

Assessments of Posterior Orientation Errors after Anterior Cruciate Ligament injuries using deep learning based methods

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Acronyms

ACL Anterior Cruciate Ligament

AI Artificial Intelligence

CNN Convolutional Neural Network

COCO Microsoft Common Objects in Context dataset

CORAL COnsistent RAnk Logits

COTE Collective Of Transformation-based Ensembles

DARK Distribution-Aware coordinate Representation of Key-point

DNN Deep Neural Network

GAP Global Average Pooling

GPU Graphics Processing Unit

Grad-CAM Gradient-weighted Class Activation Mapping

HIVE-COTE Hierarchical Vote Collective of Transformation-based Ensembles

HPE Human Pose Estimation

HRNet High-Resolution Net

POE Postural Orientation Error

ReLU Rectified Linear Unit

SLS Single Leg Squat

SOTA State of the Art

TSC Time Series Classification

UCR University of California, Riverside

XCM Explainable Convolutional Neural Network for Multivariate Time Series Classification

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Chapter 1

Introduction

Among the physically active young to middle aged population injuries to e.g. knee or hip are common. In a study by Thorborg et al. 49% of the questioned sub-elite football players in Denmark reported they had issues with hip and/or groin pain during the previous season [59]. Among serious injuries rupture of the Anterior Cruciate Ligament (ACL) is one of the more severe and common. Moses et al. show annual ACL injury incidence rates of up to 1.62% for amateur athletes [44]. Treatment of such injuries is a debated subject and whether surgery yields better results is difficult to say [32, 43]. Independently of the treatment the patient needs to undergo a long rehabilitation process. Apart from the rehabilitation an injury may also lead to long term physical impairments, such as joint instability [2] and increased risk of knee osteoarthritis (OA) [40], as well as increased risk of depression [14] and re-injury [50].

The ACL can be seen in Figure 1.0.1 and is one of the ligaments connecting the femur (thigh bone) with the tibia (shin bone) and is one of the key structures for providing stability in the knee [17]. Injuries to the ACL commonly occurs without any direct contact from e.g. other athletes. Instead a typical injury mechanism is a sudden change of direction or velocity while the knee bears weight [66].

1.1 Postural Orientation Errors

The ability to uphold the alignment of body segments, both in relation to each other and the surroundings, is called postural orientation [24]. Altered postural orientation, or Postural Orientation Errors (POEs), has been seen to increase the risk of suffering new injuries [23], hence this is an important measure during rehabilitation and before return to sports. 3D motion capture systems are considered to be the "gold standard" for measurement of postural orientation. This is, however, an expensive and time consuming procedure, requiring specific resource in terms of laboratories and experts to perform the measurements. A potential alternative, more suitable for clinical use, is visual assessments of 2D measurements (i.e. videos) [4].

There is not one established method for visual assessments of postural orientation errors,

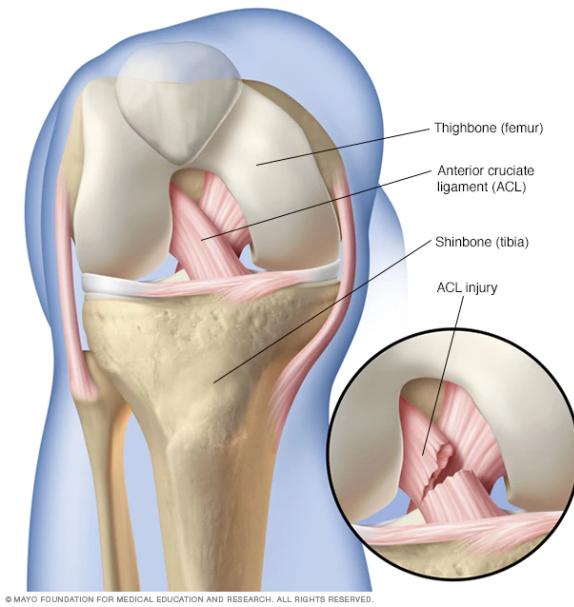


Figure 1.0.1: Illustration of the position of the ACL in the knee. Image from [13].

but Nae et al. presented a test battery where up to six segment specific POEs were assessed for five different functional tasks. Each POE was scored on an ordinal scale from 0 to 2 [45, 46]. A detailed explanation of the POE-task combinations can be found in Appendix A. This scoring system is the foundation of this thesis, but in this work we only study the femoral valgus-, deviation of trunk-, deviation of pelvis-, and knee medial to foot position-POEs for the Single Leg Squat (SLS) task. The criteria for the assessments of the POEs are presented in Table 5.2.1 and the SLS task is described below. When a patient is assessed four-five repetitions are performed, each being scored according to Table 5.2.1. A total segment-specific score is then calculated as the median of these repetitions.

Single-leg squat, SLS

The subject performs a squat standing on one leg to a knee angle of approximately 60° before returning to extension. The exercise was repeated five times and the entire movement was used to assess the POEs [4].

Although visual assessments based on 2D videos are a time and resource efficient way of evaluating POEs compared to 3D motion capture systems it is still a time consuming task. Automating such assessment tasks could allow physiotherapists to spend more time with patients and thereby hopefully improve the life quality after a traumatic injury.

1.2 Related work

A study by the National Board of Health and Welfare in Sweden from 2019 show that the use of Artificial Intelligence (AI) systems in the Swedish healthcare is still fairly limited. At the date of the report such systems were used for 59 applications, of which

Table 1.1.1: Descriptions for the visual assessment of segment specific POEs evaluated in this thesis. Table taken from [4].

Segment-specific POEs	Scoring of 0: Good (no POE)	Scoring of 1: Fair (minor POE)	Scoring of 2: Poor (major POE)
Deviation of trunk in any plane	The absence of a trunk position into forward lean, lateral lean and/or rotation indicates no POE	A slight position of the trunk into forward lean, lateral lean and/or rotation indicates minor POE	A clear position of the trunk into forward lean, lateral lean and/or rotation indicates major POE
Deviation of pelvis in any plane	The absence of pelvis into lateral deviation, pelvic tilt and/or rotation of pelvis respectively indicates no POE	A slight position of the pelvis into lateral deviation, pelvic tilt and/or rotation of pelvis respectively indicates minor POE	A clear position of the pelvis into lateral deviation, pelvic tilt and/or rotation of pelvis respectively indicates major POE
Femoral valgus	The absence of femoral valgus indicates no POE	A slight position of femoral valgus indicates minor POE	A clear position of femoral valgus indicates major POE
Knee Medial-to-Foot Position	Mid-point of patella is in line with or lateral to the second toe	Mid-point of patella is placed medial to the second toe	Mid-point of patella is clearly placed medial to the big toe

27 were based on some machine learning approach. The learning based methods were most commonly used for diagnosis and decision support mainly based on different types of image analysis [56]. Within the research community the situation is different, here machine learning applied in a medical field is very widespread. Again it is big within medical imaging fields such as radiology and ultrasound, but also EKG, anamnesis, and mental health. The introduction of wearable devices and cheaper IoT devices are deemed to be important factors for the digitalization of healthcare [60].

Machine learning has also been used in the field of physiotherapy and rehabilitation. Kianifar et al. estimated joint poses from IMU data using extended Kalman filters. Based on these joint positions they classified the quality of SLS movements using Support Vector Machines, Linear Multinomial Logistic Regression, and Decision Trees [30]. Liao et al. used combinations of Gaussian Mixture Models and Deep Neural Networks (DNNs) to calculate quality scores for movements during rehabilitation based on 3D joint positions captured with a Microsoft Kinect [36].

1.3 Focus of this work

This work should be seen as a proof of concept showing that these kinds of assessments can be automated, allowing physiotherapists to help patients in a more efficient way. Due to limitations in time and labeled data only four POEs for the SLS task was evaluated. After

some initial studies it was decided to use 2D body joint positions, i.e. 3D reconstruction from the videos was not evaluated.

SKRIV LITE MER H'R HOPPAS LAG, TYP OM JAG KOMMER P[NGT VID RESULTAT ELLER NGT...

1.4 Thesis organization

After this first chapter, where the background and rationale for this thesis has been presented, some deep learning background is introduced in Chapter 2. Chapter 3 and 4 presents methods for estimating human body joints and classifying time series, both important for this work. The method developed as part of this thesis is provided in Chapter 5. Finally the results are presented in Chapter 6 and discussed in Chapter 7.

1.5 avgr'nsningar eller typ m]l med detta arbete

typ om att bara SLS analyseras? och lite s[nt.. kanske att 3d inte utv'rderas? eller att det utv'rderades litgrann??

skriv om risker med bias fr dataset osv... kansek ska n'mnas i dl-kapitlet?

Chapter 2

Background - Deep learning

A supervised machine learning problem can be described as finding a mapping between some input and output data, e.g. an image and a category, based on labeled input-output combinations. The idea with such methods is that a mapping found for the available data also should represent unseen data of the same type, i.e. it should generalize. To be able to get a measure of this generalization the available data is commonly divided into two parts, training data and test data. The training data is used to find the mapping and the test data is used to evaluate how well it performs on unseen data [8].

This chapter gives a brief introduction to a special type of machine learning called deep learning, which forms the basis of this work.

FIXAA DEN HAR SECTION INDELNINGEN...

2.1 Deep Neural Networks

DNNs are combinations of linear and non-linear functions trained to approximate some other, potentially very complicated, function. The output of the network is formed as $f(x) = f_n \circ f_{n-1} \circ \dots \circ f_1 \circ f_0(x)$ resulting in the layer terminology since the output from one function is passed as input to the subsequent one [21].

Below the layers used in our work are briefly explained.

Dense layer

The dense, or fully connected, layer is the basic model for a feedforward network. The outputs of such a layer is formed as linear combinations of the inputs and bias terms. Usually a non-linear activation function is applied to this to be able to capture more general behaviors, resulting in the output

$$y_i = h\left(\sum_{j=1}^D w_{ij}x_j + b_i\right). \quad (2.1)$$

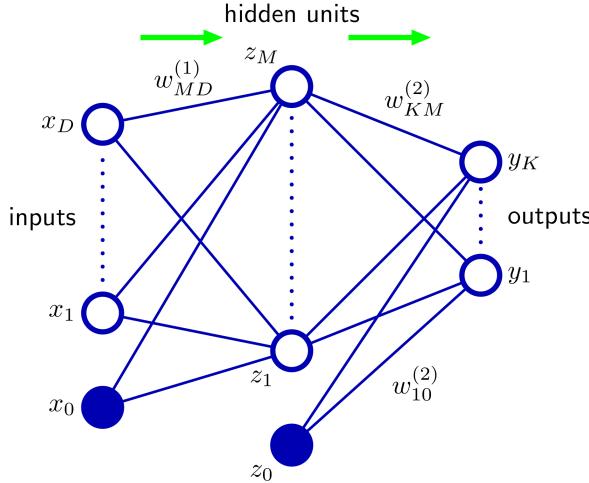


Figure 2.1.1: Feedforward neural network with two densely connected layers. Each line corresponds to one trainable parameter. x_0 and z_0 can be seen as ones added to the inputs introducing the bias terms [8].

$h(\cdot)$ is a, possibly non-linear, activation function. $x_j, j \in \{1, \dots, D\}$ are the inputs to the layer, w_{ij} and b_i are the weights and biases learned during training [8]. A network with two dense layers is shown in Figure 2.1.1.

Convolutional layers

Convolutional layers have proved successful for feature extraction from for instance time series or images. A reason for this is that they are equivariant to translation, meaning that patterns in a time series will be recognized in the same way no matter at which time steps they occur. The 1D convolution operation can be seen in (2.2). When applied to for instance images it is performed in two dimensions.

$$(x * w)(t) = \sum_{a=-\infty}^{\infty} x(a)w(t-a) \quad (2.2)$$

x is the input and w is the kernel or filter which consist of the trainable parameters. As the kernel size is not affected by the input size the convolutional layer can be applied to inputs of different size, which is not possible with for instance the fully connected layer [21].

Pooling layers

Pooling layers are used to reduce the dimensionality of feature maps. Common types of poolings are the max and the average pooling methods. Traditional max pooling represents nearby numbers by its maximum value while average pooling uses their average. This type of max pooling has proved efficient together with convolutional layers for computer vision tasks. Figure 2.1.2 illustrates how the pooling works. It can also be performed globally, i.e. on the entire feature map, which can be a way of handling

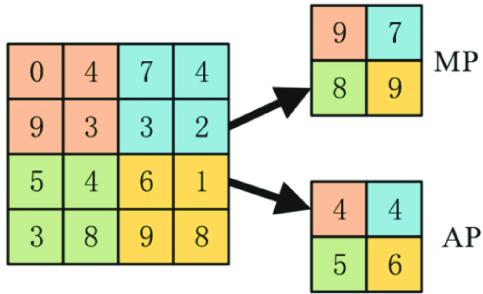


Figure 2.1.2: Illustration of max and average pooling with pooling size 2×2 and stride 2×2 . Image from [63].

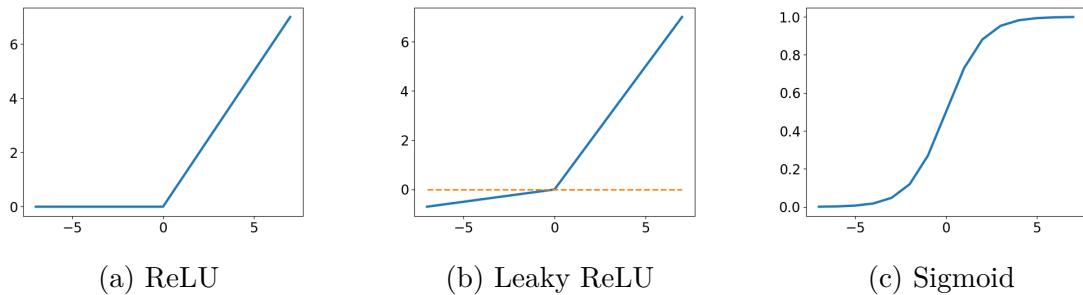


Figure 2.1.3: Different activation functions, note that the slope of leaky ReLU for negative numbers is exaggerated for visualization purposes.

differently sized data. For a Time Series Classification (TSC) problem it is for instance possible to use size agnostic convolutional layers as feature extractors followed by a Global Average Pooling (GAP) layer resulting in a fixed size of the data to be classified [12].

Activation functions

The activation functions in a neural network has two main tasks. The first one is to introduce non-linearity to an otherwise linear model. For a dense layer performed with the function $h(\cdot)$ in (2.1). A common such function is Rectified Linear Unit (ReLU), $h(z) = \max\{0, z\}$. Benefits with ReLU is that it in its active region ($z > 0$) does not have a suppressing effect on the gradient and it is easily computable. A drawback, however, is that the gradient is zero in its inactive region ($z < 0$) meaning gradient based training methods does not work here. An alternative to avoid this issue is the leaky ReLU given by $h(z) = \max\{0.01z, z\}$. ReLU and leaky ReLU are shown in Figure 2.1.3a and 2.1.3b respectively. Activation functions are also used for the output of the network, e.g. to obtain outputs representing probabilities. The sigmoid function, $h(z) = 1/(1+\exp(-z))$, shown in Figure 2.1.3c, can be used for this. The sigmoid function will saturate the output between 0 and 1, however, if the model has several outputs e.g. representing the probabilities of the input belonging to different classes the total probability will not sum to 1. In this case the softmax function, $h(z)_i = \exp(z_i)/\sum_{j=1}^K \exp(z_j)$, can be used instead [21].

Table 2.2.1: Evaluation metrics using quantities in Definition 1.

Precision	$\frac{TP}{TP+FP}$
Recall	$\frac{TP}{TP+FN}$
F1 score	$2 \frac{\text{Precision} \cdot \text{Recall}}{\text{Precision} + \text{Recall}}$
Accuracy	$\frac{TP+TN}{TP+FP+TN+FN}$

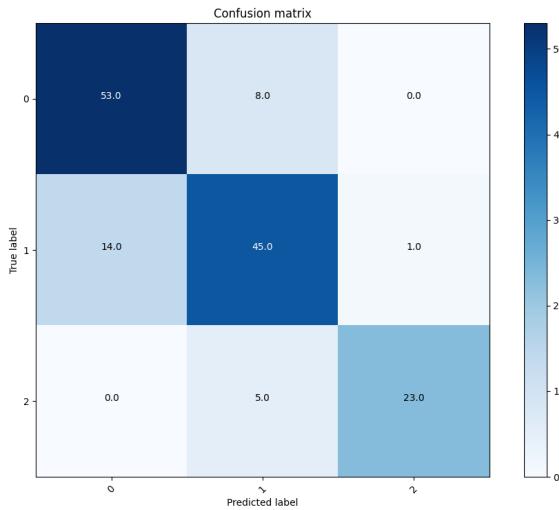


Figure 2.2.1: An example of a confusion matrix. The entries on the diagonal are correctly classified, while the position of an off-diagonal entry shows what kind of error has been made. The true class is given by the row and the predicted class by the column.

2.2 Evaluation metrics

To be able to evaluate and compare models some evaluation metrics are needed. Table 2.2.1 shows four common classification metrics and the way they are calculated from the quantities defined in Definition 1.

FIXA FORMATERING P[DENNA DEFINITON

Definition 1. *True positives, TP: Correctly classified positive samples*

False positives, FP: Incorrectly classified positive samples

True negatives, TN: Correctly classified negative samples

False negatives, FN: Incorrectly classified negative samples

Another way to present the result of a classification task is using the confusion matrix. This is a matrix where the columns corresponds to the predicted classes and the rows to the correct classes. Hence, this metric shows what kind of errors the model performs. An example of a confusion matrix is shown in Figure 2.2.1.

2.3 Training of

During training of a network a loss function, \mathcal{L} , which describes the desired behavior, is evaluated on the training data. To improve the performance of the model its parameters are changed to minimize this loss. In deep learning problems this optimization is usually performed with some gradient descent inspired method, shown in (2.3), where the parameters are updated in the direction which reduces the loss the most. With a large training data set the computation of the gradient quickly becomes expensive. A remedy for this has been to use stochastic or mini-batch gradient descent methods. Such algorithms use one or a few data points from the training set to estimate the gradient for each parameter update. Algorithms common today often use momentum, where previous gradients affect the parameter update direction, and adaptive learning rates (step size of parameter update), allowing different learning rate for different parameters [21]. One example of such a method is the Adam optimizer [31].

$$\mathbf{W}_{k+1} = \mathbf{W}_k - \alpha \mathbf{D} \quad (2.3)$$

where:

\mathbf{W}_k = model parameters at iteration k

α = learning rate or step size

\mathbf{D} = parameter update direction, e.g. $\frac{\partial \mathcal{L}}{\partial \mathbf{W}}$ or a weighted average of earlier gradients

The gradients of the loss with respect to the model parameters are calculated using the back-propagation algorithm [53] which recursively uses the chain rule, (2.4), to propagate the loss gradient through the network.

$$\frac{dz}{dx} = \frac{dz}{dy} \frac{dy}{dx} \quad (2.4)$$

For a network where f_0, f_1, \dots, f_n denotes the outputs of the $n + 1$ layers, with corresponding layer parameters $\mathbf{w}_0, \mathbf{w}_1, \dots, \mathbf{w}_n$ and loss function \mathcal{L} the gradient is calculated by first performing a forward pass of input \mathbf{x} . This allows for computation of the the gradient w.r.t. the output of the final layer, f_n , either analytically or using automatic differentiation. As both the structure and the parameters of the layers are known this can be used to calculate the gradient w.r.t. the parameters in that layer, \mathbf{w}_n , as well as the output of the previous layer, f_{n-1} . By applying (2.5a) recursively the gradient is propagated through the network and from this (2.5b) gives the gradients needed for the optimization.

$$\frac{\partial \mathcal{L}}{\partial f_k} = \frac{\partial \mathcal{L}}{\partial f_{k+1}} \frac{\partial f_{k+1}}{\partial f_k} \quad (2.5a)$$

$$\frac{\partial \mathcal{L}}{\partial \mathbf{w}_k} = \frac{\partial \mathcal{L}}{\partial f_k} \frac{\partial f_k}{\partial \mathbf{w}_k} \quad (2.5b)$$

Loss functions

For a classification problem with K mutually exclusive classes the categorical cross-entropy is commonly used. With this loss the labels are one-hot encoded meaning that each label is represented by K binary variables, i.e. $y_n \in \mathbb{Z}_2^K$. Each variable represents a class and $y_n^{(k)} = 1$ for the k corresponding to the class of the label and 0 otherwise. The final layer of the model has K outputs with softmax activation. The loss to be minimized is shown in (2.6) [8].

$$\mathcal{L}(\mathbf{x}, \mathbf{W}) = - \sum_{n=1}^N \sum_{k=1}^K \lambda^{(k)} y_i^{(k)} \log \hat{y}_n^{(k)}(x_n, \mathbf{W}) \quad (2.6)$$

where: $y_n^{(k)}$ = the correct binary label of class k for data point n in the training set
 $\hat{y}_n^{(k)}$ = the corresponding prediction from the model
 $\lambda^{(k)}$ = weight for class k .

The categorical cross-entropy will aim to maximize the predicted probability for the correct class. However, incorrect probabilities have no direct effect on the loss. To be able to affect what kind of errors the model makes in its predictions a modification of this loss can be used. This modified loss, here referred to as confusion-entropy, introduces a matrix, U , which can be seen as a target confusion matrix distribution. Entries in U rewards predictions at the corresponding positions in the confusion matrix, including possibly incorrect classifications. The confusion-entropy loss is shown in (2.7) [1].

$$\mathcal{L}(\mathbf{x}, \mathbf{W}, U) = - \sum_{i=1}^K \sum_{j=1}^K u_{ij} \log \sum_{n=1}^N y_n^{(i)} \hat{y}_n^{(j)}(x_n, \mathbf{W}). \quad (2.7)$$

2.4 Historical background of deep learning

In 1943 McCulloch and Pitts [41] presented a mathematical model of a neuron which at the time had limited capabilities (e.g. it did not learn), but lay the foundations for much of what today is considered to be deep learning. Ivakhnenko and Lapa [28] introduced what would later be called deep learning with the first multi-layered network in 1965. The first convolutional network was introduced by Fukushima in 1980 [20]. A few years later, in 1989, LeCun et al. [34] showed it possible to train such networks with backpropagation and illustrated their effectiveness for computer vision problems. In 2009 Raina et al. [51] suggested that DNNs could efficiently be trained on Graphics Processing Units (GPUs). Krizhevsky et al. [33] used this when they with AlexNet proved it possible to train deeper networks which also greatly outperformed models of the time at computer vision tasks. Since then deep learning based methods has been adopted in various fields, such as computer vision, natural language processing, and even autonomous vehicles [47].

2.5 Explainability

Much of the recent progress in the deep learning space is inherently incomprehensible for us humans, due to its black-box nature and the size of the models [16]. However, explainability is important at many stages of the development of an AI-system. When the systems performance is at sub-human levels it simplifies for human experts to improve it. When the system achieves similar results human experts it can help enforce trust to the system. Finally, in a scenario where the AI outperforms humans it can help us get a better understanding of the problem [54]. With these methods playing a bigger role in fields such as healthcare the importance of explainable decisions also grows from a legal and ethical perspective [5].

