

# Functional Bootstrapping

Aka Programmable Bootstrapping (PBS) [AKP25]

- Évaluer des LUT jusqu'à 8-bits en SIMD sur 64k éléments en ~50s (~0.7ms amorti)
- Évaluer Sign LUT multi-précision jusqu'à 32-bits (4 digits 8-bit) en ~191s (~3ms amorti)
- Pas de bench pour des LUT multi-précision quelconques...
  - Apparemment juste à suivre le blueprint de [GBA21]
  - Évaluation de fonctions privées mentionnée mais pas implémentée

# Références

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