# Politecnico di Milano Formal Methods for Concurrent and Real-Time Systems

Computer Controller Automatic Transmission (Mandatory Part, Optional Part coming soon)

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1 CCAT CLASS 5

#### 1 CCAT Class

The ComputerControlledAutomaticTransmission class is formalized thanks to the code reported in Listing 1 while Figure 1 shows the big picture of our complete designed.

Listing 1: ComputerControlledAutomaticTransmission.trio

```
class ComputerControlledAutomaticTransmission
1
2
3
   import:
4
       HydraulicSystem,
5
       Planetary Gear Set,
       TransmissionControlUnit,
6
7
       VehicleSpeedSensor.
       EngineSpeedSensor;
8
9
10
   signature:
11
12
   visible:
13
       torqueConverterState,
       vehicleSpeed,
14
       engineSpeed;
15
16
17
   temporal domain: real;
18
19
   domains:
20
       TorqueConverterState: { Attached , Detached };
21
22
   items:
23
       TD total torqueConverterState: TorqueConverterState;
24
       TD total vehicleSpeed: integer;
25
       TD total engineSpeed: integer;
26
27
   modules:
       hydraulicSystem: HydraulicSystem;
28
29
       planetaryGearSet: PlanetaryGearSet;
       transmissionControlUnit: TransmissionControlUnit;
30
31
       vehicleSpeedSensor: VehicleSpeedSensor;
       engineSpeedSensor: EngineSpeedSensor;
32
33
34 | connections :
35
       (direct EngineSpeedSensor.actualSpeed, engineSpeed)
       (direct vehicleSpeedSensor.actualSpeed, vehicleSpeed)
36
```

```
37
        (direct planetaryGearSet.transmissionShaftState,
           torqueConverterState)
38
39
        (direct planetary Gear Set. gear Shift,
           hydraulicSystem . gearShift )
        (direct planetary Gear Set. gear Drive,
40
           hydraulicSystem . gearDrive )
        (direct planetary Gear Set. gear Park,
41
           hydraulicSystem.gearPark)
        (direct planetary Gear Set. gear Reverse,
42
           hydraulicSystem . gearReverse )
        (direct hydraulicSystem.controlGearShift,
43
           transmissionControlUnit.controlGearShift)
44
        (direct transmissionControlUnit.receiveEngineSpeed,
           engineSpeedSensor.sendSpeed)
        (direct transmissionControlUnit.receiveVehicleSpeed,
45
           vehicleSpeedSensor.sendSpeed)
46
47
   end
```

