algorithm from the JDK 11, which is typically faster than traditional one pivot Quick-sort. This algorithm offers $\Theta(n \log(n))$ average time complexity but in the worst case, its time complexity is cubic. This problem was partially solved by reading the input data in parts and performing the transformation on each part, result in a much smaller length n and thus better run time at the expense of a slightly worse transformation result. As all chunks are individual transformations, they can also be computed in parallel without much effort.

bits per rle number	ratio in %	bits per symbol in $\frac{bits}{symbol}$
3	95.41	7.63
2	91.39	7.31

Table 4.4: Initial BWT implementation on byte wise RLE

While it was only applicable to textual data and very slow, even when divided into smaller parts and computed in parallel, it improved the overall results of byte wise RLE by 16% to a compression ratio of slightly over 7 $\frac{bits}{symbol}$ as table 4.4 depicts,

which seemed like a good start. Regular binary RLE did not really benefit from this transformation as expected but on vertical interpretation, consecutive characters result in successive bits on every significance. Still this implementation had to be dropped and switched against one that could handle arbitrary input to be able to transform all files. This time all files could be processed and the resulting compression with byte wise RLE improved further as shown in table 4.5.

bits per rle number	ratio in %	bits per symbol in $\frac{bits}{symbol}$
3	91.62	7.33
2	89.46	7.15

Table 4.5: Burrows Wheeler Transformation on byte wise RLE

In Section 2.4 the Burrows-Wheeler-Transformation inversion was performed using a Matrix M containing all cyclic rotations of the input word, sorted in lexicographic order. However this is has a bad complexity and the inverting process does not even has access to this Matrix M.

In general a Burrows-Wheeler-Transformation should also increase the runs in the implementation of Section 3.3.2 and 3.3.3 so those preprocessing steps were also applied in combination. To do so, it was first swapped against an sufficient implementation provided by a paper from m. Burrows and D. J. Wheeler [4] from 1994. Their method is also the one described in Section 3.3.1 and could handle arbitrary input but it also had some downsides like the additional index I of the transformation, which had to be persisted as well. The major downside of this implementation although was the rather slow. To overcome this issue and the saving of additional indices, the implementation used had to be swapped once more against one that was first described by [13] in 2009 which claimed to perform in linear time complexity.

In form of the C library libdivsufsort a working implementation of BWTS was found, the bijective Burrows-Wheeler-Scott-Transformation described in [7]. This kind of Burrows-Wheeler-Transformation does not require additional information, no start and stop symbols neither and index of its original position. Briefly, it does not construct a matrix of all cyclic rotations, instead it is computed with a suffix array sorted with DivSufSort, described in [6] which is the fastest currently known method of constructing the transformation. To use it properly the code was ported to Kotlin but there are also ports of this library in Java and Go available which are recommended because the original code is neither documented nor readable.

The simple binary RLE did not really benefit from this transformation which is to be expected, because it generates repetitions of bytes, but if a byte needs many short runs it will still expand in size because the average runs are not that much influenced. For example just the letter e needs 6 different runs, no matter on which position or surrounded by what letters. The byte wise implementation on the other hand did very strongly benefit from this transformation, it will always create longer runs of bytes. Swapping the implementation of the Burrows-Wheeler-Transformation resulted in way better results, the simple byte wise RLE archives compression ratios around 59 % of its original size while using 4 bits per run, see table 4.6. This was mainly because of the longer repetitions possible after the transformation was

performed on the whole input instead of small chunks. This drastic increase was still a little astonishing but obviously average runs of characters increased so much, that 4 bits per run achieved the maximum result. Another reason for this vast improvement compared to the old implementations is the lack of additional information needed to store because we do no longer need to store the transformation index of every chunk or additional characters.

bits per rle number	ratio in %	bits per symbol in $\frac{bits}{symbol}$
8	74.42	5.95
7	69.90	5.59
6	65.58	5.24
5	61.71	4.93
4	58.98	4.71
3	59.18	4.73
2	67.69	5.41

