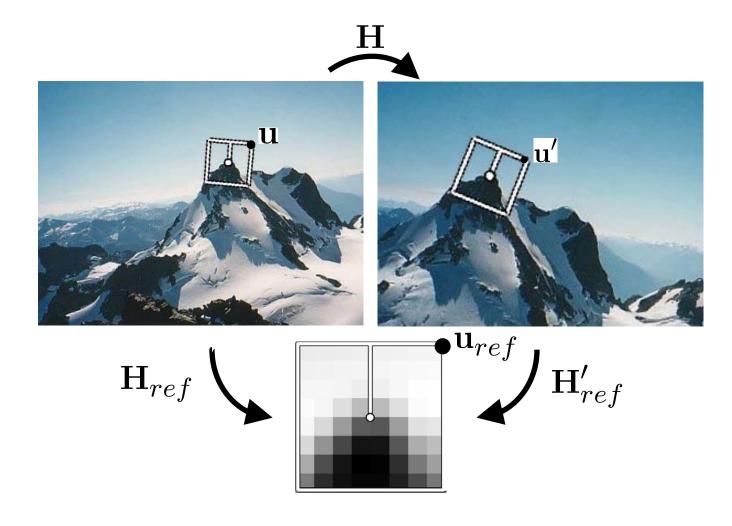
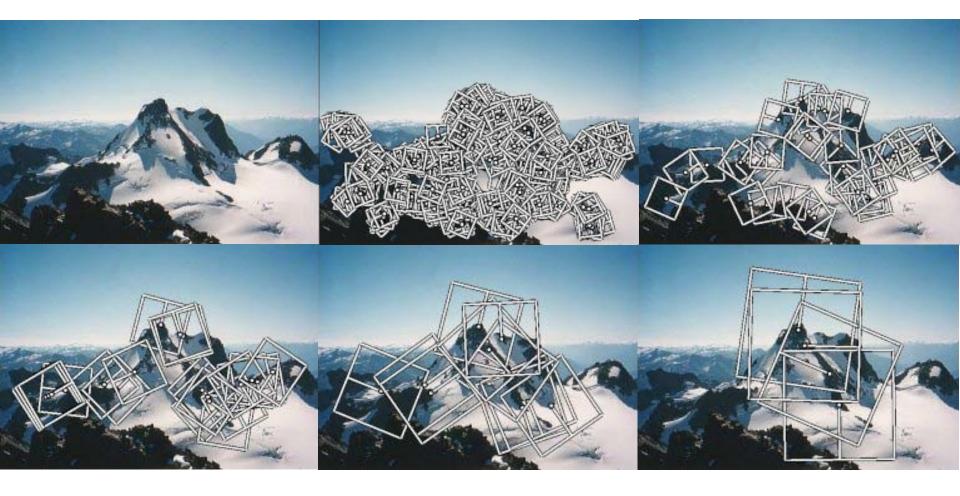
# The SIFT (Scale Invariant Feature Transform) Detector and Descriptor

developed by David Lowe University of British Columbia Initial paper ICCV 1999 Newer journal paper IJCV 2004

