



photos to their satisfaction, any further cropping would not be desirable.

As mentioned above, our method amounts to the construction of a certain kind of tree structure, and this description is divided into two parts. Section 2.1 describes how to obtain the tree; and Sec. 2.2 describes how to render an output page from a tree (*i.e.*, compute a location and an absolute area for each photo).

## 2.1. Generating the binary tree

We generate the binary tree by adding photos one at a time, as illustrated in Fig. 2. We will fill in more details about the tree structure as we go along; but for now, it is sufficient to know that each node corresponds to a box in the layout. Each interior node represents a bounding box around the boxes of its children, and each terminal node represents a cell where a photo is placed.

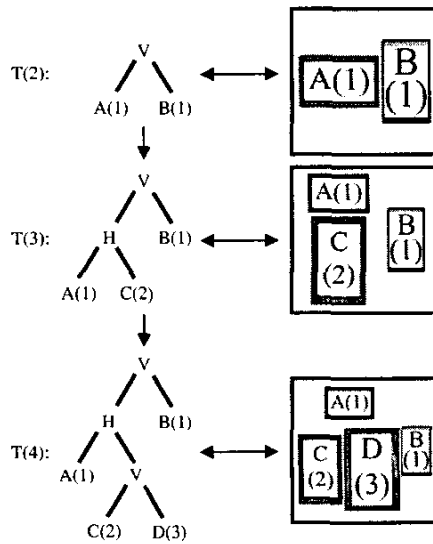


Fig. 2. Page layout generation process. Numbers in parentheses are relative areas.

We start with a page layout having only one photo, and we add photos one at a time until all photos are included. Formally, denoting the total number of photos as  $N$ , the page layout is determined as the last in an increasing sequence of binary trees

$$T(1), T(2), \dots, T(N)$$

where  $T(k)$  for  $k \geq 1$  denotes a tree with  $k$  terminal nodes. Notice that each of the intermediate trees  $\{T(k) : 1 \leq k \leq N-1\}$  generates a viable layout.

The way we add the next photo to the page is to introduce a new cell in the previous layout. Formally, this is accomplished by augmenting the previous tree. As illustrated in the figure, we select a subtree, and then displace the subtree with a new internal node. The new internal node becomes the parent of (a) a new terminal node corresponding to the new cell, and (b) the subtree that was displaced. (In the figure, the “selected subtrees” happen to be terminal nodes; but generally, any subtree could be selected, including subtrees rooted at internal nodes.)

To choose which cell which we introduce in the previous layout, we evaluate a collection of candidate layouts, where each candidate layout is the previous layout with the next photo inserted into a different new cell, and we select the cell for which the resulting layout has a highest score. To put this formally, assume that the  $k$ -th intermediate layout, represented with the tree  $T(k)$ , has a set  $\mathcal{L}$  of possible new cells. We will write the tree structure  $T(k)$  augmented by adding new cell  $l \in \mathcal{L}$  as  $T(k; l)$ . Then the next intermediate layout is determined as

$$T(k+1) = T(k; L)$$

where

$$L = \arg \max_{l \in \mathcal{L}} [\text{score}(T(k; l))]$$

and where  $\text{score}(\cdot)$  is the scoring function mentioned above.

Notice that the cost of adding each next photo to the layout increases linearly with the number of photos. To be more precise, for intermediate tree  $T(k)$ ,  $|\mathcal{L}| = 2(2k-1)$ , since there are  $(2k-1)$  nodes in  $T(k)$  and the new cell can be positioned either vertically or horizontally relative to the box of the displaced subtree. However, pages tend to have sufficiently few photos that the computational cost of evaluating all possible candidate layouts is not excessive.

## 2.2. Rendering the output page from the binary tree

The input to this process, illustrated in Fig. 3, is a tree structure where each terminal node has an aspect ratio and a relative area proportion, and each interior node indicates either a horizontal or vertical division. The first step is to characterize bounding boxes for the nodes, and the second step is to allocate a precise region of page space to each node. These regions are nested like the tree structure. We will refer to the regions allocated to terminal nodes as *cells*. Once a cell is known, the position of the photo assigned to it is determined by centering the photo in the cell. The area of the photo is figured using a formula given below.

