



Complexity

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Summary

01 – Algorithmic Complexity

02 – Code Complexity: Design Patterns

03 – Project

Small notes before starting

- Let's all code in Python !
- We will be using GitHub for sharing projects and slides: <https://github.com/finish-off-school/course-complexity>
- Projects are to be submitted via pull requests to this repo ! (we can have a discussion on it afterwards)
- Content is taken from Max Lai @ PyCon APAC 2022 and Dimo Brockhoff @ CMAP & Centrale-Supelec

Any questions: diviyan@fentech.ai

What is this course ?

Better code quality !

- An algorithm, or script can be coded in many different ways !
- There isn't one single "best" implementation, but lots of bad practices can be seen
- The rules of "good code" :
 - A efficient implementation (that executes rather quickly)
 - A maintainable code that allows for easy debugging
 - A modular code that can be easily upgraded

Example:

```
## Format supply plan et input_sp
id_cols = [out_sc.sp_date,
out_sc.sp_source, sc.warehouse, sc.product]
supply_plan =
supply_plan.set_index(id_cols)
input_sp =
input_sp.set_index(id_cols)[out_sc.sp_qty].to_
dict() #type: ignore

## Define initial_qty and is_old column
supply_plan["initial_qty"] =
supply_plan.index.map(input_sp).fillna(0)
supply_plan["is_old"] =
supply_plan["initial_qty"] > 0

supply_plan = supply_plan.reset_index()
supply_plan =
supply_plan[~supply_plan["is_old"]]
supply_plan.drop(columns=["initial_qty",
"is_old"], inplace=True)
```



```
id_cols = [out_sc.sp_date,
out_sc.sp_source, sc.warehouse, sc.product]
supply_plan = pd.concat(
    [initial_sp, supply_plan],
ignore_index=True # type: ignore
).drop_duplicates(subset=id_cols,
keep="first")
```

01 – Algorithmic Complexity

Algorithm

(noun.)

Word used by programmers when they do not want to explain what they did.

Why Algorithms & Complexity?

Algorithm

(noun.)

Word used by programmers when they
do not want to explain what they did.

[...] an algorithm is a set of instructions, typically to
solve a class of problems or perform a computation.

[from wikipedia]

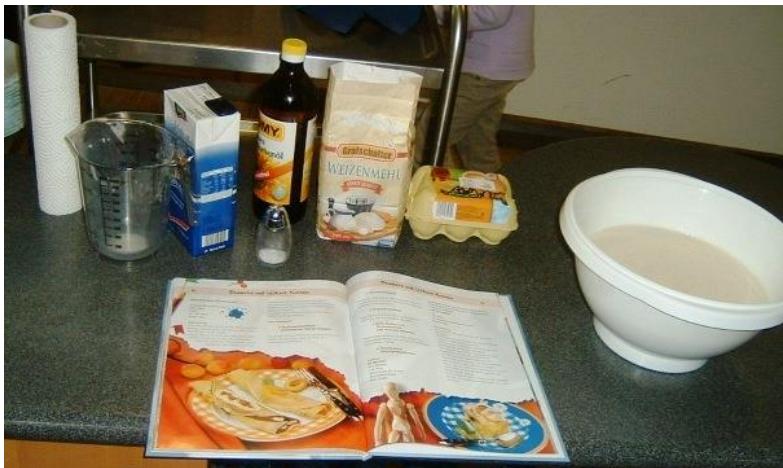
Algorithms widespread in almost every aspect of the “real-world”

- (automatic) problem solving
- sorting
- accessing data in data structures
- ...

Mnemonic: Algorithm = Recipe

Recipe:

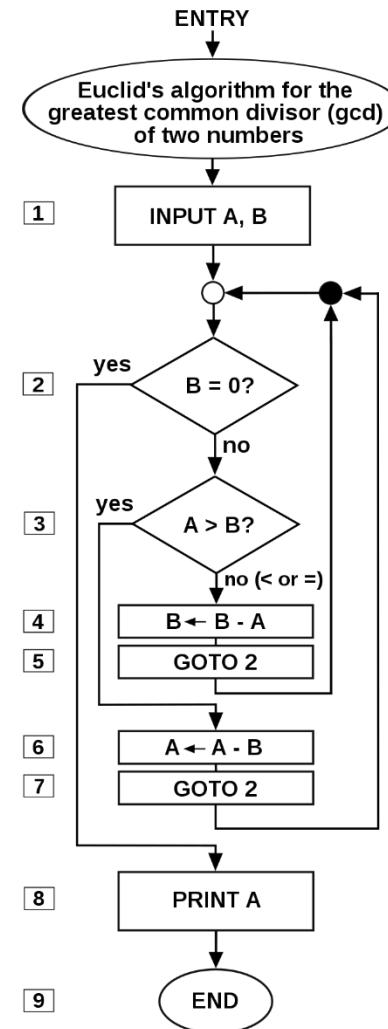
- Cook cooks a meal



Peng

Algorithm:

- A computer solves a problem



Somepics

Mnemonic: Algorithm = Recipe

Recipe:

- Cook cooks a meal

Algorithm:

- A computer solves a problem
- Independent of cook, type of pan, type of stove/oven/...
- Independent of programmer, computer, programming language, ...
- Actually, a computer is running an *implementation* of an algorithm

Example: Sorting

Aim: Sort a set of cards/words/data

[Google, for example, has to sort all webpages according to the relevance of your search]

Re-formulation: minimize the “unsortedness”

E F C A D B
B A C F D E
A B C D E F

sortedness increases



Example: Sorting

Classical Questions:

- What is the underlying algorithm?
(How do I solve a problem?)
- How long does it run to solve the problem?
(How long does it take? Which guarantees can I give? How fast is the algorithm progressing?)
- Is there a better algorithm or did I find the optimal one?
related to the complexity part of the lecture

Basics II: The O-Notation

Excursion: The O-Notation

Motivation:

- we often want to characterize how quickly a function $f(x)$ grows asymptotically
- e.g. we might want to say that an algorithm takes quadratically many steps (in n) to find the optimum of a problem with n (binary) variables, it is never exactly n^2 , but maybe $n^2 + 1$ or $(n + 1)^2$

Big-O Notation

should be known, here mainly restating the definition:

Definition 1 We write $f(x) = O(g(x))$ iff there exists a constant $c > 0$ and an $x_0 > 0$ such that $|f(x)| \leq c \cdot g(x)$ holds for all $x > x_0$

we also view $O(g(x))$ as the set of all functions growing at most as quickly as $g(x)$ and write $f(x) \in O(g(x))$

Big-O: Examples

- $f(x) + c = O(f(x))$ [as long as $f(x)$ does not converge to zero]
- $c \cdot f(x) = O(f(x))$
- $f(x) \cdot g(x) = O(f(x) \cdot g(x))$
- $3n^4 + n^2 - 7 = O(n^4)$

Intuition of the Big-O:

- if $f(x) = O(g(x))$ then $g(x)$ gives an upper bound (asymptotically) for f
- constants don't play a role
- with Big-O, you should have ' \leq ' in mind

Excursion: The O-Notation

Further definitions to generalize from ' \leq ' to ' \geq ' and '=':

- $f(x) = \Omega(g(x))$ if $g(x) = O(f(x))$
- $f(x) = \Theta(g(x))$ if $f(x) = O(g(x))$ and $g(x) = O(f(x))$

Note: Definitions equivalent to ' $<$ ' and ' $>$ ' exist as well, but are not needed in this course

Exercise O-Notation

Please order the following functions in terms of their asymptotic behavior (from smallest to largest):

- $\exp(n^2)$
- $\log n$
- $\ln n / \ln \ln n$
- n
- $n \log n$
- $\exp(n)$
- $\ln(n!)$

Give for two of the relations a formal proof.

Exercise O-Notation (Solution)

Correct ordering:

$$\frac{\ln(n)}{\ln(\ln(n))} = O(\log n)$$

$$\log n = O(n)$$

$$n = O(n \log n)$$

$$n \log n = \Theta(\ln(n!))$$

$$\ln(n!) = O(e^n)$$

$$e^n = O(e^{n^2})$$

but for example $e^{n^2} \neq O(e^n)$

One exemplary proof:

$$\frac{\ln(n)}{\ln(\ln(n))} = O(\log n):$$

$$\left| \frac{\ln(n)}{\ln(\ln(n))} \right| = \left| \frac{\log(n)}{\log(e) \ln(\ln(n))} \right| \leq \frac{3\log(n)}{\ln(\ln(n))} \leq 3 \log(n)$$

for $n > 1$ for $n > 15$

Exercise O-Notation (Solution)

One more proof: $\ln n! = O(n \log n)$

- Stirling's approximation: $n! \sim \sqrt{2\pi n} (n/e)^n$ or even
$$\sqrt{2\pi} n^{n+1/2} e^{-n} \leq n! \leq e n^{n+1/2} e^{-n}$$
- $\ln n! \leq \ln(en^{n+\frac{1}{2}}e^{-n}) = 1 + \left(n + \frac{1}{2}\right) \ln n - n$
$$\leq \left(n + \frac{1}{2}\right) \ln n \leq 2n \ln n = 2n \frac{\log n}{\log e} = c \cdot n \log n$$
 okay for $c = 2/\log e$ and all $n \in \mathbb{N}$
- $n \ln n = O(\ln n!)$ proven in a similar vein

If it's not clear yet: Youtube

- https://www.youtube.com/watch?v=__vX2sjlpXU

basic data structures

Why Data Structures? What are those?

A data structure is a **data organization, management, and storage format** that enables **efficient access and modification**.

