

# Inference on multiverse meta-analysis

A multivariate permutation testing approach

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Multiverse

# Multiverse (Steegen et al., 2016)

- ▶ Real-world data analysis involve **several choices at each step**
- ▶ There are **many plausible alternatives** to the chosen analysis
- ▶ The **impact of alternatives** is often neglected or strongly underrated

# Inference on multiverse

- ▶ The increase in complexity after taking into account scenarios is usually handled only descriptively
- ▶ The specification curve (Simonsohn et al., 2020) is the only inferential method but is limited to standard linear models

## Note

There is a lack of a general and valid inferential framework for multiverse analysis



## POST-SELECTION INFERENCE IN MULTIVERSE ANALYSIS (PIMA): AN INFERENCE FRAMEWORK BASED ON THE SIGN FLIPPING SCORE TEST

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# PIMA

- ▶ Use a multivariate extension of the sign-flip score test (Hemerik et al., 2020)
- ▶ Works on generalized linear models (and meta-analysis)
- ▶ Controls the family-wise error rate
- ▶ Provides an overall multiverse p-value and corrected p-values for each included scenario

## Multiverse meta-analysis



# Meta-analysis

We can define a (random-effects) meta-analysis model as:

$$y_i = \mu_\theta + \delta_i + \epsilon_i$$

$$\delta_i \sim \mathcal{N}(0, \tau^2)$$

$$\epsilon_i \sim \mathcal{N}(0, \sigma_{\epsilon_i}^2)$$

Where  $\mu_\theta$  is the average true effect,  $\delta_i$  is the random-effect of the study  $i$  ( $\theta_i = \mu_\theta + \delta_i$ ) and  $\epsilon_i$  is the sampling error of the study  $i$ . When  $\tau^2 = 0$  we have an equal-effects (or fixed-effect) model.

# Meta-analysis many choices

Meta-analysis is a prototypical case of multiverse analysis:

- ▶ Should the study  $x$  be excluded for theoretical or statistical (e.g., outliers) reasons?
- ▶ Should we use an equal or random-effects model?
- ▶ Which value should take the pre-post missing correlation?
- ▶ ...

# Multiverse meta-analysis example

We collected  $k$  randomized controlled trials on the effectiveness of short-term memory training. The authors used multiple memory measures that are safe to combine.

- ▶ pre-post correlations are missing
- ▶ correlations between outcomes are missing
- ▶ we have  $n$  outliers
- ▶ we have  $n$  papers that we are not sure to include
- ▶ we could run an equal or random-effects model
- ▶ ...

## Multiverse meta-analysis example

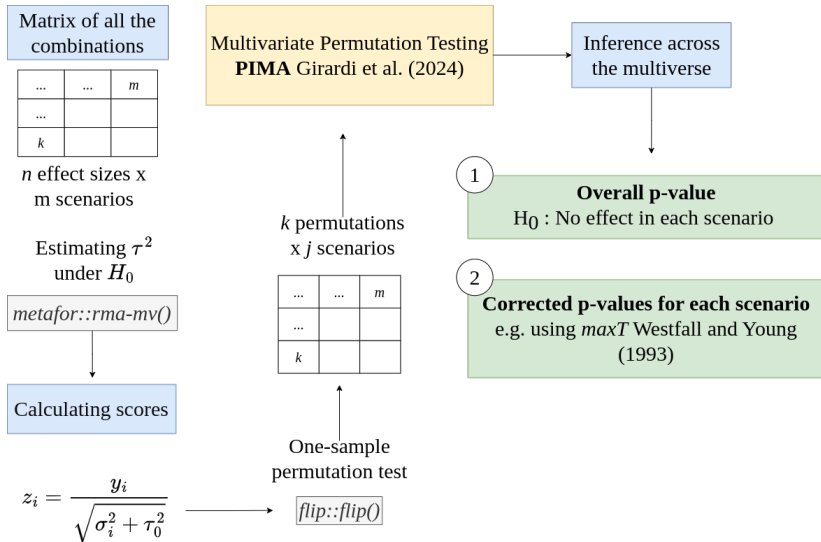
Even for the relatively simple previous example, we could have:

- ▶ pre-post  $\rho \rightarrow 5$  values
- ▶ outcomes  $\rho \rightarrow 5$  values
- ▶ 5 outliers
- ▶ 3 papers including/not including
- ▶ 2 equal vs random-effects

With all combinations, we have 750 **PLAUSIBLE** models with the same datasets.