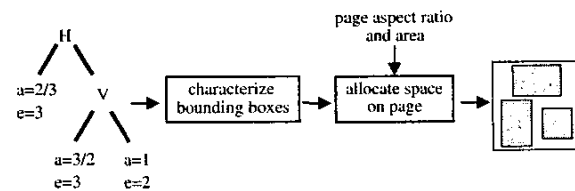


Fig. 3. How to render an output page from a tree structure.

### 2.2.1. Characterizing bounding boxes

The objective of this step is to compute an aspect ratio and a relative area for each node in the tree. This is only necessary for the interior nodes, since the terminal nodes are associated with photos, whose aspects and relative areas are fixed. Each bounding box is determined by the boxes it encloses, so this process starts at the terminal nodes and works toward the root, in the order of a depth-first search as illustrated in Fig. 4.

The formulas for the aspect and relative area of any interior node are given below. To understand these formulas intuitively, notice that for any rectangle with aspect  $a$  and relative area  $e$ , the quantities  $\sqrt{ae}$  and  $\sqrt{e/a}$  are the *relative height* and *relative width* respectively, in the same way that  $e$  is the relative area.

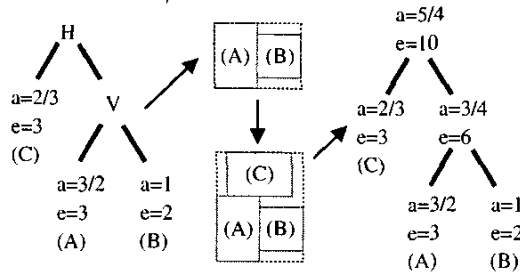


Fig. 4. Computing bounding boxes.

The aspect ratio  $a$  and relative area  $e$  for any interior node are functions of the aspects and relative areas of its two children. Denote as  $(a_r, e_r)$  the aspect and relative area of the right-hand child, and  $(a_l, e_l)$  for the left. Then if the two children represent boxes arranged side by side,

$$a = \frac{\sqrt{a'l'e'}}{\sqrt{e_l/a_l} + \sqrt{e_r/a_r}} \quad (1)$$

$$e = \sqrt{a'l'e'} \left( \sqrt{e_l/a_l} + \sqrt{e_r/a_r} \right) \quad (2)$$

where

$$\sqrt{a'l'e'} = \max_{i \in \{r, l\}} [\sqrt{a_i e_i}] \quad (3)$$

The aspect ratio in (1) is the ratio of a relative height divided by the sum of two relative widths, and the relative area in (2) is the product of the same. Finding the maximum in (3) determines which box is relatively taller, and therefore governs the height of the box. Now, if the two children represent boxes arranged one on top of the other,

$$a = \frac{\sqrt{a_l e_l} + \sqrt{a_r e_r}}{\sqrt{e'/a'}} \quad (4)$$

$$e = (\sqrt{a_l e_l} + \sqrt{a_r e_r}) \sqrt{e'/a'}$$

where

$$\sqrt{e'/a'} = \max_{i \in \{r, l\}} [\sqrt{e_i/a_i}] \quad (4)$$

In this case, (4) determines which box is relatively wider, and therefore governs the width of the box.

The bounding box of the root is particularly important because it conveys the shape and relative area of the entire layout. We refer to it as the *principal bounding box*.

Since relative areas are consistent throughout the tree, we can score a layout as soon as the bounding boxes are known. For a tree  $T$ , the fraction of the page covered by photo is

$$\text{score}(T) = \mathcal{G} \frac{\sum_{i=1}^N e_i \min\{a_{pbb}, a_{page}\}}{e_{pbb} \max\{a_{pbb}, a_{page}\}}$$

where  $\mathcal{G}$  is a positive constant described below;  $N$  is the number of photos;  $e_i$  is the relative area of photo  $i$ ;  $e_{pbb}$  and  $a_{pbb}$  are the relative area and aspect of the principal bounding box; and  $a_{page}$  is the aspect of the usable area of the page.