## Review: Matt Brown's Canonical Frames

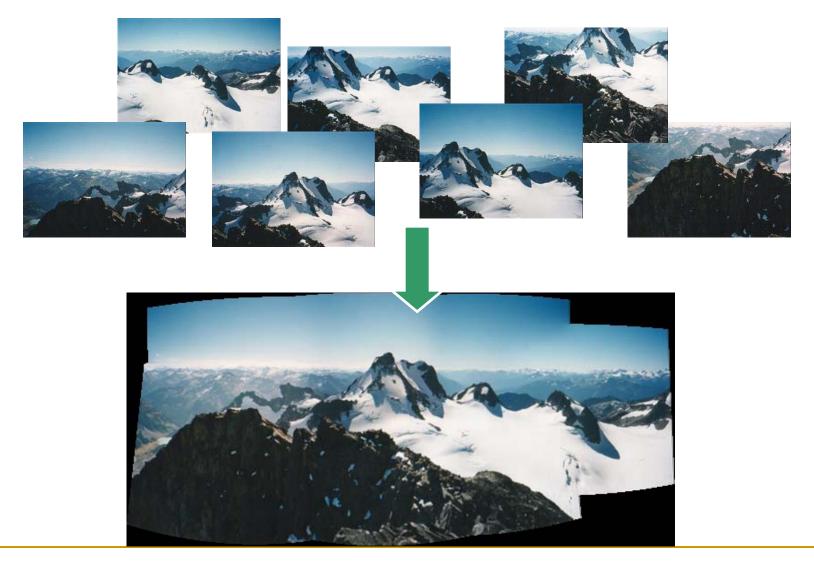


#### Multi-Scale Oriented Patches



Extract oriented patches at multiple scales

## Application: Image Stitching



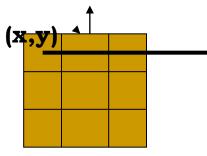
#### Ideas from Matt's Multi-Scale Oriented Patches

- 1. Detect an <u>interesting patch</u> with an <u>interest</u> <u>operator</u>. Patches are <u>translation</u> <u>invariant</u>.
- 2. Determine its dominant orientation.
- 3. Rotate the patch so that the dominant orientation points upward. This makes the patches rotation invariant.
- 4. Do this at <u>multiple scales</u>, converting them all to one scale through sampling.
- 5. Convert to illumination "invariant" form

## Implementation Concern: How do you rotate a patch?

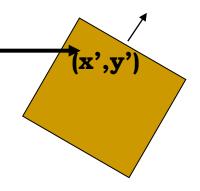
- Start with an "empty" patch whose dominant direction is "up".
- For each pixel in your patch, compute the position in the detected image patch. It will be in floating point and will fall between the image pixels.
- Interpolate the values of the 4 closest pixels in the image, to get a value for the pixel in your patch.

## Rotating a Patch



empty canonical patch

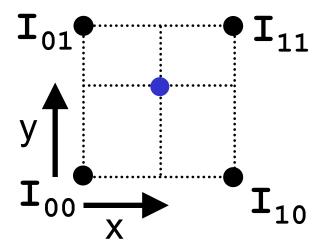
$$T \begin{bmatrix} x' = x \cos\theta - y \sin\theta \\ y' = x \sin\theta + y \cos\theta \end{bmatrix}$$
counterclockwise rotation



patch detected in the image

## Using Bilinear Interpolation

Use all 4 adjacent samples



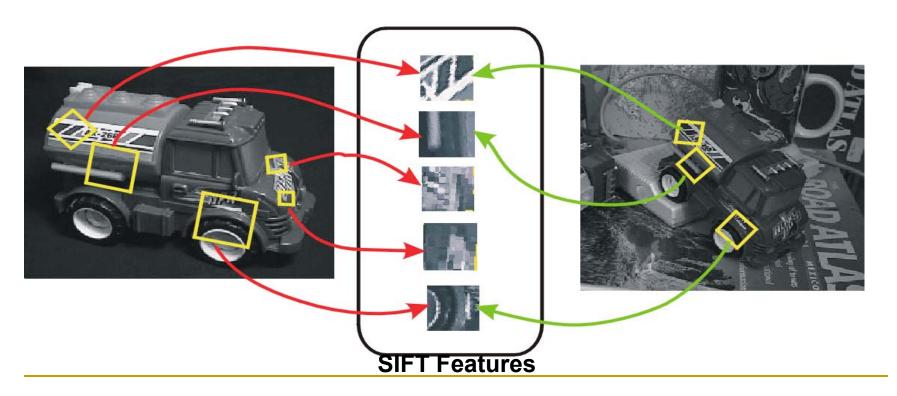
#### SIFT: Motivation

- The Harris operator is not invariant to scale and correlation is not invariant to rotation<sup>1.</sup>
- For better image matching, Lowe's goal was to develop an interest operator that is invariant to scale and rotation.
- Also, Lowe aimed to create a descriptor that was robust to the variations corresponding to typical viewing conditions. <u>The descriptor is the most-used</u> <u>part of SIFT.</u>

<sup>1</sup>But Schmid and Mohr developed a rotation invariant descriptor for it in 1997.

