Improvise a Jazz Solo with an LSTM Network

Welcome to your final programming assignment of this week! In this notebook, you will implement a model that uses an LSTM to generate music. At the end, you'll even be able to listen to your own music!



By the end of this assignment, you'll be able to:

- Apply an LSTM to a music generation task
- Generate your own jazz music with deep learning
- Use the flexible Functional API to create complex models

This is going to be a fun one. Let's get started!

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Packages

Run the following cell to load all the packages you'll need. This may take a few minutes!

```
In [1]: import IPython
        import sys
        import matplotlib.pyplot as plt
        import numpy as np
        import tensorflow as tf
        from music21 import *
        from grammar import *
        from qa import *
        from preprocess import *
        from music utils import *
        from data utils import *
        from outputs import *
        from test_utils import *
        from tensorflow.keras.layers import Dense, Activation, Dropout, Inp
        ut, LSTM, Reshape, Lambda, RepeatVector
        from tensorflow.keras.models import Model
        from tensorflow.keras.optimizers import Adam
        from tensorflow.keras.utils import to categorical
```

1 - Problem Statement

You would like to create a jazz music piece specially for a friend's birthday. However, you don't know how to play any instruments, or how to compose music. Fortunately, you know deep learning and will solve this problem using an LSTM network!

You will train a network to generate novel jazz solos in a style representative of a body of performed work.

1.1 - Dataset

To get started, you'll train your algorithm on a corpus of Jazz music. Run the cell below to listen to a snippet of the audio from the training set:

The preprocessing of the musical data has been taken care of already, which for this notebook means it's been rendered in terms of musical "values."

What are musical "values"? (optional)

You can informally think of each "value" as a note, which comprises a pitch and duration. For example, if you press down a specific piano key for 0.5 seconds, then you have just played a note. In music theory, a "value" is actually more complicated than this -- specifically, it also captures the information needed to play multiple notes at the same time. For example, when playing a music piece, you might press down two piano keys at the same time (playing multiple notes at the same time generates what's called a "chord"). But you don't need to worry about the details of music theory for this assignment.

Music as a sequence of values

- For the purposes of this assignment, all you need to know is that you'll obtain a dataset of values, and will use an RNN model to generate sequences of values.
- Your music generation system will use 90 unique values.

Run the following code to load the raw music data and preprocess it into values. This might take a few minutes!

You have just loaded the following:

- x: This is an (m, T_x , 90) dimensional array.
 - You have m training examples, each of which is a snippet of $T_x = 30$ musical values.
 - At each time step, the input is one of 90 different possible values, represented as a one-hot vector.
 - For example, X[i,t,:] is a one-hot vector representing the value of the i-th example at time t.
- Y: a $(T_v, m, 90)$ dimensional array
 - This is essentially the same as x, but shifted one step to the left (to the past).
 - Notice that the data in Y is **reordered** to be dimension $(T_y, m, 90)$, where $T_y = T_x$. This format makes it more convenient to feed into the LSTM later.
 - Similar to the dinosaur assignment, you're using the previous values to predict the next value.
 - So your sequence model will try to predict $y^{\langle t \rangle}$ given $x^{\langle 1 \rangle}, \dots, x^{\langle t \rangle}$.
- n values: The number of unique values in this dataset. This should be 90.
- indices values: python dictionary mapping integers 0 through 89 to musical values.
- chords: Chords used in the input midi

1.2 - Model Overview

Here is the architecture of the model you'll use. It's similar to the Dinosaurus model, except that you'll implement it in Keras.

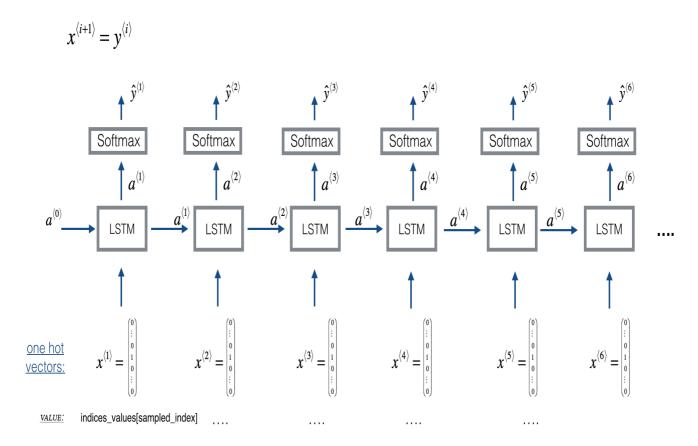


Figure 1: Basic LSTM model

- $X=(x^{\langle 1 \rangle}, x^{\langle 2 \rangle}, \cdots, x^{\langle T_x \rangle})$ is a window of size T_x scanned over the musical corpus.
- Each $x^{\langle t \rangle}$ is an index corresponding to a value.
- $\hat{y}^{\langle t \rangle}$ is the prediction for the next value.
- You'll be training the model on random snippets of 30 values taken from a much longer piece of music.
 - Thus, you won't bother to set the first input $x^{\langle 1 \rangle} = \vec{0}$, since most of these snippets of audio start somewhere in the middle of a piece of music.
 - You're setting each of the snippets to have the same length $T_x=30$ to make vectorization easier.

Overview of Section 2 and 3

In Section 2, you're going to train a model that predicts the next note in a style similar to the jazz music it's trained on. The training is contained in the weights and biases of the model.

Then, in Section 3, you're going to use those weights and biases in a new model that predicts a series of notes, and using the previous note to predict the next note.

 The weights and biases are transferred to the new model using the global shared layers (LSTM cell, densor, reshaper) described below

2 - Building the Model

Now, you'll build and train a model that will learn musical patterns.

- The model takes input X of shape $(m, T_x, 90)$ and labels Y of shape $(T_v, m, 90)$.
- You'll use an LSTM with hidden states that have $n_a = 64$ dimensions.

```
In [6]: # number of dimensions for the hidden state of each LSTM cell.
    n_a = 64
```

Sequence generation uses a for-loop

- If you're building an RNN where, at test time, the entire input sequence $x^{\langle 1 \rangle}, x^{\langle 2 \rangle}, \dots, x^{\langle T_x \rangle}$ is given in advance, then Keras has simple built-in functions to build the model.
- However, for sequence generation, at test time you won't know all the values of $x^{\langle t \rangle}$ in advance.
- Instead, you'll generate them one at a time using $x^{\langle t \rangle} = y^{\langle t-1 \rangle}$.
 - The input at time "t" is the prediction at the previous time step "t-1".
- So you'll need to implement your own for-loop to iterate over the time steps.

Shareable weights

- The function djmodel() will call the LSTM layer T_x times using a for-loop.
- It is important that all T_x copies have the same weights.
 - The T_x steps should have shared weights that aren't re-initialized.
- Referencing a globally defined shared layer will utilize the same layer-object instance at each time step.
- The key steps for implementing layers with shareable weights in Keras are:
- 1. Define the layer objects (you'll use global variables for this).
- 2. Call these objects when propagating the input.

3 types of layers

- The layer objects you need for global variables have been defined.
 - Just run the next cell to create them!
- Please read the Keras documentation and understand these layers:
 - Reshape() (https://www.tensorflow.org/api_docs/python/tf/keras/layers/Reshape): Reshapes an output to a certain shape.
 - LSTM() (https://www.tensorflow.org/api_docs/python/tf/keras/layers/LSTM): Long Short-Term Memory layer
 - <u>Dense() (https://www.tensorflow.org/api_docs/python/tf/keras/layers/Dense)</u>: A regular fully-connected neural network layer.

```
In [7]: n_values = 90 # number of music values
    reshaper = Reshape((1, n_values)) # Used in Step 2
    .B of djmodel(), below
    LSTM_cell = LSTM(n_a, return_state = True) # Used in Step 2
    .C
    densor = Dense(n_values, activation='softmax') # Used in Step 2
    .D
```

- reshaper, LSTM_cell and densor are globally defined layer objects that you'll use to implement djmodel().
- In order to propagate a Keras tensor object X through one of these layers, use layer object().
 - For one input, use layer_object(X)
 - For more than one input, put the inputs in a list: layer object([X1,X2])

Exercise 1 - djmodel

Implement djmodel().