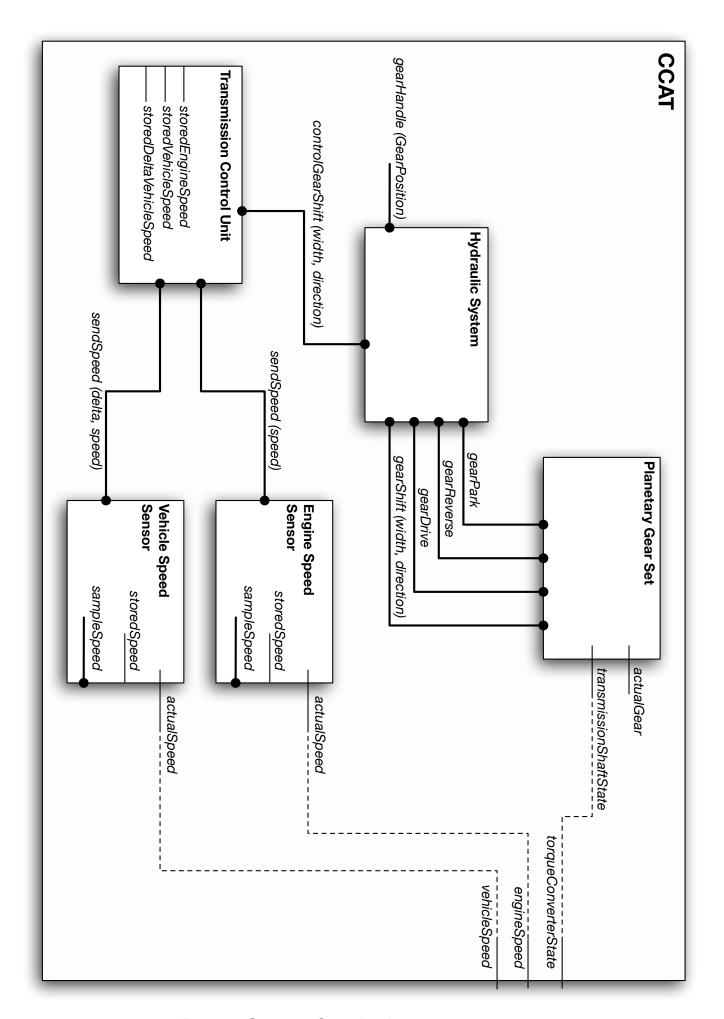


Figure 1: Computer Controller Automatic Transmission

## 2 Vehicle/EngineSpeedSensor Classes

The VehicleSpeedSensor is formalized thanks to the code reported in Listing 2 while the EngineSpeedSensor is formalized thanks to the code reported in Listing 3.

During the formalization of sensors we decided to simplify the design assuming that every time a sampleSpeed event occurs the state variable actualSpeed - which is time dependent and total - is automatically updated with the actual measured speed. This means we don't provide any axioms formalizing this behavior.

Moreover, we specified the starting point of the constant frequency sample chain saying that sometimes in the past there was a sampleSpeed occurrence. Further more, we guarante that sampleSpeed events will accure at constant frequency. In addition, if the sensor has memory we imposed that the storedValue is equal to 0. These can be consider just like the "initial conditions" of the system.

At the end, we guaranteed a sensor performs the needed action if and only if a sample event occur.

We didn't write any axioms specifying the fact that a sendSpeed event is mutually exclusive with itself due to the total time dependent parameter it accepts.

Listing 2: VehicleSpeedSensor.trio

```
class VehicleSpeedSensor (const sampleInterval, const
1
      sampleDelay)
2
3
   signature:
4
5
   visible:
6
        actualSpeed,
7
       sendSpeed;
8
9
   temporal domain: real;
10
11
   items:
12
       TI sampleInterval: real;
13
       TI sampleDelay: real;
       TD total storedSpeed: integer;
14
15
       TD total actualSpeed: integer;
       event sendSpeed (integer, integer);
16
17
        event sampleSpeed;
18
```

```
19 axioms:
   vars:
20
21
       deltaSpeed: integer;
22
       speed: integer;
23
   formulae:
24
       SpeedValues:
25
            actualSpeed >= 0 and storedSpeed >= 0;
26
27
       BeginSample:
28
           SomP (storedSpeed = 0 & sampleSpeed);
29
30
       Sampling Definition:
31
           sampleSpeed implies Futr (sampleSpeed,
               sampleInterval) and not Lasts (sampleSpeed,
               sampleInterval);
32
33
       SamplingAction:
34
            sampleSpeed implies Futr (deltaSpeed = actualSpeed
              - storedSpeed and speed = actualSpeed and
               sendSpeed (deltaSpeed, speed) and Lasts
               (storedSpeed = actualSpeed, sampleInterval),
               sampleDelay);
35
36
       SendSpeed:
37
            deltaSpeed = actualSpeed - storedSpeed and
               actualSpeed = speed and sendSpeed (deltaSpeed,
               speed) implies Past (sampleSpeed, sampleDelay);
38
39
   end
```

Listing 3: EngineSpeedSensor.trio

```
class EngineSpeedSensor (const sampleInterval, const
1
      sampleDelay)
2
3
   signature:
4
   visible: actualSpeed, sendSpeed;
5
6
   temporal domain: real;
7
8
9
   items:
10
       TI sampleInterval: real;
       TI sampleDelay: real;
11
```

```
12
       TD total actualSpeed: integer;
13
       event sendSpeed (integer);
       event sampleSpeed;
14
15
16 axioms:
17
   vars:
18
       speed: integer;
19 formulae:
20
       SpeedValues:
21
            actualSpeed >= 0;
22
23
       BeginSample:
24
           SomP (sampleSpeed);
25
26
        Sampling Definition:
            sampleSpeed implies Futr (sampleSpeed,
27
               sampleInterval) and not Lasts (sampleSpeed,
               sampleInterval);
28
29
       SampleSpeedActions:
30
            sampleSpeed implies Futr (actualSpeed = speed and
               sendSpeed (speed), sampleDelay);
31
32
       SendSpeed:
            actualSpeed = speed and sendSpeed (speed) implies
33
               Past (sampleSpeed, sampleDelay);
34
35
   end
```

## 3 PlanetaryGearSet Class

The *PlanetaryGearSet* class is formalized thanks to the code reported in Listing 4.

The Planetary Gear Set guarantees that every time a gear shift event occurs the actualGear will be maintained until the shift is finished.

Inside this component are defined all axioms limiting gear shifts to effective ones only (e.g. it is impossibile to shift down a gear if actualGear is First). The Planetary Gear Set permits to shift up to two gear at the same time (as the specification asks), however, the Transmission Control Unit doesn't use this possibility because in a real Planetary Gear Set this is not possibile.

Moreover, through the formalization of the Planetary Gear Set we impose that we can't receive a gear shift event if we are in the middle of a gear shift. Different gear shifting times are defined for different gears and different steps.

The gears Drive, Park, and Reverse can be selected if and only if the transmission shaft is decoupled from the engine.

The state of the Planetary Gear Set changes if and only if an event occurs.

Listing 4: PlanetaryGearSet.trio

```
class PlanetaryGearSet (const singleGearShiftDelay, const
       dualGearShiftDelay, const driveGearShiftDelay, const
       parkGearShiftDelay, const reverseGearShiftDelay)
2
3
   signature:
4
5
   visible:
6
       actualGear.
7
       transmissionShaftState;
8
        gearShift,
9
        gearDrive,
        gearPark,
10
11
        gearReverse,
12
   temporal domain: real;
13
14
15
16
        Gear: {First, Second, Third, Park, Reverse};
        TransmissionShaftState: { Attached, Detached };
17
18
        ShiftWidth: 1..2;
        ShiftDirection: {Up, Down};
19
20
21
   items:
22
       TI singleGearShiftDelay: real;
```

```
23
       TI dualGearShiftDelay: real;
       TI driveGearShiftDelay: real;
24
25
       TI parkGearShiftDelay: real;
26
       TI reverseGearShiftDelay: real;
27
       TD total actualGear: Gear:
       TD total transmissionShaftState:
28
           TransmissionShaftState:
29
       event gearShift (ShiftWidth, ShiftDirection);
30
       event gearDrive;
       event gearPark;
31
32
       event gearReverse;
33
34
  axioms:
35
   vars:
       gearShiftWidth: ShiftWidth;
36
37
       gearShiftWidth2: ShiftWidth;
38
       gearShiftDirection: ShiftDirection;
       gearShiftDirection2: ShiftDirection;
39
40
       gear: Gear;
41
   formulae:
42
       Annotations:
43
            actualGear = Park implies transmissionShaftState =
               Detached:
44
45
       GearDriveShift:
            (actualGear = Reverse and gearDrive implies (Lasts
46
               (actualGear = Reverse, driveGearShiftDelay) and
               Futr (actualGear = First,
               driveGearShiftDelay))) and
47
            (actualGear = Park and gearDrive implies (Lasts
               (actualGear = Park, driveGearShiftDelay) and
               Futr (actualGear = First,
               driveGearShiftDelay))) and
48
            (actualGear = First or actualGear = Second or
               actualGear = Third implies not gearDrive) and
            (gearDrive iff transmissionShaftState = Detached);
49
50
        GearShiftsFirst:
51
52
            (actualGear = First implies Alw (not gearDrive and
               not ex gearShiftWidth (gearShiftDirection = Down
                and gearShift (gearShiftWidth,
               gearShiftDirection)))) and
53
            (actualGear = First and gearShiftWidth = 1 and
```

```
gearShiftDirection = Up and gearShift
               (gearShiftWidth, gearShiftDirection) implies
               Lasts (actualGear = First,
               singleGearShiftDelay) and Futr (actualGear =
              Second, singleGearShiftDelay)) and
           (actualGear = First and gearShiftWidth = 2 and
54
               gearShiftDirection = Up and gearShift
               (gearShiftWidth, gearShiftDirection) implies
               Lasts (actualGear = First, dualGearShiftDelay)
              and Futr (actualGear = Third,
               dualGearShiftDelay);
55
       GearShiftsSecond:
56
           (actualGear = Second implies Alw (not gearDrive and
57
                not gearPark and not gearReverse and not ex
               gearShiftDirection (gearShiftWidth = 2 and
               gearShift (gearShiftWidth,
               gearShiftDirection)))) and
           (actualGear = Second and gearShiftWidth = 1 and 
58
               gearShiftDirection = Up and gearShift
               (gearShiftWidth, gearShiftDirection) implies
               Lasts (actualGear = Second,
               singleGearShiftDelay) and Futr (actualGear =
               Third, singleGearShiftDelay)) and
           (actualGear = Second and gearShiftWidth = 1 and
59
               gearShiftDirection = Down and gearShift
               (gearShiftWidth, gearShiftDirection) implies
               Lasts (actualGear = Second,
               singleGearShiftDelay) and Futr (actualGear =
               First , singleGearShiftDelay ) );
60
61
       GearShiftsThird:
62
           (actualGear = Third implies Alw (not gearDrive and
              not gearPark and not gearReverse and not ex
               gearShiftWidth (gearShiftDirection = Up and
               gearShift (gearShiftWidth,
               gearShiftDirection)))) and
63
           (actualGear = Third and gearShiftWidth = 1 and 
               gearShiftDirection = Down  and  gearShift
               (gearShiftWidth, gearShiftDirection) implies
               Lasts (actualGear = Third,
               singleGearShiftDelay) and Futr (actualGear =
              Second, singleGearShiftDelay)) and
```

```
(actualGear = Third and gearShiftWidth = 2 and
64
               gearShiftDirection = Down and gearShift
               (gearShiftWidth, gearShiftDirection) implies
               Lasts (actualGear = Third, dualGearShiftDelay)
              and Futr (actualGear = First,
               dualGearShiftDelay));
65
66
       GearShiftsReverse:
67
           (actualGear = Reverse implies Alw (not gearReverse
              and all gearShiftWidth, gearShiftDirection (not
               gearShift (gearShiftWidth,
               gearShiftDirection)))) and
           (actualGear = Reverse implies SomF (gearDrive or
68
               gearPark)) and (actualGear = First and
               gearReverse implies Lasts (actualGear = First,
               reverseGearShiftDelay) and Futr (actualGear =
               Reverse, reverseGearShiftDelay)) and
           (actualGear = Park and gearReverse implies Lasts
69
               (actualGear = Park, reverseGearShiftDelay) and
               Futr (actualGear = Reverse,
               reverseGearShiftDelay)) and
70
           (gearReverse iff transmissionShaftState =
               Detached):
71
72
       GearShiftsPark:
           (actualGear = Park implies Alw (not gearPark and
73
               all gearShiftWidth, gearShiftDirection (not
               gearShift (gearShiftWidth,
               gearShiftDirection)))) and
74
           (actualGear = Park implies SomF (gearDrive or
               gearReverse)) and
           (actualGear = First and gearPark implies Lasts
75
               (actualGear = First, parkGearShiftDelay) and
              Futr (actualGear = Park, parkGearShiftDelay))
76
           (actualGear = Reverse and gearPark implies Lasts
               (actualGear = Reverse, parkGearShiftDelay) and
              Futr (actualGear = Park, parkGearShiftDelay)Futr
               (actualGear = Park, parkGearShiftDelay)) and
77
           (gearPark iff transmissionShaftState = Detached);
78
       GearShiftsTimings:
79
           all gearShiftDirection ((actualGear = First or
               actualGear = Second or actualGear = Third) and
```

```
gearShiftWidth = 1 and gearShift
              (gearShiftWidth, gearShiftDirection) implies not
               Lasts (gearDrive or gearPark or gearReverse or
              ex gearShiftWidth2, gearShiftDirection2
              (gearShift (gearShiftWidth2,
              gearShiftDirection2)), singleGearShiftDelay))
80
           all gearShiftDirection ((actualGear = First or
              actualGear = Third) and gearShiftWidth = 2 and
              gearShift (gearShiftWidth, gearShiftDirection)
              implies not Lasts (gearDrive or gearPark or
              gearReverse or ex gearShiftWidth2,
              gearShiftDirection2 (gearShift (gearShiftWidth2,
               gearShiftDirection2)), dualGearShiftDelay)) and
           ((actualGear = Reverse and gearDrive) implies not
81
              Lasts (gearDrive or gearPark or gearReverse or
              ex gearShiftWidth2, gearShiftDirection2
              (gearShift (gearShiftWidth2,
              gearShiftDirection2)), driveGearShiftDelay)) and
82
           ((actualGear = Reverse and gearPark) implies not
              Lasts (gearDrive or gearPark or gearReverse or
              ex gearShiftWidth2, gearShiftDirection2
              (gearShift (gearShiftWidth2,
              gearShiftDirection2)), parkGearShiftDelay)) and
83
           ((actualGear = Park and gearDrive) implies not
              Lasts (gearDriver or gearPark or gearReverse or
              ex gearShiftWidth2, gearShiftDirection2
              (gearShift (gearShiftWidth2,
              gearShiftDirection2)), driveGearShiftDelay)) and
           ((actualGear = Park and gearReverse) implies not
84
              Lasts (gearDrive or gearPark or gearReverse or
              ex gearShiftWidth2, gearShiftDirection2
              (gearShift (gearShiftWidth2,
              gearShiftDirection2)), reverseGearShiftDelay));
85
86
       Nothing:
87
           all gear (actualGear = gear and not (all
              gearShiftWidth, gearShiftDirection (gearShift
              (gearShiftWidth, gearShiftDirection)) or
              gearDrive or gearPark or gearReverse) implies
              UpToNow (actualGear = gear) and NowOn
              (actualGear = gear));
88
```

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**end** 

## 4 HydraulicSystem Class

The *HydraulicSystem* class is formalized thanks to the code reported in Listing 5.

The first assumption we made before modelling the Hydraulic System was that every valve and electrovalve configuration imposes the same fluid propagation delay; this means that for every command that the Hydraulic System propagates the delay will always be the same. This behavior is formalized with the time independent constant fluidPropagationDelay.

The manual valve, which permit the driver to manually select the gear mode, is modelled thanks to the gearHandle event and the GearHandle axiom. During the time in which the Hydraulic System propagate a command there can be no gearHandle event which somehow means the fluid propagation is faster then the driver reaction time (which is a realistic assumption).

Moreover, thanks to the MutualExclusion axiom, it's impossibile to generate two gearHandle event at the same time which means that the gear handle can't be for example in Park and Drive mode at the same instant.

Listing 5: HydraulicSystem.trio

```
class HydraulicSystem (const fluidPropagationDelay)
 1
 2
 3
   signature:
 4
 5
   visible:
 6
        gearHandle,
 7
        gearShift,
 8
        gearDrive,
 9
        gearPark,
10
        gearReverse,
11
        controlGearShift;
12
   temporal domain: real;
13
14
15
   domains:
16
        GearPosition: {Drive, Park, Reverse};
17
        ShiftWidth: 1..2;
18
        ShiftDirection: {Up, Down};
19
20
   items:
        TI fluidPropagationDelay: real;
21
22
        event gearHandle (GearPosition);
23
        event gearShift (ShiftWidth, ShiftDirection);
24
        event gearDrive;
```

```
25
       event gearPark;
26
       event gearReverse;
27
       event controlGearShift (ShiftWidth, ShiftDirection);
28
29
   axioms:
30
   vars:
31
       gear: GearPosition;
32
       gear2: GearPosition;
33
       gearShiftWidth: ShiftWidth;
       gearShiftWidth2: ShiftWidth;
34
35
        gearShiftDirection: ShiftDirection;
36
       gearShiftDirection2: ShiftDirection;
37
   formulae:
       GearHandleCommand:
38
39
            (gear = Drive and gearHandle (gear) implies not
               Lasts (all gear2 (gear2 \Leftrightarrow gear implies
               gearHandle (gear2) or ex gearShiftWidth,
               gearShiftDirection (controlGearShift
               (gearShiftWidth, gearShiftDirection))),
               fluidPropagationDelay) and Futr (gearDrive,
               fluidPropagationDelay) and
40
            (gear = Park and gearHandle (gear) implies not
               Lasts (all gear2 (gear2 \Leftrightarrow gear implies
               gearHandle (gear2) or ex gearShiftWidth,
               gearShiftDirection (controlGearShift
               (gearShiftWidth, gearShiftDirection))),
               fluidPropagationDelay) and Futr (gearPark,
               fluidPropagationDelay) and
41
            (gear = Reverse and gearHandle (gear) implies not
               Lasts (all gear2 (gear2 <> gear implies
               gearHandle (gear2) or ex gearShiftWidth,
               gearShiftDirection (controlGearShift
               (gearShiftWidth, gearShiftDirection))),
               fluidPropagationDelay) and Futr (gearReverse,
               fluid Propagation Delay);
42
       PropagateGearShiftCommand:
43
44
            all gearShiftWidth, gearShiftDirection
               (controlGearShift (gearShiftWidth,
               gearShiftDirection) implies not Lasts (gearDrive
                or gearPark or gearReverse or ex
               gearShiftWidth2, gearShiftDirection2
               (controlGearShift (gearShiftWidth2,
```

```
gearShiftDirection2)), fluidPropagationDelay)
and Futr (gearShift (gearShiftWidth,
gearShiftDirection), fluidPropagationDelay));

45
46
47
MutualExclusions:
all gear (gearHandle (gear) implies all gear2 (gear
$<> gear2 implies not gearHandle (gear2)));

48
49 end
```

#### 5 TransmissionControlUnit Class

The *TransmissionControlUnit* class is formalized thanks to the code reported in Listing 6.

Our first formalization of the Transmission Control Unit didn't take in account the possibility to have asynchronous sensors; the latest version of the Transmission Control Unit permits to manage asynchronous sensors thanks to internal memory modelled with three time dependent total values.

When handle the necessity to scale gears till the First with the assumption that the human reaction is way slower than sampling frequency and mechanical reactions, so, when the vehicle stops, the axiom which handle the gear scale manage to be "active" the necessary amount of times to scale all the gears.

The Transmission Control Unit guarantees that it doesn't raise more than one gear shift event per instant and it receives at most one event per instant from each sensor (this is described also in Section 2 and so guaranteed in VehicleSpeedSensor and EngineSpeedSensor class).