#### Idea of SIFT

 Image content is transformed into <u>local feature</u> <u>coordinates</u> that are <u>invariant</u> to <u>translation</u>, <u>rotation</u>, <u>scale</u>, and <u>other imaging parameters</u>



## Claimed Advantages of SIFT

- Locality: features are local, so robust to occlusion and clutter (no prior segmentation)
- Distinctiveness: individual features can be matched to a large database of objects
- Quantity: many features can be generated for even small objects
- Efficiency: close to real-time performance
- Extensibility: can easily be extended to wide range of differing feature types, with each adding robustness

## Overall Procedure at a High Level

#### 1. Scale-space extrema detection

Search over multiple scales and image locations.

#### 2. Keypoint localization

Fit a model to detrmine location and scale. Select keypoints based on a measure of stability.

#### 3. Orientation assignment

Compute best orientation(s) for each keypoint region.

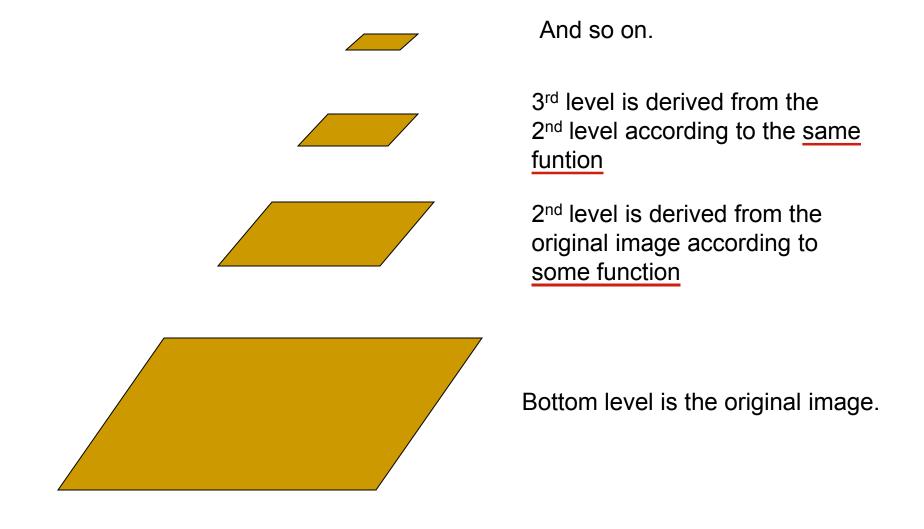
#### 4. Keypoint description

Use <u>local image gradients</u> at <u>selected scale</u> and <u>rotation</u> to <u>describe each keypoint region</u>.

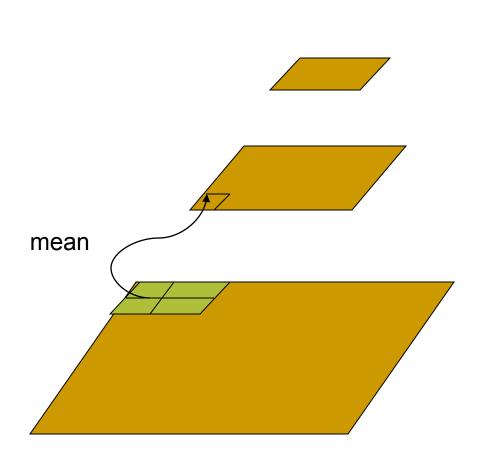
## 1. Scale-space extrema detection

- Goal: Identify locations and scales that can be repeatably assigned under different views of the same scene or object.
- Method: search for stable features across multiple scales using a continuous function of scale.
- Prior work has shown that under a variety of assumptions, the best function is a Gaussian function.
- The scale space of an image is a function *L(x,y,σ)* that is produced from the convolution of a Gaussian kernel (at different scales) with the input image.

## Aside: Image Pyramids



## Aside: Mean Pyramid



And so on.

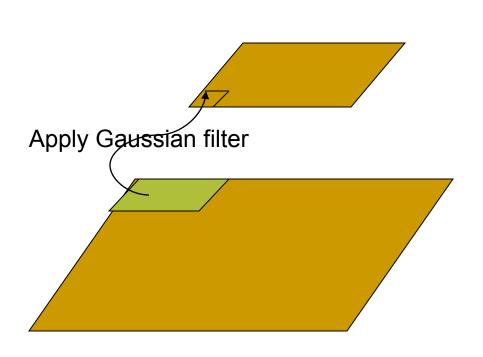
At 3<sup>rd</sup> level, each pixel is the mean of 4 pixels in the 2<sup>nd</sup> level.