Table 4.6: Modified Burrows Wheeler Transformation on byte wise RLE

This BWTS generates extreme long runs of identical byte values, which in turn enhances the performance of the byte wise RLE vastly. If we take a closer look we can see in table 4.7 that all files have a compression ratio below 100 while the total size is nearly reduced to half. The file *geo* is still close to uncompressed but half of the files only need less than 5 $\frac{bits}{symbol}$. The file *pic* is still the best compressible with only 2.12 $\frac{bits}{symbol}$.

file	size original	size encoded	ratio in %	$\frac{bits}{symbol}$
bib	111261	59285	53.28	4.26
book1	768771	590879	76.86	6.15
book2	610856	374742	61.35	4.91
geo	102400	101192	98.82	7.91
news	377109	246047	65.25	5.22
obj1	21504	16467	76.58	6.13
obj2	246814	126626	51.30	4.10
paper1	53161	34130	64.20	5.14
paper2	82199	56507	68.74	5.50
pic	513216	136074	26.51	2.12
progc	39611	24312	61.38	4.91
progl	71646	31466	43.92	3.51
progp	49379	20862	42.25	3.38
trans	93695	32835	35.04	2.80
all files	3145718	1855520	58.98	4.71

Table 4.7: Calgary Corpus encoded with byte wise RLE after a Burrows-Wheeler-Transformation

There should still room for some optimizations because as seen in Section 4.1.2, the remapping of the input resulted in longer runs on the higher order bits and the vertical interpretation made it possible to encode different sections with different maximum run lengths. It was expected that applying the Burrows-Wheeler-

Transformation to the vertical encoding variant should improve its efficiency as much as the byte wise RLE did benefit, which turned out to be wrong. It did indeed perform at its best when applying the BWT and the mapping but it did not outperform the combination of BWT and byte wise RLE.

TODO: rework

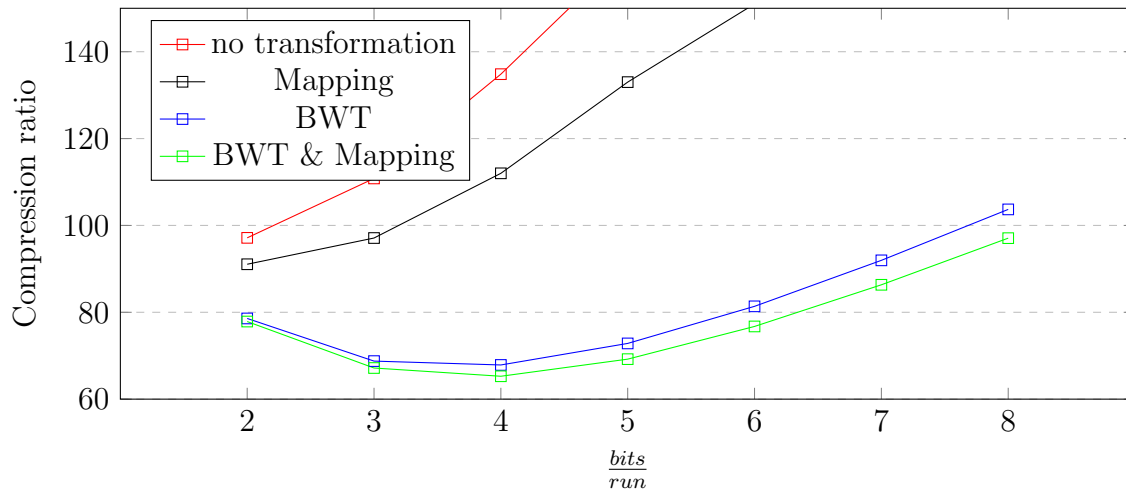


Figure 4.2: Different run lengths with and without transformations

TODO: rework

In Section 4.1.2 different run lengths for different significant bits provided an edge over just fixed maximum run length, so this combination was also tried out. After testing all combinations of possible and reasonable variables it was found that using a Burrows-Wheeler-Transformation and byte remapping as preprocessing steps, parse the transformed data in vertical order and then using 3 bits per run for low significant bits and 7 for the 3 most significant bits, run length encoding performs at its peak. Using this setup, the Calgary Corpus can be compressed down to 58.1 % of its original size while using only $4.65 \frac{\text{bits}}{\text{symbol}}$ as shown in figure ???. This was the best result achieved so far and the detailed compression results are shown below.