Inputs (given)

- The Input() layer is used for defining the input x as well as the initial hidden state 'a0' and cell state c0.
- The shape parameter takes a tuple that does not include the batch dimension (m).
 - For example,

```
X = Input(shape=(Tx, n_values)) # X has 3 dimensions and not 2:
(m, Tx, n values)
```

Step 1: Outputs

• Create an empty list "outputs" to save the outputs of the LSTM Cell at every time step.

Step 2: Loop through time steps

• Loop for $t \in 1, ..., T_x$:

2A. Select the 't' time-step vector from x.

- X has the shape (m, Tx, n_values).
- The shape of the 't' selection should be (n_values,).
- Recall that if you were implementing in numpy instead of Keras, you would extract a slice from a 3D numpy array like this:

```
var1 = array1[:,1,:]
```

2B. Reshape x to be (1, n_values).

• Use the reshaper() layer. This is a function that takes the previous layer as its input argument.

2C. Run x through one step of LSTM cell.

- Initialize the LSTM cell with the previous step's hidden state a and cell state c.
- Use the following formatting:

```
next_hidden_state, _, next_cell_state = LSTM_cell(inputs=input_x, in
itial state=[previous hidden state, previous cell state])
```

• Choose appropriate variables for inputs, hidden state and cell state.

2D. Dense layer

• Propagate the LSTM's hidden state through a dense+softmax layer using densor.

2E. Append output

• Append the output to the list of "outputs".

Step 3: After the loop, create the model

- Use the Keras Model object to create a model. There are two ways to instantiate the Model object. One is by subclassing, which you won't use here. Instead, you'll use the highly flexible Functional API, which you may remember from an earlier assignment in this course! With the Functional API, you'll start from your Input, then specify the model's forward pass with chained layer calls, and finally create the model from inputs and outputs.
- Specify the inputs and output like so:

```
model = Model(inputs=[input_x, initial_hidden_state, initial_cell_st
ate], outputs=the_outputs)
```

- Then, choose the appropriate variables for the input tensor, hidden state, cell state, and output.
- See the documentation for <u>Model (https://www.tensorflow.org/api_docs/python/tf/keras/Model)</u>

```
In [8]: # UNQ C1 (UNIQUE CELL IDENTIFIER, DO NOT EDIT)
        # GRADED FUNCTION: djmodel
        def djmodel(Tx, LSTM cell, densor, reshaper):
             Implement the djmodel composed of Tx LSTM cells where each cell
        is responsible
             for learning the following note based on the previous note and
             Each cell has the following schema:
                     [X \{t\}, a \{t-1\}, c0 \{t-1\}] \rightarrow RESHAPE() \rightarrow LSTM() \rightarrow DE
        NSE()
             Arguments:
                 Tx -- length of the sequences in the corpus
                 LSTM_cell -- LSTM layer instance
                 densor -- Dense layer instance
                 reshaper -- Reshape layer instance
             Returns:
                 model -- a keras instance model with inputs [X, a0, c0]
             # Get the shape of input values
             n values = densor.units
             # Get the number of the hidden state vector
            n_a = LSTM_cell.units
             # Define the input layer and specify the shape
             X = Input(shape=(Tx, n values))
             # Define the initial hidden state a0 and initial cell state c0
             # using `Input`
             a0 = Input(shape=(n a,), name='a0')
             c0 = Input(shape=(n a,), name='c0')
```

```
a = a0
    c = c0
    ### START CODE HERE ###
    # Step 1: Create empty list to append the outputs while you ite
rate (≈1 line)
   outputs = []
    # Step 2: Loop over tx
    for t in range(Tx):
        # Step 2.A: select the "t"th time step vector from X.
        x = X[:,t,:]
        # Step 2.B: Use reshaper to reshape x to be (1, n values) (
≈1 line)
        x = reshaper(x)
        # Step 2.C: Perform one step of the LSTM cell
        a, , c = LSTM cell(inputs=x, initial state=[a, c])
        # Step 2.D: Apply densor to the hidden state output of LSTM
Cell
        out = densor(a)
        # Step 2.E: add the output to "outputs"
        outputs.append(out)
    # Step 3: Create model instance
    model = Model(inputs=[X, a0, c0], outputs=outputs)
    ### END CODE HERE ###
    return model
```

Create the model object

- Run the following cell to define your model.
- We will use Tx=30.
- This cell may take a few seconds to run.

```
In [9]: model = djmodel(Tx=30, LSTM_cell=LSTM_cell, densor=densor, reshaper
=reshaper)

In [10]: # UNIT TEST
output = summary(model)
comparator(output, djmodel_out)

All tests passed!

In [11]: # Check your model
model.summary()

Model: "functional_1"
```

Layer (type) onnected to	- Output Shape	Param #	C ===
<pre>input_1 (InputLayer)</pre>	[(None, 30, 90)]	0	
<pre>tf_op_layer_strided_slice (Tens nput_1[0][0]</pre>	[(None, 90)]	0	i
reshape (Reshape) f_op_layer_strided_slice[0][0]	(None, 1, 90)	0	t
f_op_layer_strided_slice_1[0][0]			t
f_op_layer_strided_slice_2[0][0]			t
<pre>f_op_layer_strided_slice_3[0][0]</pre>			t
<pre>f_op_layer_strided_slice_4[0][0]</pre>			t
<pre>f_op_layer_strided_slice_5[0][0]</pre>			t
<pre>f_op_layer_strided_slice_6[0][0]</pre>			t
<pre>f_op_layer_strided_slice_7[0][0]</pre>			t
<pre>f_op_layer_strided_slice_8[0][0]</pre>			t
<pre>f_op_layer_strided_slice_9[0][0]</pre>			t
f_op_layer_strided_slice_10[0][0)		t
f_op_layer_strided_slice_11[0][0)		t
f_op_layer_strided_slice_12[0][0)		t
<pre>f_op_layer_strided_slice_13[0][0]</pre>			t
<pre>f_op_layer_strided_slice_14[0][0]</pre>			t
<pre>f_op_layer_strided_slice_15[0][0]</pre>			t
<pre>f_op_layer_strided_slice_16[0][0]</pre>			t
f_op_layer_strided_slice_17[0][0			t
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_ 1_ 1			t

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<pre>f_op_layer_strided_slice_27[0][</pre>					t
<pre>f_op_layer_strided_slice_28[0][</pre>	0				t
<pre>f_op_layer_strided_slice_29[0][</pre>	0				
a0 (InputLayer)	_ [(None,	64)]		0	
c0 (InputLayer)	[(None,	64)]		0	
tf_op_layer_strided_slice_1 (Tenput_1[0][0]	[(None,	90)]		0	i
<pre>lstm (LSTM) eshape[0][0]</pre>	_ [(None,	64),	(None,	39680	r
0[0][0]					a
0[0][0]					С
eshape[1][0]					r
stm[0][0]					1
stm[0][2]					1
eshape[2][0]					r
stm[1][0]					1
stm[1][2]					1
eshape[3][0]					r
stm[2][0]					1

