smallantimagmas

A fork of smallgrp package for small antiassociative magmas

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smallantimagmas automatic generated documentation

1.1 smallantimagmas automatic generated documentation of properties

1.1.1 IsAntiassociative (for IsMagma)

▷ `IsAntiassociative(`*M*`)` (property)

Returns: `true` or `false`

identifies whether magma *M* is antiassociative.

Example

```
gap> IsAntiassociative(OneSmallGroup(16));
false
gap> IsAntiassociative(OneSmallAntimagma(2));
true
gap> IsAntiassociative(OneSmallAntimagma(3));
true
```

1.1.2 IsLeftCyclic (for IsMagma)

▷ `IsLeftCyclic(`*M*`)` (property)

Returns: `true` or `false`

if magma is left cyclic *m*.

1.1.3 IsRightCyclic (for IsMagma)

▷ `IsRightCyclic(`*M*`)` (property)

Returns: `true` or `false`

if magma is left cyclic *m*.

1.1.4 IsLeftCancellative (for IsMagma)

▷ `IsLeftCancellative(`*M*`)` (property)

Returns: `true` or `false`

if magma is left cancellative *m*.

Example

```
gap> M := SmallAntimagma(2, 1);
<magma with 2 generators>
gap> Display( MultiplicationTable(M) );
[ [  2,  1 ],
  [  2,  1 ] ]
gap> IsRightCancellative(M);
false
gap> IsLeftCancellative(M);
true
gap> List(AllSmallAntimagmas(2), M -> IsLeftCancellative(M));
[ true, false ]
```

1.1.5 IsRightCancellative (for IsMagma)

▷ IsRightCancellative(*M*) (property)

Returns: true or false

if magma is right cancellative *m*.

Example

```
gap> List(AllSmallAntimagmas(2), M -> IsRightCancellative(M));
[ false, true ]
```

1.1.6 IsCancellative (for IsMagma)

▷ IsCancellative(*M*) (property)

Returns: true or false

if magma is cancellative *m*.

Example

```
gap> List(AllSmallAntimagmas(2), M -> IsCancellative(M));
[ false, false ]
```

1.2 smallantimagmas automatic generated documentation of attributes

1.2.1 AssociativityIndex (for IsMagma)

▷ AssociativityIndex(*M*) (attribute)

identifies associativity index of *M*.

Example

```
gap> OneSmallAntimagma(2);
<magma with 2 generators>
gap> AssociativityIndex(OneSmallAntimagma(2));
0
gap> OneSmallGroup(4);
<pc group of size 4 with 2 generators>
gap> AssociativityIndex(OneSmallGroup(4));
64
gap> AssociativityIndex(OneSmallGroup(4)) = 4 ^ 3;
true
```

1.2.2 DiagonalOfMultiplicationTable (for IsMagma)

▷ DiagonalOfMultiplicationTable(*M*) (attribute)

computes diaognal of multiplication table of *M*.

Example

```
gap> List(AllSmallAntimagmas(3), M -> DiagonalOfMultiplicationTable((M)));
[ [ 2, 1, 1 ], [ 2, 1, 1 ],
  [ 2, 3, 2 ], [ 2, 1, 1 ],
  [ 2, 1, 1 ], [ 2, 1, 2 ],
  [ 2, 3, 2 ], [ 2, 1, 2 ],
  [ 2, 3, 1 ], [ 2, 3, 1 ]
]
```

1.2.3 CommutativityIndex (for IsMagma)

▷ CommutativityIndex(*M*) (attribute)

identifies commutativity index of *M*.

Example

1.2.4 AnticommutativityIndex (for IsMagma)

▷ AnticommutativityIndex(*M*) (attribute)

calculates anticommutativity index of *M*.

Example

1.2.5 SquaresIndex (for IsMagma)

▷ SquaresIndex(*M*) (attribute)

computes squares index of *M* so the order of $\{m^2 | m \in \}$.

Example

```
gap> List(AllSmallAntimagmas(2), M -> List(M, m -> m * m) );
[ [ m2, m1 ], [ m2, m1 ] ]
gap> List(AllSmallAntimagmas(2), M -> SquaresIndex(M ));
[ 2, 2 ]
gap> List(AllSmallAntimagmas(3), M -> SquaresIndex(M ));
[ 2, 2, 2, 2, 2, 2, 2, 2, 3, 3 ]
```

1.2.6 IdSmallAntimagma (for IsMagma)

▷ IdSmallAntimagma(*M*) (attribute)

identifies class of antiassociative magma *M*.

Example
```
gap> IsAntiassociative(OneSmallGroup(16));
false
gap> IsAntiassociative(OneSmallAntimagma(2));
true
gap> IsAntiassociative(OneSmallAntimagma(3));
true
```

1.2.7 LeftOrder (for IsExtLElement)

▷ `LeftOrder(`*[m]*`)` (attribute)

returns a left order of element *m*.

1.2.8 RightOrder (for IsExtRElement)

▷ `RightOrder(`*[m]*`)` (attribute)

returns a right order of element *m*.

1.2.9 LeftOrdersOfElements (for IsMagma)

▷ `LeftOrdersOfElements(`*[m]*`)` (attribute)

returns a left order of element *m*.

1.2.10 RightOrdersOfElements (for IsMagma)

▷ `RightOrdersOfElements(`*[m]*`)` (attribute)

returns a left order of element *m*.

1.3 smallantimagmas automatic generated documentation of global functions

1.3.1 AllSubmagmas

▷ `AllSubmagmas(`*M*`)` (function)

builds a collection of non-isomorphic submagmas of *M*.

Example
```
gap> AllSmallAntimagmas(2);
[ <magma with 2 generators>, <magma with 2 generators> ]
gap> List(AllSmallAntimagmas(2), M -> AllSubmagmas(M));
[ [ <magma with 1 generator> ], [ <magma with 1 generator> ] ]
```

1.3.2 MagmaIsomorphismInvariantsMatch

▷ MagmaIsomorphismInvariantsMatch(*M*) (function)

computes isomorphism invariants of *M*.

1.3.3 IsMagmaIsomorphic

▷ IsMagmaIsomorphic(*M*, *N*) (function)

identifies whether magmas *M*, *N* are isomorphic.

Example

```
gap> M := SmallAntimagma(2, 1);
<magma with 2 generators>
gap> N := SmallAntimagma(2, 2);
<magma with 2 generators>
gap> T := MagmaByMultiplicationTable([ [2, 1], [2, 1] ]);
<magma with 2 generators>
gap> IsMagmaIsomorphic(M, M);
true
gap> IsMagmaIsomorphic(M, T);
true
gap> IsMagmaIsomorphic(M, N);
false
```

1.3.4 IsMagmaAntiisomorphic

▷ IsMagmaAntiisomorphic(*[M, N]*) (function)

identifies whether magmas *M*, *N* are antiisomorphic.

Example

```
gap> N := SmallAntimagma(2, 1);
<magma with 2 generators>
gap> M := SmallAntimagma(2, 1);
<magma with 2 generators>
gap> N := SmallAntimagma(2, 2);
<magma with 2 generators>
gap> IsMagmaAntiisomorphic(M, M);
false
gap> IsMagmaAntiisomorphic(M, N);
true
gap> IsMagmaAntiisomorphic(M, TransposedMagma(M));
true
```

1.3.5 TransposedMagma

▷ TransposedMagma(*[M]*) (function)

generates transposed magma *M*.

Example

```
gap> M := SmallAntimagma(2, 1);
<magma with 2 generators>
gap> IsMagmaAntiisomorphic(M, TransposedMagma(M));
true
gap> IsMagmaIsomorphic(M, TransposedMagma(TransposedMagma(M)));
true
gap> M := SmallAntimagma(2, 1);
<magma with 2 generators>
gap> Display(MultiplicationTable(M));
[ [  2,  1 ],
  [  2,  1 ] ]
gap> Display(MultiplicationTable(TransposedMagma(M)));
[ [  2,  2 ],
  [  1,  1 ] ]
```

1.3.6 LeftPower

▷ `LeftPower(`*`[m, k]`*`)` (function)

returns a left k-power of element m.

1.3.7 RightPower

▷ `RightPower(`*`[m, k]`*`)` (function)

returns a right k-power of element m.