More precisely, a data structure is a collection of data values, the relationships among them, and the functions or operations that can be applied to the data.

from wikipedia

Why important to know?

- Only with knowledge of data structures can you program well
- Knowledge of them is important to design efficient algorithms

Data Structures and Algorithm Complexity

Depending on how data is stored, it is more or less efficient to

- Add data
- Remove data
- Search for data

Common Complexities

Complexity	Running Time	
constant	$O(1)$	independent of data size
logarithmic	$O(\log(n))$	often base 2, grows relatively slowly with data size
linear	$O(n)$	nearly same amount of steps than data points
	$O(n \log(n))$	Common, still efficient in practice if n not huge
quadratic	$O(n^2)$	Often not any more efficient with large data sets
...		
exponential	$O(2^n), O(n!), \dots$	Should be avoided 😊

see also: <https://introprogramming.info/english-intro-csharp-book/read-online/chapter-19-data-structures-and-algorithm-complexity>

Best, Worst and Average Cases

Algorithm complexity can be given as best, worst or average cases:

Worst case:

- Assumes the worst possible scenario
- Algorithm can never perform worse
- Corresponds to an upper bound (on runtime, space requirements, ...)
- Most common

Best case:

- Best possible scenario
- Algorithm is never quicker/better/more efficient/...

Average case:

- Complexity averaged over all possible scenarios
- Often difficult to analyze

Arrays

Array: a fixed chunk of memory of constant size that can contain a given number of n elements of a given type

- think of a vector or a table
- in python:
 - `import numpy as np`
 - `a = np.array([1, 2, 3])`
 - `a[1]` returns 2 [python counts from 0!]

Common operations and their complexity:

- Get(i) and Update(i) in constant time
- but Remove(i), Move j in between positions i and $i+1$, ... are not possible in constant time, because necessary memory alterations not local
- To know whether a given item is in the array: linear time

Searching in Sorted Arrays

- Assume a sorted array $a[1] < a[2] < \dots < a[n]$.
- How long will it take to find the smallest element $\geq k$?
(Best case, worse case, average case)

Searching in Sorted Arrays

- Assume a sorted array $a[1] < a[2] < \dots < a[n]$.
- How long will it take to find the smallest element $\geq k$?
Or to decide whether a value a is in the array?
(best case, worse case, average case)

Linear search

- go through array from $a[1]$ to $a[n]$ until entry found
- still $\Theta(n)$ in the worst case
- average case the same (if we assume that each item is queried with equal probability)

Searching in Sorted Arrays

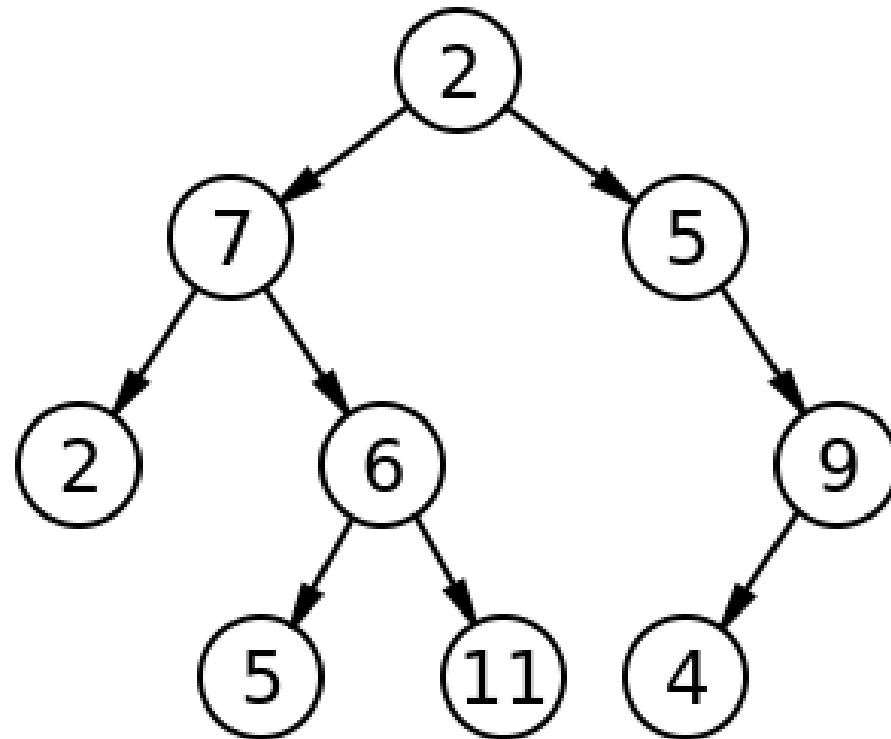
Binary search

- Look at position $[n/2]$ first
- Is it the sought after entry? If yes, stop
- If not: search recursively in left or right interval, depending on whether the middle entry is larger or smaller than the sought after entry

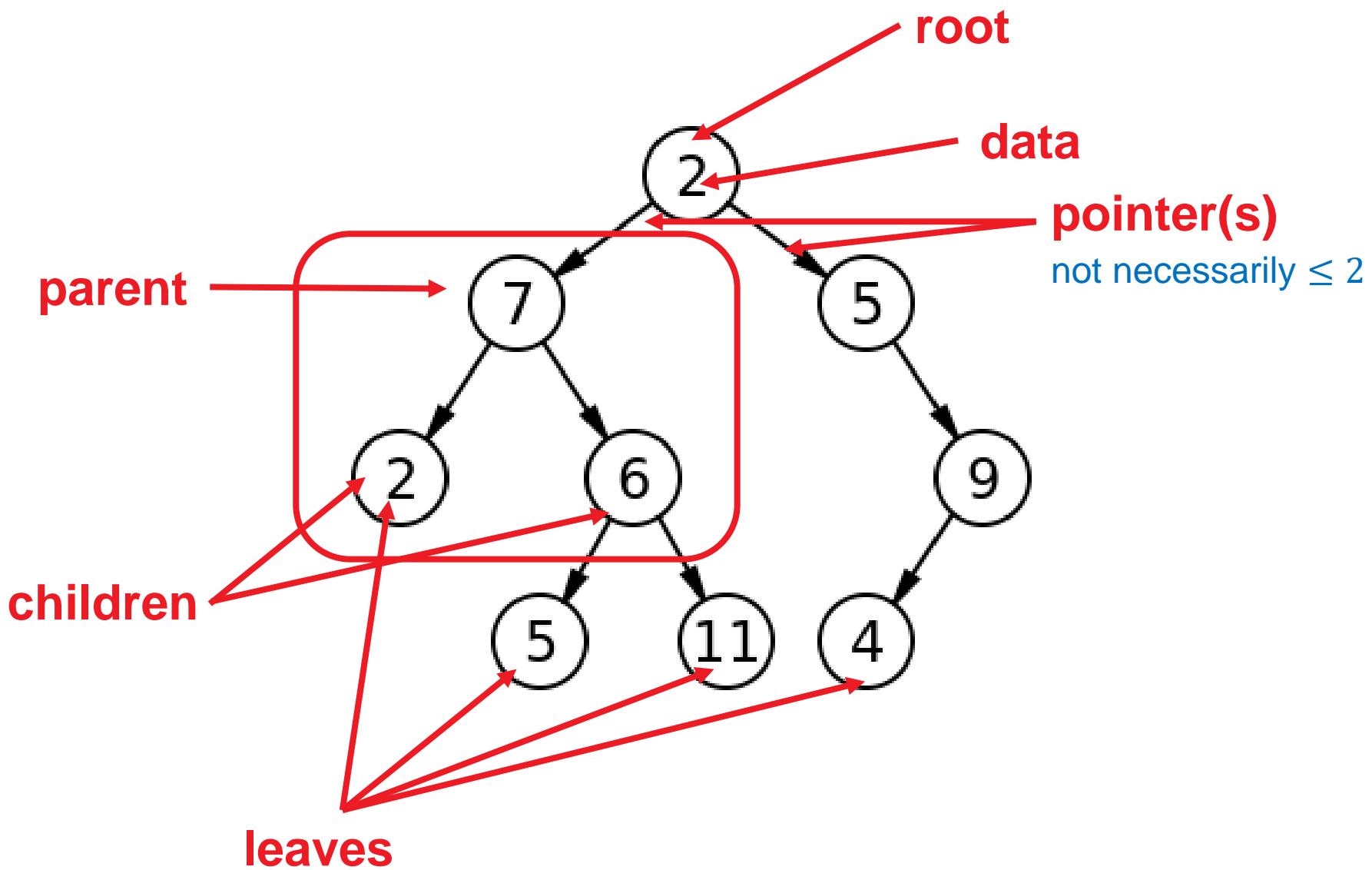
Runtimes

- Best case: 1
- Worst case:
 - sought after entry not in array
 - simple case: $n = 2^k - 1$ array elements
 - array-part where entry could be located is of length $2^{k-1} - 1$
 - by induction: maximally k comparisons needed
 - $k = \Theta(\log(n))$

Trees



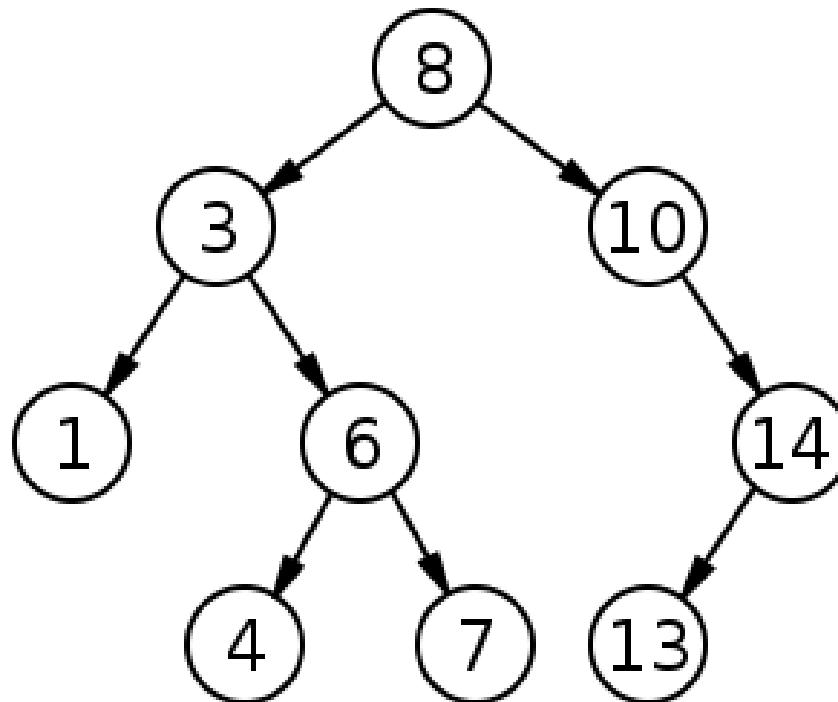
Trees



Back to Trees as Data Structure

Binary Search Tree

- a tree with degree ≤ 2
- children sorted such that the left subtree always contains values smaller than the corresponding root and the right subtree only values larger



Class Exercise: Filling a Binary Search Tree

Round 1:

Each online student: give an integer to be filled into tree

Round 2:

In class: tell where the next integer inserts

Binary Search Tree: Complexities

Search

- similar to binary search in array (go left or right until found)
- $\mathcal{O}(\log(n))$ if tree is well balanced
- $\Theta(n)$ in worst case (linear list)

Insertion

- first like search to determine the parent of the new node
- then add in $\mathcal{O}(1)$ [we are always at a leaf or have an “empty child”]

Remove (more tricky)

- if node has no child, remove it
- if node has a single child, replace node by its child
- if node has two children: find left-most tree entry L larger than the to-be-removed node, copy its value to the to-be-removed node, and remove L according to the two above rules
- cost: $\mathcal{O}(\text{tree depth})$, in worst case: $\Theta(n)$

Binary Trees: Can We Do Better?

Binary Search Tree

average case (random inserts)

search	insert	delete	Search	Insert	Delete
$\mathcal{O}(\log(n))$	$\mathcal{O}(\log(n))$	$\mathcal{O}(\log(n))$	$\Theta(n)$	$\Theta(n)$	$\Theta(n)$

worst case

Guarantee a balanced tree:

- AVL trees
- B trees
- Red-Black trees
- ...

average case (random inserts)

search	insert	delete	search	insert	delete
$\mathcal{O}(\log(n))$	$\mathcal{O}(\log(n))$	$\mathcal{O}(\log(n))$	$\mathcal{O}(\log(n))$	$\mathcal{O}(\log(n))$	$\mathcal{O}(\log(n))$

worst case

Can We Do Even Better on Average?

Balanced Trees

average case (random inserts)

search	insert	delete	search	insert	delete
$\mathcal{O}(\log(n))$	$\mathcal{O}(\log(n))$	$\mathcal{O}(\log(n))$	$\mathcal{O}(\log(n))$	$\mathcal{O}(\log(n))$	$\mathcal{O}(\log(n))$

worst case

?

average case (random inserts)

search	insert	delete	search	insert	delete
$\Theta(1)$	$\Theta(1)$	$\Theta(1)$	$\Theta(n)$	$\Theta(n)$	$\Theta(n)$

worst case

Dictionaries

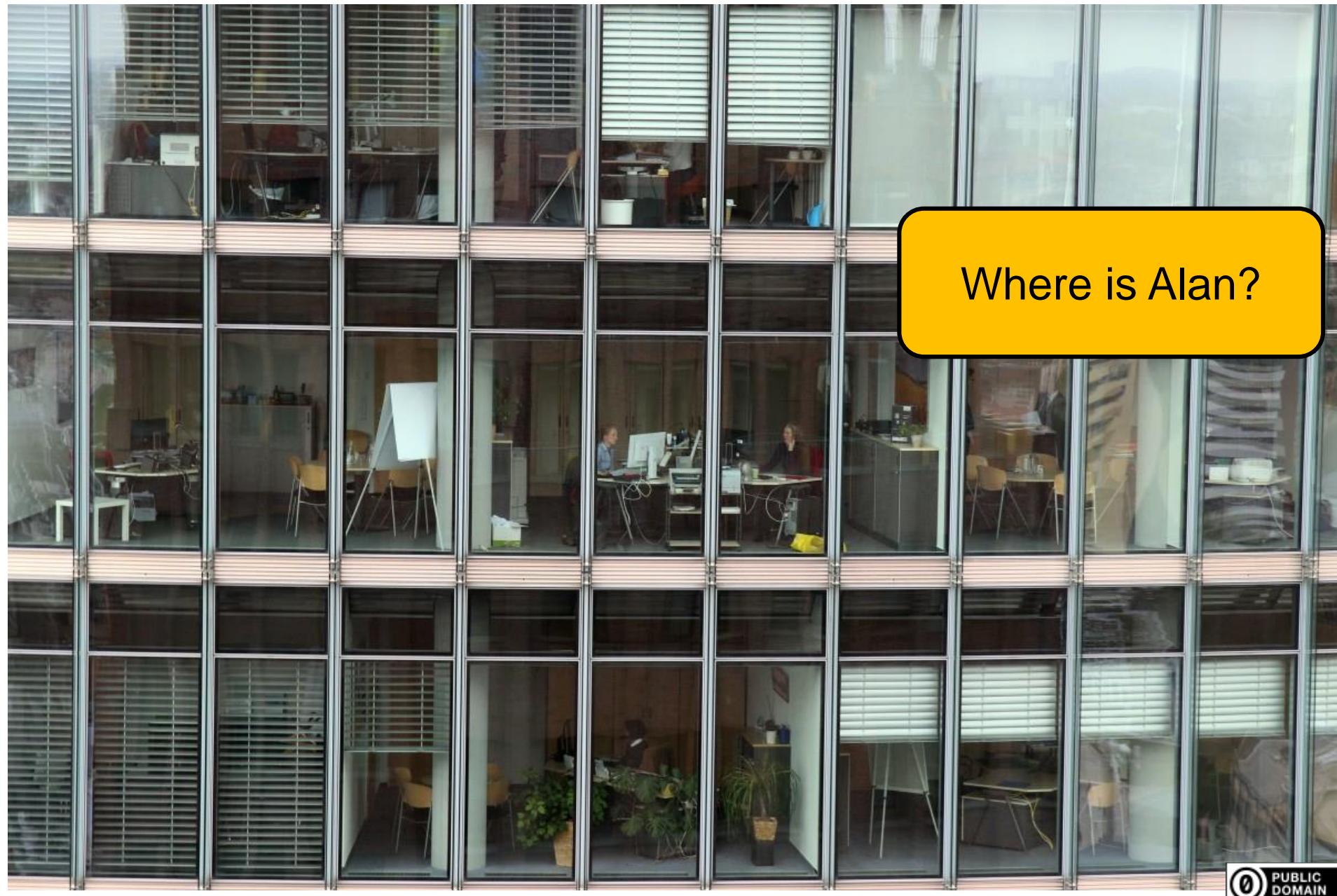
In python:

```
my_dict = { 'Joe': 113, 'Pete': 7, 'Alan': '110' }
print("my_dict['Joe']: " + my_dict['Joe'])
gives my_dict['Joe']: 113 as output
```

- the immutables 'Joe', 'Pete', and 'Alan' are the keys
- 113, 7, and 110 are the values (or the stored data)

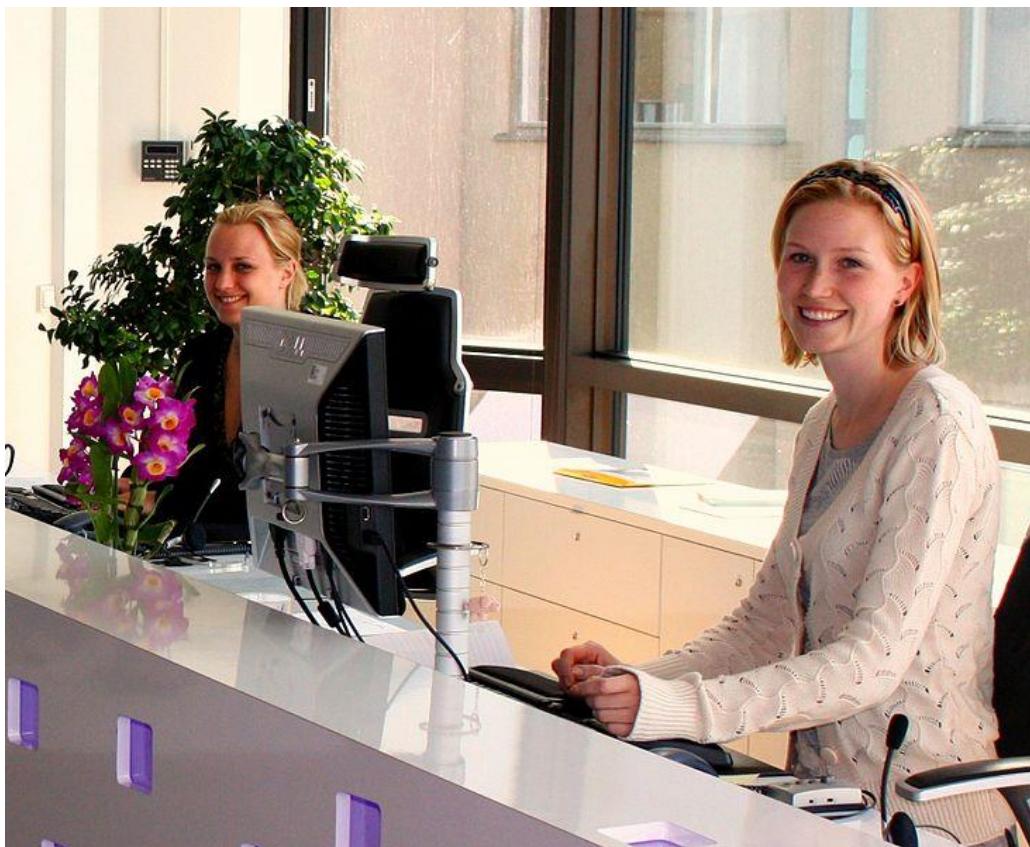
Next: Why dictionaries and how are they implemented?

Dictionaries



Where is Alan?

- Go through all offices one by one?
like in list and array
- No, you would ask the receptionist for the office number



Evan Bench

Dictionaries Implemented as Hashtables

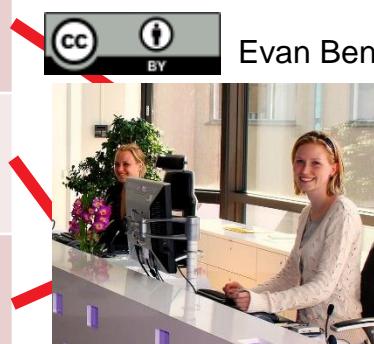
Names

Alan

Joe

Pete

...



Evan Bench

Offices

7

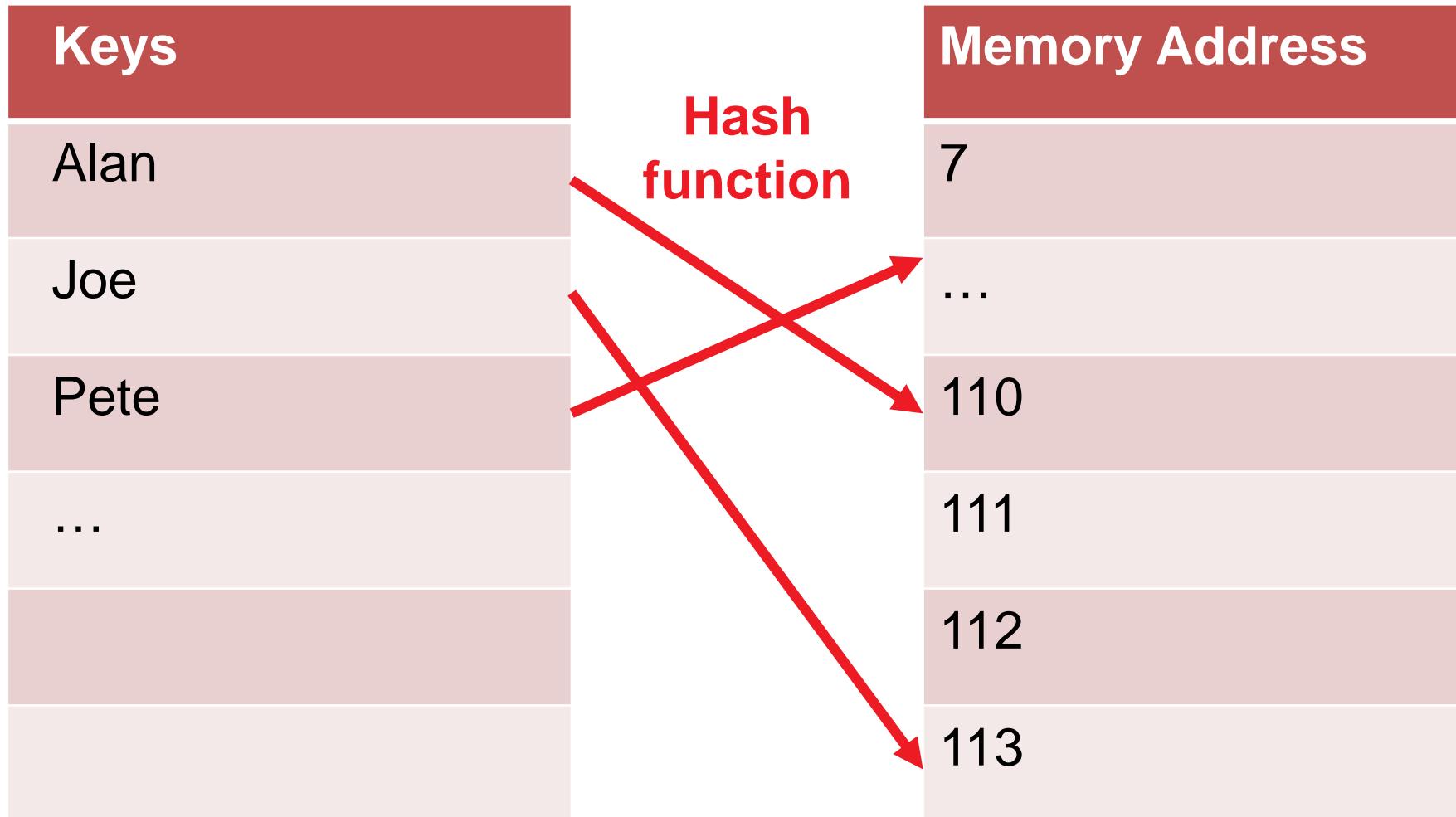
110

111

112

113

Dictionaries Implemented as Hashtables



Possible hash function: $h = z \bmod n$

Hash Functions

...should be

- deterministic: find data again
- uniform: use allocated memory space well
[more tricky with variable length keys such as strings]

Problems to address in practice:

- how to deal with collisions (e.g. via multiple hash functions)
- deleting needs to insert dummy keys when a collision appeared
- what if the hash table is full? → resizing

All this gives a **constant average performance** in practice
and a **worst case of $\Theta(n)$** for insert/remove/search

Not more details here, but if you are interested:

For more details on python's dictionary:

<https://www.youtube.com/watch?v=C4Kc8xzcA68>

Quick Recap Data Structures

- **Arrays**: fast access, slow search, no insert
- **(Linked) Lists**: slow access, slow search, but insert/remove in constant time
 - Hence python lists are implemented as dynamic arrays (once array is full, a larger chunk of memory gets allocated)
<http://www.laurentluce.com/posts/python-list-implementation/>
- **Trees**: $\log(n)$ access, $\log(n)$ add/remove
- **Dictionaries**: constant average performance in practice and a linear worst case for insert/remove/search

see also <https://www.bigocheatsheet.com/>

Exercise: Sorting

Aim: Sort a set of numbers

Questions:

- What is the underlying algorithm you used?
- How long did it take to sort?
 - What is a good measure?
- Is there a better algorithm or did you find the optimal one?

Overview of Today's Lecture

Sorting

- Insertion sort
- Insertion sort with binary search
- Mergesort
- Timsort idea

Exercise

- Comparison of sorting algorithms

Essential vs. Non-Essential Operations

In sorting, we distinguish

- comparison- and non-comparison-based sorting
- in the former, we distinguish further:
 - comparisons as essential operations
 - they are comparable over computer architectures, operating systems, implementations, (historic) time
 - they can take more time than other operations, e.g. when we compare trees w.r.t. their lexicographic DFS sorting
 - other non-essential operations: additions, multiplications, shifts/swaps in arrays, ...

Insertion Sort

Idea:

for k from 1 to n-1:

- assume array $a[1] \dots a[k]$ is already sorted
- insert $a[k+1]$ correctly into $a[1] \dots a[k+1]$

swapping $a[k+1]$ with all other numbers larger than $a[k+1]$

6 5 3 1 8 7 2 4



Swfung8

see also https://en.wikipedia.org/wiki/Insertion_sort

Insertion Sort: Analysis

Worst case:

- reverse ordering: insert always to the beginning
- then $1 + 2 + 3 + \dots + (n - 1) = \Theta(n^2)$ comparisons needed

Average Case:

- even here: $\Theta(n^2)$ comparisons needed (without proof)

Insertion Sort with Binary Search

Idea for an improved version:

use binary search for the right position of new entry in sorted subarray

- to insert array element $a[i]$, we need $\lceil \log(i - 1) \rceil$ comparisons in worst case (= depth of the binary tree search)
- overall, therefore

$$\sum_{2 \leq i \leq n} \lceil \log(i - 1) \rceil = \sum_{1 \leq i \leq n-1} \lceil \log(i) \rceil < \log(n!) + n$$

comparisons are needed

- from last time, we know that

$$\log(n!) \leq \log(en^{n+\frac{1}{2}} e^{-n}) = n \log(n) - n \log(e) + \frac{1}{2}(\log(n)) + \log(e)$$

in total, insertion sort with binary search needs

$$n \log(n) - 0.4426n + \mathcal{O}(\log(n))$$

comparisons in the worst case.