	1
stm[2][2]	r
eshape[4][0]	1
stm[3][0]	1
stm[3][2]	r
eshape[5][0]	1
stm[4][0]	1
stm[4][2]	
eshape[6][0]	r 1
stm[5][0]	1
stm[5][2]	
eshape[7][0]	r 1
stm[6][0]	
stm[6][2]	1
eshape[8][0]	r
stm[7][0]	1
stm[7][2]	1
eshape[9][0]	r
stm[8][0]	1
stm[8][2]	1
eshape[10][0]	r
stm[9][0]	1
stm[9][2]	1
eshape[11][0]	r
stm[10][0]	1
stm[10][2]	1
eshape[12][0]	r
	1

stm[11][0]	
stm[11][2]	1
eshape[13][0]	r
stm[12][0]	1
	1
stm[12][2]	r
eshape[14][0]	1
stm[13][0]	1
stm[13][2]	r
eshape[15][0]	1
stm[14][0]	1
stm[14][2]	r
eshape[16][0]	1
stm[15][0]	1
stm[15][2]	r
eshape[17][0]	1
stm[16][0]	1
stm[16][2]	r
eshape[18][0]	1
stm[17][0]	1
stm[17][2]	r
eshape[19][0]	1
stm[18][0]	1
stm[18][2]	r
eshape[20][0]	1
stm[19][0]	1
stm[19][2]	
eshape[21][0]	r

a+m(201(01	1
stm[20][0]	1
stm[20][2]	r
eshape[22][0]	1
stm[21][0]	1
stm[21][2]	r
eshape[23][0]	1
stm[22][0]	1
stm[22][2]	r
eshape[24][0]	1
stm[23][0]	
stm[23][2]	1
eshape[25][0]	r
stm[24][0]	1
stm[24][2]	1
eshape[26][0]	r
stm[25][0]	1
stm[25][2]	1
eshape[27][0]	r
stm[26][0]	1
stm[26][2]	1
eshape[28][0]	r
stm[27][0]	1
stm[27][2]	1
eshape[29][0]	r
	1
stm[28][0]	1
stm[28][2]	

<pre>tf_op_layer_strided_slice_2 (Te [(None, nput_1[0][0]</pre>	90)]	0	i
<pre>tf_op_layer_strided_slice_3 (Te [(None, nput_1[0][0]</pre>	90)]	0	i
<pre>tf_op_layer_strided_slice_4 (Te [(None, nput_1[0][0]</pre>	90)]	0	i
<pre>tf_op_layer_strided_slice_5 (Te [(None, nput_1[0][0]</pre>	90)]	0	i
<pre>tf_op_layer_strided_slice_6 (Te [(None, nput_1[0][0]</pre>	90)]	0	i
<pre>tf_op_layer_strided_slice_7 (Te [(None, nput_1[0][0]</pre>	90)]	0	i
<pre>tf_op_layer_strided_slice_8 (Te [(None, nput_1[0][0]</pre>	90)]	0	i
<pre>tf_op_layer_strided_slice_9 (Te [(None, nput_1[0][0]</pre>	90)]	0	i
<pre>tf_op_layer_strided_slice_10 (T [(None, nput_1[0][0]</pre>	90)]	0	i
<pre>tf_op_layer_strided_slice_11 (T [(None, nput_1[0][0]</pre>	90)]	0	i
<pre>tf_op_layer_strided_slice_12 (T [(None, nput_1[0][0]</pre>	90)]	0	i
<pre>tf_op_layer_strided_slice_13 (T [(None, nput_1[0][0]</pre>	90)]	0	i
<pre>tf_op_layer_strided_slice_14 (T [(None, nput_1[0][0]</pre>	90)]	0	i
			_

<pre>tf_op_layer_strided_slice_15 nput_1[0][0]</pre>	(T [(None,	90)]	0	i
tf_op_layer_strided_slice_16 nput_1[0][0]	(T [(None,	90)]	0	i
tf_op_layer_strided_slice_17 nput_1[0][0]	(T [(None,	90)]	0	i
tf_op_layer_strided_slice_18 nput_1[0][0]	(T [(None,	90)]	0	i
tf_op_layer_strided_slice_19 nput_1[0][0]	(T [(None,	90)]	0	i
tf_op_layer_strided_slice_20 nput_1[0][0]	(T [(None,	90)]	0	i
tf_op_layer_strided_slice_21 nput_1[0][0]	(T [(None,	90)]	0	i
tf_op_layer_strided_slice_22 nput_1[0][0]	(T [(None,	90)]	0	i
tf_op_layer_strided_slice_23 nput_1[0][0]	(T [(None,	90)]	0	i
tf_op_layer_strided_slice_24 nput_1[0][0]	(T [(None,	90)]	0	i
tf_op_layer_strided_slice_25 nput_1[0][0]	(T [(None,	90)]	0	i
tf_op_layer_strided_slice_26 nput_1[0][0]	(T [(None,	90)]	0	i
tf_op_layer_strided_slice_27 nput_1[0][0]	(T [(None,	90)]	0	i
tf_op_layer_strided_slice_28	(T)	None,	90)]	0	i

nput_1[0][0]

tf_op_layer_strided_slinput_1[0][0]	ce_29 (T [(None, 90)]	0	i
dense (Dense) stm[0][0]	(None, 90)	5850	1
stm[1][0]			1
stm[2][0]			1
stm[3][0]			1
stm[4][0]			1
stm[5][0]			1
stm[6][0]			1
stm[7][0]			1
stm[8][0]			1
stm[9][0]			1
stm[10][0]			1
stm[11][0]			1
stm[12][0]			1
stm[13][0]			1
stm[14][0]			1
stm[15][0]			1
stm[16][0]			1
stm[17][0]			
stm[18][0]			1
stm[19][0]			1
stm[20][0]			1
stm[21][0]			1
stm[22][0]			1

```
1
stm[23][0]
                                                            1
stm[24][0]
                                                            1
stm[25][0]
                                                            1
stm[26][0]
                                                            1
stm[27][0]
                                                            1
stm[28][0]
                                                            1
stm[29][0]
_____
Total params: 45,530
Trainable params: 45,530
Non-trainable params: 0
```

Expected Output

Scroll to the bottom of the output, and you'll see the following:

```
Total params: 45,530
Trainable params: 45,530
Non-trainable params: 0
```

Compile the model for training

- You now need to compile your model to be trained.
- · We will use:
 - optimizer: Adam optimizer
 - Loss function: categorical cross-entropy (for multi-class classification)

```
In [12]: opt = Adam(lr=0.01, beta_1=0.9, beta_2=0.999, decay=0.01)
    model.compile(optimizer=opt, loss='categorical_crossentropy', metri cs=['accuracy'])
```

Initialize hidden state and cell state

Finally, let's initialize a0 and c0 for the LSTM's initial state to be zero.

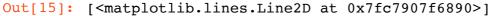
```
In [13]: m = 60
         a0 = np.zeros((m, n a))
         c0 = np.zeros((m, n_a))
```

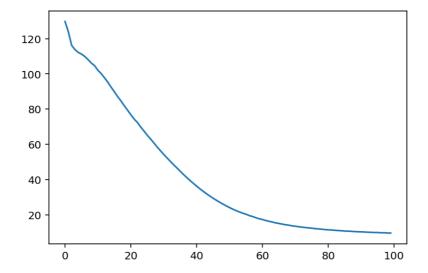
Train the model

You're now ready to fit the model!

