



# **Christian Werner**

(Quantitative geneticist and biostatistician) EiB, CIMMYT, Texcoco (Mexico)

# Filippo Biscarini



(Biostatistician, bioinformatician and quantitative geneticist) CNR-IBBA, Milan (Italy)

# Oscar González-Recio



(Computational biologist and quantitative geneticist) INIA-UPM, Madrid (Spain)





# simple testing

- inference → is there a difference between groups?
  - e.g. AA vs AB vs BB
- significance is related to the size and variance of this difference
- p-value: likelihood of the data under H<sub>0</sub> (no difference)
  - small p-value  $\rightarrow$  small likelihood of the data under  $H_0 \rightarrow$  significant difference
  - large p-value → there is a high chance of observing these data if there is no difference between groups
- $\alpha = 0.05 \rightarrow$  threshold: 5% of rejecting H<sub>0</sub> when it is true (Type I error).
  - false positive: significant result when there is no difference (H<sub>0</sub> is true)



## multiple testing

- many tests → many false positives
  - e.g. 2000 (independent) tests, α=0.05 → How many expected false positives?
     100 false positives by chance alone
- multiple testing problem
- GWAS:
  - many SNPs, many statistical tests, many p-values





# How to cope with the problem

- Increase the sample size (e.g. Bio Banks)
- Reduce the number of tests
  - Based on LD
  - Choose relevant regions (functional analysis)
- Decrease the significance threshold
  - Bonferroni correction
  - False discovery rate
  - o q values
  - Go Bayesian...



#### **Bonferroni** correction

- Bonferroni, mathematician (1892 1960)
- adjust the significance threshold:
  - New significance threshold  $\leq \alpha/m$

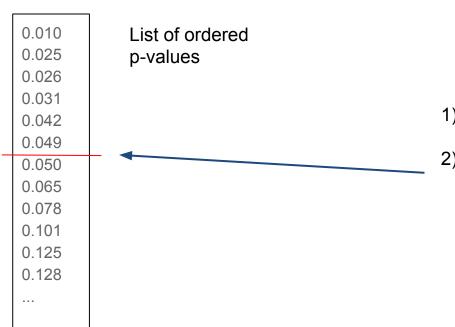
[m: number of tests (markers)]

- Bonferroni correction tends to be too conservative
  - few false positives
  - many false negatives



# **False discovery rate (FDR)**

Decrease the significance threshold



- 1) If I apply a threshold alpha to decide on significance, how much can I trust the results?
- 2) Where should I draw a line (threshold) of significance so that at most e.g. 10% of results are false positives?



# False discovery rate (FDR)

- FDR: how many of the positive results are false positives?
- Benjamini & Hochberg (1995), Storey (2002), Storey & Tibshirani (2003)
- Significance level = 0.05 → 5% of all tests on average will be false positives (assuming independency)
- FDR = 0.05 → 5% of significant tests will on average be false positives

fewer false positives!

# **False discovery rate (FDR)**

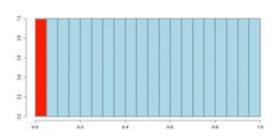
			True condition				
		Total population	Condition positive	Condition negative	$= \frac{\Sigma \text{ Condition positive}}{\Sigma \text{ Total population}}$	Σ True pos	curacy (ACC) = sitive + Σ True negative Total population
Pred	edicted endition	Predicted condition positive	True positive	False positive, Type I error	Positive predictive value  (PPV), Precision =  Σ True positive  Σ Predicted condition positive	False discovery rate (FDR) =  Σ False positive  Σ Predicted condition positive	
cond		Predicted condition negative	False negative, Type II error	True negative	False omission rate (FOR) = $\frac{\Sigma}{\Gamma}$ False negative $\frac{\Sigma}{\Gamma}$ Predicted condition negative	Negative predictive value (NPV) = $\frac{\Sigma \text{ True negative}}{\Sigma \text{ Predicted condition negative}}$	
			True positive rate (TPR), Recall, Sensitivity, probability of detection, Power $= \frac{\Sigma \text{ True positive}}{\Sigma \text{ Condition positive}}$	False positive rate (FPR), Fall-out, probability of false alarm $= \frac{\Sigma \text{ False positive}}{\Sigma \text{ Condition negative}}$	Positive likelihood ratio (LR+) = TPR FPR	Diagnostic odds ratio (DOR) = LR+LR-	F <sub>1</sub> score = 2 · Precision · Recall Precision + Recall
			False negative rate (FNR), Miss rate = Σ False negative Σ Condition positive	Specificity (SPC), Selectivity, True negative rate (TNR) = Σ True negative Σ Condition negative	Negative likelihood ratio (LR-) = FNR TNR		

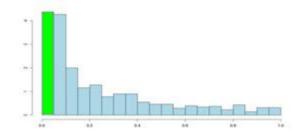






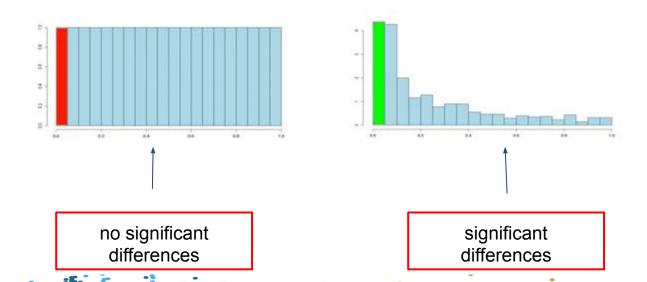
 q-values: proxies for FDR based on the distribution of p-values





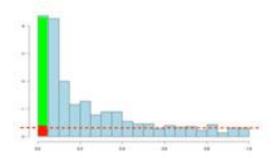


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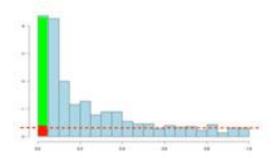
- the q-value approach tries to find the proportion of significant results which are likely to be false positives
- intuitively, it finds the height (density) at which the distribution of p-values flattens out





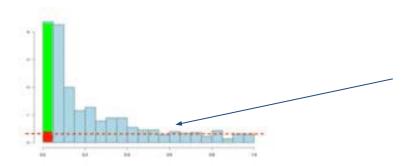


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here the distribution is similar to the case where there is no actual difference

 this proportion of false positives is then incorporated in the calculation of adjusted p-values (q-values)





## interpretation of q-values

- Significance level = 0.01 → probability of the p-value under H<sub>0</sub>
- q-value = 0.02 → probability of the SNP being a false positive
- Significance level = 0.01 → 1% chance of false positives (e.g. 7900 SNPs → 79 false positives expected)
- q-value = 0.02 → 2% of positive results may be false positives (e.g. 800 SNPs with q-value ≤ 0.02 → 16 false positives expected)

interpretation of the single SNP

interpretation of the distribution of SNPs



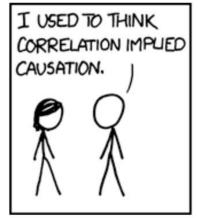
- What's wrong with q-values?
  - They assume p-value is the probability of rejecting the null hypothesis when it is true
  - They do not consider that p-values are drawn from a probability distribution, and assume an infinite repetition of the experiment (obtaining different p-values for each experiment).

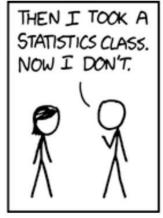


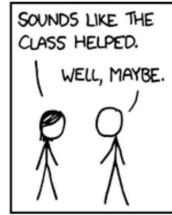


#### **REMEMBER**

Correlation does not imply causation







https://xkcd.com/552/

Make your rationale choice



#### **NEXT LECTURE**

# Power of GWAS experiments