Listing 6: TransmissionControlUnit.trio

```
class TransmissionControlUnit
1
2
3
   signature:
4
5
   visible:
6
        controlGearShift.
7
        receiveEngineSpeed,
8
        receiveVehicleSpeed;
9
10
   temporal domain: real;
11
12
   domains:
        ShiftWidth: 1..2;
13
14
        ShiftDirection: {Up, Down};
15
16
   items:
17
       TD total storedEngineSpeed: integer;
       TD total storedDeltaVehicleSpeed: integer;
18
19
       TD total storedVehicleSpeed: integer;
20
        event controlGearShift (ShiftWidth, ShiftDirection);
        event receiveEngineSpeed (integer);
21
22
        event receiveVehicleSpeed (integer, integer);
23
24
   axioms:
25
   vars:
```

```
26
       engineSpeed: integer;
27
       engineSpeed1: integer;
28
       engineSpeed2: integer;
29
       deltaVehicleSpeed: integer;
30
       deltaVehicleSpeed1: integer;
31
       deltaVehicleSpeed2: integer;
32
       vehicleSpeed: integer;
33
       vehicleSpeed1: integer;
34
       vehicleSpeed2: integer;
35
       gearShiftWidth1: ShiftWidth;
       gearShiftWidth2: ShiftWidth;
36
37
       gearShiftDirection1: ShiftDirection;
       gearShiftDirection2: ShiftDirection;
38
39
   formulae:
40
       GearShifts:
41
           (receiveEngineSpeed (engineSpeed) and
               receiveVehicleSpeed (deltaVehicleSpeed,
               vehicleSpeed) and engineSpeed >= 3000 and
               vehicleSpeed > 0 implies gearShiftWidth1 = 1 and
                gearShiftDirection1 = Up and controlGearShift
               (gearShiftWidth1, gearShiftDirection1)) and
42
           (receiveEngineSpeed (engineSpeed) and all
               deltaVehicleSpeed, vehicleSpeed (not
               receiveVehicleSpeed (deltaVehicleSpeed,
               vehicleSpeed)) and engineSpeed >= 3000 and
               storedVehicleSpeed > 0 implies gearShiftWidth1 =
               1 and gearShiftDirection1 = Up and
               controlGearShift (gearShiftWidth1,
               gearShiftDirection1)) and
43
           (all engineSpeed (not receiveEngineSpeed
               (engineSpeed)) and receiveVehicleSpeed
               (deltaVehicleSpeed, vehicleSpeed) and
               storedEngineSpeed >= 3000 and vehicleSpeed > 0
               implies gearShiftWidth1 = 1 and
               gearShiftDirection1 = Up and controlGearShift
               (gearShiftWidth1, gearShiftDirection1)) and
44
           (receiveEngineSpeed (engineSpeed) and
               receiveVehicleSpeed (deltaVehicleSpeed,
               vehicleSpeed) and engineSpeed <= 1500 and
               deltaVehicleSpeed <= 0 implies gearShiftWidth1 =
               1 and gearShiftDirection1 = Down and
               controlGearShift (gearShiftWidth1,
               gearShiftDirection1)) and
```

```
45
           (receiveEngineSpeed (engineSpeed) and all
               deltaVehicleSpeed, vehicleSpeed (not
               receiveVehicleSpeed (deltaVehicleSpeed,
               vehicleSpeed)) and engineSpeed <= 1500 and
               storedDeltaVehicleSpeed <= 0 implies
               gearShiftWidth1 = 1 and gearShiftDirection1 = 1
              Down and controlGearShift (gearShiftWidth1,
               gearShiftDirection1)) and
46
           (all engineSpeed (not receiveEngineSpeed
               (engineSpeed)) and receiveVehicleSpeed
               (deltaVehicleSpeed, vehicleSpeed) and
               storedEngineSpeed <= 1500 and (deltaVehicleSpeed
               <= 0 or vehicleSpeed = 0) implies
               gearShiftWidth1 = 1 and gearShiftDirection1 = 1
              Down and controlGearShift (gearShiftWidth1,
               gearShiftDirection1)) and
47
           (receiveEngineSpeed (engineSpeed) and
               receiveVehicleSpeed (deltaVehicleSpeed,
               vehicleSpeed) and engineSpeed <= 1500 and
               deltaVehicleSpeed > 0 implies all
               gearShiftWidth1, gearShiftDirection1 (not
               controlGearShift (gearShiftWidth1,
               gearShiftDirection1))) and
           (receiveEngineSpeed (engineSpeed) and all
48
               deltaVehicleSpeed, vehicleSpeed (not
               receiveVehicleSpeed (deltaVehicleSpeed,
               vehicleSpeed)) and engineSpeed <= 1500 and
               storedDeltaVehicleSpeed >= 0 and
               storedVehicleSpeed > 0 implies all
               gearShiftWidth1, gearShiftDirection1 (not
               controlGearShift (gearShiftWidth1,
               gearShiftDirection1))) and
49
           (all engineSpeed (not receiveEngineSpeed
               (engineSpeed)) and receiveVehicleSpeed
               (deltaVehicleSpeed, vehicleSpeed) and
              storedEngineSpeed <= 1500 and deltaVehicleSpeed