- You'll turn Y into a list, since the cost function expects Y to be provided in this format.
 - list(Y) is a list with 30 items, where each of the list items is of shape (60,90).
 - Train for 100 epochs (This will take a few minutes).

```
In [14]:
         history = model.fit([X, a0, c0], list(Y), epochs=100, verbose = 0)
In [15]: print(f"loss at epoch 1: {history.history['loss'][0]}")
         print(f"loss at epoch 100: {history.history['loss'][99]}")
         plt.plot(history.history['loss'])
         loss at epoch 1: 129.75904846191406
         loss at epoch 100: 9.682165145874023
```





Expected Output

The model loss will start high, (100 or so), and after 100 epochs, it should be in the single digits. These won't be the exact number that you'll see, due to random initialization of weights. For example:

```
loss at epoch 1: 129.88641357421875 ...
```

Scroll to the bottom to check Epoch 100

```
loss at epoch 100: 9.21483039855957
```

Now that you have trained a model, let's go to the final section to implement an inference algorithm, and generate some music!

3 - Generating Music

You now have a trained model which has learned the patterns of a jazz soloist. You can now use this model to synthesize new music!

3.1 - Predicting & Sampling

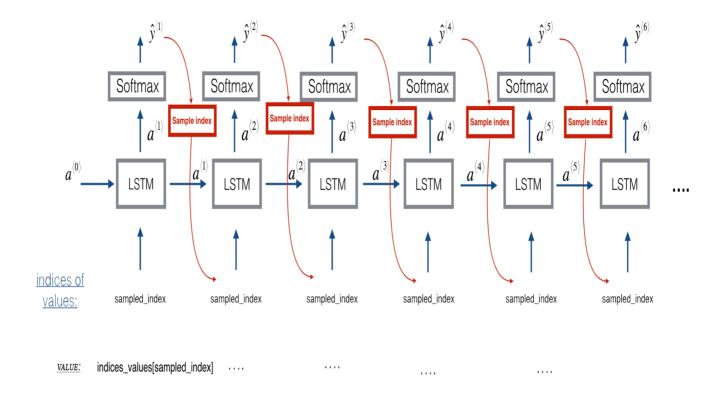


Figure 2: Generating new values in an LSTM

At each step of sampling, you will:

- Take as input the activation 'a 'and cell state 'c' from the previous state of the LSTM.
- Forward propagate by one step.
- Get a new output activation, as well as cell state.
- The new activation 'a' can then be used to generate the output using the fully connected layer, densor.

Initialization

- You'll initialize the following to be zeros:
 - x0
 - hidden state a0
 - cell state c0

Exercise 2 - music inference model

Implement music inference model() to sample a sequence of musical values.

Here are some of the key steps you'll need to implement inside the for-loop that generates the T_y output characters:

Step 1: Create an empty list "outputs" to save the outputs of the LSTM Cell at every time step.

Step 2.A: Use LSTM_Cell , which takes in the input layer, as well as the previous step's 'c' and 'a' to generate the current step's 'c' and 'a'.

```
next_hidden_state, _, next_cell_state = LSTM_cell(input_x, initial_stat
e=[previous hidden state, previous cell state])
```

- Choose the appropriate variables for input x, hidden state, and cell state
- **2.B**: Compute the output by applying densor to compute a softmax on 'a 'to get the output for the current step.
- 2.C: Append the output to the list outputs .
- **2.D**: Convert the last output into a new input for the next time step. You will do this in 2 substeps:
 - Get the index of the maximum value of the predicted output using tf.math.argmax along the last axis.
 - Convert the index into its n_values-one-hot encoding using tf.one_hot.
- **2.E**: Use RepeatVector(1)(x) to convert the output of the one-hot enconding with shape=(None, 90) into a tensor with shape=(None, 1, 90)

Step 3: Inference Model:

This is how to use the Keras Model object:

```
model = Model(inputs=[input_x, initial_hidden_state, initial_cell_state
], outputs=the_outputs)
```

• Choose the appropriate variables for the input tensor, hidden state, cell state, and output.

Hint: the inputs to the model are the **initial** inputs and states.

```
In [18]: # UNO C2 (UNIQUE CELL IDENTIFIER, DO NOT EDIT)
         # GRADED FUNCTION: music inference model
         def music inference model(LSTM cell, densor, Ty=100):
             Uses the trained "LSTM cell" and "densor" from model() to gener
         ate a sequence of values.
             Arguments:
             LSTM cell -- the trained "LSTM cell" from model(), Keras layer
         object
             densor -- the trained "densor" from model(), Keras layer object
             Ty -- integer, number of time steps to generate
             Returns:
             inference model -- Keras model instance
             # Get the shape of input values
             n values = densor.units
             # Get the number of the hidden state vector
             n a = LSTM cell.units
             # Define the input of your model with a shape
             x0 = Input(shape=(1, n values))
             # Define s0, initial hidden state for the decoder LSTM
             a0 = Input(shape=(n a,), name='a0')
             c0 = Input(shape=(n a,), name='c0')
             a = a0
             c = c0
             x = x0
             ### START CODE HERE ###
             # Step 1: Create an empty list of "outputs" to later store your
         predicted values (≈1 line)
             outputs = []
             # Step 2: Loop over Ty and generate a value at every time step
```

```
for t in range(Ty):
        # Step 2.A: Perform one step of LSTM cell. Use "x", not "x0
" (≈1 line)
        a, , c = LSTM cell(inputs=x, initial state=[a, c])
        # Step 2.B: Apply Dense layer to the hidden state output of
the LSTM cell (≈1 line)
        out = densor(a)
        # Step 2.C: Append the prediction "out" to "outputs". out.s
hape = (None, 90) (\approx1 line)
        outputs.append(out)
        # Step 2.D:
        # Select the next value according to "out",
        # Set "x" to be the one-hot representation of the selected
value
        # See instructions above.
        x = tf.math.argmax(out, axis= -1)
        x = tf.one hot(x, depth = n values)
        # Step 2.E:
        # Use RepeatVector(1) to convert x into a tensor with shape
=(None, 1, 90)
        x = RepeatVector(1)(x)
    # Step 3: Create model instance with the correct "inputs" and "
outputs" (≈1 line)
    inference model = Model(inputs=[x0, a0, c0], outputs=outputs)
    ### END CODE HERE ###
    return inference model
```

Run the cell below to define your inference model. This model is hard coded to generate 50 values.

input_3 (InputLayer)		1, 90)]	0	
a0 (InputLayer)	_ [(None,	64)]	0	
c0 (InputLayer)	_ [(None,	64)]	0	
lstm (LSTM) nput_3[0][0]	 [(None,	64), (None,	39680	i
0[0][0]0				a
0[0][0]				С
epeat_vector_1[0][0]				r
stm[31][0]				1
stm[31][2]				1
epeat_vector_2[0][0]				r
stm[32][0]				1
stm[32][2]				1
epeat_vector_3[0][0]				r
stm[33][0]				1
stm[33][2]				1
epeat_vector_4[0][0]				r
stm[34][0]				1
stm[34][2]				1
epeat_vector_5[0][0]				r
stm[35][0]				1
stm[35][2]				1
epeat_vector_6[0][0]				r
stm[36][0]				1
stm[36][2]				1
				r

epeat_vector_7[0][0]	
stm[37][0]	1
stm[37][2]	1
epeat_vector_8[0][0]	r
stm[38][0]	1
stm[38][2]	1
epeat_vector_9[0][0]	r
stm[39][0]	1
stm[39][2]	1
epeat_vector_10[0][0]	r
stm[40][0]	1
stm[40][2]	1
epeat_vector_11[0][0]	r
stm[41][0]	1
stm[41][2]	1
epeat_vector_12[0][0]	r
stm[42][0]	1
stm[42][2]	1
epeat_vector_13[0][0]	r
stm[43][0]	1
	1
stm[43][2]	r
epeat_vector_14[0][0]	1
stm[44][0]	1
stm[44][2]	r
epeat_vector_15[0][0]	1
stm[45][0]	1
stm[45][2]	