PIMA on meta-analysis

# General Workflow



# Fast meta-analysis using permutations

Follmann & Proschan (1999) proposed a standard permutation test by re-computing  $\tau^2$  and  $\mu_\theta$  after each permutation.

We proposed a faster approach, especially for multiverse analysis with several scenarios.

1. Estimating  $\tau^2$  when  $H_0 : \mu_\theta = 0$  maximizing the log-likelihood fixing  $\mu_\theta = 0$
2. Calculating observed scores as  $z_i = \frac{y_i}{\sqrt{v_i + \tau_0^2}}$
3. Doing  $B$  permutations flipping the sign of scores  $z_i$
4. Repeat for each scenario of the multiverse

A simulated example



## Simulating a multiverse analysis

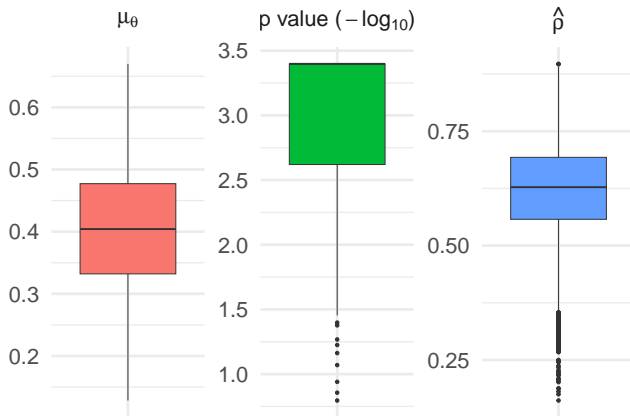
We simulated a meta-analysis with  $k = 30$  and  $m = 162$  sampling from a multivariate normal distribution.

We can describe a multiverse meta-analysis reporting summary statistics of the  $m$  estimated  $\mu_\theta$  and the correlation between scenarios.

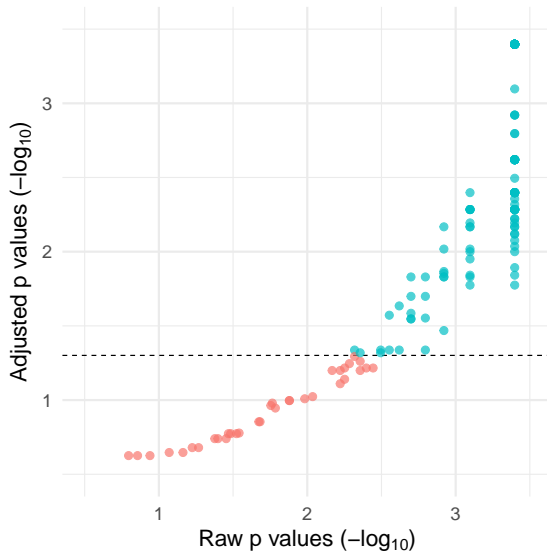
### Overall inference

The multiverse is associated with an **overall p-value**  $< 0.001$ , an **average effect of** 0.403 ( $SD = 0.112$ ) and an **average correlation of** 0.620 ( $SD = 0.102$ )

# Simulating a multiverse analysis



# Impact of multiplicity correction



## (valid) Post-hoc selective inference

### Legal P-Hacking :)

After the overall test and p values correction, the survived scenarios (the blue dots) can be selectively commented, without inflating the type-1 error.

## Guidelines for multiverse meta-analysis

# Guidelines for multiverse meta-analysis

1. Multiverse meta-analysis must contain only **PLAUSIBLE** models. Including implausible models (e.g., assuming a pre-post correlation of 0.95) reduces the statistical power.
2. As with any other inferential test, multiverse analysis should be **PLANNED** otherwise no control of type-1 error.
3. Like in standard meta-analysis, the quality of the conclusions is related to the input data and the choice of multiverse scenarios.

Future steps

## Future steps

- ▶ extending to multilevel and multivariate meta-analysis (the permutation approach is not straightforward)
- ▶ create an R package for multiverse meta-analyses with ad-hoc functions to analyze, report, and visualize the results
- ▶ create a data simulation framework for simulating a plausible multiverse for power and design analysis



# References

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Download the slides:

