

Overpersistence bias in individual income expectations and its aggregate implications

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Edinburgh, 11 December 2016

Motivation

Households make decisions under uncertainty

→ income risk is one of the most important sources of risk

Income expectations important for

- consumption vs savings
- durable vs non-durable consumption

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This paper:

- ① What are typical features of household income expectations?
- ② How do these features affect consumption/savings choices?
Aggregate Implications?

This Paper

1) **household income expectations in micro data:**

- systematic bias: current income predicts expectation error - households overestimate persistence

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2) **effects of household income expectations on consumption choices:**

- partial equilibrium model with durable and non-durable consumption
- allowing for biased income expectations
- overpersistence belief: low income people do not want to borrow even though their borrowing constraint is not binding

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1) household income expectations in micro data:

- systematic bias: current income predicts expectation error - households overestimate persistence

2) effects of household income expectations on consumption choices:

- partial equilibrium model with durable and non-durable consumption
- allowing for biased income expectations
- overpersistence belief: low income people do not want to borrow even though their borrowing constraint is not binding

3) aggregate implications:

- MPC of low income households lower under biased expectations
⇒ fiscal transfers less effective

Data

Michigan Survey of Consumers

Data

Survey characteristics:

- 500 observations each month (micro data since 1987M7)
- content: household characteristics, expectations about unemployment, inflation, interest rates, purchasing conditions and individual income expectations
- mix of repeated cross-section and short panel:
 - short panel dimension: 1/3 re-interviewed after 6 months

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Forecast Errors:

$$\psi_{i,t} = \hat{g}_{i,t+1|t} - g_{i,t+1}$$

where $g_{i,t+1} = Y_{i,t+1}/Y_{i,t}$

Challenge: Time Structure

Data

- aim: compare expectation with realization
- challenge: time structure of expectations vs realizations
 - expectations: expected income growth in **next 12 months**
 - income realization: total household income in last **calendar year**

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 - realization only for households interviewed in 2nd half of year
 - overlap of expectations and realizations not perfect (max 6 / 12 months)

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 - overlap of expectations and realizations not perfect (max 6 / 12 months)
- solution: impute income growth realization (using households with same characteristics but in different month)

Challenge: Time Structure

Data

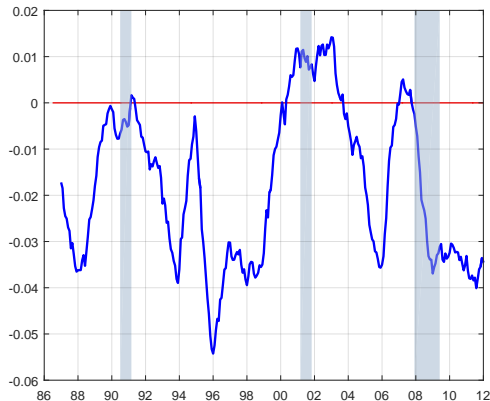
Specifications:

- baseline: realizations imputed, all months
 - advantage:
 - increases overlap
 - maximizes observations
- robustness:
 - July only, directly reported data: no imputation
 - January only, imputed: perfect overlap

Forecast Errors in Real Income Growth

Data

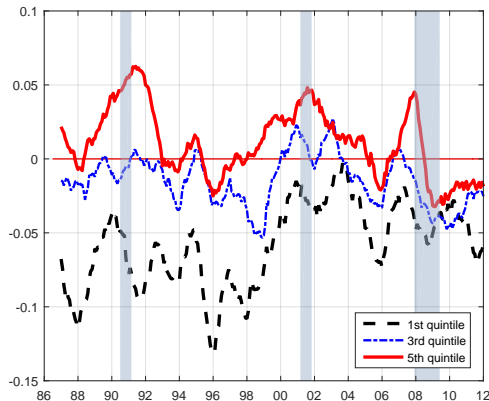
Figure: Mean forecast error



Forecast Errors in Real Income Growth

Data

Figure: Mean forecast error by income



observation:

- low income households too pessimistic
- high income households too optimistic

Forecast Errors on Observables

	(1) real	(2) real	(3) real	(4) nominal	(5) inflation
<u>Income Quintile</u>					
1 (low)	-0.052*** (0.006)	-0.046** (0.018)	-0.075*** (0.021)	-0.049*** (0.007)	0.004*** (0.000)
2	-0.018*** (0.006)	-0.013 (0.017)	-0.038* (0.020)	-0.016*** (0.006)	0.002*** (0.000)
4	0.019*** (0.005)	0.026* (0.013)	0.025 (0.016)	0.018*** (0.005)	-0.002*** (0.000)
5 (high)	0.035*** (0.006)	0.046*** (0.015)	0.067*** (0.017)	0.032*** (0.006)	-0.004*** (0.000)
<u>Education</u>					
no high school	0.014 (0.013)	0.015 (0.029)	0.000 (0.036)	0.019 (0.013)	0.002** (0.001)
college	-0.014*** (0.004)	-0.024** (0.012)	-0.032** (0.013)	-0.017*** (0.004)	-0.003*** (0.000)
<u>Age</u>					
age	-0.004*** (0.001)	-0.003 (0.003)	-0.006 (0.004)	-0.004*** (0.002)	0.000*** (0.000)
age × age	0.000** (0.000)	0.000 (0.000)	0.000 (0.000)	0.000* (0.000)	-0.000*** (0.000)
Sample	MAIN	JAN	JULY	MAIN	INF
Imputation	yes	yes	no	yes	no
Observations	58369	6973	2805	58369	88017

* $p < 0.1$, ** $p < 0.05$, *** $p < 0.01$. Standard errors in parentheses.

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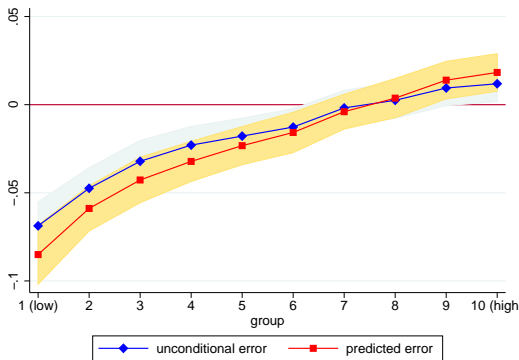
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Forecast Errors in Real Income Growth

Data

Figure: Mean forecast errors by income



→ robust to controlling for household characteristics!

Overpersistence Belief

Data

Assumption

- Individual income Y has transitory (T) and persistent (P) component¹
- Households overestimate persistence in P

Theorem

(a) $\exists! \bar{P}$:

$$E[\log(Y_{it+1}|t) - \log(Y_{it+1}) | P_{it} > \bar{P}] > 0$$

and vice versa for $P_{it} < \bar{P}$

(b) let $\Delta_{it} \equiv P_{it} - \bar{P}$, then

$$\frac{\partial E[\log(Y_{it+1}|t) - \log(Y_{it+1}) | \Delta_{it}]}{\partial \Delta_{it}} > 0$$

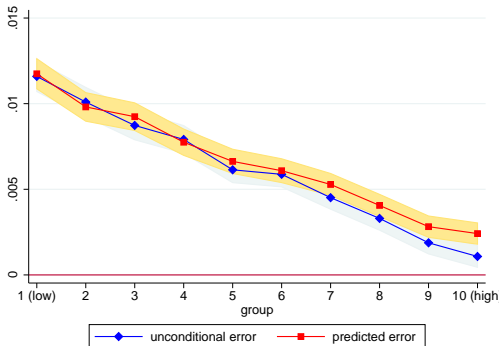
► alternative mechanisms (not consistent with data)

¹ T : lognormal, P : AR(1) in logs with normal innovations

Forecast Errors in Aggregates

Data

Figure: Forecast errors in inflation by income



- people overestimate inflation across the whole income distribution
- similar to unemployment expectations = too pessimistic across whole income distribution

Summary Empirical Findings

Data

① Overpersistence Bias in Income Expectations:

- low income households too pessimistic
- high income households too optimistic

② Aggregate Pessimism:

all income groups too pessimistic about aggregates

Model

- partial equilibrium analysis, infinite horizon
- household obtains utility from two goods:
 - non-durable consumption
 - durable good
- household can invest in two assets:
 - durable good: adjustment costs & depreciation
 - liquid asset: earns risk-free interest
 - borrowing possible at higher interest rate
- only source of risk: exogenous income

Household Optimization Problem

Model

$$\max_{\{c_t\}_{t=0}^{\infty}, \{d_t\}_{t=0}^{\infty}, \{s_t\}_{t=0}^{\infty}} \mathbb{E} \sum_{t=0}^{\infty} \beta^t U(c_t, d_t)$$

$$s.t. \quad c_t + d_t + s_t + A(d_t, d_{t-1}) \leq R(s_{t-1}) + Y_t + (1 - \delta)d_{t-1}$$

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$$U(c, d) = \frac{\left[\left((1 - \theta)c^{\frac{\xi-1}{\xi}} + \theta(\bar{d} + d)^{\frac{\xi-1}{\xi}} \right)^{\frac{\xi}{\xi-1}} \right]^{1-\gamma}}{1 - \gamma}$$

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$$A(d_t, d_{t-1}) = \begin{cases} 0 & \text{if } d_t = (1 - \delta)d_{t-1} \\ F^d(1 - \delta)d_{t-1} & \text{otherwise} \end{cases}$$

Household Optimization Problem

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$$Y_{it} = Z_t \cdot P_{it} \cdot T_{it}$$

- Components to income:
 - aggregate persistent (Z)
 - idiosyncratic persistent (P)
 - transitory (T)

Household Optimization Problem

Model

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$$s.t. \quad c_t + d_t + s_t + A(d_t, d_{t-1}) \leq R(s_{t-1}) + Y_t + (1 - \delta)d_{t-1}$$

$$R(s_t) = [1 + r(s_t)]s_t, \text{ where } r(s_t) = \begin{cases} r^l & \text{if } s_t > 0 \\ r^b & \text{if } -(\kappa_y P_t + \kappa_d d_t) \leq s_t \leq 0 \end{cases}$$

Income process

Model

$$Y_{it} = Z_t \cdot P_{it} \cdot T_{it}$$

Income process

Model

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- transitory shock:

$$T_{it} \sim \log N \left(-\frac{\sigma_T^2}{2}, \sigma_T^2 \right)$$

Income process

Model

$$Y_{it} = Z_t \cdot P_{it} \cdot T_{it}$$

- persistent idiosyncratic shock:

$$\log P_{it} = \rho \log P_{it-1} + \epsilon_{it}^P, \quad \epsilon_{it}^P \sim N(0, \sigma_P^2)$$

Income process

Model

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Overpersistence Bias:

$$\log P_{it} = \hat{\rho} \log P_{it-1} + \epsilon_{it}^P, \quad \epsilon_{it}^P \sim N(0, \sigma_P^2)$$

→ find $\hat{\rho}$ to match the observed forecasting errors

Income process

Model

$$Y_{it} = Z_t \cdot P_{it} \cdot T_{it}$$

- persistent aggregate state:

$$\mathbb{Z} = \begin{bmatrix} Z^h \\ Z^l \end{bmatrix}, \quad \Pi_Z = \begin{bmatrix} \pi_{11} & 1 - \pi_{11} \\ 1 - \pi_{22} & \pi_{22} \end{bmatrix}$$

Income process

Model

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- persistent aggregate state:

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Aggregate Pessimism:

$$\hat{Z}_{t+1} = \mu \mathbb{E} Z_{t+1} = \mu \Pi_Z Z_t.$$

Parameters of the Environment

Calibration

Parameter		Value
<u>technology:</u>		
interest rate (lending)	r^l	0.0016
interest rate (borrowing)	r^b	0.02
loan-to-income constraint	κ_y	0.56
loan-to-value constraint	κ_d	0.6
depreciation rate	δ	0.05
adjustment costs	F^d	0.3
<u>income:</u>		
persistence of idiosyncratic income process	ρ	0.9774
std dev of idiosyncratic persistent shocks	σ_P	0.0424
std dev of idiosyncratic transitory shocks	σ_V	0.1
high aggregate income state	Z^h	1.0040
low aggregate income state	Z^l	0.9790
prob. of entering recession	$1 - \pi_{11}$	6.85%
prob. of leaving recession	$1 - \pi_{22}$	36.04%