	Т
epeat_vector_16[0][0]	1
stm[46][0]	1
stm[46][2]	r
epeat_vector_17[0][0]	1
stm[47][0]	1
stm[47][2]	
epeat_vector_18[0][0]	r
stm[48][0]	1
stm[48][2]	1
epeat_vector_19[0][0]	r
stm[49][0]	1
stm[49][2]	1
epeat_vector_20[0][0]	r
stm[50][0]	1
stm[50][2]	1
epeat_vector_21[0][0]	r
stm[51][0]	1
stm[51][2]	1
epeat_vector_22[0][0]	r
stm[52][0]	1
stm[52][2]	1
	r
epeat_vector_23[0][0]	1
stm[53][0]	1
stm[53][2]	r
epeat_vector_24[0][0]	1
stm[54][0]	1

stm[54][2]	
epeat_vector_25[0][0]	r
stm[55][0]	1
stm[55][2]	1
epeat_vector_26[0][0]	r
stm[56][0]	1
stm[56][2]	1
epeat_vector_27[0][0]	r
stm[57][0]	1
stm[57][2]	1
epeat_vector_28[0][0]	r
stm[58][0]	1
stm[58][2]	1
epeat_vector_29[0][0]	r
stm[59][0]	1
stm[59][2]	1
epeat_vector_30[0][0]	r
stm[60][0]	1
stm[60][2]	1
	r
epeat_vector_31[0][0]	1
stm[61][0]	1
stm[61][2]	r
epeat_vector_32[0][0]	1
stm[62][0]	1
stm[62][2]	r
epeat_vector_33[0][0]	1
stm[63][0]	

	Τ
stm[63][2]	r
epeat_vector_34[0][0]	1
stm[64][0]	1
stm[64][2]	r
epeat_vector_35[0][0]	1
stm[65][0]	1
stm[65][2]	
epeat_vector_36[0][0]	r
stm[66][0]	1
stm[66][2]	1
epeat_vector_37[0][0]	r
stm[67][0]	1
stm[67][2]	1
epeat_vector_38[0][0]	r
stm[68][0]	1
stm[68][2]	1
epeat_vector_39[0][0]	r
stm[69][0]	1
stm[69][2]	1
epeat_vector_40[0][0]	r
stm[70][0]	1
	1
stm[70][2]	r
epeat_vector_41[0][0]	1
stm[71][0]	1
stm[71][2]	r
epeat_vector_42[0][0]	1

stm[72][0]			1
stm[72][2]			r
epeat_vector_43[0][0]			1
stm[73][0]			1
stm[73][2]			r
epeat_vector_44[0][0]			1
stm[74][0]			1
stm[74][2]			r
epeat_vector_45[0][0]			1
stm[75][0]			1
stm[75][2]			
epeat_vector_46[0][0]			r 1
stm[76][0]			1
stm[76][2]			
epeat_vector_47[0][0]			r
stm[77][0]			1
stm[77][2]			
epeat_vector_48[0][0]			r
stm[78][0]			1
stm[78][2]			1
epeat_vector_49[0][0]			r
stm[79][0]			1
stm[79][2]			1
dongo (Dongo)	(None 90)	5850	
<pre>dense (Dense) stm[31][0]</pre>	(None, 90)	3030	1
stm[32][0]			1
stm[33][0]			Τ

	1
stm[34][0]	1
stm[35][0]	1
stm[36][0]	1
stm[37][0]	
stm[38][0]	1
stm[39][0]	1
stm[40][0]	1
stm[41][0]	1
stm[42][0]	1
stm[43][0]	1
stm[44][0]	1
stm[45][0]	1
stm[46][0]	1
stm[47][0]	1
stm[48][0]	1
stm[49][0]	1
stm[50][0]	1
stm[51][0]	1
stm[52][0]	1
stm[53][0]	1
stm[54][0]	1
stm[55][0]	1
stm[56][0]	1
stm[57][0]	1
stm[58][0]	1
stm[59][0]	1
	1

stm[60][0]		1
stm[61][0]		1
stm[62][0]		1
stm[63][0]		1
stm[64][0]		1
stm[65][0]		1
stm[66][0]		1
stm[67][0]		1
stm[68][0]		1
stm[69][0]		1
stm[70][0]		1
stm[71][0]		1
stm[72][0]		1
stm[73][0]		1
stm[74][0]		1
stm[75][0]		1
stm[76][0]		1
stm[77][0]		1
stm[78][0]		1
stm[79][0]		1
stm[80][0]		1
tf_op_layer_ArgMax_1 (TensorFlo [(None,)] ense[31][0]	0	d
tf_op_layer_OneHot_1 (TensorFlo [(None, 90)] f_op_layer_ArgMax_1[0][0]	0	t
repeat_vector_1 (RepeatVector) (None, 1, 90) f_op_layer_OneHot_1[0][0]	0	t

tf_op_layer_ArgMax_2 (TensorFlo ense[32][0]	[(None,)]	0	d
tf_op_layer_OneHot_2 (TensorFlo f_op_layer_ArgMax_2[0][0]	[(None, 90)]	0	t
repeat_vector_2 (RepeatVector) f_op_layer_OneHot_2[0][0]	(None, 1, 90)	0	t
tf_op_layer_ArgMax_3 (TensorFlo ense[33][0]	[(None,)]	0	d
tf_op_layer_OneHot_3 (TensorFlo f_op_layer_ArgMax_3[0][0]	[(None, 90)]	0	t
repeat_vector_3 (RepeatVector) f_op_layer_OneHot_3[0][0]	(None, 1, 90)	0	t
tf_op_layer_ArgMax_4 (TensorFloense[34][0]	[(None,)]	0	d
tf_op_layer_OneHot_4 (TensorFlof_op_layer_ArgMax_4[0][0]	[(None, 90)]	0	t
repeat_vector_4 (RepeatVector) f_op_layer_OneHot_4[0][0]	(None, 1, 90)	0	t
tf_op_layer_ArgMax_5 (TensorFloense[35][0]	[(None,)]	0	d
tf_op_layer_OneHot_5 (TensorFlof_op_layer_ArgMax_5[0][0]	[(None, 90)]	0	t
repeat_vector_5 (RepeatVector) f_op_layer_OneHot_5[0][0]	(None, 1, 90)	0	t
tf_op_layer_ArgMax_6 (TensorFloense[36][0]	[(None,)]	0	d
			_

<pre>tf_op_layer_OneHot_6 (TensorFlo f_op_layer_ArgMax_6[0][0]</pre>	[(None, 90)]	0	t
<pre>repeat_vector_6 (RepeatVector) f_op_layer_OneHot_6[0][0]</pre>	(None, 1, 90)	0	t
tf_op_layer_ArgMax_7 (TensorFloense[37][0]	[(None,)]	0	d
tf_op_layer_OneHot_7 (TensorFlo f_op_layer_ArgMax_7[0][0]	[(None, 90)]	0	t
repeat_vector_7 (RepeatVector) f_op_layer_OneHot_7[0][0]	(None, 1, 90)	0	t
tf_op_layer_ArgMax_8 (TensorFlo ense[38][0]	[(None,)]	0	d
tf_op_layer_OneHot_8 (TensorFlo f_op_layer_ArgMax_8[0][0]	[(None, 90)]	0	t
<pre>repeat_vector_8 (RepeatVector) f_op_layer_OneHot_8[0][0]</pre>	(None, 1, 90)	0	t
tf_op_layer_ArgMax_9 (TensorFlo ense[39][0]	[(None,)]	0	d
tf_op_layer_OneHot_9 (TensorFlo f_op_layer_ArgMax_9[0][0]	[(None, 90)]	0	t
repeat_vector_9 (RepeatVector) f_op_layer_OneHot_9[0][0]	(None, 1, 90)	0	t
tf_op_layer_ArgMax_10 (TensorFl ense[40][0]	[(None,)]	0	d
tf_op_layer_OneHot_10 (TensorFl f_op_layer_ArgMax_10[0][0]	[(None, 90)]	0	t
	_		

