

DISTRIBUTION FUNCTION

$$F(x) = P(Y \leq x)$$

$P \dots$  IN  $R$  (PNORM)

INVERSE LINK FUNCTION

$$g^{-1}()$$

INVERSE DISTRIBUTION  
FUNCTION  $\rightarrow$

$$\bar{F}^{-1}(P) = x$$

$Q \dots$  IN  $R$  (Q NORM)

LINK FUNCTION

$$g()$$

**Table 15.1** Some Common Link Functions and Their Inverses

Link	$\eta_i = g(\mu_i)$	$\mu_i = g^{-1}(\eta_i)$
Identity	$\mu_i$	$\eta_i$
Log	$\log_e \mu_i$	$e^{\eta_i}$
Inverse	$\mu_i^{-1}$	$\eta_i^{-1}$
Inverse-square	$\mu_i^{-2}$	$\eta_i^{-1/2}$
Square-root	$\sqrt{\mu_i}$	$\eta_i^2$
Logit	$\log_e \frac{\mu_i}{1 - \mu_i}$	$\frac{1}{1 + e^{-\eta_i}}$
Probit	$\Phi^{-1}(\mu_i)$	$\Phi(\eta_i)$
Log-log	$-\log_e[-\log_e(\mu_i)]$	$\exp[-\exp(-\eta_i)]$
Complementary log-log	$\log_e[-\log_e(1 - \mu_i)]$	$1 - \exp[-\exp(\eta_i)]$

NOTE:  $\mu_i$  is the expected value of the response;  $\eta_i$  is the linear predictor; and  $\Phi(\cdot)$  is the cumulative distribution function of the standard-normal distribution.