Gradient-weighted Class Activation Mapping (Grad-CAM)

Although most deep learning models are not interpretable there are post-hoc methods which tries to explain decisions. Selvaraju et al. [54] suggested one such method, called Gradient-weighted Class Activation Mapping (Grad-CAM), where an activation map is calculated which shows what parts of the data is important for the decisions. Considering a neural network with convolutional layers as feature extractors followed by GAP and dense layers for classification Grad-CAM is based on the final part of the network. Let y_c be the output corresponding to class c and A be the final feature map of height H , width W , and with F filters. The Grad-CAM activation, M_{GC} , is then calculated as follows:

$$\begin{aligned} w_k^c &= \frac{1}{H \times W} \sum_{i=1}^H \sum_{j=1}^W \frac{\partial y_c}{\partial A_{ij}^k} \\ M_{GC} &= \text{ReLU}\left(\sum_{k=1}^F w_k^c A^k\right) \end{aligned} \tag{2.8}$$

The resulting activation map is importance values $\in \mathbb{R}^{H \times W}$. If the input is a time series this means that by designing the network to not alter the time dimension an importance value is obtained for each time step.

2.6 Consistent Rank Logits (CORAL)

Categorical data with a natural ordering are considered to be ordinal, examples of such data are the response to some medical treatment (e.g. poor, fair, good) [3] or the age of a person [9].

When classifying ordinal data it is desirable to exploit the fact that the categories are ordered [3]. An ordinal classification problem, or ordinal regression as it is also referred to, can be formulated as assigning labels, $y \in \mathcal{Y} = \{\mathcal{C}_0, \mathcal{C}_1, \dots, \mathcal{C}_{K-1}\}$, to inputs \mathbf{x} , where

the classes $\mathcal{C}_0 \prec \mathcal{C}_1 \prec \dots \prec \mathcal{C}_{K-1}$ according to some ordering relation [9].

Li and Lin [35] presented a method for ordinal regression where the combined result of $K - 1$ binary classifiers for K classes were used. Each classifier checked whether the rank of the sample class was larger than rank $r_k \in \{r_1, \dots, r_{K-1}\}$. Niu et al. [49] developed this further using a multi-output Convolutional Neural Network (CNN) as $K - 1$ binary classifiers, called OR-CNN. The classifiers share all weights except the ones in the output layer. This method achieved State of the Art (SOTA) performance on datasets where age was estimated based on facial images. However, consistency was not guaranteed in the predictions, e.g. sometimes simultaneously predicting an age under 20 and over 30. Cao et al. [9] addressed this issue with COnsistent RAnk Logits (CORAL) which is an architecture-agnostic method that can extend any neural network based classifier. Similarly to OR-CNN CORAL uses $K - 1$ binary classifiers, here however sharing all weights parameters apart from the biases in the output layer. Instead of representing the labels as one-hot encodings they are now formed as $K - 1$ binary labels, i.e. $y_n \in \mathbb{Z}_2^{K-1}$, where $y_n^{(k)} = 1$ if the rank of the class is greater than r_k and 0 otherwise. By minimizing the loss function

$$\mathcal{L}(\mathbf{x}, \mathbf{W}, \mathbf{b}) = - \sum_{n=1}^N \sum_{k=1}^{K-1} \lambda^{(k)} [\log(\sigma(g(\mathbf{x}_n, \mathbf{W}) + b_k)) y_n^{(k)} + \log(1 - \sigma(g(\mathbf{x}_n, \mathbf{W}) + b_k)) (1 - y_n^{(k)})], \quad (2.9)$$

where:	\mathbf{W}	= all model parameters except biases of final layer
	\mathbf{b}	= bias weights of final layer
	$\lambda^{(k)}$	= loss weight for class k
	$g(\mathbf{x}_n, \mathbf{W})$	= output of penultimate layer
	$\sigma(z)$	= logistic sigmoid function, $1/(1 + \exp(-z))$
	$\sigma(g(\mathbf{x}_n, \mathbf{W}) + b_k)$	= predicted output of binary classifier k

it can be shown that

$$b_1 \geq b_2 \geq \dots \geq b_{K-1}. \quad (2.10)$$

The proof can be found in [9] and from this and the shared weights it follows that

$$\widehat{P}(y_n > r_1) \geq \widehat{P}(y_n > r_2) \geq \dots \geq \widehat{P}(y_n > r_{K-1}) \quad (2.11)$$

since the only thing that differs between the predictions is the bias. The probabilities for

the individual classes are computed from this as

$$\begin{aligned}\widehat{P}(\mathcal{C}_0) &= 1 - \widehat{P}(y_n > r_1) \\ \widehat{P}(\mathcal{C}_1) &= \widehat{P}(y_n > r_1) - \widehat{P}(y_n > r_2) \\ &\vdots \\ \widehat{P}(\mathcal{C}_{K-1}) &= \widehat{P}(y_n > r_{K-1}).\end{aligned}\tag{2.12}$$

Chapter 3

Related work - Human Pose Estimation

Human Pose Estimation (HPE) is a well explored problem which, like many other computer vision tasks has developed rapidly in the recent years. The reasons behind this progress can mainly be explained by two factors. Firstly the emergence of computing power discussed in Section 2.4, allowing more expressive deep learning models. Secondly several datasets with images labeled with human body joints has been made available [10]. These datasets not only provide data, but also introduces competition in the research community making it possible to compare the results of different approaches.

3.1 Datasets

In this work models trained on the Microsoft Common Objects in Context dataset (COCO) dataset are used. COCO consists of 328k images containing 91 different object types. The images come from Google, Bing, and Flickr image search and are mainly hand annotated through Amazon Mechanical Turk. The interesting part of the dataset for this work is the one with human poses. In total there are 250k instances of people labeled with joint locations [37]. The joints, 17 per person, in the dataset can be seen in Figure 3.1.1a. Along with the datasets containing body keypoints mentioned above there are also datasets with dense keypoints for specific bodyparts, e.g. OneHand10k [64]. COCO-wholebody [29] is an attempt to combine these two types of datasets by extending COCO with dense keypoints at hands, feet, and faces. The resulting 133 joints can be seen in Figure 3.1.1b.

3.2 Background - Human pose estimation

The HPE problem has been explored since long before the most recent deep learning era. Pictoral Structures were introduced by Fishler and Elschlager in the 1970s. This meant identifying individual parts or features in images modeled with pair-wise spring-

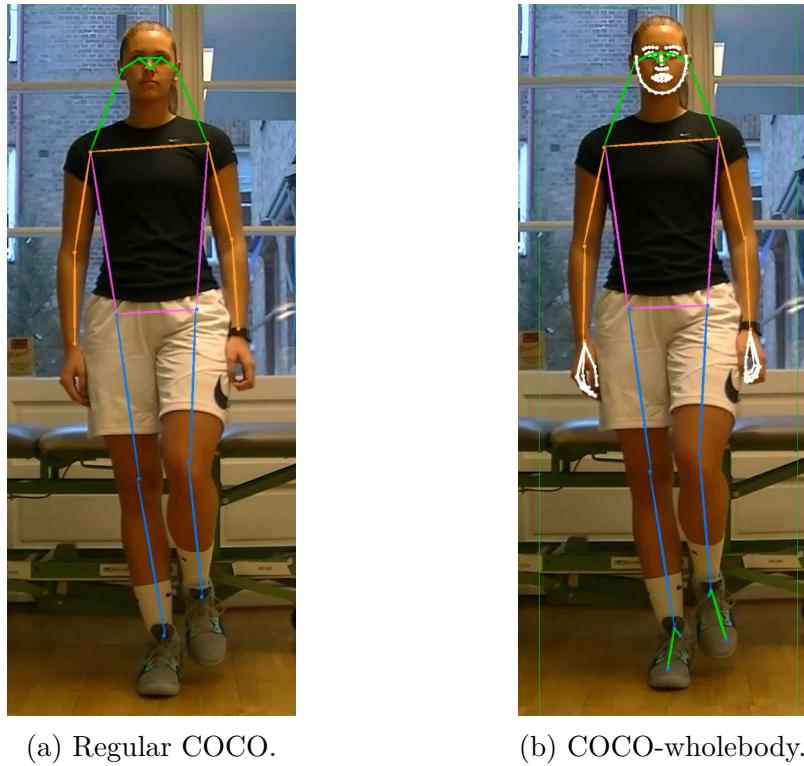


Figure 3.1.1: Keypoints for the two COCO datasets.