At 2<sup>nd</sup> level, each pixel is the mean of 4 pixels in the original image.

Bottom level is the original image.

### Aside: Gaussian Pyramid

At each level, image is smoothed and reduced in size.

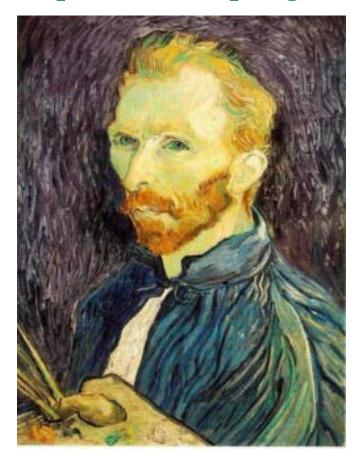


And so on.

At 2<sup>nd</sup> level, each pixel is the result of applying a <u>Gaussian mask</u> to the first level and then subsampling to reduce the size.

Bottom level is the original image.

#### Example: Subsampling with Gaussian pre-filtering



Gaussian 1/2



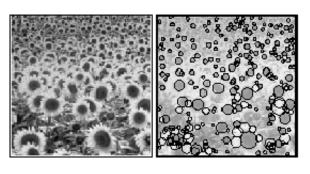
G 1/4

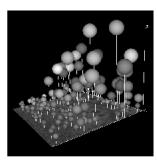


G 1/8

## Lowe's Scale-space Interest Points

- Laplacian of Gaussian kernel
  - Scale normalised (x by scale<sup>2</sup>)
  - Proposed by Lindeberg
- Scale-space detection
  - Find local maxima across scale/space
  - A good "blob" detector

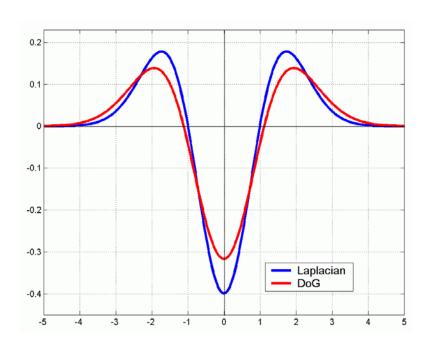




$$G(x,y,\sigma) = \frac{1}{\sqrt{2\pi}\sigma} e^{-\frac{1}{2}\frac{x^2+y^2}{\sigma^2}}$$

$$\nabla^2 G(x, y, \sigma) = \frac{\partial^2 G}{\partial x^2} + \frac{\partial^2 G}{\partial y^2}$$

## Lowe's Scale-space Interest Points: Difference of Gaussians



 Gaussian is an ad hoc solution of heat diffusion equation

$$\frac{\partial G}{\partial \sigma} = \sigma \nabla^2 G.$$

Hence

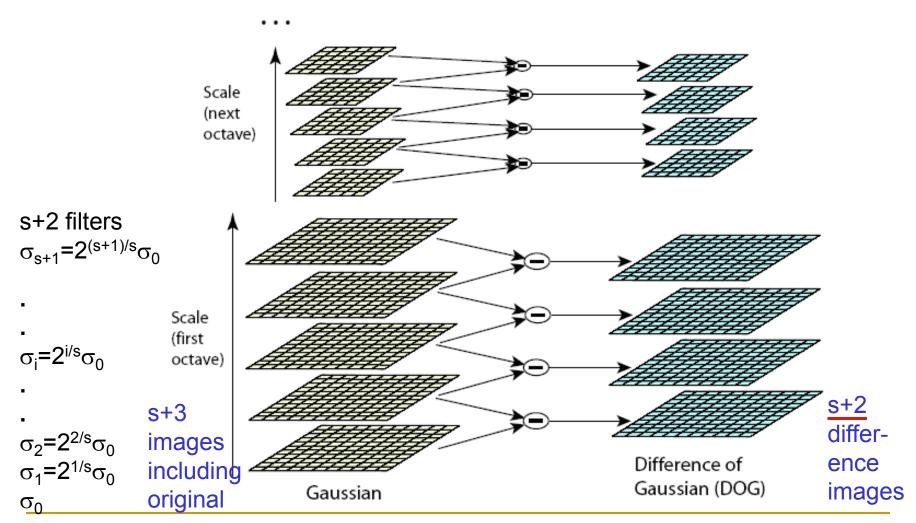
$$G(x, y, k\sigma) - G(x, y, \sigma) \approx (k-1)\sigma^2 \nabla^2 G.$$

k is not necessarily very small in practice

## Lowe's Pyramid Scheme

- Scale space is separated into octaves:
  - Octave 1 uses scale σ
  - Octave 2 uses scale 2σ
  - etc.
- In each octave, the initial image is repeatedly convolved with Gaussians to produce a set of scale space images.
- Adjacent Gaussians are subtracted to produce the DOG
- After each octave, the Gaussian image is down-sampled by a factor of 2 to produce an image ¼ the size to start the next level.

