

no class next Sun. Oct. 11

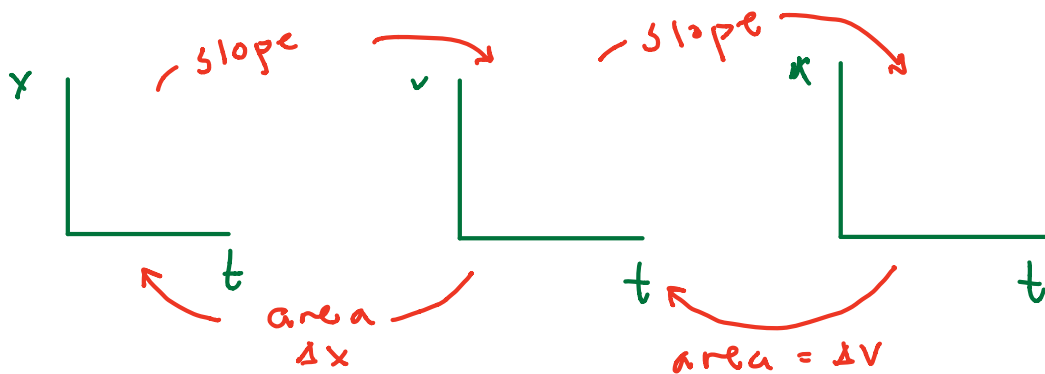
Kinematics

$$\Delta x = v_0 \Delta t + \frac{1}{2} a \Delta t^2$$

$$v = v_0 + a \Delta t$$

$$v^2 = v_0^2 + 2a \Delta x$$

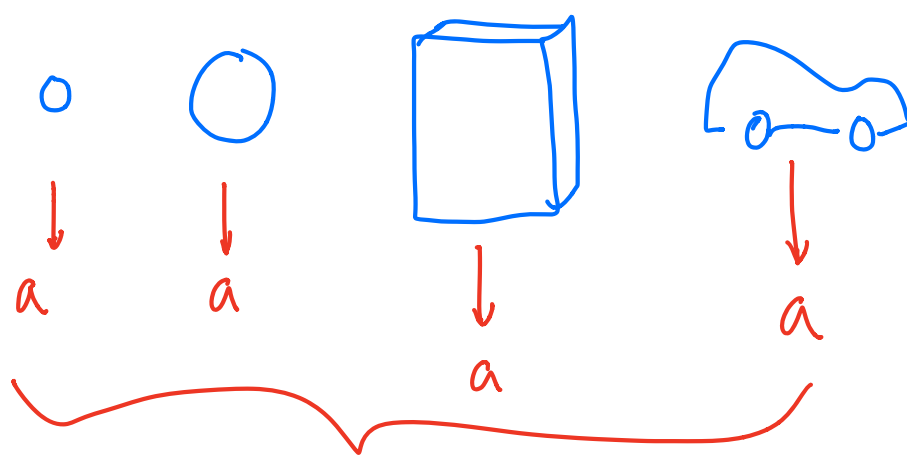
$$\bar{v} = \frac{v_0 + v}{2} = \frac{\Delta x}{\Delta t}$$



Free Fall

motion under the influence
of ONLY gravity





the same acceleration

near Earth's surface

$a = 9.8 \text{ m/s}^2 \text{ DOWN}$

g = the acceleration due to gravity (magnitude)

$$g_{\text{Earth}} = 9.8 \text{ m/s}^2$$

$$g_{\text{moon}} = 1.6 \text{ m/s}^2$$

an object is dropped. How far does it fall in 3s?

$$\hookrightarrow v_0 = 0 \text{ m/s}$$



$$v_0 = 0 \text{ m/s}$$

$$v =$$

$$a = 9.8 \text{ m/s}^2$$

$$\Delta t = 3 \text{ s}$$

$$\Delta x = ?$$

$$\Delta x = \cancel{v_0 \Delta t} + \frac{1}{2} a \Delta t^2$$

$$= \frac{1}{2} (9.8 \text{ m/s}^2) (3 \text{ s})^2$$

$$= 44.1 \text{ m} \quad (45 \text{ m if } a = 10)$$



$$\text{use } g = 10 \text{ m/s}^2$$

How high does it reach?