Another Possible Sorting Idea:

- sort first and second half of the array independently
- then merge the pre-sorted halves:
 - take the smaller of the smallest two values each time

$\text{Mergesort}(a_1, \dots, a_n)$

if $n = 1$ then stop

if $n > 1$ then:

- $(b_1, \dots, b_{\lfloor n/2 \rfloor}) = \text{Mergesort}(a_1, \dots, a_{\lfloor n/2 \rfloor})$
- $(c_1, \dots, c_{\lfloor n/2 \rfloor}) = \text{Mergesort}(a_{\lfloor n/2 \rfloor + 1}, \dots, a_n)$
- return $(d_1, \dots, d_n) = \text{Merge}(b_1, \dots, b_{\lfloor n/2 \rfloor}, c_1, \dots, c_{\lfloor n/2 \rfloor})$

Mergesort

Another Possible Sorting Idea:

- sort first and then merge
 - take the

Mergesort(

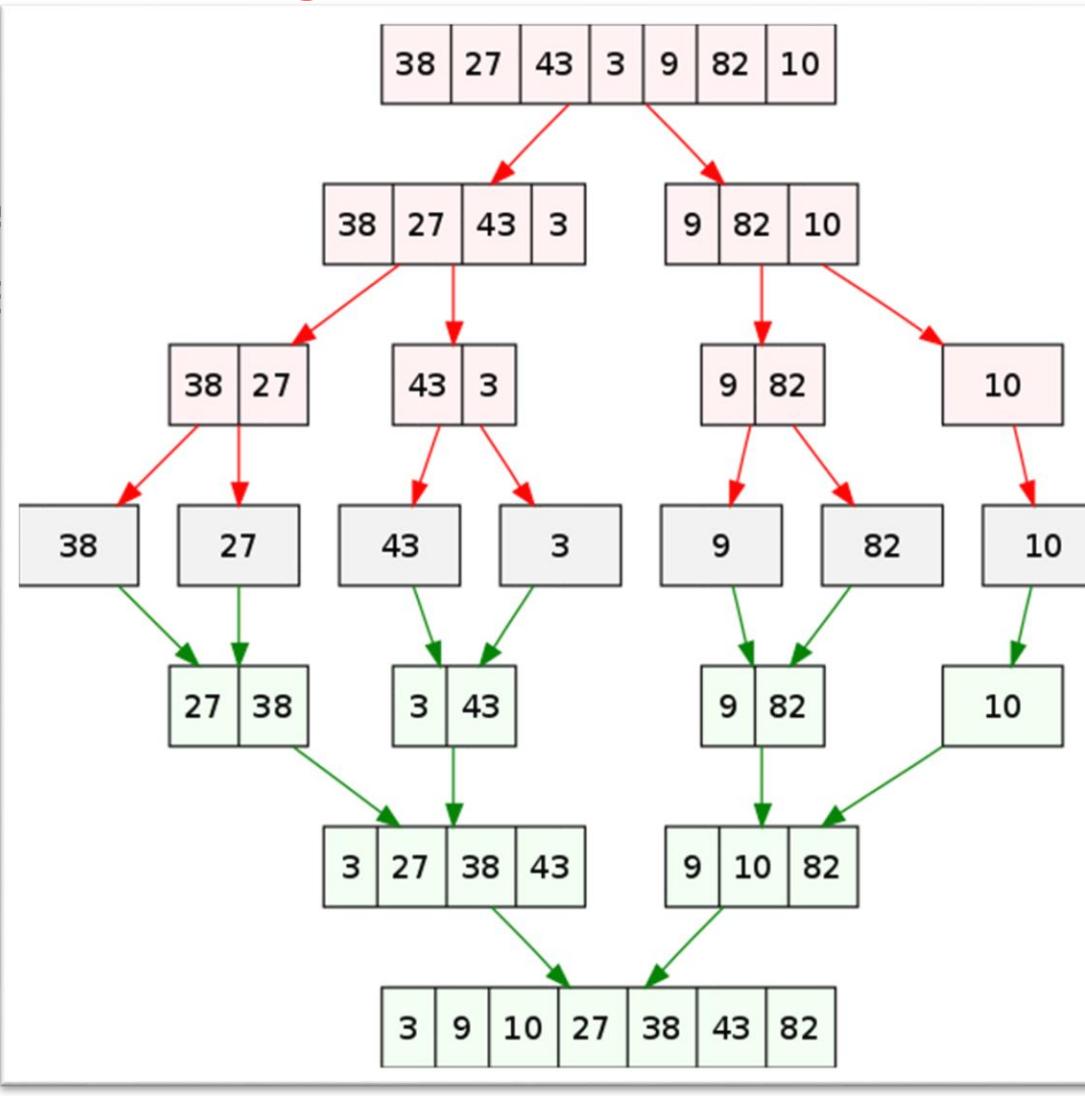
if $n = 1$

if $n > 1$

- $(b_1,$

- $(c_1,$

- return



ne

$\lfloor n/2 \rfloor$)

Mergesort: Runtime

- the number of essential comparisons $C(n)$ when sorting n items with Mergesort is

$$C(1) = 0, \quad C(n) = C\left(\left\lceil \frac{n}{2} \right\rceil\right) + C\left(\left\lfloor \frac{n}{2} \right\rfloor\right) + n - 1 \quad \text{merging}$$

sorting left half sorting right half

- without proof, $C(n) = n \log(n) + n - 1$ if $n = 2^k$

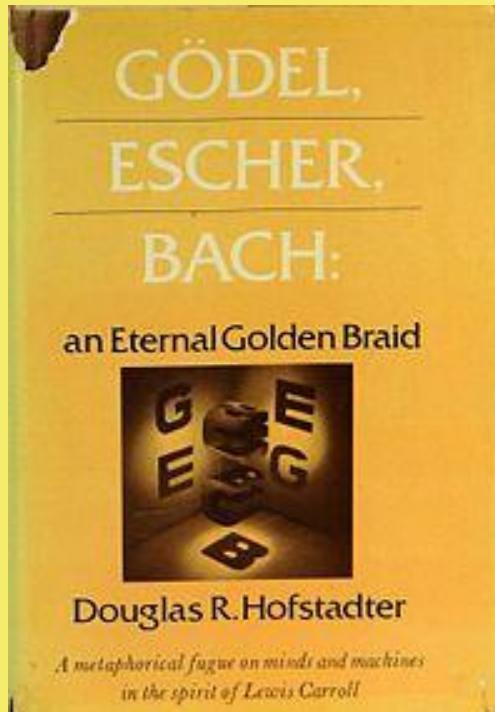
Remarks:

Mergesort is practical for huge data sets, that don't fit into memory

Mergesort is a recursive algorithm (= calls itself)

...solves a problem by solving smaller sub-problems first

Recommended Read



- “for leisure” – remark: it is quite hard to understand!
- https://en.wikipedia.org/wiki/G%C3%B6del,_Escher,_Bach

Python's Sorting: Timsort

- python uses a combination of Mergesort with insertion sort
<https://en.wikipedia.org/wiki/Timsort>
- insertion sort for small arrays quicker than merging from $n=1$ (can be done in memory/cache)
- in addition, Timsort searches for subarrays which are already sorted (called "natural runs") and that are handled as blocks
- worst case runtime of $\mathcal{O}(n \log(n))$, actually $\mathcal{O}(n \log(N))$ with N being the number of natural runs
- best case: $\mathcal{O}(n)$

Lower Bound for Comparison-Based Sorting

- Insertion Sort, standard: $\Theta(n^2)$
- Insertion Sort with binary search: $n \log(n) - 0.4426n + \mathcal{O}(\log(n))$
- Mergesort: $n \log(n) + n - 1$ if $n = 2^k$

Can we do better than $n \log(n)$?

- No! [at least for comparison-based sorting]
- Lower bound for comparison-based sorting of $\Omega(n \log(n))$
without proof here

(Home-) Exercise in Python (question 3)

Comparing sorting algorithms in python

Goals:

- learn about Mergesort (and how to implement it)
- observe the differences in runtime between your own Mergesort and python's internal Timsort
- learn how to do a scientific (numerical) experiment and how to report the results

(Home-) Exercise in Python (question 3)

TODOs:

- ① implement your own Mergesort e.g. based on lists
<http://www.cmap.polytechnique.fr/~dimo.brockhoff/algorithmsandcomplexity/2020/schedule.php>
- ② compare the differences in runtime between your own Mergesort and python's internal Timsort ('`sorted(...)`') on randomly generated lists of integers
- ③ plot the times to sort 100 lists of equal length n with both algorithms for different values of $n \in \{10, 100, 1\,000, 10\,000\}$

Tip:

```
>>> import timeit  
>>> timeit.timeit('your code', number=100)
```

Another (even more important) Tip:

use the "?" to get help on a module (and "???" to inspect the code)

Conclusions

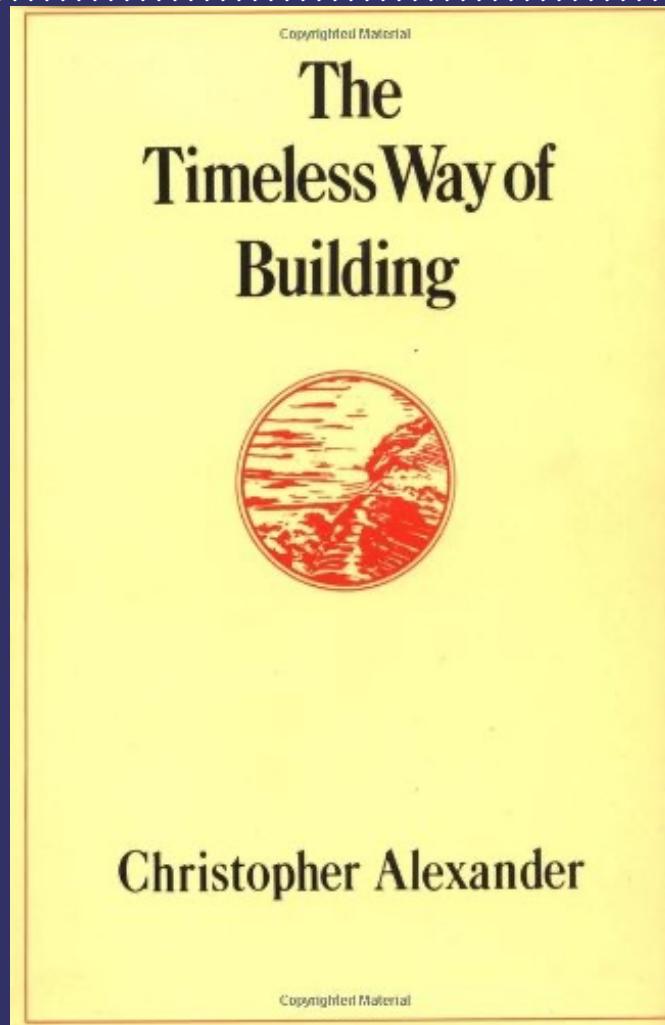
I hope it became clear...