## Lowe's Pyramid Scheme

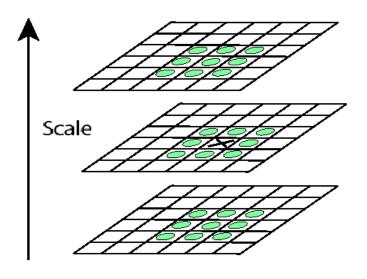


The parameter **s** determines the number of images per octave.

## Key point localization

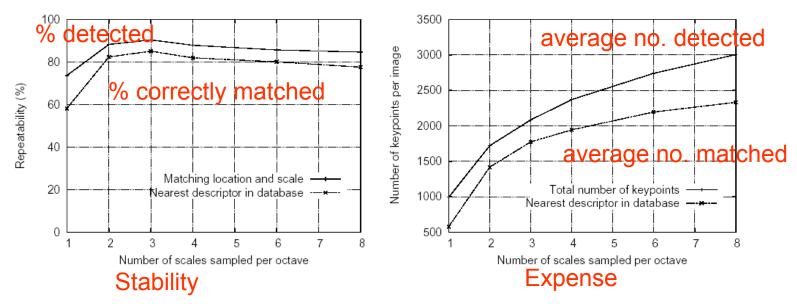
s+2 difference images.top and bottom ignored.s planes searched.

- Detect maxima and minima of difference-of-Gaussian in scale space
- Each point is compared to its 8 neighbors in the current image and 9 neighbors each in the scales above and below



For each max or min found, output is the **location** and the **scale**.

Scale-space extrema detection: experimental results over 32 images that were synthetically transformed and noise added.



#### Sampling in scale for efficiency

- How many scales should be used per octave? S=?
  - More scales evaluated, more keypoints found
  - S < 3, stable keypoints increased too</li>
  - S > 3, stable keypoints decreased
  - S = 3, maximum stable keypoints found

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## Keypoint localization

- Once a keypoint candidate is found, perform a detailed fit to nearby data to determine
  - location, scale, and ratio of principal curvatures
- In initial work keypoints were found at location and scale of a central sample point.
- In newer work, they fit a 3D quadratic function to improve interpolation accuracy.
- The Hessian matrix was used to eliminate edge responses.

## Eliminating the Edge Response

Reject flats:

$$|D(\hat{\mathbf{x}})| < 0.03$$

Reject edges:

$$\mathbf{H} = \begin{bmatrix} D_{xx} & D_{xy} \\ D_{xy} & D_{yy} \end{bmatrix}$$

 $\mathbf{H} = \left| egin{array}{cc} D_{xx} & D_{xy} \\ D_{xy} & D_{yy} \end{array} \right| \left| egin{array}{cc} \operatorname{Let} \ \alpha \ \ \text{be the eigenvalue with} \\ \operatorname{larger magnitude and} \ \beta \ \ \text{the smaller.} \end{array} \right|$ 

$$Tr(\mathbf{H}) = D_{xx} + D_{yy} = \alpha + \beta,$$
$$Det(\mathbf{H}) = D_{xx}D_{yy} - (D_{xy})^2 = \alpha\beta.$$

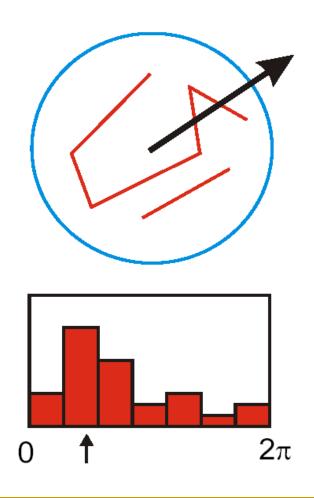
Let 
$$r = \alpha/\beta$$
.  
So  $\alpha = r\beta$ 

$$\frac{\mathrm{Tr}(\mathbf{H})^2}{\mathrm{Det}(\mathbf{H})} = \frac{(\alpha+\beta)^2}{\alpha\beta} = \frac{(r\beta+\beta)^2}{r\beta^2} = \frac{(r+1)^2}{r}, \quad \text{(r+1)}^2/r \text{ is at a min when the}$$

2 eigenvalues are equal.

