

Digital Control Technologies and Architectures - 01PDCYP, 01PDCOV, 01PDCLP

M. Canale

Laboratory practice 7

Objectives: MPC control design of CT systems using MPCtools, review on algebraic design.

Problem 1 (MPC design for zero-regulation of the state using MPCtools.)

Consider the mass-damper system introduced in Laboratory practice 4 described by the following state space representation in continuous time.

$$\begin{aligned}\dot{x}(t) &= \begin{bmatrix} 0 & 1 \\ 0 & -1 \end{bmatrix} x(t) + \begin{bmatrix} 0 \\ 1 \end{bmatrix} u(t), \quad x(0) = \begin{bmatrix} 1 \\ 0 \end{bmatrix} \\ y(t) &= \begin{bmatrix} 1 & 0 \end{bmatrix} x(t)\end{aligned}$$

Assume a sampling time $T_s = 0.05$ s and suppose that the system state can be measured. Design an MPC controller using MPCtools aimed at regulating to zero the state of the system (within a tolerance of 10^{-4}) considering a regulation time $t_{\text{reg}} \approx 2.5$ s with a tolerance of 5% and accounting for the following constraints:

$$\begin{cases} |u(k+i|k)| \leq 5.5, \quad i = 0, \dots, H_p - 1 \\ |\Delta u(k+i|k)| \leq 3, \quad i = 0, \dots, H_p - 1 \end{cases}$$

Develop the design procedure through

- MatLab script file named `sxxxxxxx_design_MPC.m` following the naming described below for the relevant transfer functions and variables:
 - $Q \rightarrow$ weight matrix Q ;
 - $R \rightarrow$ weight matrix R ;
 - $H_p \rightarrow$ prediction horizon H_p ;
 - $H_c \rightarrow$ control horizon H_c ;
 - $T_s \rightarrow$ sampling time T_s .
- Simulink file named `sxxxxxxx_sim_MPC.slx`.

Save all the design results in the `sxxxxxxx_MPC.mat` file using the statement `save sxxxxxxx_MPC` at the MatLab prompt `>>`

`→ >> save sxxxxxxx_MPC`

In all of the above files, replace `sxxxxxxx` with your own id.

Problem 2 (Review on Algebraic design)

Given the continuous time LTI system described by the transfer function,

$$G_{cont}(s) = \frac{40}{s^2 + 4s - 10}$$

design a digital controller $C(z)$ using a 1dof architecture to meet the following requirements:

- 1.a $|y_{d_2}^\infty| \leq 5 \cdot 10^{-4}$ in the presence of disturbance $d_2(k T_s) = 0.1 k T_s$;
- 1.b $|y_{d_1}^\infty| \leq 5 \cdot 10^{-5}$ in the presence of disturbance $d_1(k T_s) = 0.7 \varepsilon(k T_s)$;
2. $\hat{s} \leq 25\%$;
3. $t_{s,1\%} \leq 2.5$ s;
4. $t_r \leq 0.9$ s.

Assume a sampling time $T_s = 5$ ms. (Hint: in case of unsatisfaction of the requirement on \hat{s} , try to reduce the time constant of the additional poles)

Develop the design procedure through

- MatLab script file named `sxxxxxxx_design.m` following the naming described below for the relevant transfer functions and variables:
 - `Gcont` \rightarrow continuous time plant transfer function $G_{cont}(s)$;
 - `G` \rightarrow discrete time plant transfer function $G(z)$;
 - `C` \rightarrow discrete time cascade controller transfer function $C(z)$;
 - `Ts` \rightarrow sampling time T_s ;
 - `zeta` \rightarrow damping coefficient ζ , `wn` \rightarrow natural frequency ω_n ;
 - `M_S` \rightarrow Sylvester matrix M_S .
- Simulink file named `sxxxxxxx_sim.slx`.

Save all the design results in the `sxxxxxxx.mat` file using the statement `save sxxxxxxx` at the MatLab prompt `>>`

`\rightarrow >> save sxxxxxxx`

In all of the above files, replace `sxxxxxxx` with your own id.