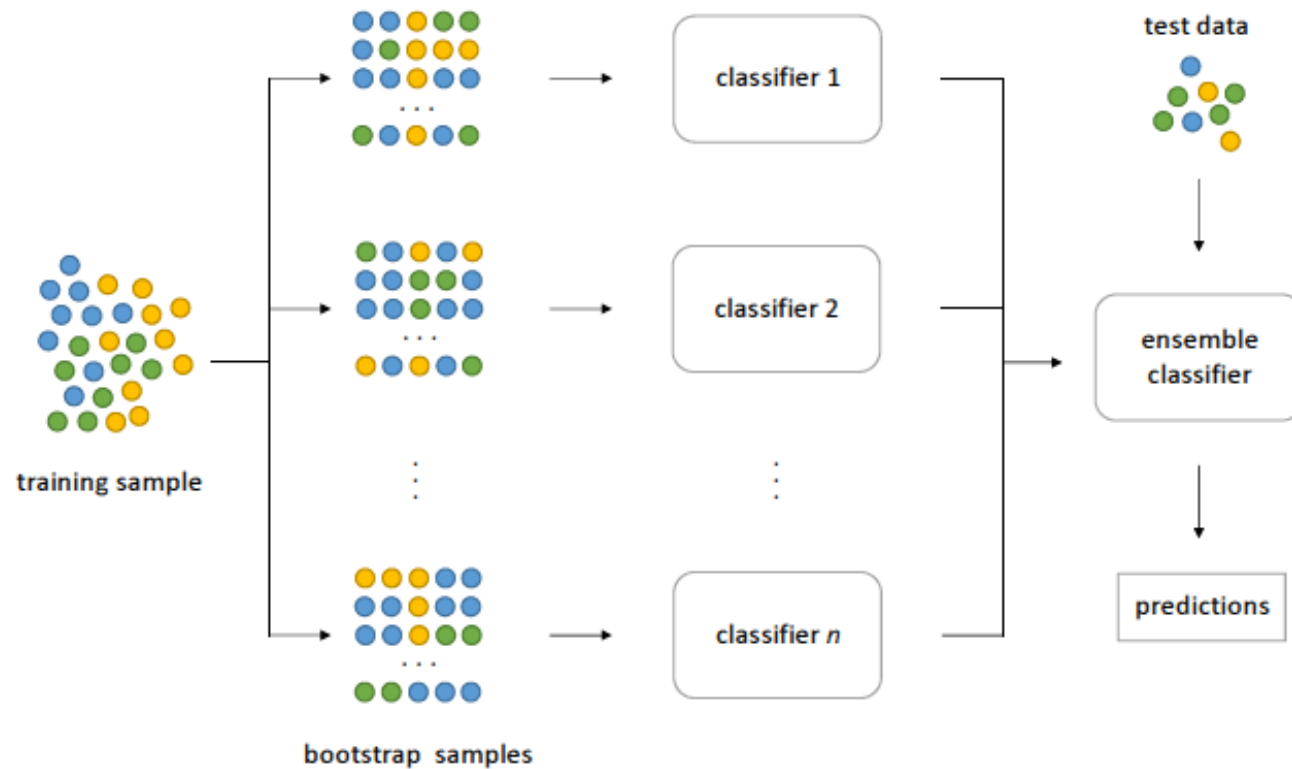




# Boosting

# Bagging: Bootstrap Aggregating



- Classifiers are built in parallel
- Classifiers are trained on subsamples of the data
- Every classifier has a similar weight towards the final prediction

Figure 5: The bagging approach. Several classifier are trained on bootstrap samples of the training data. Predictions on test data are obtained combining the predictions of the trained classifiers with a majority voting scheme.