like connections [19]. After the progress of deep learning mentioned in Section 2.4 Toshev and Szegedy [61] presented DeepPose, the first HPE method based on DNNs, in 2014. Today’s HPE methods are generally categorized as top-down or bottom-up approaches. This has to do with how they handle multiple persons. Bottom-up models starts by finding all keypoints for all persons in an image and then match them together to form persons. Top-down models on the other hand starts by finding bounding boxes for all individuals and then identifies keypoints for one person at a time. The sequential nature of the top-down methods and the fact that two models are needed means that bottom-up models scale better with the number of persons to analyze. However top-down models tends to be more accurate [11].

3.3 Pose estimation models

Below the HPE models used in our work are presented. As we are interested in single person recognition the model used is of top-down type.

3.3.1 High-Resolution Net (HRNet)

Sun et al. presented the High-Resolution Net (HRNet) [57] architecture in 2019, initially for HPE, but also for other computer vision tasks such as semantic segmentation and object detection. Such problems had traditionally been solved using networks built on high-to-low resolution convolutions with increasing numbers of feature maps (e.g ResNet [22], VGGNet [55]). The classification task was solved in the low-resolution

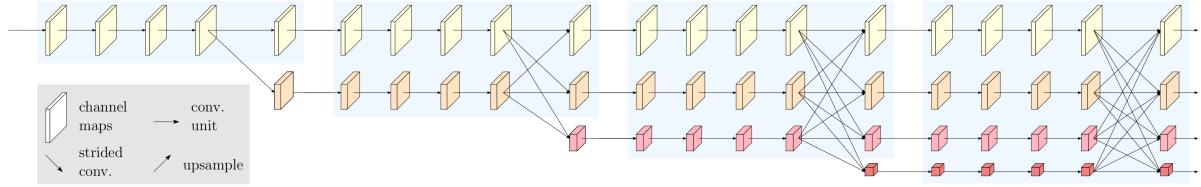


Figure 3.3.1: Network architecture for HRNet. The top row shows high resolution representations with fewer number of feature maps. Each step downwards reduces the resolution with a factor of two while the number of feature maps are doubled [62].

space and then transformed back to form the high-resolution representation needed for e.g. the HPE. Sun et al's proposed architecture preserves a high resolution representation throughout the network. It does so while also producing low-resolution/high dimensional representations suitable for classification.

The network architecture is shown in Figure 3.3.1 and consists of four stages (blue blocks in depth direction in Figure) with convolutional layers. After each stage a new low-resolution representation is created by performing strided convolutions. At these instances the existing representations also exchange information by either nearest neighbor upsampling or strided convolutions. The K estimated keypoints are represented as heatmaps, $\{\mathbf{H}_1, \dots, \mathbf{H}_K\}$, indicating the locations. These heatmaps are formed from the last high-resolution feature map (top right in Figure 3.3.1). Corresponding ground truth heatmaps are generated by applying 2D Gaussians to the correct keypoint locations and the model is trained by minimizing the mean squared error between these [57]. Although a high resolution heatmap is desirable as it gives smaller quantization errors, the computational cost increases quadratically with the size [67]. Hence, the performance of the model can be improved by extracting the region of interest from the input image. This can for instance be done using an object detection model trained to find humans.

Object detectors usually work by first producing a large number of regions of interest in the image which are then classified to either belong to some object class or the background. Faster R-CNN by Ren et al. [52] is an example of such a detector where these steps are performed by a single CNN. The model outputs bounding boxes and class scores for the objects in the image deemed not to be part of the background.

3.3.2 Distribution-Aware coordinate Representation of Key-point (DARK)

As discussed above a high resolution heatmap should result in higher accuracy, but is computationally expensive. Zhang et al. propose a method they call Distribution-Aware coordinate Representation of Key-point (DARK) [67] to reduce the quantization error by i) analyzing the distributions of the predicted heatmaps, and ii) creating the training heatmaps in a slightly new fashion.

The actual keypoint location is found at the maximal activation of the heatmap. Since it is smaller than the actual image this turns into a sub-pixel localisation problem. Newel

et al. [48] empirically found that a weighted average between the two highest activations, according to (3.1), yielded a good result.

$$\mathbf{p} = \mathbf{m} + \frac{1}{4} \frac{\mathbf{s} - \mathbf{m}}{\|\mathbf{s} - \mathbf{m}\|_2} \quad (3.1)$$

where: \mathbf{p} = predicted maximum
 \mathbf{m} = highest activation
 \mathbf{s} = second highest activation

This has been the de facto standard heatmap decoding, but Zhang et al. suggests using the fact that the heatmaps used for training usually are created as 2D Gaussian distributions, i.e. that the heatmaps can be expressed as (3.2).

$$\mathcal{G}(\mathbf{x}; \boldsymbol{\mu}, \Sigma) = \frac{1}{2\pi |\Sigma|^{\frac{1}{2}}} \exp \left(-\frac{1}{2} (\mathbf{x} - \boldsymbol{\mu})^\top \Sigma^{-1} (\mathbf{x} - \boldsymbol{\mu}) \right) \quad (3.2)$$

where: $\boldsymbol{\mu}$ = maximum of heatmap
 \mathbf{x} = pixel location
 Σ = diagonal covariance matrix

By Taylor expanding of the logarithm of (3.2) in the point \mathbf{m} , i.e. the point with the highest sampled activation, an expression for $\boldsymbol{\mu}$ is obtained:

$$\boldsymbol{\mu} = \mathbf{m} - \left(\mathcal{D}''(\mathbf{m}) \right)^{-1} \mathcal{D}'(\mathbf{m}) \quad (3.3)$$

where: $\mathcal{D}(\mathbf{x}) = -\frac{1}{2} (\mathbf{x} - \boldsymbol{\mu})^\top \Sigma^{-1} (\mathbf{x} - \boldsymbol{\mu})$,
 i.e. the non constant term in the logarithm of G (3.2)

The derivatives $\mathcal{D}'(\mathbf{m})$ and $\mathcal{D}''(\mathbf{m})$ are efficiently estimated from the heatmap. As this approach strongly assumes a Gaussian structure it is proposed to modulate the heatmap before estimating the maximal activation. This is done by performing a convolution with a Gaussian kernel with the same covariance as the one used for the training data.

The second improvement suggested by Zhang et al. concerns the creation of the training heatmaps. Traditionally these have been created from the quantized keypoint locations, resulting in a slightly biased heatmap. In Figure 3.3.2 this would correspond to having the peak activation in the purple dot. By instead using the non-quantized location an unbiased heatmap is obtained. This would correspond to having the peak off-grid, in the blue dot in Figure 3.3.2.

