## Controle - COVID

November 1, 2022

### 1 Modelo 3

$$\frac{dS}{dt} = -\frac{\beta(t)(1 - \psi(t))}{N}SI_T - \tau(t)S$$

$$\frac{dE}{dt} = \frac{\beta(t)(1 - \psi(t))SI_T}{N} - \kappa E$$

$$\frac{dV}{dt} = \tau(t)S - \phi V$$

$$\frac{dS_V}{dt} = \phi(1 - \epsilon)V - \frac{\beta_V(t)(1 - \psi(t))S_VI_T}{N}$$

$$\frac{dE_V}{dt} = \frac{\beta_V(t)(1 - \psi(t))S_VI_T}{N} - \kappa_V E_V$$

$$\frac{dI_A}{dt} = (1 - p)\kappa E - \gamma_A I_A$$

$$\frac{dI_V}{dt} = p\kappa E - \gamma_S I_S$$

$$\frac{dI_VA}{dt} = (1 - p_V)\kappa_V E_V - \gamma_V A I_V A$$

$$\frac{dI_VS}{dt} = p_V \kappa_V E_V - \gamma_V S I_V S$$

$$\frac{dH}{dt} = h\xi \gamma_S I_S + (1 - \mu_U + \omega_U \mu_U) \gamma_U U - \gamma_H H$$

$$\frac{dU}{dt} = h(1 - \xi)\gamma_S I_S + \omega_H \gamma_H H - \gamma_U U$$

$$\frac{dU_V}{dt} = h_V(1 - \xi_V)\gamma_V S I_V S + \omega_H \gamma_V H_V - \gamma_U U_V$$

$$\frac{dH_V}{dt} = h_V \xi_V \gamma_V S I_V S + (1 - \mu_V U + \omega_U \mu_V U) \gamma_V U U_V - \gamma_V H_V$$

$$\frac{dH_V}{dt} = \gamma_A I_A + (1 - h)\gamma_S I_S + (1 - \mu_H) (1 - \omega_H) \gamma_H H$$

$$\frac{dR_V}{dt} = \gamma_V A I_V A + (1 - h_V)\gamma_V S I_V S + (1 - \mu_V H_V) (1 - \omega_H) (\gamma_V H_V) + \phi \epsilon V$$

$$\frac{dD}{dt} = (1 - \omega_H) (\mu_H \gamma_H H + \mu_V H \gamma_V H_V) + (1 - \omega_U) (\mu_U \gamma_U U + \mu_V U \gamma_V U U_V)$$

$$I_T = I_S + \delta I_A + \delta_{VA} I_{VA} + \delta_{VS} I_{VS}$$

Versao do modelo 3 com compartimentos que envovle vacina em vermelho

$$\frac{dS}{dt} = -\frac{\beta(t)}{N}SI_T - \tau(t)S$$

$$\frac{dE}{dt} = \frac{\beta(t)SI_T}{N} - \kappa E$$

$$\frac{dV}{dt} = \tau(t)S - \phi V$$

$$\frac{dS_V}{dt} = \phi(1 - \epsilon)V - \frac{\beta_V(t)(1 - \psi(t))S_VI_T}{N}$$

$$\frac{dE_V}{dt} = \frac{\beta_V(t)(1 - \psi(t))S_VI_T}{N} - \kappa_V E_V$$

$$\frac{dI_A}{dt} = (1 - p)\kappa E - \gamma_A I_A$$

$$\frac{dI_S}{dt} = p\kappa E - \gamma_S I_S$$

$$\frac{dI_{VA}}{dt} = (1 - p_V) \kappa_V E_V - \gamma_{VA} I_{VA}$$

$$\frac{dI_{VS}}{dt} = p_V \kappa_V E_V - \gamma_{VS} I_{VS}$$

$$\frac{dH}{dt} = h\xi \gamma_S I_S + (1 - \mu_U + \omega_U \mu_U) \gamma_U U - \gamma_H H$$

$$\frac{dU}{dt} = h(1 - \xi) \gamma_S I_S + \omega_H \gamma_H H - \gamma_U U$$

$$\frac{dU_V}{dt} = h_V (1 - \xi_V) \gamma_{VS} I_{VS} + \omega_H \gamma_V H H_V - \gamma_U U_V$$

$$\frac{dH_V}{dt} = h_V \xi_V \gamma_V S I_{VS} + (1 - \mu_V U + \omega_U \mu_V U) \gamma_V U U_V - \gamma_{VH} H_V$$

$$\frac{dR}{dt} = \gamma_A I_A + (1 - h) \gamma_S I_S + (1 - \mu_H) (1 - \omega_H) \gamma_H H$$

$$\frac{dR_V}{dt} = \gamma_{VA} I_{VA} + (1 - h_V) \gamma_{VS} I_{VS} + (1 - \mu_{VH}) (1 - \omega_H) (\gamma_{VH} H_V) + \phi \epsilon V$$

$$\frac{dD}{dt} = (1 - \omega_H) (\mu_H \gamma_H H + \mu_V H \gamma_V H H_V) + (1 - \omega_U) (\mu_U \gamma_U U + \mu_V U \gamma_V U U_V)$$

$$I_T = I_S + \delta I_A + \delta_{VA} I_{VA} + \delta_{VS} I_{VS}$$

#### 2 Modelo 2

$$\frac{dS}{dt} = -\frac{\beta(t)(1 - \psi(t))}{N}SI_T - \tau(t)S.$$

$$\frac{dE}{dt} = \frac{\beta(t)(1 - \psi(t))SI_T}{N} - \kappa E$$

$$\frac{dV}{dt} = \tau(t)S - \gamma_S S_V - \gamma_R R_V$$

$$\frac{dS_V}{dt} = \tau(t)(1 - \epsilon)S + \gamma_V S_V - \frac{\beta_V(t)(1 - \psi(t))S_V I_T}{N}$$

$$\frac{dE_V}{dt} = \frac{\beta_V(t)(1 - \psi(t))S_V I_T}{N} - \kappa_V E_V$$

$$\frac{dI_A}{dt} = (1 - p)\kappa E - \gamma_A I_A$$

$$\frac{dI_S}{dt} = p\kappa E - \gamma_S I_S$$

$$\frac{dI_{VA}}{dt} = (1 - p_V) \kappa_V E_V - \gamma_{VA} I_{VA}$$

$$\frac{dI_{VS}}{dt} = p_V \kappa_V E_V - \gamma_{VS} I_{VS}$$

$$\frac{dH}{dt} = h\xi \gamma_S I_S + (1 - \mu_U + \omega_U \mu_U) \gamma_U U - \gamma_H H$$

$$\frac{dU}{dt} = h(1 - \xi)\gamma_S I_S + \omega_H \gamma_H H - \gamma_U U$$

$$\frac{dU_V}{dt} = h_V (1 - \xi_V) \gamma_{VS} I_{VS} + \omega_H \gamma_{VH} H_V - \gamma_U U_V$$

$$\frac{dH_V}{dt} = h_V \xi_V \gamma_{VS} I_{VS} + (1 - \mu_V U + \omega_U \mu_V U) \gamma_{VU} U - \gamma_{VH} H_V$$

$$\frac{dR}{dt} = \gamma_A I_A + (1 - h)\gamma_S I_S + (1 - \mu_H) (1 - \omega_H) \gamma_H H$$

$$\frac{dR_V}{dt} = \gamma_R V + \gamma_{VA} I_{VA} + (1 - h_V) \gamma_{VS} I_{VS} + (1 - \mu_{VH}) (1 - \omega_H) (\gamma_{VH} H_V) + \tau(t) \epsilon S$$

$$\frac{dD}{dt} = (1 - \omega_H) (\mu_H \gamma_H H + \mu_{VH} \gamma_{VH} H_V) + (1 - \omega_U) (\mu_U \gamma_U U + \mu_{VU} \gamma_{VU} U_V)$$

