

Model output and classification

Class 0	Class 1	Class 2
0.8	0.15	0.05
0.2	0.3	0.5
0.2	0.6	0.2
0.1	0.8	0.1

The models ouput an array with probabilities for each class.



Model output and classification

Class 0	Class 1	Class 2	Pred
0.8	0.15	0.05	0
0.2	0.3	0.5	2
0.2	0.6	0.2	1
0.1	0.8	0.1	1

The prediction is the class with the highest probability



Confusion Matrix

Predicted

	0	1	2	3
0	Correct	Incorrect	Incorrect	Incorrect
1	Incorrect	Correct	Incorrect	Incorrect
2	Incorrect	Incorrect	Correct	Incorrect
3	Incorrect	Incorrect	Incorrect	Correct

- In the diagonal: correctly classified observations
- Sum of diagonal: # of correctly classified observations
- Outside diagonal: incorrectly classified observations
- Sum of matrix: total # of observations
- We can't speal of positive and negative class any more.
- Now we talk about classes, referencing each class.
- One or more classes can be the minority class or classes.



Accuracy in multiclass

Predicted

	0	1	2	3
0	5	1	1	1
1	0	4	1	2
2	0	1	2	0
3	1	0	0	1

$$Accuracy = \frac{Number\ of\ correct\ predictions}{Total\ number\ of\ predictions}$$

- Correctly classified = 12
- > Total observations = 20
- \triangleright Accuracy = 12 / 20 * 100 = 60%



Predicted

Real / Actual

	0	1	2	3
0	5	1	1	1
1	0	4	1	2
2	0	1	2	0
3	1	0	0	1

True Positive Rate (Recall or Sensitivity)

✓ TP rate = TP /
$$(TP + FN)$$

Positive Predictive Value (Precision)

$$\checkmark$$
 PP value = TP / (TP + FP)



True Positive Rate (Recall or Sensitivity)

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 TP rate = TP / (TP + FN)

Positive Predictive Value (Precision)

Predicted

	0	1	2	3
0	5	1	1	1
1	0	4	1	2
2	0	1	2	0
3	1	0	0	1

Recall: from the total class, how many correctly classified?

Class
$$0 = 5 / (5 + 1 + 1 + 1) = 5 / 8 = 0.625$$

Class
$$1 = 4 / (4 + 1 + 2) = 4 / 7 = 0.571$$

Class
$$2 = 2 / (2 + 1) = 2 / 3 = 0.667$$

Class
$$3 = 1 / (1 + 1) = 1 / 2 = 0.5$$



True Positive Rate (Recall or Sensitivity)

Positive Predictive Value (Precision)

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	0	1	2	3
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Class
$$3 = 1 / (1 + 1) = 1 / 2 = 0.5$$

Class
$$0 = 5 / (5 + 1) = 5 / 6 = 0.833$$

Class
$$1 = 4 / (4 + 1 + 1) = 4 / 6 = 0.667$$

Class
$$2 = 2 / (2 + 1 + 1) = 2 / 4 = 0.5$$

Class
$$3 = 1 / (1 + 2 + 1) = 1 / 4 = 0.25$$

Precision: from the total predicted class, how many were true?



True Positive Rate (Recall or Sensitivity)

✓ TP rate = TP /
$$(TP + FN)$$

Positive Predictive Value (Precision)

Predicted

	0	1	2	3
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$$3 = 1 / (1 + 2 + 1) = 1 / 4 = 0.25$$

How do we make sense of all these values?

Precision: from the total predicted class, how many were true?

Macro: take the average

Predicted

Real / Actual

	0	1	2	3
0	5	1	1	1
1	0	4	1	2
2	0	1	2	0
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Class
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Mean Recall = **0.59**

Class
$$0 = 5 / (5 + 1) = 5 / 6 = 0.833$$

Class
$$1 = 4 / (4 + 1 + 1) = 4 / 6 = 0.667$$

Class
$$2 = 2 / (2 + 1 + 1) = 2 / 4 = 0.5$$

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Mean Recall = 0.59

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Class
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Class
$$3 = 1 / (1 + 2 + 1) = 1 / 4 = 0.25$$



Mean Precision = **0.563**



Weight the average

Take the mean of each metric weighted by the support

Predicted

		0	1	2	3
	0	5	1	1	1
7	1	0	4	1	2
5	2	0	1	2	0
שמט	3	1	0	0	1

Recall	Support	
Class 0 = 0.625	8	
Class 1 = 0.571	7	
Class 2 = 0.667	3	
Class 3 = 0.5	2	

Class
$$0 = 5 / (5 + 1) = 5 / 6 \neq 0.833$$

Class $1 = 4 / (4 + 1 + 1) = 4 / 6 \neq 0.667$
Class $2 = 2 / (2 + 1 + 1) = 2 / 4 \neq 0.5$
Class $3 = 1 / (1 + 2 + 1) = 1 / 4 \neq 0.25$



Weight the average

Take the mean of each metric weighted by the support

Predicted

		0	1	2	3
Real / Actual	0	5	1	1	1
Ac	1	0	4	1	2
<u>_</u>	2	0	1	2	0
Rec	3	1	0	0	1

Recall	Support
Class 0 = 0.625	8
Class 1 = 0.571	7

Class
$$2 = 0.667$$
 3
Class $3 = 0.5$ 2

Weighted Recall =

$$(0.625*8 + 0.571*7 + 0.667*3 + 0.5*2)$$

$$(8 + 7 + 3 + 2) =$$

0.599

Class
$$0 = 5 / (5 + 1) = 5 / 6 = 0.833$$

Class
$$1 = 4 / (4 + 1 + 1) = 4 / 6 \neq 0.667$$

Class
$$2 = 2 / (2 + 1 + 1) = 2 / 4 = 0.5$$

Class
$$3 = 1 / (1 + 2 + 1) = 1 / 4 = 0.25$$



Weighted Precision =

$$(0.833*8 + 0.667*7 + 0.5*3 + 0.25*2)$$

$$(8 + 7 + 3 + 2) =$$

0.665



Micro:

Predicted

	0	1	2	3
0	5	1	1	1
1	0	4	1	2
2	0	1	2	0
3	1	0	0	1

- Micro-averaging uses a 1 vs rest approach
- Considers all TP, TN and FP together



Micro:

Predicted

Real / Actual

	0	1	2	3
0	5	1	1	1
1	0	4	1	2
2	0	1	2	0
3	1	0	0	1

True Positive Rate (Recall or Sensitivity)

Positive Predictive Value (Precision)

• TP =
$$5 + 4 + 2 + 1 = 11$$

•
$$FP = 1 + 1 + 1 + 1 + 1 + 1 + 2 = 8$$

•
$$FN = 1 + 1 + 1 + 1 + 2 + 1 + 1 = 8$$

Recall =
$$11 / (11 + 8) = 0.57$$





THANK YOU

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