Belief and Preference Parameters

Calibration

Parameter		Value
<u>beliefs:</u>		
persistence of P	$\hat{\rho}$	0.9831
pessimism	μ	0.9778
<u>preferences:</u>		
discount factor	β	0.9825
risk aversion	γ	1.5
weight of durable goods in utility	θ	0.075
elasticity of substitution in utility	ξ	3
free durable services	d	0.5

Beliefs about Persistence

Calibration

Overpersistence bias (fitted): $\hat{\rho} = 0.9831$, (true $\rho = 0.9774$)

Aggregate pessimism (fitted): $\mu = 0.9778$

Table: Mean expectation errors in income growth

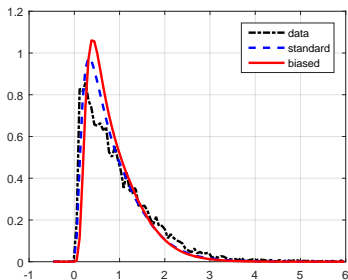
	data	model
income quintile 1	-0.072	-0.068
income quintile 2	-0.037	-0.040
income quintile 3	-0.019	-0.021
income quintile 4	-0.000	-0.004
income quintile 5	0.016	0.020

Note: These depend only on parameters in DGP of income!

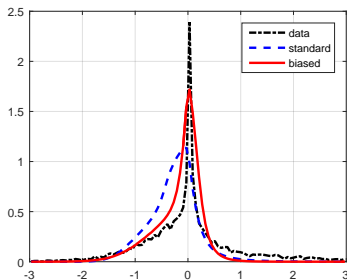
Preferences parameters

Calibration

Pick $\beta, \gamma, \theta, \xi$ and \bar{d} to match the whole distribution of d and s



(a) d , aggregate



(b) s , aggregate

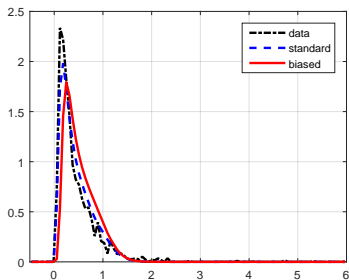
► details

Results

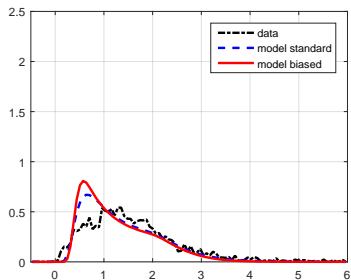
Distribution of durable stock

Results

Figure: Durable stock d by income



(a) first quintile



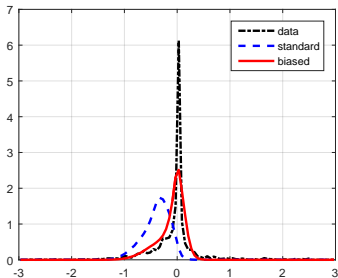
(b) fifth quintile

observation: durables not much affected by bias

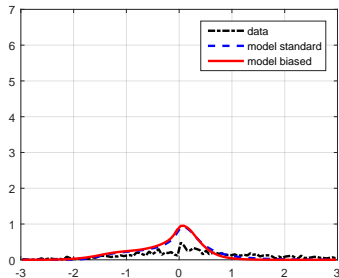
Distribution of liquid savings

Results

Figure: Liquid savings s by income



(a) first quintile



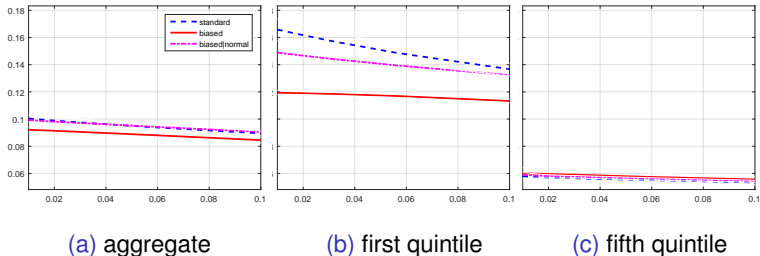
(b) fifth quintile

observation: low income households borrow less
→ do not borrow even though borrowing constraint not binding!