$$I_T = I_S + \delta I_A + \delta_V A I_{VA} + \delta_V S I_{VS}$$

# Parameters - using data until september 2020 before vaccination in Bahia

| Variable      | Description  | Interval          | value              | condition                   |
|---------------|--|-------------------|--------------------|-----------------------------|
| N             | population   | -                 | 14,873,064 (fixed) |                             |
| β             | transmission rate of non-vaccinated individuals                  | $\beta_1 [0, 2]$  | 0.96 (estimated)   |                             |
| $\beta_V$     | transmission rate of vaccinated individuals.                     | $\beta_{V1}[0,1]$ | 0.48 (estimated)   | $\beta_V = 0.5\beta$        |
| $\tau$        | vaccination rate.  |                   | 1/10000 (unit??)   | average rate                |
| δ             | mild symptoms infectivity factor for non-vaccinated cases        | [0, 0.75]         | 0.31 (estimated)   | $(\delta < 1)$              |
| $\delta_{VA}$ | mild symptoms infectivity factor for vaccinated cases            | [0, 0.75]         | 0.31 (fixed)       | $\delta \geq \delta_{VA}$   |
| $\delta_{VS}$ | reduced infectivity factor due to vaccination                    | [0, 0.75]         | 0.31 (fixed)       | $\delta_{VS} > \delta_{VA}$ |
| $\phi$        | inverse time for immunity  | [0.05, 0.1]       | 0.07 (fixed)       | average time for immunity   |
| $\epsilon$    | vaccine efficacy   | [0.5, 0.9]        | 0.7 (fixed)        | average efficacy            |
| $\kappa$      | inverse of exposed period for non vaccinated susceptible         | [1/6, 1/3]        | 1/4 (fixed)        |                             |
| $\kappa_V$    | inverse of exposed period for vaccinated susceptible.            | [1/5, 1/2]        | 1/3 (fixed)        | $\kappa_V > \kappa$         |
| p             | proportion of non-vaccinated latent to symptomatic cases.        | [0.13, 0.5]       | 0.2  (fixed)       |                             |
| $p_v$         | proportion of vaccinated latent to symptomatic cases.            | [0.065, 0.25]     | 0.1 (fixed)        | $p_V < p$                   |
| $\gamma_A$    | mean infected period for non vaccinated assymptomatic cases.     | [1/3.7, 1/3.24]   | 1/3.5 (fixed)      |                             |
| $\gamma_S$    | mean infected period for non vaccinated symptomatic cases.       | [1/5,1/3]         | 1/4 (fixed)        |                             |
| $\gamma_{VA}$ | mean infected period for vaccinated assymptomatic cases.         | [1/3.7 1/3.24]    | 1/3.5 (fixed)      | $\gamma_{VA} \ge \gamma_A$  |
| $\gamma_{VS}$ | mean infected period for vaccinated symptomatic cases.           | [1/5,1/3]         | 1/4 (fixed)        | $\gamma_{VS} \ge \gamma_S$  |
| h             | proportion of hospitalized symptomatic non-vaccinated cases.     | [0.05, 0.25]      | 0.06 (estimated)   |                             |
| $h_V$         | proportion of hospitalized symptomatic vaccinated cases.         | [0,0.05]          | 0.012 (fixed)      | $h >> h_V$                  |
| $(1 - \xi)$   | proportion of symptomatic non-vaccinated cases who need ICU.     | [0.01, 0.5]       | 0.47 (fixed)       |                             |
| $(1-\xi_V)$   | proportion of vaccinated cases who needs ICU                     | [0,0.1]           | 0.1 (fixed)        | $\xi_V >> \xi$              |
| $\gamma_H$    | mean (clinical) hospitalization period for non-vaccinated cases. | [1/12,1/4]        | 0.18 (fixed)       |                             |
| $\gamma_{VH}$ | mean (clinical) hospitalization period for vaccinated cases.     | [1/6,1/2]         | 0.36 (fixed)       | $\gamma_{VH} > \gamma_{H}$  |
| $\gamma_U$    | inverse of mean ICU bed for non-vaccinated cases.                | [1/12, 1/3]       | 0.13 (fixed)       |                             |
| $\gamma_{VU}$ | inverse of mean ICU bed for vaccinated cases.                    | [1/6, 1/2]        | 0.26 (fixed)       | $\gamma_{VU} > \gamma_{U}$  |
| $\omega_H$    | proportion of hospitalized cases that goes to ICU.               | [0.1,0.3]         | 0.14 (fixed)       |                             |
| $\omega_U$    | proportion of ICU cases that goes back to hospitalization        | [0.1, 0.3]        | 0.29 (fixed)       |                             |
| $\mu_H$       | death rate of non-vaccinated hospitalized cases.                 | [0.1,0.2]         | 0.15 (fixed)       |                             |
| $\mu_U$       | death rate of ICU non-vaccinated hospitalized cases.             | [0.4, 0.5]        | 0.4 (fixed)        |                             |
| $\mu_{VH}$    | death rate of vaccinated (clinical) hospitalized cases.          | [0.02, 0.04]      | 0.03 (fixed)       | $\mu_{VH} \approx \mu_H/5$  |
| $\mu_{VU}$    | death rate of vaccinated ICU hospitalized cases.                 | [0.08, 0.1]       | 0.08 (fixed)       | $\mu_{VU} \approx \mu_U/5$  |