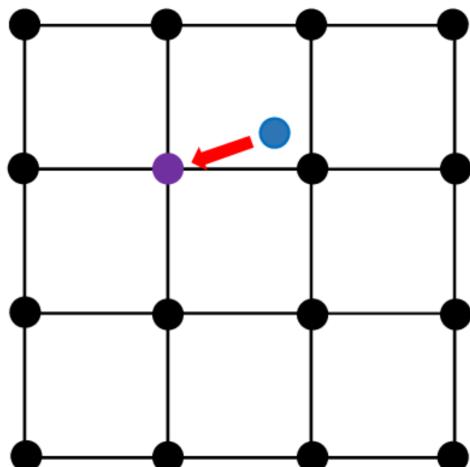


Figure 3.3.2: Quantization error due to off-grid keypoint location. Correct location (blue) represented by on-grid coordinate, here using floor quantization [67]. SKRIV ANTAGLIGEN NAGOT BATTRE HAR!!!!

Chapter 4

Related work - Time Series Classification

4.1 Background - Time series classification

Time series are sequences of data ordered in time [H'R KANSKE TA EN FIN DEFINITION FR[N ANDREAS...].

SKA JAG HA DESSA DEFINITIONER? HANVISAR JAG TILL DEM NGNSTANS?

Definition 2. *A univariate time series of length n, with ordered indices*

$$X = [x_1, x_2, \dots, x_n]^\top$$

Definition 3. *A multivariate time series of length n, with M channels*

$$\mathbf{X} = [X_1, \dots, X_M]$$

The TSC task is about finding a function, $f : \mathbb{R}^{n \times M} \rightarrow \mathbb{R}$, that assigns one label to each, possibly multivariate, time series. The problem bares strong resemblance with that of image classification, but with the two spatial dimensions replaced by one temporal dimension. Despite this the use of end-to-end deep learning models is not as dominant in the TSC community [26]. Similarly to the fields of computer vision various datasets has emerged recently. This has been important for the development of TSC as it allows for fair comparison between methods. One of the most widely used dataset collections today is the University of California, Riverside (UCR) archive [15] containing 85 different time series datasets.

Traditionally a nearest neighbor method together with dynamic time warping has been used for classification [7]. Simply put, this means that a time series during classification is

compared to the training data and assigned the class of the most similar time series. Lines and Bagnall suggested a method where an ensemble of 11 nearest neighbor classifiers with different similarity measures [39] yielded SOTA results. Bagnall et al. [6] developed the idea of ensemble based classifiers with Collective Of Transformation-based Ensembles (COTE), where 35 different classifiers using different transforms was used. Lines et al. [38] extended COTE further with two new classifiers resulting in Hierarchical Vote Collective of Transformation-based Ensembles (HIVE-COTE). One drawback with HIVE-COTE is the computational intensity, both during training and test time. Training time is large partly due to one of the transforms used is the Shapelet Transform with a time complexity of $O(n^2l^4)$, n being the number of time series and l the length of them. Due to the nature of the nearest neighbor algorithm the result of the 37 classifiers during test time needs to be compared to the corresponding result for each time series in the training set, yielding this method impractical for real-time use [26].

In 2016 Zheng et al. [68] presented a neural network model based on convolutional layers for the classification task. Wang et al. [65] developed these ideas and presented models with performance close to that of COTE on the UCR archive. The development of neural network based classification has since then continued and below the two architectures inspiring our model are presented.

4.2 Deep learning architectures

The last few years the number of proposed neural network based time series classifiers has increased drastically. Below the two most influential architectures for our work are presented.

4.2.1 InceptionTime

InceptionTime, presented by Fawaz et al. [27], is, as the name suggests, inspired by Inception [58] which is an architecture successful in computer vision tasks. It is comprised of several stacked Inception modules consisting of differently sized convolutions as well as pooling layers. To reduce the number of parameters in the network 1×1 convolutions are often used as a dimensionality reduction. One such module can be seen in Figure 4.2.1a. The architecture of Fawaz et al. is similar, but with only one temporal dimension instead of two spatial dimensions. As with the computer vision task the dimensionality is reduced, here through a bottleneck of size m . The bottleneck is achieved by convolutions with m filters of length 1. The InceptionTime module is shown in Figure 4.2.1b.

Figure 4.2.2 shows how stacked modules makes up the InceptionTime architecture. Residual connections are used to decrease the risk of vanishing gradients once the network becomes deeper, as suggested by He et al. [22]. The InceptionTime modules are followed by a GAP layer which averages each time series over its time dimension. The classification is performed by fully connected layers with softmax activations.

Many deep learning based time series classifiers experiences a significant variance in

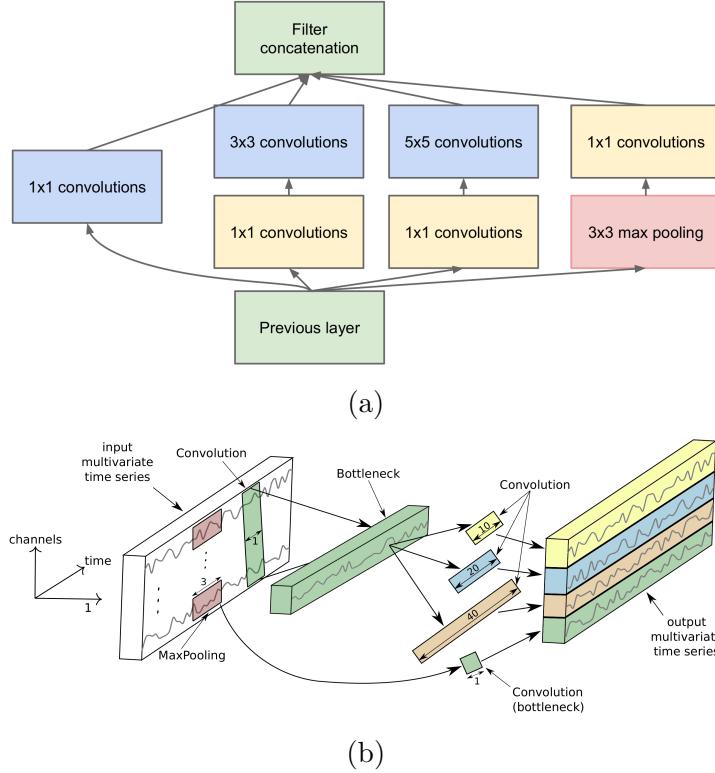


Figure 4.2.1: Inception modules for computer vision (a) with dimensionality reduction ahead of the 3×3 and 5×5 convolutions and InceptionTime module for TSC (b), here illustrated with a bottleneck size of 1. Figures from [58] and [27] respectively.

their accuracy, especially when evaluated on the UCR archive with rather small training sets [25]. To overcome this Fawaz et al. suggest the use of an ensemble of identical InceptionTime networks, but with randomly initialized weights before training. The ensemble's output is then calculated as the average of the outputs of the individual models. Such an ensemble of five models achieves a performance similar to that of HIVE-COTE on the UCR archive.

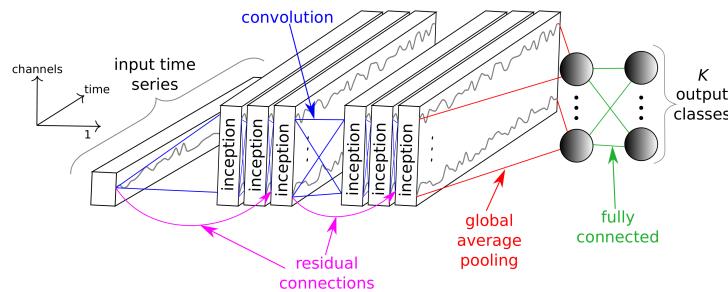


Figure 4.2.2: InceptionTime architecture for TSC [27].