...what **sorting** is about and how fast we can do it

02 – Code Complexity: Design Patterns

What Are Design Patterns

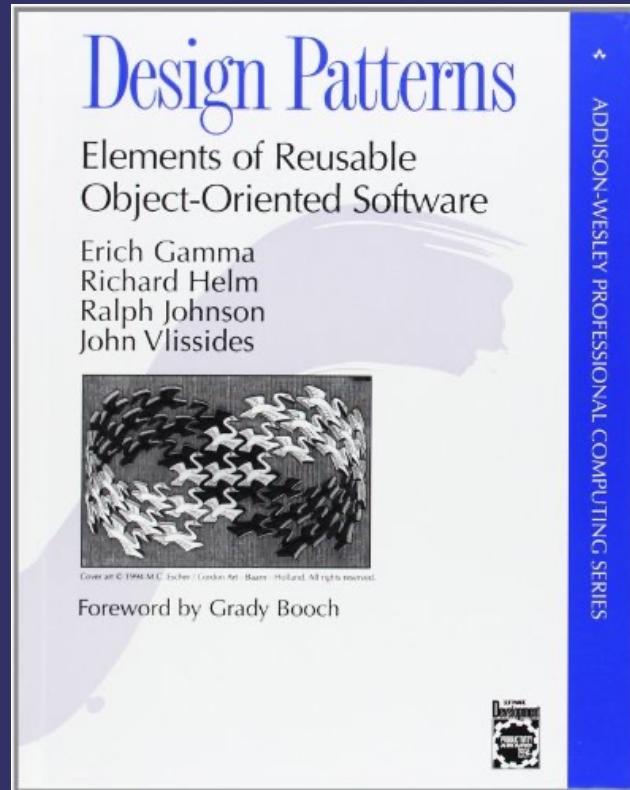
The Birth of Patterns



Each pattern is a three-part rule, which express a **relation** between a certain **context**, a **problem**, and a **solution**.



Software Design Pattern



A pattern is a proven solution
to a problem
in a context.

Source: <https://wiki.c2.com/?PatternDefinitionThread>



Why Design Patterns

- Design patterns help with reuse and communication
 - Reuse solutions : do not have to reinvent solutions for commonly recurring problems
 - Establish common terminology : provide a common point of reference during the analysis and design phase of a project
- Design patterns give a higher perspective on analysis and design
 - This frees you from the tyranny of dealing with the details too early



Design Pattern Descriptions

- Name
- Intent, problem and context
- Solution, implementation guidelines
- Participants and collaborators
- Positive and negative consequences

Pattern descriptions are often independent of programming language or implementation details



Design Patterns Catalog <<GOF>>

Creational patterns	Structural patterns	Behavioral patterns
<ul style="list-style-type: none">• Factory Method• Abstract Factory• Builder• Prototype• Singleton	<ul style="list-style-type: none">• Adapter• Bridge• Composite• Decorator• Facade• Flyweight• Proxy	<ul style="list-style-type: none">• Chain of Responsibility• Interpreter• Iterator• Mediator• Memento• Observer• State• Strategy• Template Method• Visitor



Planning for Change

- The Open/Closed Principle
 - open for extension
 - closed for modification



Draw All Shape (POP)-1

```
def draw_all_shapes(shapes: List):
    for shape in shapes:
        if isinstance(shape, Circle):
            draw_circle(shape)
        elif isinstance(shape, Rectangle):
            draw_rectangle(shape)
```

If we want to add **another shape class**?

```
class Circle(object):
    def __init__(self, point, radius):
        self.center = point
        self.radius = radius

class Rectangle(object):
    def __init__(self, point, height, width):
        self.top_left = point
        self.height = height
        self.width = width

def draw_circle(circle):
    print('drawing circle:', circle)

def draw_rectangle(rectangle):
    print('drawing rectangle:', rectangle)
```

Draw All Shape (POP)-2

```
def draw_all_shapes(shapes: List):
    for shape in shapes:
        if isinstance(shape, Circle):
            draw_circle(shape)
        elif isinstance(shape, Rectangle):
            draw_rectangle(shape)
        elif isinstance(shape, Square):
            draw_square(shape)
```

```
class Circle(object):
    def __init__(self, point, radius):
        self.center = point
        self.radius = radius

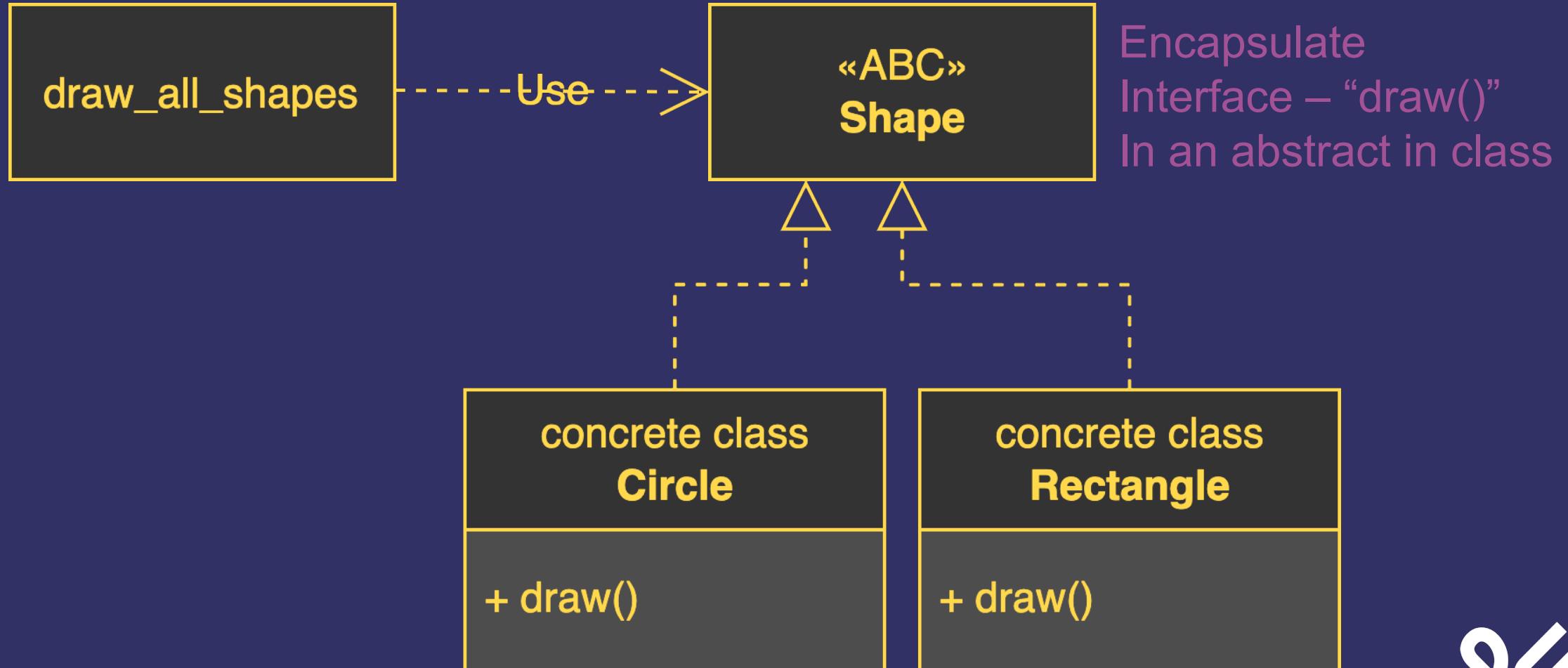
class Rectangle(object):
    def __init__(self, point, height, width):
        self.top_left = point
        self.height = height
        self.width = width

def draw_circle(circle):
    print('drawing circle:', circle)

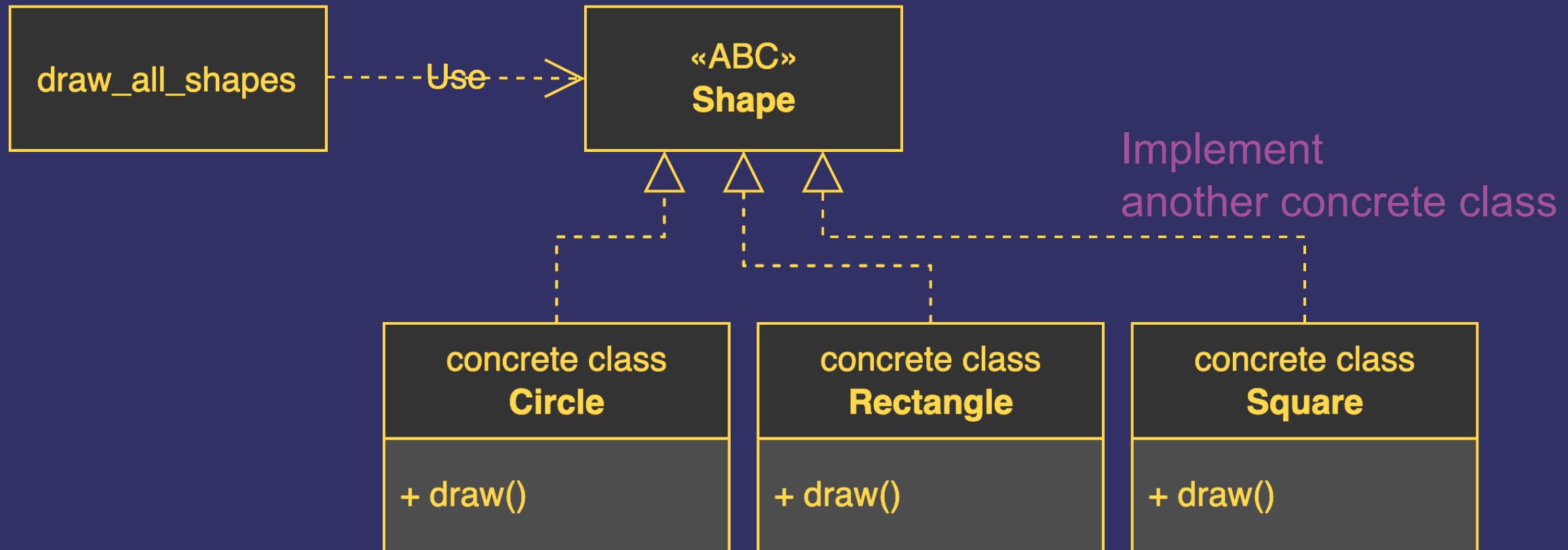
class Square(object):
    def __init__(self, point, side):
        self.top_left = point
        self.side = side

def draw_square(square):
    print('drawing square:', square)
```