#### 4 Modelo 1

$$\begin{split} \frac{dS}{dt} &= -\frac{\beta(t)(1-\psi(t))}{N}SI_T - \tau(t)S. \\ \frac{dE}{dt} &= \frac{\beta(t)(1-\psi(t))SI_T}{N} - \kappa E \\ \frac{dS_V}{dt} &= \tau(t)S - \frac{\beta_V(t)(1-\psi(t))S_VI_T}{N} - \phi \epsilon S_V \\ \frac{dE_V}{dt} &= \frac{\beta_V(t)(1-\psi(t))S_VI_T}{N} - \kappa_V E_V \\ \frac{dI_A}{dt} &= (1-p)\kappa E - \gamma_A I_A \\ \frac{dI_S}{dt} &= p\kappa E - \gamma_S I_S \\ \frac{dI_{VA}}{dt} &= (1-p_V)\kappa_V E_V - \gamma_{VA} I_{VA} \\ \frac{dI_{VS}}{dt} &= p_V \kappa_V E_V - \gamma_{VS} I_{VS} \\ \frac{dH}{dt} &= h\xi \gamma_S I_S + (1-\mu_U + \omega_U \mu_U) \gamma_U U - \gamma_H H \\ \frac{dU}{dt} &= h(1-\xi)\gamma_S I_S + \omega_H \gamma_H H - \gamma_U U \\ \frac{dU_V}{dt} &= h_V(1-\xi_V)\gamma_{VS} I_{VS} + \omega_H \gamma_{VH} H_V - \gamma_U U_V \\ \frac{dH_V}{dt} &= h_V \xi_V \gamma_{VS} I_{VS} + (1-\mu_{VU} + \omega_U \mu_{VU}) \gamma_{VU} U_V - \gamma_{VH} H_V \\ \frac{dR}{dt} &= \gamma_A I_A + (1-h)\gamma_S I_S + (1-\mu_H)(1-\omega_H) \gamma_H H \\ \frac{dR_V}{dt} &= \gamma_{VA} I_{VA} + (1-h_V)\gamma_{VS} I_{VS} + (1-\mu_{VH})(1-\omega_H) (\gamma_{VH} H_V) + \phi \epsilon S_V \\ \frac{dD}{dt} &= (1-\omega_H) (\mu_H \gamma_H H + \mu_{VH} \gamma_{VH} H_V) + (1-\omega_U) (\mu_U \gamma_U U + \mu_{VU} \gamma_{VU} U_V) \\ I_T &= I_S + \delta I_A + \delta_{VA} I_{VA} + \delta_{VS} I_{VS} \end{split}$$