Propensity to Consume

Results

Figure: MPC out of unexpected transfer (non-durable goods)



- observation:
- overall: lower MPC with biased expectations
 - low income: lower MPC with biased expectations

Propensity to Consume

Results

	model		data	
	biased beliefs	rational beliefs	stimulus 2001 ¹	stimulus 2008 ²
MPC low income	0.12	0.16	0.60	0.24
MPC high income	0.06	0.06	0.26	0.21
low/high	1.88	2.61	2.33	1.16

observation: model with rational beliefs overestimates ratio of MPCs
(low to high income)

→ overestimates effectiveness of fiscal stimulus!

¹Johnson, Parker and Souleles (AER 2006)

²Parker, Souleles, Johnson and McClelland (AER 2013)

Summary

1) household income expectation in micro data:

- data: Michigan Survey of Consumers
- findings: current income predicts expectation error
- interpretation: households overestimate persistence of income

2) model of durable and non-durable consumption:

- partial equilibrium model, allowing for overpersistence bias
- overpersistence bias: low income households do not want to borrow even though they could
⇒ allows model to fit low end of liquid asset distribution!

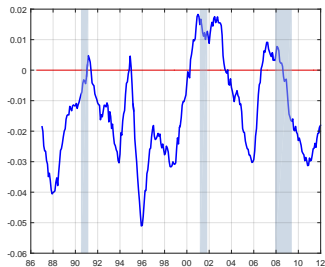
3) aggregate implications:

- MPC smaller for low income households
⇒ model with rational expectations overestimates effectiveness of stimulus

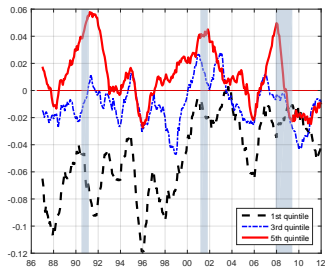
Questions about Income Expectations

- income:
 - Q1a: *During the next 12 months, do you expect your income to be higher or lower than during the past year?*
 - Q1b: *By about what percent do you expect your income to (increase/decrease) during the next 12 months?*
- inflation:
 - Q2a: *During the next 12 months, do you think that prices in general will go up, or go down, or stay where they are now?*
 - Q2b: *By about what percent do you expect prices to go (up/down) on the average, during the next 12 months?*

Forecast Errors in Nominal Income Growth



(a) mean nominal error



(b) nominal error by income

Alternative Mechanisms - not consistent with data

- Learning:

not consistent: forecast errors do not improve with age [▶ graph](#)

- Extrapolation of Recent Past:

not consistent: income expectations do not extrapolate from recent income growth [▶ regression](#)

- Unobservable: Persistent vs Transitory Shocks:

not consistent: cannot generate systematic bias based on past shock realizations (Kalman Filtering (also conditionally) optimal and unbiased)

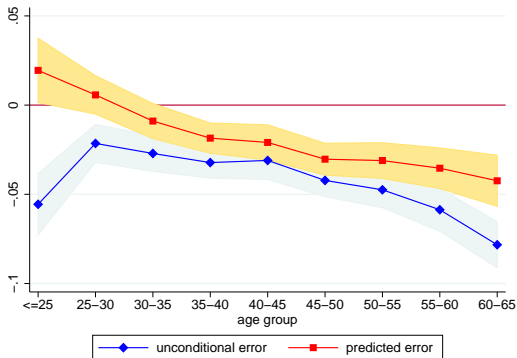
- Systematically Wrong Expectations about Aggregates:

not consistent: across income distribution households too pessimistic about aggregates (inflation and unemployment rate)

[▶ back](#)

Forecast Errors By Age

Figure: Forecast errors by income



observation: forecast errors do not improve with age!