<pre>repeat_vector_10 (RepeatVector) f_op_layer_OneHot_10[0][0]</pre>	(None, 1, 90)	0	t
tf_op_layer_ArgMax_11 (TensorFl ense[41][0]	[(None,)]	0	d
tf_op_layer_OneHot_11 (TensorFl f_op_layer_ArgMax_11[0][0]	[(None, 90)]	0	t
repeat_vector_11 (RepeatVector) f_op_layer_OneHot_11[0][0]	(None, 1, 90)	0	t
tf_op_layer_ArgMax_12 (TensorFl ense[42][0]	[(None,)]	0	d
tf_op_layer_OneHot_12 (TensorFl f_op_layer_ArgMax_12[0][0]	[(None, 90)]	0	t
repeat_vector_12 (RepeatVector) f_op_layer_OneHot_12[0][0]	(None, 1, 90)	0	t
tf_op_layer_ArgMax_13 (TensorFl ense[43][0]	[(None,)]	0	d
tf_op_layer_OneHot_13 (TensorFl f_op_layer_ArgMax_13[0][0]	[(None, 90)]	0	t
repeat_vector_13 (RepeatVector) f_op_layer_OneHot_13[0][0]	(None, 1, 90)	0	t
tf_op_layer_ArgMax_14 (TensorFl ense[44][0]	[(None,)]	0	d
tf_op_layer_OneHot_14 (TensorFl f_op_layer_ArgMax_14[0][0]	[(None, 90)]	0	t
repeat_vector_14 (RepeatVector) f_op_layer_OneHot_14[0][0]	(None, 1, 90)	0	t
tf_op_layer_ArgMax_15 (TensorFl	[(None,)]	0	d

ense[45][0]

tf_op_layer_OneHot_15 (TensorFl f_op_layer_ArgMax_15[0][0]	[(None, 90)]	0	t
repeat_vector_15 (RepeatVector) f_op_layer_OneHot_15[0][0]	(None, 1, 90)	0	t
tf_op_layer_ArgMax_16 (TensorFl ense[46][0]	[(None,)]	0	d
tf_op_layer_OneHot_16 (TensorFl f_op_layer_ArgMax_16[0][0]	[(None, 90)]	0	t
repeat_vector_16 (RepeatVector) f_op_layer_OneHot_16[0][0]	(None, 1, 90)	0	t
tf_op_layer_ArgMax_17 (TensorFl ense[47][0]	[(None,)]	0	d
tf_op_layer_OneHot_17 (TensorFl f_op_layer_ArgMax_17[0][0]	[(None, 90)]	0	t
repeat_vector_17 (RepeatVector) f_op_layer_OneHot_17[0][0]	(None, 1, 90)	0	t
tf_op_layer_ArgMax_18 (TensorFl ense[48][0]	[(None,)]	0	d
tf_op_layer_OneHot_18 (TensorFl f_op_layer_ArgMax_18[0][0]	[(None, 90)]	0	t
repeat_vector_18 (RepeatVector) f_op_layer_OneHot_18[0][0]	(None, 1, 90)	0	t
tf_op_layer_ArgMax_19 (TensorFl ense[49][0]	[(None,)]	0	d
tf_op_layer_OneHot_19 (TensorFl f_op_layer_ArgMax_19[0][0]	[(None, 90)]	0	t

<pre>repeat_vector_19 (RepeatVector) f_op_layer_OneHot_19[0][0]</pre>	(None, 1, 90)	0	t
tf_op_layer_ArgMax_20 (TensorFl ense[50][0]	[(None,)]	0	d
tf_op_layer_OneHot_20 (TensorFl f_op_layer_ArgMax_20[0][0]	[(None, 90)]	0	t
repeat_vector_20 (RepeatVector) f_op_layer_OneHot_20[0][0]	(None, 1, 90)	0	t
tf_op_layer_ArgMax_21 (TensorFl ense[51][0]	[(None,)]	0	d
tf_op_layer_OneHot_21 (TensorFl f_op_layer_ArgMax_21[0][0]	[(None, 90)]	0	t
repeat_vector_21 (RepeatVector) f_op_layer_OneHot_21[0][0]	(None, 1, 90)	0	t
tf_op_layer_ArgMax_22 (TensorFl ense[52][0]	[(None,)]	0	d
tf_op_layer_OneHot_22 (TensorFl f_op_layer_ArgMax_22[0][0]	[(None, 90)]	0	t
repeat_vector_22 (RepeatVector) f_op_layer_OneHot_22[0][0]	(None, 1, 90)	0	t
tf_op_layer_ArgMax_23 (TensorFl ense[53][0]	[(None,)]	0	d
tf_op_layer_OneHot_23 (TensorFl f_op_layer_ArgMax_23[0][0]	[(None, 90)]	0	t
repeat_vector_23 (RepeatVector) f_op_layer_OneHot_23[0][0]	(None, 1, 90)	0	t

tf_op_layer_ArgMax_24 (TensorFl [(ense[54][0]	None,)]) d
tf_op_layer_OneHot_24 (TensorFl [(f_op_layer_ArgMax_24[0][0]	None, 90)] () t
repeat_vector_24 (RepeatVector) (Nf_op_layer_OneHot_24[0][0]	one, 1, 90) () t
tf_op_layer_ArgMax_25 (TensorFl [(ense[55][0]	None,)]) d
tf_op_layer_OneHot_25 (TensorFl [(f_op_layer_ArgMax_25[0][0]	None, 90)]) t
repeat_vector_25 (RepeatVector) (Nf_op_layer_OneHot_25[0][0]	one, 1, 90) () t
tf_op_layer_ArgMax_26 (TensorFl [(ense[56][0]	None,)]) d
tf_op_layer_OneHot_26 (TensorFl [(f_op_layer_ArgMax_26[0][0]	None, 90)] (t
repeat_vector_26 (RepeatVector) (Nf_op_layer_OneHot_26[0][0]	one, 1, 90) () t
tf_op_layer_ArgMax_27 (TensorFl [(ense[57][0]	None,)]) d
tf_op_layer_OneHot_27 (TensorFl [(f_op_layer_ArgMax_27[0][0]	None, 90)] (t
repeat_vector_27 (RepeatVector) (Nf_op_layer_OneHot_27[0][0]	one, 1, 90) () t
tf_op_layer_ArgMax_28 (TensorFl [(ense[58][0]	None,)]) d