| Variable        | Description  | Interval           | value              | condition                   |
|-----------------|--|--------------------|--------------------|-----------------------------|
| N               | population   | -                  | 14,873,064 (fixed) |                             |
| β               | transmission rate of non-vaccinated individuals                  | $\beta_1 \ [0, 2]$ | 0.96 (estimated)   |                             |
| $\dot{\beta}_V$ | transmission rate of vaccinated individuals.                     | $\beta_{V1}[0,1]$  | 0.48 (estimated)   | $\beta_V < \beta$           |
| $\tau$          | vaccination rate.  | , , , , ,          | 1/10000 (unit??)   |                             |
| δ               | mild symptoms infectivity factor for non-vaccinated cases        | [0, 0.75]          | 0.31 (estimated)   | $\delta < 1$                |
| $\delta_{VA}$   | mild symptoms infectivity factor for vaccinated cases            | [0, 0.75]          | 0.31 (fixed)       | $\delta \geq \delta_{VA}$   |
| $\delta_{VS}$   | reduced infectivity factor due to vaccination                    | [0, 0.75]          | 0.31 (fixed)       | $\delta_{VS} > \delta_{VA}$ |
| $\phi$          | inverse time for immunity  | [0.05, 0.1]        | 0.07 (fixed)       | average time for immunity   |
| $t_0$           | average time for vaccine effect                                  | [12, 18]           | 15 (fixed)         |                             |
| $\epsilon$      | vaccine efficacy   | [0.5, 0.9]         | 0.7 (fixed)        |                             |
| $\kappa$        | inverse of exposed period for non vaccinated susceptible         | [1/6, 1/3]         | 1/4 (fixed)        |                             |
| $\kappa_V$      | inverse of exposed period for vaccinated susceptible.            | [1/5, 1/2]         | 1/3 (fixed)        | $\kappa_V > \kappa$         |
| p               | proportion of non-vaccinated latent to symptomatic cases.        | [0.13, 0.5]        | 0.2 (fixed)        |                             |
| $p_v$           | proportion of vaccinated latent to symptomatic cases.            | [0.065, 0.25]      | 0.1 (fixed)        | $p_V < p$                   |
| $\gamma_A$      | mean infected period for non vaccinated assymptomatic cases.     | [1/3.7, 1/3.24]    | 1/3.5 (fixed)      |                             |
| $\gamma_S$      | mean infected period for non vaccinated symptomatic cases.       | [1/5,1/3]          | 1/4 (fixed)        |                             |
| $\gamma_{VA}$   | mean infected period for vaccinated assymptomatic cases.         | [1/3.7 1/3.24]     | 1/3.5 (fixed)      | $\gamma_{VA} \ge \gamma_A$  |
| $\gamma_{VS}$   | mean infected period for vaccinated symptomatic cases.           | [1/5,1/3]          | 1/4 (fixed)        | $\gamma_{VS} \ge \gamma_S$  |
| h               | proportion of hospitalized symptomatic non-vaccinated cases.     | [0.05, 0.25]       | 0.06 (estimated)   |                             |
| $h_V$           | proportion of hospitalized symptomatic vaccinated cases.         | [0,0.05]           | 0.012  (fixed)     | $h >> h_V$                  |
| $(1 - \xi)$     | proportion of symptomatic non-vaccinated cases who need ICU.     | [0.01, 0.5]        | 0.47  (fixed)      |                             |
| $(1 - \xi_V)$   | proportion of vaccinated cases who needs ICU                     | [0,0.1]            | 0.1  (fixed)       | $\xi_V >> \xi$              |
| $\gamma_H$      | mean (clinical) hospitalization period for non-vaccinated cases. | [1/12,1/4]         | 0.18 (fixed)       |                             |
| $\gamma_{VH}$   | mean (clinical) hospitalization period for vaccinated cases.     | [1/6,1/2]          | 0.36  (fixed)      | $\gamma_{VH} > \gamma_H$    |
| $\gamma_U$      | inverse of mean ICU bed for non-vaccinated cases.                | [1/12, 1/3]        | 0.13 (fixed)       |                             |
| $\gamma_{VU}$   | inverse of mean ICU bed for vaccinated cases.                    | [1/6, 1/2]         | 0.26  (fixed)      | $\gamma_{VU} > \gamma_{U}$  |
| $\omega_H$      | proportion of hospitalized cases that goes to ICU.               | [0.1,0.3]          | 0.14  (fixed)      |                             |
| $\omega_U$      | proportion of ICU cases that goes back to hospitalization        | [0.1, 0.3]         | 0.29 (fixed)       |                             |
| $\mu_H$         | death rate of non-vaccinated hospitalized cases.                 | [0.1, 0.2]         | 0.15  (fixed)      |                             |
| $\mu_U$         | death rate of ICU non-vaccinated hospitalized cases.             | [0.4, 0.5]         | 0.4 (fixed)        |                             |
| $\mu_{VH}$      | death rate of vaccinated (clinical) hospitalized cases.          | [0.02, 0.04]       | 0.03  (fixed)      | $\mu_{VH} < \mu_H$          |
| $\mu_{VU}$      | death rate of vaccinated ICU hospitalized cases.                 | [0.08, 0.1]        | 0.08 (fixed)       | $\mu_{VU} < \mu_{U}$        |