Metrics, final assignment

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This is the last assignment for the course 5304 Econometrics. It is ungraded, which is why I could do it in R instead of Stata. Note that this is my first R markdown document.

Importing the data

We begin by reading the stata file. Turns out we need the library "readstata13" to do this.

```
library(readstata13)
df <- read.dta13("/Volumes/GoogleDrive/Min enhet/Learning/MSc/Econometrics/Metrics/IHDS_2012_Data.dta")</pre>
```

```
head(df)
##
              STATEID
                                DISTRICT IDPSU
                                                       IDHH
                                                                IDPERSON EW6
## 1
        Tamil Nadu 33 Tiruchchirappalli 331509 3315090911 331509091102
## 2
       Maharashtra 27
                                  Satara 273108 2731081701 273108170102
## 3
       Maharashtra 27
                                Yavatmal 271401 2714010311 271401031104
## 4 Uttar Pradesh 09
                               Chandauli 96603 0966031911 096603191104
## 5
       Maharashtra 27
                                   Jalna 271804 2718040211 271804021104
                                                                          24
                                Yavatmal 271401 2714010811 271401081102
## 6
       Maharashtra 27
##
              EW8 FH5CK FP5 SPR05 SPED5
                                                             SPED6
## 1
      3rd class 3
                           2
                                53
                                    No 0
                                                       6th class 6
                       3
                           2
                                50
                                    No 0
## 2 Secondary 10
                                                      Secondary 10
## 3 Bachelors 15
                      2
                           2
                                32
                                    No 0 1 year post-secondary 13
                      3
                           2
## 4 9th class 9
                                39
                                    No 0
                                                High Secondary 12
## 5
                      2
                           2
                                27
                                    <NA>
           none 0
                                                            none 0
                      5
## 6
           none 0
                                48
                                    No 0
                                                            none 0
```

We have a few variables containing demographic information on individuals in India (2012).

```
library(tidyverse)
df <- df %>% filter(EW6 <= 60) %>% filter(EW6 >= 20)
df <- df %>% mutate(three_plus = FH5CK >= 3)
```

We need to reformat the variable EW8 before it is usable in any regression:

```
df$EW8 <- as.character(df$EW8)
df <- df %>% mutate(EW8 = substr(EW8, nchar(EW8) - 1,nchar(EW8)))
df$EW8 <- strtoi(df$EW8)</pre>
```

Linear probability model

The first task is to use the lpm to estimate marginal probabilities of having three or more children using woman's age and education level.

The linear probability model is simply the regression dependent variable on independent variables. We use the age of the women (EW6), and their years of education (EW8) to predict the probability that they have at least 3 children. We'd expect the unbiased estimates to be positive for age and negative for years of education. I use the option na.exlude so that predictions will insert NA were no prediction could be made.

```
library(pander)
lpm <- lm(three_plus ~ EW6 + EW8, data = df, na.action = na.exclude)
pander(lpm)</pre>
```

Table 1: Fitting linear model: three_plus $\sim EW6 + EW8$

	Estimate	Std. Error	t value	$\Pr(> t)$
(Intercept)	0.1081	0.01604	6.742	1.619e-11
$\mathbf{EW6}$	0.0153	0.0003842	39.82	0
EW8	-0.0346	0.0007262	-47.64	0

The marginal effect associated with being one year older is 0.015 percentage points more likely to have three or more children and the marginal effect associated with having one more year of schooling is -0.035 percentage points less likely to have three or more children. The signs are what we expected them to be.

Next, let's find out the range of the predictions:

```
df <- df %>% mutate(pred_lpm= predict(lpm, type = "response", na.action = na.exclude))
pct_in_range <- round(sum(df$pred_lpm >= 0 & df$pred_lpm <= 1, na.rm=T)/length(df$pred_lpm),3)*100</pre>
```

The range of the observations is [-0.12, 1.03] and 96.8% of the observations lie inside the unit interval. It is not ideal to predict probabilities higher than 1 or smaller than 0, so let's move on to theoretically justified models.

Probit

We perform the same steps using a probit model. This comes with the advantage of not yielding any predictions outside the unit interval. However, it is somewhat more tedious to obtain marginal effects as these can't be read from the coefficients and the predicted values are similar to the lpm anyway.

```
probit <- glm(three_plus ~ EW6 + EW8, family = binomial(link = "probit"), data = df, na.action = na.exc
pander(summary(probit))
```

	Estimate	Std. Error	z value	$\Pr(> z)$
(Intercept)	-1.214	0.05051	-24.04	1.158e-127
$\mathbf{EW6}$	0.04643	0.001257	36.95	6.703e-299
EW8	-0.1031	0.002376	-43.37	0

(Dispersion parameter for binomial family taken to be 1)

Null deviance:	20979 on 15159 degrees of freedom
Residual deviance:	16713 on 15157 degrees of freedom

Predict values and obtain range of predicted values:

```
df <- df %>% mutate(pred_probit= predict(probit, type = "response", na.action = na.exclude))
pct_in_range_p <- round(sum(df$pred_probit >= 0 & df$pred_probit <= 1, na.rm=T)/sum(!is.na(df$pred_prob</pre>
```

The range of the predictions is [0.03, 0.94] and 100% of the observations lie inside the unit interval.

```
library(margins)
margin_probit <- margins(probit, at = list(EW6 = mean(df$EW6), EW8 = mean(df$EW8, na.rm = TRUE)))
margin_probit_spec <- margins(probit, at = list(EW6 = 20, EW8 = 12))
pander(summary(margin_probit)[0:7])</pre>
```

factor	EW6	EW8	AME	SE	Z	p
EW6	36.66	5.642	0.01844	0.0004991 0.0009423	36.96	5.668e-299
EW8	36.66	5.642	-0.04094		-43.45	0

pander(summary(margin probit spec)[0:7])

factor	EW6	EW8	AME	SE	Z	p
EW6	20	12	0.005815	0.0001719	33.82	8.847e-251
EW8	20	12	-0.01291	0.0004711	-27.4	2.601e-165

The AME column gives the marginal effects at values specified by EW6, and EW8.

Logit

We are also told to do the same thing using the logit, essentially repeating the steps from above once more, but with the logit instead of the probit. These two yield very similar predictions, but have different properties that can be useful depending on application.

logit <- glm(three_plus ~ EW6 + EW8, family = binomial(link = "logit"), data = df, na.action = na.exclupander(summary(logit))</pre>

	Estimate	Std. Error	z value	$\Pr(> z)$
(Intercept)	-2.023	0.08473	-23.88	5.128e-126
$\mathbf{EW6}$	0.07746	0.002153	35.97	2.08e-283
EW8	-0.1709	0.00407	-42	0

(Dispersion parameter for binomial family taken to be 1)

Null deviance:	20979 on 15159 degrees of freedom
Residual deviance:	16722 on 15157 degrees of freedom

The range of the predictions is given by:

```
df <- df %>% mutate(pred_logit= predict(logit, type = "response", na.action = na.exclude))
pct_in_range <- round(sum(df$pred_logit >= 0 & df$pred_logit <= 1, na.rm=T)/sum(!is.na(df$pred_logit)),</pre>
```

The range of the predictions is [0.04, 0.93] and 100% of the observations lie inside the unit interval.

```
margin_logit <- margins(logit, at = list(EW6 = mean(df$EW6), EW8 = mean(df$EW8, na.rm = TRUE)))
margin_logit_spec <- margins(logit, at = list(EW6 = 20, EW8 = 12))
pander(summary(margin_logit)[0:7])</pre>
```

factor	EW6	EW8	AME	SE	Z	p
EW6	36.66	5.642	0.01926	0.0005352	35.98	1.485e-283
EW8	36.66	5.642	-0.0425	0.001009	-42.13	0

pander(summary(margin_logit_spec)[0:7])

factor	EW6	EW8	AME	SE	Z	p
EW6	20	12	0.005315	0.0001516	35.06	2.9e-269
EW8	20	12	-0.01173	0.0004102	-28.6	7.479e-180

The AME column gives the marginal effects at values specified by EW6, and EW8.

To summarize the marginal effect at the mean value of both variables:

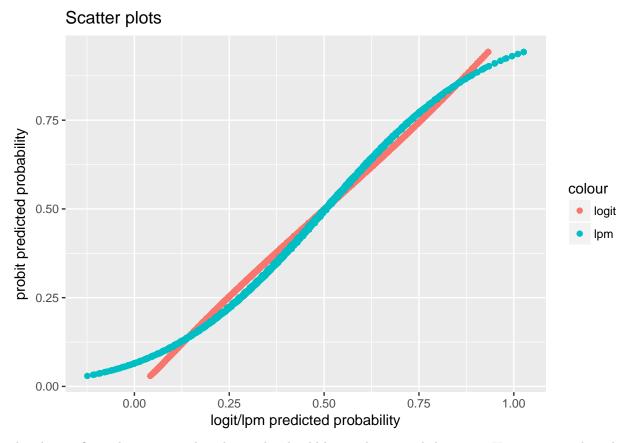
LPM: 0.015 and -0.035
Probit: 0.0184439, -0.040941
Logit: 0.0192591, -0.0425004

Probit and logit look very similar indeed. And LPM is not far off either, suggesting this simple model might be preferable if we only care about marginal effects, especially around the mean.

Scatter plot

Before wrapping up, I plot both the logit and the lpm against the probit to see how the predictions differed.

```
df %>%
ggplot() +
geom_point(aes(pred_logit, pred_probit, colour = "logit")) +
geom_point(aes(pred_lpm, pred_probit, colour = "lpm")) +
xlab("logit/lpm predicted probability") +
ylab("probit predicted probability") +
ggtitle("Scatter plots")
```



The plot confirms the intuition that the results should be similar around the mean. However, it is clear that the lpm yields bad predictions around the extreme values.