Extrapolation of recent Past?

	(1) exp. growth (real)	(2) exp. growth (real)	(3) exp. growth (nominal)	(4) exp. growth (nominal)
past expectation	0.372*** (0.016)	0.374*** (0.016)	0.373*** (0.016)	0.374*** (0.016)
past realized growth		-0.021*** (0.004)		-0.022*** (0.004)
<u>Income Quintile</u>				
1st	0.004 (0.004)	0.007 (0.004)	0.007 (0.004)	0.009** (0.004)
2nd	0.002 (0.004)	0.003 (0.004)	0.004 (0.004)	0.005 (0.004)
4th	-0.005 (0.004)	-0.006* (0.004)	-0.005 (0.003)	-0.006* (0.003)
5th	-0.008** (0.004)	-0.010** (0.004)	-0.008** (0.004)	-0.010** (0.004)
Constant	0.061*** (0.022)	0.059*** (0.022)	0.070*** (0.022)	0.068*** (0.021)
Observations	15931	15931	17210	17210
R^2	0.185	0.187	0.182	0.184

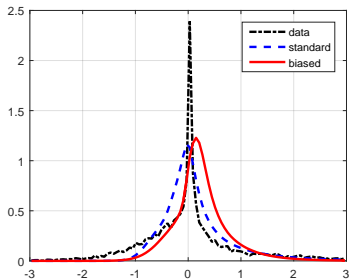
* $p < 0.1$, ** $p < 0.05$, *** $p < 0.01$. Standard errors in parentheses.

observation: households do not extrapolate from recent past!

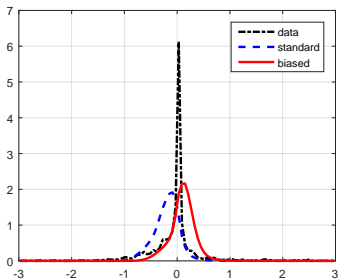
Model Calibrated for Rational Agents

Results

Figure: Liquid savings s by income



(a) aggregate



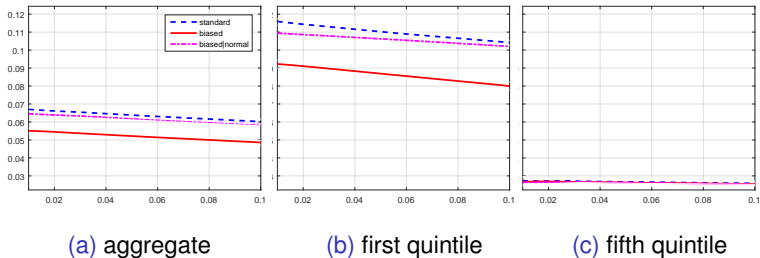
(b) first quintile

observation: results hold for model calibrated for rational expectations!

Propensity to Consume

Results

Figure: MPC out of unexpected transfer (non-durable goods)



observation: results hold for model calibrated for rational expectations!

Preferences parameters

Calibration

5 parameters left: $\Omega = \{\beta, \gamma, \theta, \xi, \bar{d}\}$

$$\Omega = \arg \min \sum_X \left(\sum_i^{\bar{I}_X} |q_i(X) - \tilde{q}_i(X)| \right)$$

Table: Model fit

		quantile							mode
		0.05	0.10	0.25	0.50	0.75	0.80	0.90	
liquid assets	data	-1.29	-0.88	-0.30	0.03	0.76	1.36	5.46	-0.02
	model	-1.04	-0.79	-0.37	-0.05	0.10	0.14	0.25	0.01
durables	data	0.13	0.20	0.39	0.79	1.43	1.62	2.21	0.23
	model	0.24	0.30	0.44	0.72	1.16	1.29	1.65	0.40

Note: Selected moments generated by the model compared to Survey of Consumer Finances.