<pre>tf_op_layer_OneHot_28 (TensorFl f_op_layer_ArgMax_28[0][0]</pre>	[(None, 90)]	0	t
repeat_vector_28 (RepeatVector) f_op_layer_OneHot_28[0][0]	(None, 1, 90)	0	t
tf_op_layer_ArgMax_29 (TensorFl ense[59][0]	[(None,)]	0	d
tf_op_layer_OneHot_29 (TensorFl f_op_layer_ArgMax_29[0][0]	[(None, 90)]	0	t
<pre>repeat_vector_29 (RepeatVector) f_op_layer_OneHot_29[0][0]</pre>	(None, 1, 90)	0	t
tf_op_layer_ArgMax_30 (TensorFl ense[60][0]	[(None,)]	0	d
tf_op_layer_OneHot_30 (TensorFl f_op_layer_ArgMax_30[0][0]	[(None, 90)]	0	t
repeat_vector_30 (RepeatVector) f_op_layer_OneHot_30[0][0]	(None, 1, 90)	0	t
tf_op_layer_ArgMax_31 (TensorFl ense[61][0]	[(None,)]	0	d
tf_op_layer_OneHot_31 (TensorFl f_op_layer_ArgMax_31[0][0]	[(None, 90)]	0	t
repeat_vector_31 (RepeatVector) f_op_layer_OneHot_31[0][0]	(None, 1, 90)	0	t
tf_op_layer_ArgMax_32 (TensorFl ense[62][0]	[(None,)]	0	d
tf_op_layer_OneHot_32 (TensorFl f_op_layer_ArgMax_32[0][0]	[(None, 90)]	0	t
repeat_vector_32 (RepeatVector)	(None, 1, 90)	0	t

f_op_layer_OneHot_32[0][0]

<pre>tf_op_layer_ArgMax_33 (TensorFl [(None,)] ense[63][0]</pre>	0	d
<pre>tf_op_layer_OneHot_33 (TensorFl [(None, 90)] f_op_layer_ArgMax_33[0][0]</pre>	0	t
repeat_vector_33 (RepeatVector) (None, 1, 90) f_op_layer_OneHot_33[0][0]	0	t
tf_op_layer_ArgMax_34 (TensorFl [(None,)] ense[64][0]	0	d
tf_op_layer_OneHot_34 (TensorFl [(None, 90)] f_op_layer_ArgMax_34[0][0]	0	t
repeat_vector_34 (RepeatVector) (None, 1, 90) f_op_layer_OneHot_34[0][0]	0	t
tf_op_layer_ArgMax_35 (TensorFl [(None,)] ense[65][0]	0	d
tf_op_layer_OneHot_35 (TensorFl [(None, 90)] f_op_layer_ArgMax_35[0][0]	0	t
repeat_vector_35 (RepeatVector) (None, 1, 90) f_op_layer_OneHot_35[0][0]	0	t
tf_op_layer_ArgMax_36 (TensorFl [(None,)] ense[66][0]	0	d
<pre>tf_op_layer_OneHot_36 (TensorFl [(None, 90)] f_op_layer_ArgMax_36[0][0]</pre>	0	t
repeat_vector_36 (RepeatVector) (None, 1, 90) f_op_layer_OneHot_36[0][0]	0	t
<pre>tf_op_layer_ArgMax_37 (TensorFl [(None,)] ense[67][0]</pre>	0	d

tf_op_layer_OneHot_37 (TensorFl f_op_layer_ArgMax_37[0][0]	[(None, 90)]	0	t
repeat_vector_37 (RepeatVector) f_op_layer_OneHot_37[0][0]	(None, 1, 90)	0	t
tf_op_layer_ArgMax_38 (TensorFl ense[68][0]	[(None,)]	0	d
tf_op_layer_OneHot_38 (TensorFl f_op_layer_ArgMax_38[0][0]	[(None, 90)]	0	t
repeat_vector_38 (RepeatVector) f_op_layer_OneHot_38[0][0]	(None, 1, 90)	0	t
tf_op_layer_ArgMax_39 (TensorFl ense[69][0]	[(None,)]	0	d
tf_op_layer_OneHot_39 (TensorFl f_op_layer_ArgMax_39[0][0]	[(None, 90)]	0	t
repeat_vector_39 (RepeatVector) f_op_layer_OneHot_39[0][0]	(None, 1, 90)	0	t
tf_op_layer_ArgMax_40 (TensorFl ense[70][0]	[(None,)]	0	d
tf_op_layer_OneHot_40 (TensorFl f_op_layer_ArgMax_40[0][0]	[(None, 90)]	0	t
repeat_vector_40 (RepeatVector) f_op_layer_OneHot_40[0][0]	(None, 1, 90)	0	t
tf_op_layer_ArgMax_41 (TensorFl ense[71][0]	[(None,)]	0	d
tf_op_layer_OneHot_41 (TensorFl f_op_layer_ArgMax_41[0][0]	[(None, 90)]	0	t
-		· · · · · · · · · · · · · · · · · · ·	

<pre>repeat_vector_41 (RepeatVector) f_op_layer_OneHot_41[0][0]</pre>	(None, 1, 90)	0	t
tf_op_layer_ArgMax_42 (TensorFl ense[72][0]	[(None,)]	0	d
<pre>tf_op_layer_OneHot_42 (TensorFl f_op_layer_ArgMax_42[0][0]</pre>	[(None, 90)]	0	t
repeat_vector_42 (RepeatVector) f_op_layer_OneHot_42[0][0]	(None, 1, 90)	0	t
tf_op_layer_ArgMax_43 (TensorFl ense[73][0]	[(None,)]	0	d
tf_op_layer_OneHot_43 (TensorFl f_op_layer_ArgMax_43[0][0]	[(None, 90)]	0	t
repeat_vector_43 (RepeatVector) f_op_layer_OneHot_43[0][0]	(None, 1, 90)	0	t
tf_op_layer_ArgMax_44 (TensorFl ense[74][0]	[(None,)]	0	d
tf_op_layer_OneHot_44 (TensorFl f_op_layer_ArgMax_44[0][0]	[(None, 90)]	0	t
<pre>repeat_vector_44 (RepeatVector) f_op_layer_OneHot_44[0][0]</pre>	(None, 1, 90)	0	t
tf_op_layer_ArgMax_45 (TensorFl ense[75][0]	[(None,)]	0	d
<pre>tf_op_layer_OneHot_45 (TensorFl f_op_layer_ArgMax_45[0][0]</pre>	[(None, 90)]	0	t
repeat_vector_45 (RepeatVector) f_op_layer_OneHot_45[0][0]	(None, 1, 90)	0	t

<pre>tf_op_layer_ArgMax_46 (TensorFl ense[76][0]</pre>	[(None,)]	0	d
tf_op_layer_OneHot_46 (TensorFl f_op_layer_ArgMax_46[0][0]	[(None, 90)]	0	t
<pre>repeat_vector_46 (RepeatVector) f_op_layer_OneHot_46[0][0]</pre>	(None, 1, 90)	0	t
tf_op_layer_ArgMax_47 (TensorFl ense[77][0]	[(None,)]	0	d
tf_op_layer_OneHot_47 (TensorFl f_op_layer_ArgMax_47[0][0]	[(None, 90)]	0	t
<pre>repeat_vector_47 (RepeatVector) f_op_layer_OneHot_47[0][0]</pre>	(None, 1, 90)	0	t
tf_op_layer_ArgMax_48 (TensorFl ense[78][0]	[(None,)]	0	d
tf_op_layer_OneHot_48 (TensorFl f_op_layer_ArgMax_48[0][0]	[(None, 90)]	0	t
repeat_vector_48 (RepeatVector) f_op_layer_OneHot_48[0][0]	(None, 1, 90)	0	t
tf_op_layer_ArgMax_49 (TensorFl ense[79][0]	[(None,)]	0	d
tf_op_layer_OneHot_49 (TensorFl f_op_layer_ArgMax_49[0][0]	[(None, 90)]	0	t
repeat_vector_49 (RepeatVector) f_op_layer_OneHot_49[0][0] =================================		0	t =====

Expected Output

If you scroll to the bottom of the output, you'll see:

```
Total params: 45,530
Trainable params: 45,530
Non-trainable params: 0
```

Initialize inference model

The following code creates the zero-valued vectors you will use to initialize $\, \mathbf{x} \,$ and the LSTM state variables $\, \mathbf{a} \,$ and $\, \mathbf{c} \,$.

```
In [22]: x_initializer = np.zeros((1, 1, n_values))
a_initializer = np.zeros((1, n_a))
c_initializer = np.zeros((1, n_a))
```

Exercise 3 - predict_and_sample

Implement predict_and_sample() .