file	size original	size encoded	ratio in %	$\frac{bits}{symbol}$
bib	111261	73843	66.37	5.31
book1	768771	570348	74.19	5.94
book2	610856	409639	67.06	5.36
geo	102400	145950	142.53	11.40
news	377109	275396	73.03	5.84
obj1	21504	27023	125.66	10.05
obj2	246814	213392	86.46	6.92
paper1	53161	37344	70.25	5.62
paper2	82199	56490	68.72	5.50
pic	513216	227914	44.41	3.55
progc	39611	28275	71.38	5.71
progl	71646	38144	53.24	4.26
progp	49379	27029	54.74	4.38
trans	93695	49314	52.63	4.21
all files	3145718	2184197	69.43	5.55

Table 4.8: Calgary Corpus encoded, all preprocessing steps, using bits per run: 4, 4,4, 4, 5, 7, 8, 10

One last option was the encoding of the lowest significant bits with another, more suited scheme like Huffman encoding was tried out but with rather poor results. It was found that encoding the last or the last few rows seen in 3.3.2 with did not improve overall results and it was therefore discarded. This might be related to the high improvement in RLE after a Burrows-Wheeler-Transformation and other factors like additional overhead because the mapping of the Huffman encoding has to be persisted with the encoded data. But the idea of combing the RLE methods with Huffman encoding still stuck around and was picked up again later on in a modified way in Section 4.2. No further attempts to add or improve preprocessing steps of this kind were made, instead the results were analyzed and compared with other results in section 5.

4.2 Other Processing Options

Another step worth mentioning was the encoding using Huffman codes after the Run length encoding was performed, similar to the Fax Transmission Standard mentioned in section 2.2.1, but in a dynamic way instead of predefined static codes. This idea was also used by Burrows and Wheeler in their paper [4] but instead of RLE they combined a Move to Front Coder with their transformation and then encoded the result using Huffman codes. This way it would be possible to encode more frequent results of the Move to Front Encoder or the Run Length Encoder could be encoded into shorter codes and thus save even more space. However this step is not considered preprocessing anymore but could improve the compression furthermore.

4.3 Implementation Decisions

The algorithms described have all been implemented using Kotlin, because it can be compiled for the Java Virtual Machine as well as native, so it seemed like a good

balance between native speed and higher language conciseness and fault-tolerance. Also there were some library available for Byte- and Bit-Operations on streams which proved to be quite useful.

4.4 Implementation Detail

- detailed information about specific modules and classes
- ...

4.4.1 Burrows Wheeler Transformation

- TBD

4.4.2 Byte Remapping

- show use case

4.5 Implementation Evaluation

- evaluation of implementation choices made

4.6 Summary

Am Ende sollten ggf. die wichtigsten Ergebnisse nochmal in *einem* kurzen Absatz zusammengefasst werden.

5. Evaluation

Moving on to the evaluation, we start by comparing the achieved results using different preprocessing options or combination of those. To start of it is clear that the best compression ratio was not accomplished by using a combination of different mapping techniques and a vertical interpretation of the input data but we now take a closer look at the discrepancy between each result. It is also clear that with the help of such methods, run length encoding can become a suitable compression algorithm for more than just pellet based images although it is clearly not as sophisticated as advanced state of the art compression methods mentioned in section 2.5.

5.1 Functional Evaluation

...

5.2 Benchmarks

- Benchmark with the Calgary corpus
<http://www.data-compression.info/Corpora/>

...

5.2.1 Burrows-Wheeler-Transformation

5.2.2 Vertical encoding

5.3 Conclusion

Am Ende sollten ggf. die wichtigsten Ergebnisse nochmal in *einem* kurzen Absatz zusammengefasst werden.

6. Discussion

(Keine Untergliederung mehr)

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Eidesstattliche Erklärung

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Trier, den xx. Monat 20xx