$$v_0 = +40 \text{ m/s}$$

$$v = 0 \text{ at top}$$

$$a = -10 \text{ m/s}^2$$

$$\Delta t =$$

$$\Delta x = ?$$

$$v^2 = v_0^2 + 2a\Delta x$$

$$0 = (40 \text{ m/s})^2 + 2(-10 \frac{\text{m}}{\text{s}^2})(\Delta x)$$

$$\frac{-1600 \text{ m}^2/\text{s}^2}{-20 \text{ m/s}^2} = 80 \text{ m}$$

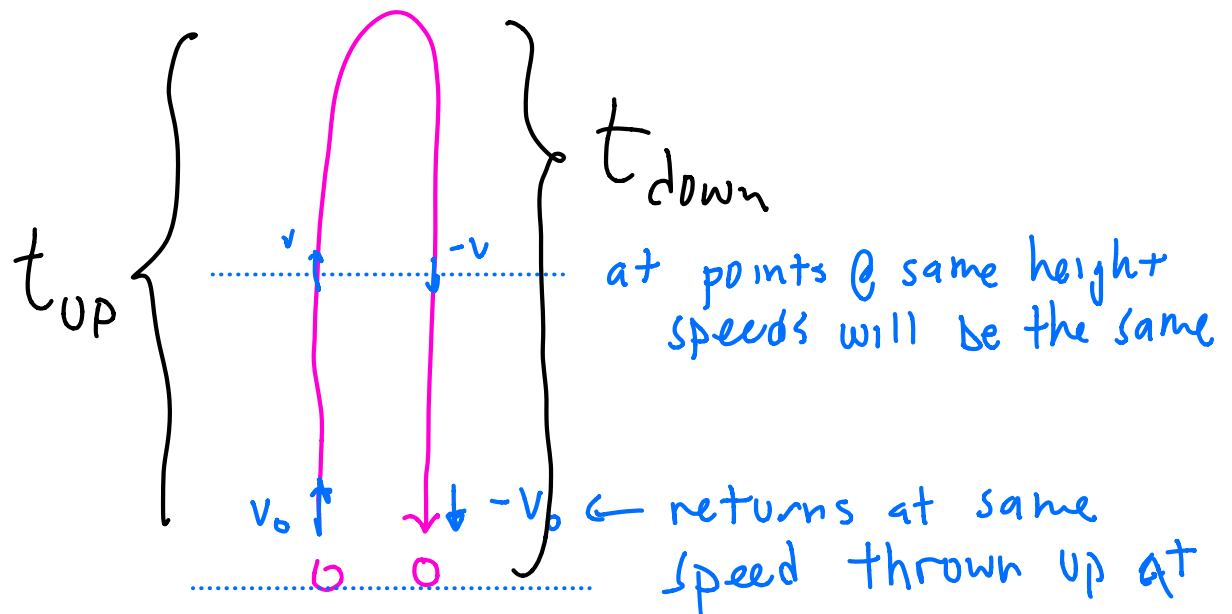
How long to reach highest point?

$$v = v_0 + a \Delta t$$

$$0 = 40 \text{ m/s} + (-10 \text{ m/s}^2) \Delta t$$

$$\Delta t = 4 \text{ s}$$

SYMMETRY in free fall

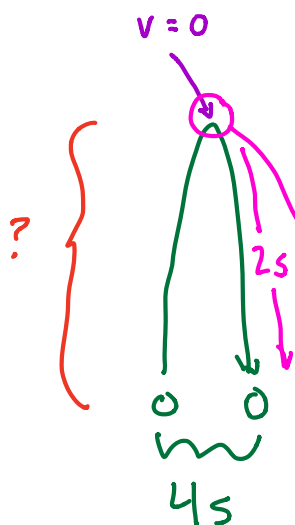


$$t_{up} = t_{down}$$

$a = g$ (downward) the ENTIRE path

at highest point : $v = 0$

$a = g$ (down)



An object thrown up returns
to its original height 4s later.