This function takes many arguments, including the inputs $x_{initializer}$, $a_{initializer}$, and $c_{initializer}$.

In order to predict the output corresponding to this input, you'll need to carry out 3 steps:

Step 1:

• Use your inference model to predict an output given your set of inputs. The output pred should be a list of length T_v where each element is a numpy-array of shape (1, n_values).

```
inference_model.predict([input_x_init, hidden_state_init, cell_state
init])
```

• Choose the appropriate input arguments to predict from the input arguments of this predict and sample function.

Step 2:

- Convert pred into a numpy array of T_v indices.
 - Each index is computed by taking the argmax of an element of the pred list.
 - Use <u>numpy.argmax</u> (https://docs.scipy.org/doc/numpy/reference/generated/numpy.argmax.html).
 - Set the axis parameter.
 - Remember that the shape of the prediction is (m, T_v, n_{values})

Step 3:

- Convert the indices into their one-hot vector representations.
 - Use to categorical (https://www.tensorflow.org/api_docs/python/tf/keras/utils/to_categorical).
 - Set the num classes parameter. Note that for grading purposes: you'll need to either:
 - Use a dimension from the given parameters of predict_and_sample() (for example, one of the dimensions of x_initializer has the value for the number of distinct classes).
 - Or just hard code the number of distinct classes (will pass the grader as well).
 - Note that using a global variable such as n_values will not work for grading purposes.

```
In [23]: # UNQ C3 (UNIQUE CELL IDENTIFIER, DO NOT EDIT)
         # GRADED FUNCTION: predict and sample
         def predict and sample(inference model, x initializer = x_initializ
         er, a initializer = a initializer,
                                c initializer = c initializer):
             Predicts the next value of values using the inference model.
             Arguments:
             inference model -- Keras model instance for inference time
             x initializer -- numpy array of shape (1, 1, 90), one-hot vecto
         r initializing the values generation
             a initializer -- numpy array of shape (1, n_a), initializing th
         e hidden state of the LSTM cell
             c_initializer -- numpy array of shape (1, n_a), initializing th
         e cell state of the LSTM cel
             Returns:
             results -- numpy-array of shape (Ty, 90), matrix of one-hot vec
         tors representing the values generated
             indices -- numpy-array of shape (Ty, 1), matrix of indices repr
         esenting the values generated
             n values = x initializer.shape[2]
             ### START CODE HERE ###
             # Step 1: Use your inference model to predict an output sequenc
         e given x initializer, a initializer and c initializer.
             pred = inference model.predict([x initializer, a initializer, c
         initializer])
             # Step 2: Convert "pred" into an np.array() of indices with the
         maximum probabilities
             indices = np.argmax(pred, axis=-1)
             # Step 3: Convert indices to one-hot vectors, the shape of the
         results should be (Ty, n values)
             results = to categorical(indices, num classes=n values)
             ### END CODE HERE ###
```

return results, indices

```
In [25]: results, indices = predict_and_sample(inference_model, x_initialize
    r, a_initializer, c_initializer)

print("np.argmax(results[12]) =", np.argmax(results[12]))
    print("np.argmax(results[17]) =", np.argmax(results[17]))
    print("list(indices[12:18]) =", list(indices[12:18]))

np.argmax(results[12]) = 7
    np.argmax(results[17]) = 23
    list(indices[12:18]) = [array([7]), array([17]), array([76]), array([71]), array([52]), array([23])]
```

Expected (Approximate) Output:

- Your results may likely differ because Keras' results are not completely predictable.
- However, if you have trained your LSTM_cell with model.fit() for exactly 100 epochs as described above:
 - You should very likely observe a sequence of indices that are not all identical. Perhaps with the following values:

```
**np.argmax(results[12])** = 26

**np.argmax(results[17])** = 7

**list(indices[12:18])** = [array([26]), array([18]), array([53]), array([27]), array([40]), array([7])]
```

3.2 - Generate Music

Finally! You're ready to generate music.

Your RNN generates a sequence of values. The following code generates music by first calling your predict_and_sample() function. These values are then post-processed into musical chords (meaning that multiple values or notes can be played at the same time).

Most computational music algorithms use some post-processing because it's difficult to generate music that sounds good without it. The post-processing does things like clean up the generated audio by making sure the same sound is not repeated too many times, or that two successive notes are not too far from each other in pitch, and so on.

One could argue that a lot of these post-processing steps are hacks; also, a lot of the music generation literature has also focused on hand-crafting post-processors, and a lot of the output quality depends on the quality of the post-processing and not just the quality of the model. But this post-processing does make a huge difference, so you should use it in your implementation as well.

Let's make some music!

Run the following cell to generate music and record it into your <code>out_stream</code> . This can take a couple of minutes.

```
In [26]:    out_stream = generate_music(inference_model, indices_values, chords
)

Predicting new values for different set of chords.
Generated 39 sounds using the predicted values for the set of chor ds ("1") and after pruning
Generated 39 sounds using the predicted values for the set of chor ds ("2") and after pruning
Generated 39 sounds using the predicted values for the set of chor ds ("3") and after pruning
Generated 39 sounds using the predicted values for the set of chor ds ("4") and after pruning
Generated 39 sounds using the predicted values for the set of chor ds ("5") and after pruning
```

Using a basic midi to wav parser you can have a rough idea about the audio clip generated by this model. The parser is very limited.

Your generated music is saved in output/my music.midi

To listen to your music, click File->Open... Then go to "output/" and download "my_music.midi". Either play it on your computer with an application that can read midi files if you have one, or use one of the free online "MIDI to mp3" conversion tools to convert this to mp3.

As a reference, here is a 30 second audio clip generated using this algorithm:

Congratulations!

You've completed this assignment, and generated your own jazz solo! The Coltranes would be proud.

By now, you've:

- Applied an LSTM to a music generation task
- Generated your own jazz music with deep learning
- Used the flexible Functional API to create a more complex model

This was a lengthy task. You should be proud of your hard work, and hopefully you have some good music to show for it. Cheers and see you next time!

What you should remember:

- A sequence model can be used to generate musical values, which are then post-processed into midi music.
- You can use a fairly similar model for tasks ranging from generating dinosaur names to generating original music, with the only major difference being the input fed to the model.
- In Keras, sequence generation involves defining layers with shared weights, which are then repeated for the different time steps $1, \ldots, T_x$.

4 - References

The ideas presented in this notebook came primarily from three computational music papers cited below. The implementation here also took significant inspiration and used many components from Ji-Sung Kim's GitHub repository.

- Ji-Sung Kim, 2016, <u>deepjazz (https://github.com/jisungk/deepjazz)</u>
- Jon Gillick, Kevin Tang and Robert Keller, 2009. <u>Learning Jazz Grammars</u> (http://ai.stanford.edu/~kdtang/papers/smc09-jazzgrammar.pdf)
- Robert Keller and David Morrison, 2007, <u>A Grammatical Approach to Automatic Improvisation</u> (http://smc07.uoa.gr/SMC07%20Proceedings/SMC07%20Paper%2055.pdf)
- François Pachet, 1999, <u>Surprising Harmonies (http://citeseerx.ist.psu.edu/viewdoc/download?doi=10.1.1.5.7473&rep=rep1&type=pdf)</u>

Finally, a shoutout to François Germain for valuable feedback.