# Boosting

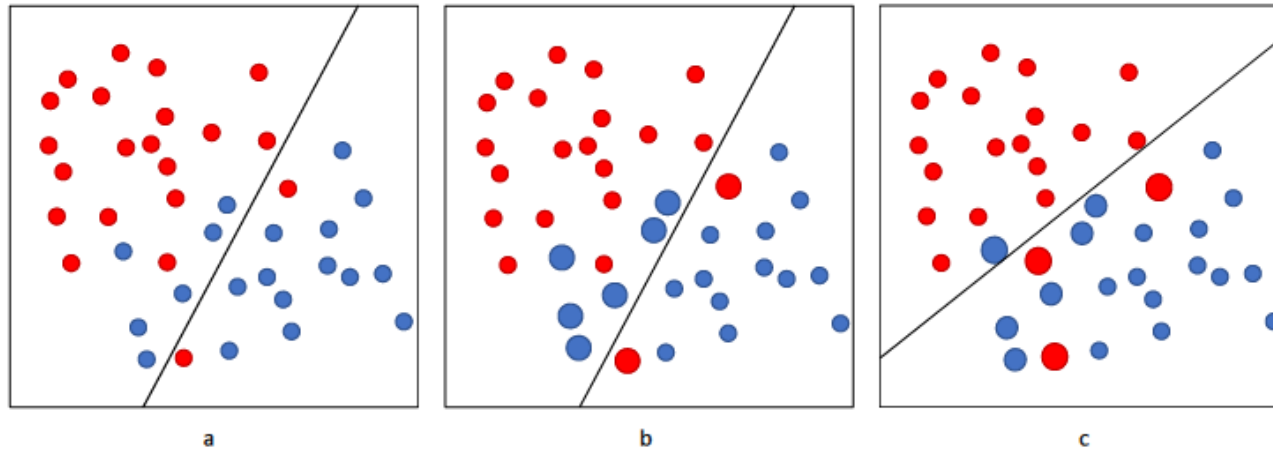


Figure 6: The boosting approach. A classifier is trained on the original data (a). The weights of misclassified instances (dot size in the figure) are increased (b). A new classifier is trained on the new data set and weights are updated accordingly (c).

- Classifiers are built sequentially
- Classifiers are trained on all data
- Observations are given **weights** which reflect how difficult they are to classify.
- Each classifier's prediction has a different **weight** towards final decision, based on their accuracy

Image taken from Data Mining: Accuracy and Error Measures for Classification and Prediction. Galdi and Tagliaferri, 2018

# Boosting

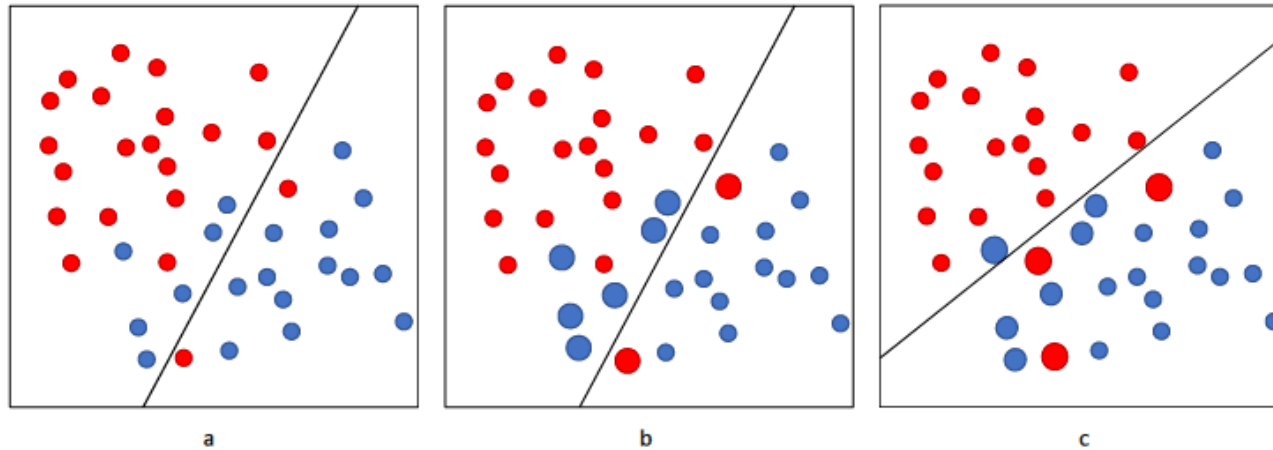
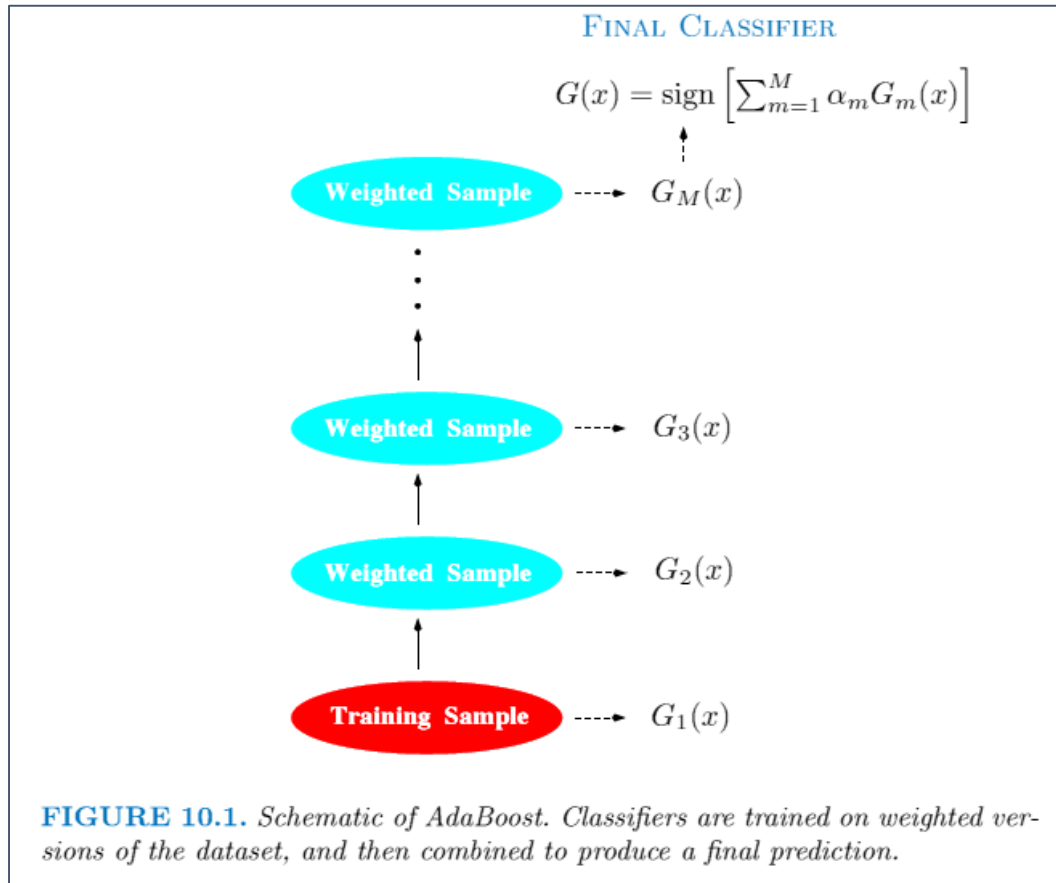