- $\neg$  r < 10
- What does this look like?

## 3. Orientation assignment



- Create histogram of local gradient directions at <u>selected</u> <u>scale</u>
- Assign <u>canonical</u>
   <u>orientation</u> at peak of smoothed histogram
- Each key specifies stable 2D coordinates (x, y, scale, orientation)

If 2 major orientations, use both.

## Keypoint localization with orientation

233x189





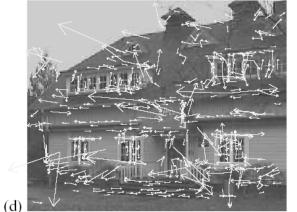
832

initial keypoints

729

keypoints after gradient threshold





536

keypoints after ratio threshold

## 4. Keypoint Descriptors

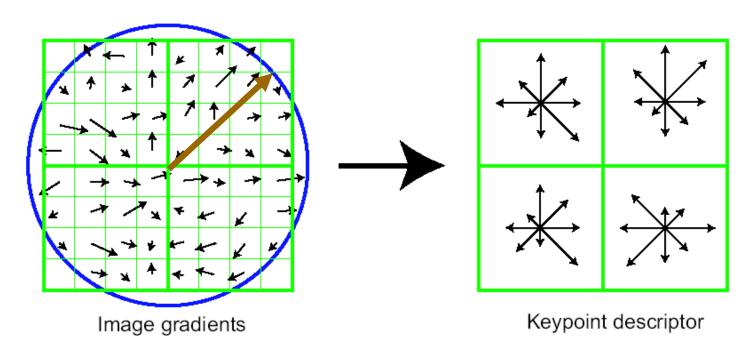
- At this point, each keypoint has
  - location
  - scale
  - orientation
- Next is to compute a descriptor for the local image region about each keypoint that is
  - highly distinctive
  - invariant as possible to variations such as changes in viewpoint and illumination

#### Normalization

Rotate the window to standard orientation

 Scale the window size based on the scale at which the point was found.

## Lowe's Keypoint Descriptor (shown with 2 X 2 descriptors over 8 X 8)

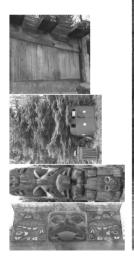


In experiments, 4x4 arrays of 8 bin histogram is used, a total of 128 features for one keypoint

## Lowe's Keypoint Descriptor

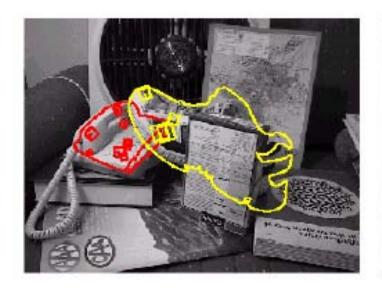
- use the normalized region about the keypoint
- compute gradient magnitude and orientation at each point in the region
- weight them by a Gaussian window overlaid on the circle
- create an <u>orientation</u> <u>histogram</u> over the 4 X 4 subregions of the window
- 4 X 4 descriptors over 16 X 16 sample array were used in practice. 4 X 4 times 8 directions gives a vector of 128 values.

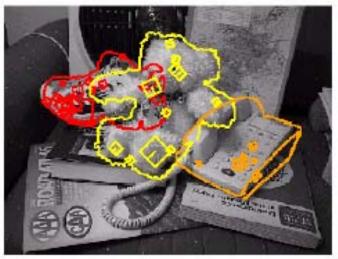
### Using SIFT for Matching "Objects"











#### Uses for SIFT

- Feature points are used also for:
  - Image alignment (homography, fundamental matrix)
  - 3D reconstruction (e.g. Photo Tourism)
  - Motion tracking
  - Object recognition
  - Indexing and database retrieval
  - Robot navigation
  - many others