Draw All Shape (OOP)-1



Draw All Shape (OOP)-3



Draw All Shape (OOP)-2

```
def draw_all_shape(shapes: List[Shape]):  
    for shape in shapes:  
        shape.draw()
```

```
class Shape(ABC):  
    @abstractmethod  
    def draw(self):  
        pass
```

```
class Circle(Shape):  
    def __init__(self, point, radius):  
        self.center = point  
        self.radius = radius  
  
    def draw(self):  
        print('drawing circle:', self)  
  
class Rectangle(Shape):  
    def __init__(self, point, height, width):  
        self.top_left = point  
        self.height = height  
        self.width = width  
  
    def draw(self):  
        print('drawing rectangle:', self)
```

Draw All Shape (OOP)-2

```
def draw_all_shape(shapes: List[Shape]):  
    for shape in shapes:  
        shape.draw()
```

```
class Shape(ABC):  
    @abstractmethod  
    def draw(self):  
        pass
```

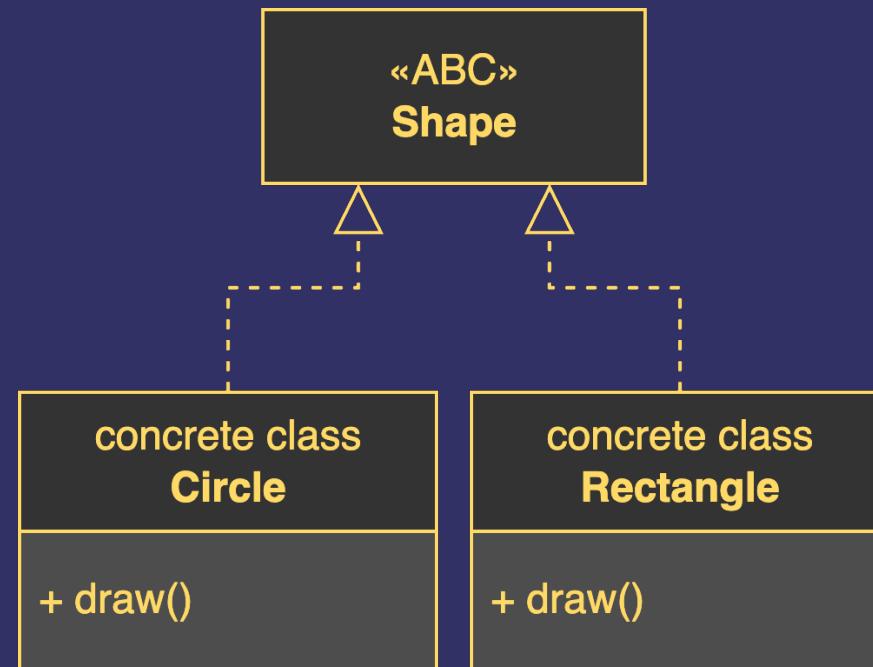
You don't need to modify existing codes.

```
class Square(Shape):  
    def __init__(self, point, side):  
        self.top_left = point  
        self.side = side  
  
    def draw(self):  
        print('drawing square:', self)
```

```
class Circle(Shape):  
    def __init__(self, point, radius):  
        self.center = point  
        self.radius = radius  
  
    def draw(self):  
        print('drawing circle:', self)  
  
class Rectangle(Shape):  
    def __init__(self, point, height, width):  
        self.top_left = point  
        self.height = height  
        self.width = width  
  
    def draw(self):  
        print('drawing rectangle:', self)
```

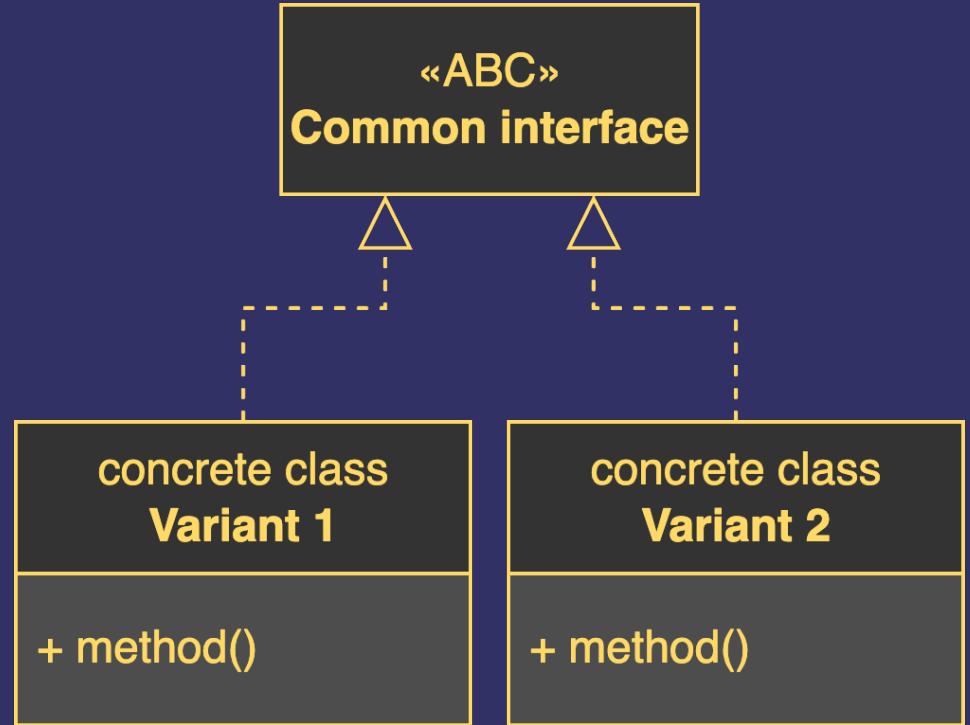
Principles for Creating Good OO Design

- Program to an interface, not an implementation
- Favor object composition over class inheritance



Thinking in Design Patterns

- Context first (design from context)
- Building by adding distinctions
- One pattern at a time
- Encapsulate variations in classes



Design Patterns in Python

Design Pattern in Dynamic Languages

- Peter Norvig states that 16 out of the 23 patterns in the original *Design Patterns* book become either “**invisible or simpler**” in a **dynamic language** (slide 9)
- [“Design Patterns in Dynamic Languages” \(1996\)](#)