1.3.8 AllSmallAntimagmas

▷ `AllSmallAntimagmas(`*`n`*`)` (function)

returns all antiassociative magmas of specified size n (a number)

Example

```
gap> AllSmallAntimagmas(2);
[ <magma with 2 generators>, <magma with 2 generators> ]
gap> AllSmallAntimagmas(3);
[
  <magma with 3 generators>, <magma with 3 generators>, <magma with 3 generators>,
  <magma with 3 generators>, <magma with 3 generators>, <magma with 3 generators>,
  <magma with 3 generators>, <magma with 3 generators>,
  <magma with 3 generators>, <magma with 3 generators>
]
```

1.3.9 NrSmallAntimagmas

▷ `NrSmallAntimagmas(`*`n`*`)` (function)

counts number of antiassociative magmas of specified size n (a number).

Example

```
gap> NrSmallAntimagmas(2);
2
gap> NrSmallAntimagmas(3);
10
gap> NrSmallAntimagmas(4);
17780
```

1.3.10 SmallAntimagma

▷ SmallAntimagma(*n*, *i*) (function)

returns antiassociative magma of id *[n, i]*.

Example

```
gap> SmallAntimagma(2, 1);
<magma with 2 generators>
gap> SmallAntimagma(4, 5);
<magma with 4 generators>
```

1.3.11 OneSmallAntimagma

▷ OneSmallAntimagma(*n*) (function)

returns a random antiassociative magma of size *n*.

Example

```
gap> OneSmallAntimagma(2);
<magma with 2 generators>

gap> OneSmallAntimagma(3);
<magma with 3 generators>
```

1.3.12 ReallyAllSmallAntimagmas

▷ ReallyAllSmallAntimagmas(*n*) (function)

returns really-all antiassociative magmas, isomorphic, of specified size *n* (a number)

Example

```
gap> ReallyAllSmallAntimagmas(2);
[ <magma with 2 generators>, <magma with 2 generators> ]
```

1.3.13 ReallyNrSmallAntimagmas

▷ ReallyNrSmallAntimagmas(*n*) (function)

counts number of antiassociative magmas of specified size *n* (a number)

Example

```
gap> ReallyNrSmallAntimagmas(3);
52
```

1.3.14 AntimagmaGeneratorPossibleDiagonals

▷ AntimagmaGeneratorPossibleDiagonals(*n*) (function)

returns all possible diagonals of multiplication table for *[n]* -antimagma.

Example

```
gap> AntimagmaGeneratorPossibleDiagonals(2);
[ [ 2, 1 ] ]
gap> AntimagmaGeneratorPossibleDiagonals(3);
[
  [ 2, 1, 1 ], [ 2, 1, 2 ], [ 2, 3, 1 ], [ 2, 3, 2 ],
  [ 3, 1, 1 ], [ 3, 1, 2 ], [ 3, 3, 1 ], [ 3, 3, 2 ]
]
```

1.3.15 AntimagmaGeneratorFilterNonIsomorphicMagmas

▷ AntimagmaGeneratorFilterNonIsomorphicMagmas(*Ms*) (function)

filters non-isomorphic magmas *m*.

1.4 smallantimagmas automatic generated documentation of methods

1.4.1 MagmaIsomorphism (for IsMagma, IsMagma)

▷ MagmaIsomorphism(*M, N*) (operation)

computes an isomoprhism between magmas *M*, *N*.

Example

```
gap> M := SmallAntimagma(2, 1);
<magma with 2 generators>
gap> N := MagmaByMultiplicationTable([ [2, 1], [2, 1] ]);
<magma with 2 generators>
gap> MagmaIsomorphism(M, N);
<mapping: Domain([ m1, m2 ]) -> Domain([ m1, m2 ]) >
```

1.4.2 MagmaAntiisomorphism (for IsMagma, IsMagma)

▷ MagmaAntiisomorphism(*M, N*) (operation)

creates an antiisomoprhism between magmas *M*, *N*.

Example

```
gap> M := SmallAntimagma(2, 1);
<magma with 2 generators>
gap> N := SmallAntimagma(2, 2);
<magma with 2 generators>
gap> MagmaAntiisomorphism(M, N);
<mapping: Domain([ m1, m2 ]) -> Domain([ m1, m2 ]) >
```

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