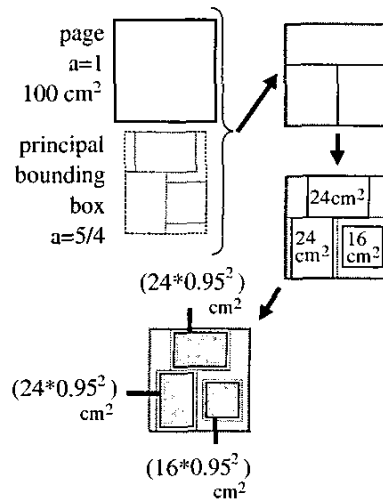


Fig. 5. Allocating space on the page.

## 2.2.2. Allocating regions of space to nodes

This process has two steps as shown in Fig. 5. First, we divide the page into cells; and second, we position each photo in its cell.

To divide the page into cells, we split rectangles as illustrated in Fig. 1, starting with the entire usable area of the page as the first rectangle. Each split is accomplished by drawing a line segment for an interior node. Starting at the root, we work down, in the order of a breadth-first search.

In the case of an interior node corresponding to a vertical division, the task is to select a horizontal position along the width of the available region. Denoting the position with a scalar  $x \in (0, 1)$ , where  $x = 0$  would represent the leftmost position and  $x = 1$  the rightmost, we compute

$$x = \frac{\sqrt{e_l/a_l}}{\sqrt{e_l/a_l} + \sqrt{e_r/a_r}}$$

where  $a_l, e_l$  and  $a_r, e_r$  are the aspects and relative areas of the bounding boxes for the left and right children of the interior node. Notice this formula makes direct use of relative widths as proportions. The analogous formula for a horizontal division uses the relative heights. Denoting the position with a scalar  $y \in (0, 1)$ , where  $y = 0$  would represent the bottom position and  $y = 1$  the top, we compute

$$y = \frac{\sqrt{e_b/a_b}}{\sqrt{e_b/a_b} + \sqrt{e_t/a_t}}$$

where  $a_b, e_b$  and  $a_t, e_t$  are respectively the aspect and relative area of the bounding boxes for the bottom and top children of the interior node.

The area  $A_i$  for photo  $i$  is computed from the relative area of the photo assigned to it:

$$A_i = \mathcal{G} \frac{e_i}{e_{pbb}} A_{pbb},$$

where  $A_{pbb}$  is an area for the principal bounding box, computed

$$A_{pbb} = A_{page} \frac{\min\{a_{pbb}, a_{page}\}}{\max\{a_{pbb}, a_{page}\}}$$

with  $A_{\text{page}}$  the area of the usable page space.  $G$  is a scalar used to shrink each photo from the maximum area it could have as dictated by parameters of the tree. Setting  $G$  between 0 and 1 creates a buffer of space around the photo. We used  $G = 0.95^2$ .

### 3. RESULTS, DISCUSSION AND CONCLUSIONS

Figure 6 presents two different layouts of the same photo collection. For the first layout, we divided the photos into groups of four, and we used a page aspect ratio of  $8\frac{1}{2} \times 11$ . For the second layout, we used a square page to simulate an album page or a compact disc (CD) case insert. Notice that the photos are arranged efficiently; for example, the wide photo at bottom of the first  $8\frac{1}{2} \times 11$  page is situated low, affording greater space for the other three photos. Also, on any given page in this figure, all photos have the same area, regardless of their aspects. This is a deliberate result of the fact that we fixed the photo relative areas to be equal.

See Fig. 7 for three layouts that have the same photos, but different assignments of relative areas. For example, in the layout at left, the area of photo A is twice that of photo B, and  $\frac{2}{3}$  the area of photo D. This demonstrates that the assignment of relative areas to photos strongly influences the layout structure as a whole.