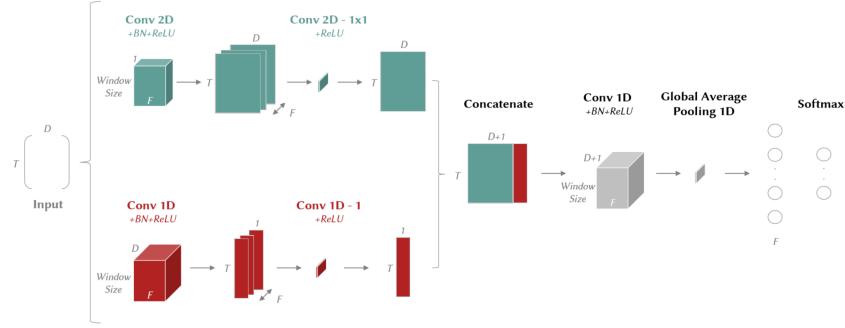


Figure 4.2.3: The XCM architecture with BN - Batch Normalization, D - number of input channels, F - number of filters, T - length of time series [18].

4.2.2 Explainable Convolutional Neural Network for Multivariate Time Series Classification (XCM)

As discussed in Section 2.5 explainability is desirable, but not inherent in most black-box deep learning models. Fauvel et al. [18] propose an architecture, Explainable Convolutional Neural Network for Multivariate Time Series Classification (XCM), which allows for tracking which time steps and which inputs are important for the classification decision. By using 2D convolutions with kernels of size $ks \times 1$, where ks is the kernel size hyperparameter, the convolution is only performed in the time dimension and the input channels are kept separated throughout the feature extraction. Through dimensionality reduction from a 1×1 2D convolution a single feature map for each input is produced. From this the importance of input channels and time steps can be traced using Grad-CAM, described in Section 2.5. In parallel to the channel specific features Fauvel et al. also suggests using 1D convolutions over all channels resulting in a combined feature map along the time dimension. The XCM architecture is depicted in Figure 4.2.3.

Chapter 5

Methods

5.1 Overview

In this chapter the system for assessing POEs will be presented. This system is naturally divided into two parts where firstly the videos are analyzed. The first subsystem extracts body part coordinates of the subjects. This information is then passed to the second subsystem where it is used to calculate a score according to [46]. The data used is presented in Section 5.2 and the two subsystems are described in Sections 5.3 and 5.4 respectively.

5.2 Data

The data available is in the form of videos each containing one subject, recorded from the front. As discussed in Chapter 1 the SLS task and the femoral valgus, pelvis, trunk, and KMFP POEs is evaluated. Each video contains four-five repetitions and for each repetition the POEs above have been scored according to Table 5.2.1. Along with the POE scores a certainty score, describing the confidence of the physiotherapist assessing the videos, is provided. This is between 0 (certain) and 2 (uncertain) and when above 0 the uncertainty direction is provided as well. This certainty score is only available for the combined (median) score for all repetitions, i.e. one certainty score per video.

In total there are 103 labeled videos and the number of repetitions per video varies slightly. This variation is due to different factors such as subject only performing four repetitions, that the entire movement was not captured in the video, or that some specific POE could not be evaluated from that specific video for some reason.

Table 5.2.1: Descriptions for the visual assessment of segment specific POEs evaluated in this thesis. Table taken from [4].

POE	Number of subjects	Number of repetitions
Trunk	103	9

5.3 Body part localization

The pose estimation is built around the open-source toolbox MMPose [42] from MMLab. Each frame is considered to be an independent image and is analyzed with a HRNet model with the DARK extension trained on the COCO-wholebody dataset¹. Both the model and the dataset is described in Section 3. The extended wholebody dataset is used since it, along with the ankle positions, also estimates the positions of the toes and heels which according to Section ?? ought to be important.

To get comparable results some of the videos were rotated and flipped before inferring the keypoints. This was needed since the videos were recorded in different orientations and the actions were performed with different legs. The rotations were based on the orientation of the subject (position of head w.r.t. the feet) in the first frame to have it standing up in the y -direction. Videos where the squats were performed with the left leg were then flipped around the y -axis to be able to use the same model for the left and right leg in a more efficient manner.

A bounding box for the subject is found using a Faster R-CNN model trained on the COCO dataset². The content of this bounding box is resized to match the input size of the HPE model used, 384×288 pixels in our case. Each video analyzed results in sequences of x - and y -coordinates for all the keypoints in the dataset used to train the model.

5.4 Classification

5.4.1 Preprocessing and dataset blabla..

Before assessing the POEs based on the body part positions a number of preprocessing steps are conducted. Firstly the data is resampled as the videos are recorded with a number of different frame rates ranging from 25 to 60 Hz. The resampling is performed using linear interpolation to a new sample frequency of 25Hz. This data is then low pass filtered through a fourth order Butterworth filter with a cutoff frequency of 2.5Hz.

While the POE assessment, see Section ??, is performed on a per repetition basis the body part coordinates are extracted on a per video basis. Hence, the sequences corresponding to the entire video is split up in the individual repetitions. This splitting algorithm is presented in Algorithm 1 and is based on finding the edges of the peaks in specific position data. For the SLS task the y -coordinate of the right shoulder is used. The number of points extracted for each repetition depends on the width of the peak. The length of the observed repetitions varies from about 1 to 8 seconds. For practical reasons, such as handling of data and training performance³, it is desirable to save the data as

¹The model used can be found here: https://mmpose.readthedocs.io/en/latest/top_down_models.html.

²The model used can be found here: https://github.com/open-mmlab/mmdetection/tree/master/configs/faster_rcnn.

³All data in one batch must have the same size. Hence, to be able to train with a batch size larger

multidimensional arrays with the same dimensions. Two different ways of solving this problem is evaluated, namely i) padding the sequences and use maskings for the padded samples in the models, and ii) alternate the sample frequency to thereby achieve sequences of the same length.

Algorithm 1: Extraction of repetitions from sequences

```
right_edges, left_edges = find_edges(sequence);
for peak, right, current_left, next_left in peaks, right_edges, left_edges do
    split_index = mean(right, next_left);
    start = max(current_left - extra_points, 0);
    end = min(right + extra_points, split_index);
    repetition = normalize_length(sequence[start:end]);
    sequence = sequence[end:];
end
```

Finally the data is normalized. All coordinates are moved to put the mean position of the first five right hip-samples in the origin and are scaled to set the distance between the right shoulder and right hip to one, according to (5.1).

$$\begin{aligned} (x, y)_i &= (x, y)_i - \overline{(x, y)}_{rh} \\ (x, y)_i &= \frac{(x, y)_i}{\|(x, y)_{rs}\|_2}, \forall i \end{aligned} \tag{5.1}$$

where: $\overline{(x, y)}_i$ = mean over first five samples for body part i
 rh = right hip
 rs = right shoulder
 i \in Available body parts

After these preprocessing steps a dataset with inputs $\in \mathbb{R}^{N \times T \times F}$ and corresponding labels $\in \mathbb{Z}_3^N$ is created. The inputs consists of N multivariate time series of length T with F channels. These channels are a subset of the extracted x - and y -coordinates as well as angles and differences between keypoints.

5.4.2 Models eller ensembles isch, kanske classifiers

For the modeling we used ensembles of different deep learning based model architectures. The reasoning behind this was based on the results of Fawaz et al. [25], suggesting that the output a deep learning model trained on a limited amount of data will vary based on the initial parameter values. By averaging the result over several models this variance will be reduced. Another reason for using an ensemble is, as can be seen in e.g. [6, 38],

than 1, which usually improves training performance [21], all data in the same batch needs to have the same dimensions.