              >= 0 and vehicleSpeed > 0 implies all
               gearShiftWidth1, gearShiftDirection1 (not
               controlGearShift (gearShiftWidth1,
               gearShiftDirection1))) and
50
           (receiveEngineSpeed (engineSpeed) and
               receiveVehicleSpeed (deltaVehicleSpeed,
               vehicleSpeed) and engineSpeed >= 1500 and
```

```
engineSpeed < 3000 implies all gearShiftWidth1,
               gearShiftDirection1 (not controlGearShift
              (gearShiftWidth1, gearShiftDirection1))) and
51
           (receiveEngineSpeed (engineSpeed) and all
               deltaVehicleSpeed, vehicleSpeed (not
               receiveVehicleSpeed (deltaVehicleSpeed,
               vehicleSpeed)) and engineSpeed >= 1500 and
               engineSpeed < 3000 implies all gearShiftWidth1,</pre>
               gearShiftDirection1 (not controlGearShift
               (gearShiftWidth1, gearShiftDirection1))) and
52
           (all engineSpeed (not receiveEngineSpeed
              (engineSpeed)) and receiveVehicleSpeed
               (deltaVehicleSpeed, vehicleSpeed) and
              storedEngineSpeed >= 1500 and storedEngineSpeed
              < 3000 implies all gearShiftWidth1,
               gearShiftDirection1 (not controlGearShift
              (gearShiftWidth1, gearShiftDirection1))) and
           (all engineSpeed (not receiveEngineSpeed
53
              (engineSpeed)) and all deltaVehicleSpeed,
               vehicleSpeed (not receiveVehicleSpeed
              (deltaVehicleSpeed, vehicleSpeed)) implies all
               gearShiftWidth1, gearShiftDirection1 (not
               controlGearShift (gearShiftWidth1,
               gearShiftDirection1));
54
55
       Receiving Event Action:
56
           all deltaVehicleSpeed1, vehicleSpeed1
              (receiveVehicleSpeed (deltaVehicleSpeed1,
               vehicleSpeed1) implies Until
               (storedDeltaVehicleSpeed = deltaVehicleSpeed1
              and storedVehicleSpeed = vehicleSpeed1, ex
               deltaVehicleSpeed2, vehicleSpeed2
              (receiveVehicleSpeed (deltaVehicleSpeed2,
               vehicleSpeed2)))) and
57
           all engineSpeed1 (receiveEngineSpeed
              (engineSpeed1) implies Until (storedEngineSpeed
              = engineSpeed1 , ex engineSpeed2
              (receiveEngineSpeed (engineSpeed2))));
58
59
       MutualExclusions:
60
           all gearShiftWidth1, gearShiftDirection1
              (controlGearShift (gearShiftWidth1,
               gearShiftDirection1) implies all
```

```
{\tt gearShiftWidth2} \;, \;\; {\tt gearShiftDirection2}
               (gearShiftWidth1 \Leftrightarrow gearShiftWidth2 and
               gearShiftDirection1 <> gearShiftDirection2
               implies not controlGearShift (gearShiftWidth2,
               gearShiftDirection2))) and
            all engineSpeed1 (receiveEngineSpeed
61
               (engineSpeed1) implies all engineSpeed2
               (engineSpeed2 <> engineSpeed1 implies not
               receiveEngineSpeed (engineSpeed2))) and
62
            all deltaVehicleSpeed1, vehicleSpeed1
               (receiveVehicleSpeed (deltaVehicleSpeed1,
               vehicleSpeed1) implies all deltaVehicleSpeed2,
               vehicleSpeed2 (deltaVehicleSpeed2 <>
               deltaVehicleSpeed1 and vehicleSpeed2 <>
               vehicleSpeed1 implies not receiveVehicleSpeed
               (deltaVehicleSpeed2, vehicleSpeed2)));
63
64
   end
```

### 6 Annotations

During the last phase of our modelling we decided not to formalize the *Torque Converter* and this decision depends on the way the Torque Converter works.

The Torque Converter is a mechanical component that works coupling and decoupling the *Transmission Shaft* and the *Engine Shaft*. It solves is duty without the necessity to receive commands from any component of the system and this is the cause we have decided to remove it from our model.

Anyway, the state of the Torque Converter is really important for the system since it gives information that permits to insert or not to insert some gears and other details that aren't taken into account in this project.

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## 7 Properties

#### Listing 7: Property 1

#### Listing 8: Property 2

```
\label{eq:gear} \begin{array}{lll} \text{gear} &=& \text{Park} & \textbf{and} & \text{gearHandle (gear)} & \textbf{and} & \text{Futr (actualGear} = \\ & \text{Park} \,, & \text{fluidPropagationDelay} \,+\, \text{parkGearShiftDelay)} & \textbf{iff} \\ & \text{Lasts (transmissionShaftState} &=& \text{Detached} \,, \\ & \text{fluidPropagationDelay} \,+\, \text{parkGearShiftDelay)} \end{array}
```