Source: <http://norvig.com/design-patterns/design-patterns.pdf>

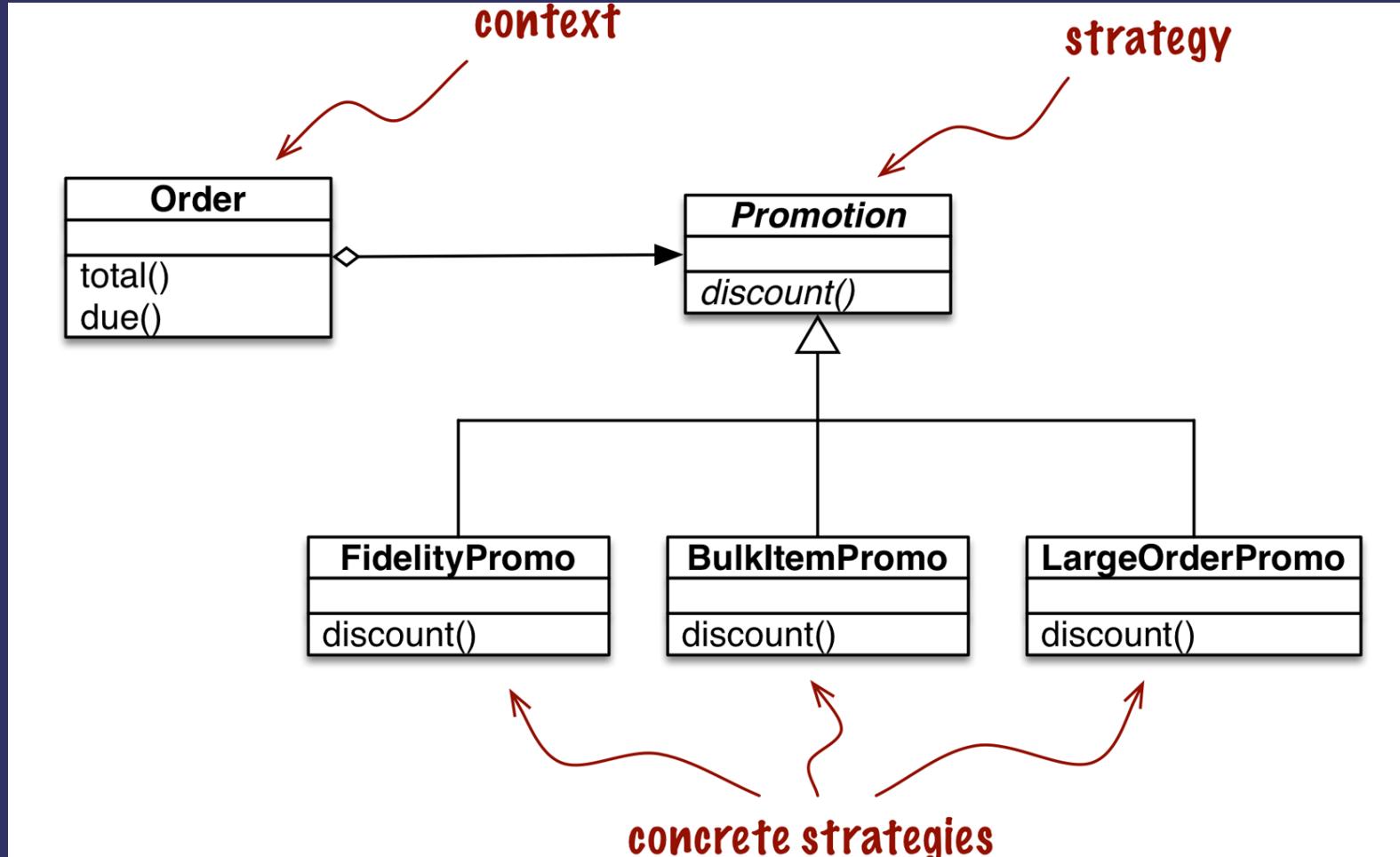


First Class Object

- Functions in Python are first-class objects.
- A “first-class object” as a program entity that can be:
 - created at runtime;
 - assigned to a variable or element in a data structure;
 - passed as an argument to a function;
 - returned as the result of a function.



Strategy pattern



Source: Fluent Python, 2nd ed., Ch.10



Function-Oriented Strategy

```
def fidelity_promotion(order): """5% discount for customers with 1000 or more fidelity points"""
    return order.total() * .05 if order.customer.fidelity >= 1000 else 0

def bulk_item_promotion(order): """10% discount for each LineItem with 20 or more units"""
    discount = 0
    for item in order.cart:
        if item.quantity >= 20:
            discount += item.total() * .1
    return discount

def large_order_promotion(order): """7% discount for orders with 10 or more distinct items"""
    distinct_items = {item.product for item in order.cart}
    if len(distinct_items) >= 10:
        return order.total() * .07
    return 0
```

Function-Oriented Strategy



function as an element in List “promos”

```
promos = [fidelity_promotion, bulk_item_promotion, large_order_promotion]

def best_promotion(order):
    return max(promo(order) for promo in promos)
```



Modules are “Singletons” in Python

- import only creates a single copy of each module
- subsequent imports of the same name keep returning the same module object
- Official Python FAQ[1]:
using a **module** is also the basis for implementing the **Singleton design pattern**, for the same reason.

[1] <https://docs.python.org/3/faq/programming.html#how-do-i-share-global-variables-across-modules>



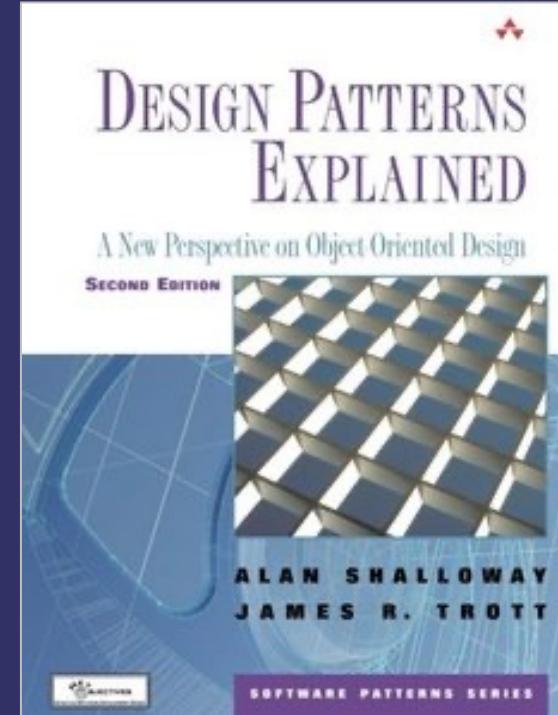
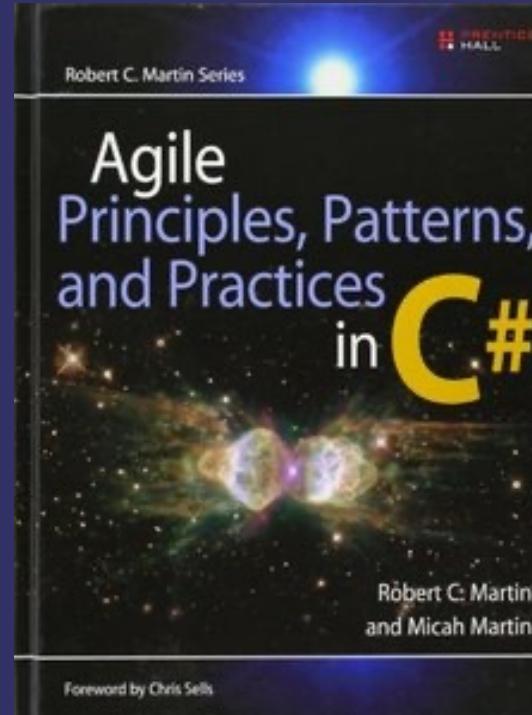
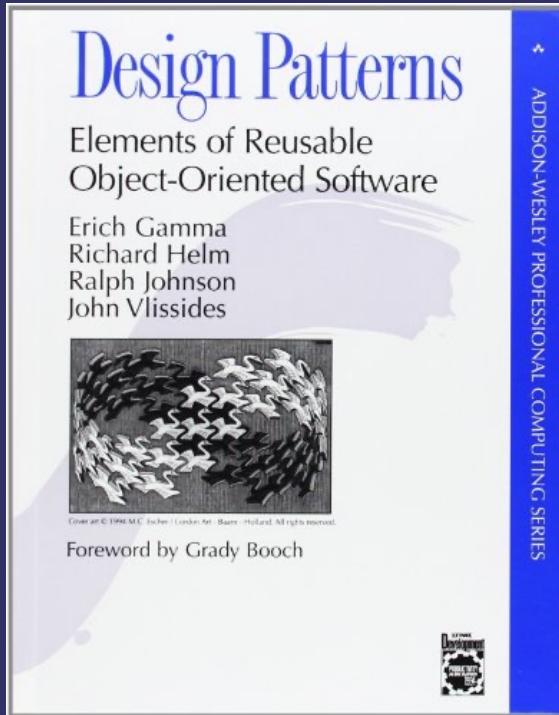
Key Takeaways

What	<ul style="list-style-type: none">• Have a context• Solve a problem• Recur• Have a name
Why	<ul style="list-style-type: none">• Reuse solutions• Establish common terminology• Give a higher perspective on design
How	<ul style="list-style-type: none">• Context first• One pattern at a time• Encapsulate variations





References



03 - Project

Project: subject

Game of war (card game)

Bataille

- Create a game system of 52 Cards
- Rules at : [https://fr.wikipedia.org/wiki/Bataille_\(jeu\)](https://fr.wikipedia.org/wiki/Bataille_(jeu)) - Bataille ouverte (players know their cards and play 1-by-1)
- Define the game rules in a Class `Game`
- 2 Players, Opponent is a random player (Plays a random card in his hand)
- Your player is a algorithm that plays the best card in his hand and in case of draw the worst as token
- main.py:
 - Create a new game: shuffle and distribute cards to the two players
 - Play until the game is finished, print the played cards at each turn
 - (turn=each player plays 1 card and the winner gets all, in case of draw: one card is put as token and they play again to win all)
 - Print the winning player and his number of cards

Project information

- Projects have to be submitted by 15/06/2023 23:59
- Create a pull request on github containing all your code and the main.py to execute it
- Everything has to be coded in python
- You will be evaluated on the quality of code (and if it works !)
- We have another course together on wednesday next week, so don't hesitate to look at the project by then to ask me questions, otherwise send a mail to diviyan@fentech.ai

Good luck !



Questions ?