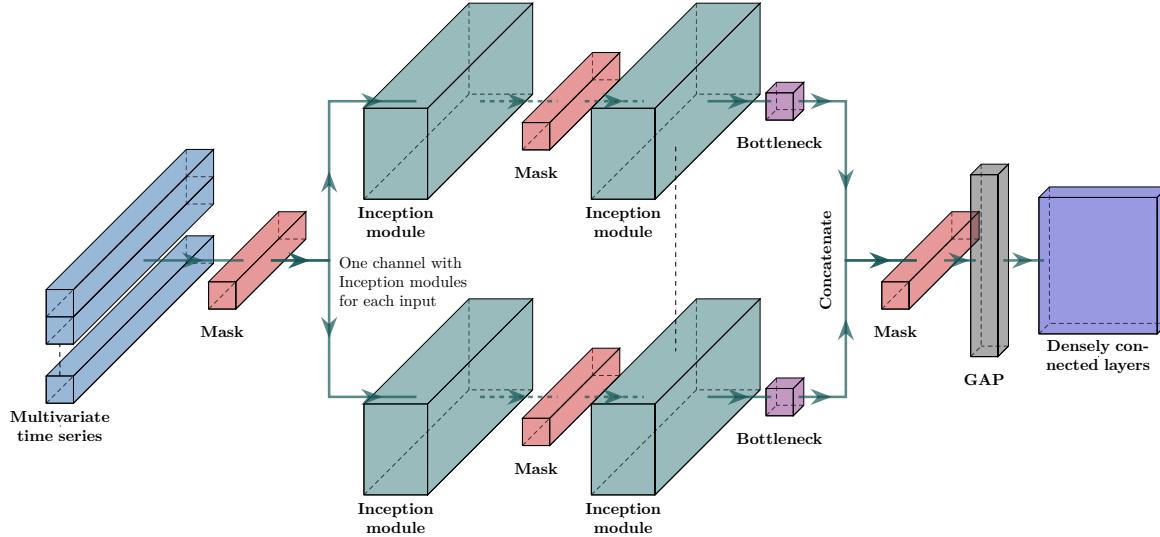


Figure 5.4.1: The X-InceptionTime architecture developed in this work.

that the combined result of many specialized models can be better than that of one more general model.

All models used have been modified to handle the padded input data discussed in Section 5.4.1. This is done by adding masking layers setting the padded samples to zero throughout the networks, illustrated in Figure 5.4.1. This reduces the impact of the padded samples to something similar to the padding performed in convolutional layers to keep the size of the feature map intact. The same mask indicates which time steps should be ignored in the GAP layer.

The models eventually used were InceptionTime (Section 4.2.1) with different loss functions as well as an architecture designed by us, inspired by XCM (Section 4.2.2) and InceptionTime. We call this model X-InceptionTime and it is presented below.

skriv om ensemble, vilka losses

X-InceptionTime

The idea with this model was to combine the explainability of XCM with the inception module from InceptionTime. This was done by separating the inputs and having individual inception modules for each input channel as can be seen in Figure 5.4.1. After the final module (the depth can be seen as a hyperparameter and needs to be tuned) a bottleneck of size one is applied reducing the dimensionality of each input channel back to $T \times 1$. The features for the individual inputs are concatenated resulting in a feature map of size $T \times F$ where each input feature is only affected by that input. This makes it possible to use Grad-CAM to get a measure of the importance of each time step for each input.

The Grad-CAM method is slightly modified and simplified for this model compared to what is presented in Section 2.5, mainly due to the one dimensional data. Consider the

final feature map A consisting of the concatenated feature maps from the separate input channels. As mentioned above $A \in \mathbb{R}^{T \times F}$ and the aim is to find importance values for each time step in each input. With the same notations as in (2.8), i.e. A_i^k corresponds to the activation of input k at time step i , the Grad-CAM, M_c^k , for class c and input k can be calculated as follows

$$\begin{aligned} w_k^c &= \frac{1}{T} \sum_{i=1}^T \frac{\partial y_c}{\partial A_i^k} \\ M_c^k &= w_k^c A^k. \end{aligned} \tag{5.2}$$

Compared to (2.8) the *ReLU* activation has been removed. This means that the importance values also contain information about which features suggesting this sample belongs to another class than c .

Along with the effect of the time steps it is also possible, thanks to the GAP layer, to get a measure of the importance of each input. The importance value, α_k^c , for input k describes how much effect this input has on the classification decision. It is given by applying the Grad-CAM method to the output of the GAP layer, B . From the feature map, A , this importance weight is calculated according to

$$\begin{aligned} B^k &= \frac{1}{T} \sum_{i=1}^T A_i^k \\ w_k^c &= \frac{\partial y_c}{\partial B^k} \\ \alpha_k^c &= w_k^c B^k. \end{aligned} \tag{5.3}$$

This was exploited to chose input features by iteratively training models, evaluating (5.4), and removing the features corresponding to the lowest W_k until the performance of the model drops significantly. This method has its drawback, the most notable that being that input features suitable for this architecture will be found. This model does not consider interaction between different features directly, hence features important through such interactions will probably not be deemed important by this method.

$$W_k = \text{mean_folds}\left(\text{normalize}\left(\sum_{i=1}^N |w_{ik}^{c_i}|\right)\right), \tag{5.4}$$

where: $\text{mean_folds}(z) = \text{average of } z \text{ over all folds}$

$$\text{normalize}(z) = \frac{z}{\|z\|_2}$$

$$c_i = \text{argmax}(\hat{y}_i), \text{ i.e. the predicted class}$$

Ensembles

The ensembles used consists of 4-8 models whose outputs are linearly combined to form the ensemble output. As discussed above this allows the ensemble to benefit from models optimized to perform well according to different metrics. In Section 5.4.3 we will present how k -fold cross-validation was used for training and validation. This was also used for design of the ensembles. The ensemble design was however performed using a different random seed when generating the folds compared to the one used for the results. This was done to achieve different training-validation combinations in an attempt to avoid bias.

coral osv. custom losses osv?

5.4.3 Training

5.4.4 Combined score

Chapter 6

Results

Chapter 7

Conclusions and Discussion

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Appendix A: POE-task combinations [45]

Segment-Specific POEs	Functional Tasks in Which Each POE Is Assessed*	Scoring of "0" Good (no POE)†	Scoring of "1" Fair (minor POE)†	Scoring of "2" Poor (major POE)†
Foot pronation	SLS	The absence of pronation of the medial arch of the foot, navicular bone and the medial malleolus indicates no POE	A slight position of pronation of the medial arch of the foot, navicular bone and the medial malleolus indicates a minor POE	A clear position of pronation of the medial arch of the foot, navicular bone and the medial malleolus indicates a major POE
KMFP	SLS	Mid-point of patella is in line with or lateral to the second toe	Mid-point of patella is placed medial to the second toe	Mid-point of patella is clearly placed medial to the big toe
	SD			
	FL			
	SLHD			
	SH			
Deviation of pelvis in any plane	SLS	The absence of pelvis into lateral deviation, pelvic tilt and/or rotation of pelvis respectively indicates no POE	A slight position of the pelvis into lateral deviation, pelvic tilt and/or rotation of pelvis respectively indicates minor POE	A clear position of the pelvis into lateral deviation, pelvic tilt and/or rotation of pelvis respectively indicates major POE
	SD			
	FL			
	SLHD			
	SH			
Deviation of trunk in any plane	SLS	The absence of a trunk position into forward lean, lateral lean and/or rotation indicates no POE	A slight position of the trunk into forward lean, lateral lean and/or rotation indicates minor POE	A clear position of the trunk into forward lean, lateral lean and/or rotation indicates major POE
	SD			
	SLHD			
	SH			
Femur medial to shank	SLS	Mid-point of medial and lateral femoral condyles is lateral to tibial tuberosity	Mid-point of medial and lateral femoral condyles is in-line with tibial tuberosity	Mid-point of medial and lateral femoral condyles is medial to tibial tuberosity
	SD			
	FL			
	SLHD			
	SH			
Femoral valgus (the angle created by the intersection of a longitudinal line and a line from mid-point patella toward ASIS)	SLS	The absence of femoral valgus indicates no POE	A slight position of femoral valgus indicates minor POE	A clear position of femoral valgus indicates major POE
	SD			
	FL			
	SLHD			
	SH			

Appendix B: wtf

this is the information