## Assignment 4 for the Applied Econometric Time series course (MSc 5314)

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Consider the bivariate error correction system

$$\Delta r_{St} = \alpha_S (r_{Lt-1} - \beta r_{St-1} - \mu) + \sum_{i=1}^{2} a_{i,11} \Delta r_{St-i} + \Delta a_{i,12} \Delta r_{Lt-i} + \epsilon_{St} \quad \alpha_S \ge 0$$

$$\Delta r_{Lt} = -\alpha_L (r_{Lt-1} - \beta r_{St-1} - \mu) + \sum_{i=1}^{2} a_{i,21} \Delta r_{St-i} + \Delta a_{i,22} \Delta r_{Lt-i} + \epsilon_{Lt} \quad \alpha_L \ge 0$$

where  $r_{St} \sim I(1)$  and  $r_{Lt} \sim I(1)$ , and  $\epsilon_{St}$  and  $\epsilon_{Lt}$  are white noise processes.

- 1a. Argue why  $r_{St}$  and  $r_{Lt}$  must be cointegrated. What is the cointegration vector? What is the long-run equilibrium?
- 1b. Formulate the null hypothesis that  $r_{Lt}$  does not Granger cause  $r_{St}$ .
- 1c. Explain the adjustment mechanism towards the long-run equilibrium if (i)  $r_{Lt-1} > \beta r_{St-1} + \mu$  and (ii)  $r_{Lt-1} < \beta r_{St-1} + \mu$  assuming  $\alpha_S, \alpha_L > 0$ , and (iii)  $r_{Lt-1} > \beta r_{St-1} + \mu$  and (iv)  $r_{Lt-1} < \beta r_{St-1} + \mu$  assuming  $\alpha_S > 0$  and  $\alpha_L = 0$ .
- 1d. Assume that  $r_{St} \sim I(1)$  and  $r_{Lt} \sim I(1)$  (as before) but not cointegrated. Why is it a problem to run the regression  $r_{St} = \mu + \beta_1 r_{Lt} + \varepsilon_t$ ?
  - 2. Do exercise 4 (but not 4f) in the textbook (pp.402-403)<sup>2</sup>. **Remark:** It is possible that the values you obtain differ from those reported in the text to the exercise since the sample is extended. However, the main conclusions should be the same.

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<sup>&</sup>lt;sup>2</sup>The data for this exercise is available on the course web in the file A4\_2019.dta. It contains quarterly observations for the 3-month T-bill (tbill) as well as the 5-year and 10-year Treasury rate (r5 and r10) for the U.S. from 1960Q1 to 2018Q3 (T = 235).