Figure 6: The boosting approach. A classifier is trained on the original data (a). The weights of misclassified instances (dot size in the figure) are increased (b). A new classifier is trained on the new data set and weights are updated accordingly (c).

- First classifier: all observations are given the same weight
- Second classifier: observations miss-classified by previous classifier have a higher weight.
- The weights are adjusted in each iteration, that is for each new classifier
- The classifiers also get a weight based on their accuracy, that weights their overall contribution to the final prediction

Image taken from Data Mining: Accuracy and Error Measures for Classification and Prediction. Galdi and Tagliaferri, 2018

# AdaBoost



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## Algorithm 10.1 *AdaBoost.M1*.

---

1. Initialize the observation weights  $w_i = 1/N$ ,  $i = 1, 2, \dots, N$ .
2. For  $m = 1$  to  $M$ :
  - (a) Fit a classifier  $G_m(x)$  to the training data using weights  $w_i$ .
  - (b) Compute
$$\text{err}_m = \frac{\sum_{i=1}^N w_i I(y_i \neq G_m(x_i))}{\sum_{i=1}^N w_i}.$$
  - (c) Compute  $\alpha_m = \log((1 - \text{err}_m)/\text{err}_m)$ .
  - (d) Set  $w_i \leftarrow w_i \cdot \exp[\alpha_m \cdot I(y_i \neq G_m(x_i))]$ ,  $i = 1, 2, \dots, N$ .
3. Output  $G(x) = \text{sign} \left[ \sum_{m=1}^M \alpha_m G_m(x) \right]$ .

Images taken from Elements of Statistical Learning, Hastie et al

# Gradient Boosting Machines

AdaBoost

$$G(x) = \text{sign} \left( \sum_{m=1}^M \alpha_m G_m(x) \right)$$



Generalized  
additive model

$$f(x) = \sum_{m=1}^M \beta_m b(x; \gamma_m),$$

- $G_m(x)$  is each classifier
- $\alpha_m$  is its weight towards the final outcome

- $b(x, \gamma_m)$  is each classifier
- For trees  $\gamma_m$  refers to the tree splits
- $\beta_m$  is its weight towards the final outcome

# Gradient Boosting Machines

Generalized  
additive model  $f(x) = \sum_{m=1}^M \beta_m b(x; \gamma_m),$

---

**Algorithm 10.2** *Forward Stagewise Additive Modeling.*

---

1. Initialize  $f_0(x) = 0$ .

2. For  $m = 1$  to  $M$ :

(a) Compute

$$(\beta_m, \gamma_m) = \arg \min_{\beta, \gamma} \sum_{i=1}^N L(y_i, f_{m-1}(x_i) + \beta b(x_i; \gamma)).$$

(b) Set  $f_m(x) = f_{m-1}(x) + \beta_m b(x; \gamma_m)$ .

---

# Gradient Boosting Machines

Generalized  
additive model  $f(x) = \sum_{m=1}^M \beta_m b(x; \gamma_m),$

---

**Algorithm 10.2** *Forward Stagewise Additive Modeling.*

---

1. Initialize  $f_0(x) = 0$ .

2. For  $m = 1$  to  $M$ :

(a) Compute

$$(\beta_m, \gamma_m) = \arg \min_{\beta, \gamma} \sum_{i=1}^N L(y_i, f_{m-1}(x_i) + \beta b(x_i; \gamma)). \Rightarrow = \overbrace{(y_i - f_{m-1}(x_i) - \beta b(x_i; \gamma))^2}^{\text{Residuals of previous classifier}} \\ = (r_{im} - \beta b(x_i; \gamma))^2,$$

(b) Set  $f_m(x) = f_{m-1}(x) + \beta_m b(x; \gamma_m)$ .

---

- At each iteration, that is, each new classifier, minimizes the difference between its predictions and the residuals of the previous classifier.



# THANK YOU

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