Figure 8 shows layouts of the same photo collection, one from software package Kodak Memory Albums (KMA), version 1.4.64 (2001); and two from the proposed result, using different relative area assignments. We selected KMA for this comparison because layouts from KMA suggest it either uses a large database of templates, or it is adaptive and does not rely on templates. Notice the areas of the photos in the layouts. We feel this comparison reinforces the conclusion that encouraging layouts can be obtained while maintaining explicit control over relative areas.

The proposed approach is somewhat rigid in that photo aspects and relative areas are not allowed to vary; photos are not allowed to overlap; and photos are not rotated. Allowing any of these attributes to change could significantly improve results. In particular, we could allow the  $a$ 's and  $e$ 's of terminal nodes to vary within tolerances. Allowing  $e$ 's to change would affect photo area ratios, and allowing  $a$ 's to vary would require cropping photos. Needless to say, more sophisticated scoring functions derived from aesthetic principles could also allow better layouts.

We assume photos have sufficient pixel resolution to guarantee satisfactory image quality, and we ignore restrictions around viewing distance and rendered pixels per inch. Empirically, this has not been a problem with 3-, 4- and 5-megapixel photos rendered on typical displays and printed pages small enough to hold in the hand.

The order in which photos are provided to the system clearly influences which layout is generated. As an attentive reviewer pointed out, it would be interesting to investigate whether there is an optimal ordering.

We have presented a fast method for arranging photos on a page, while providing explicit control over relative areas. We have found it to be reliable for generating satisfactory layouts quickly. Still, many layouts leave some room for improvement, and we hope to explore ways these layouts can be optimized.

### 4. REFERENCES

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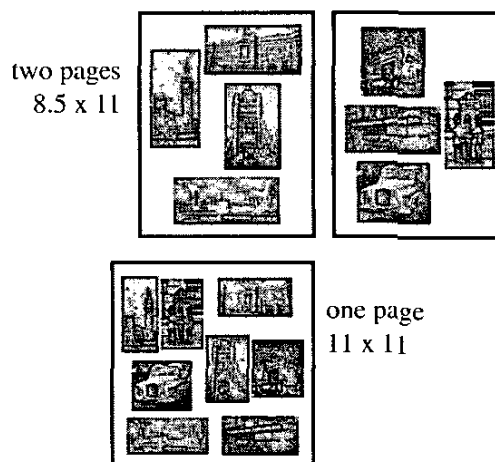


Fig. 6. Two layouts of the same photo collection, generated by the proposed method. The relative areas of the photos were all equal.

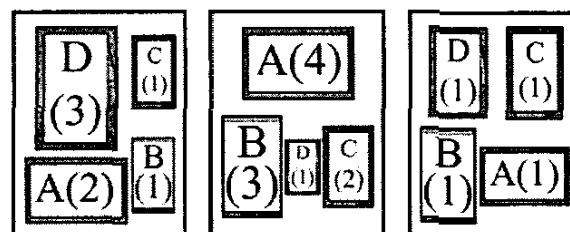


Fig. 7. Three layouts of the same four photos, with different relative area assignments.

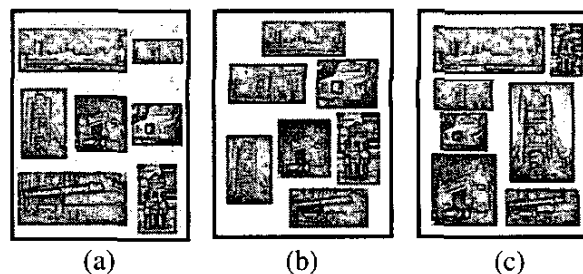


Fig. 8. Photo collection layouts from (a) Kodak Memory Albums version 1.4.64 (2001); and proposed method using relative areas (b) all equal, and (c) varying between 2 and 7.

Space-Filling Approach," *ACM Transactions on Graphics*, vol. 11, no. 1, pp. 92–99, January 1992.

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