How high did it go?

$v_0 = 0 \text{ m/s}$ (looking from top to bottom)

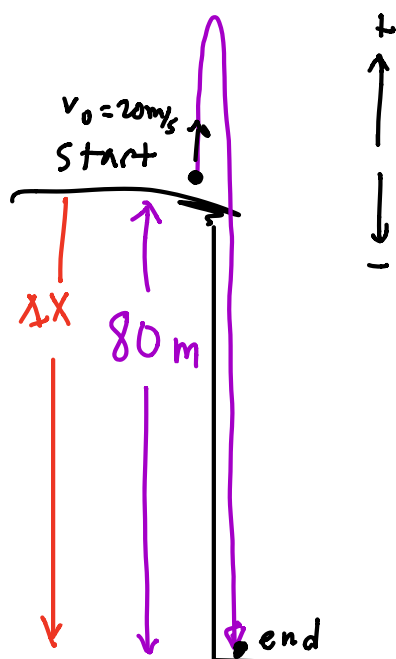
$v =$

$a = +9.8 \text{ m/s}^2$

$\Delta t = 2 \text{ s}$

$\Delta x =$

$$\begin{aligned}\Delta x &= v_0 \Delta t + \frac{1}{2} a \Delta t^2 \\ &= 0 + \frac{1}{2} (9.8 \frac{\text{m}}{\text{s}^2}) (2 \text{ s})^2 \\ &= 19.6 \text{ m}\end{aligned}$$



How long in the air?

$v_0 = +20 \text{ m/s}$

$v =$

$a = -9.8 \text{ m/s}^2$

$\Delta t =$

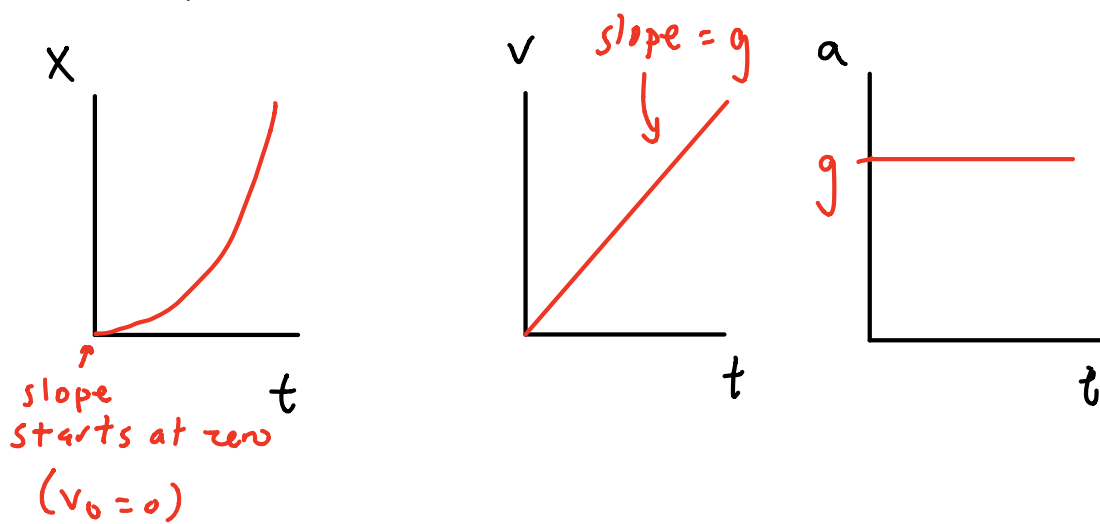
$\Delta x = -80 \text{ m}$

$$\begin{aligned}\Delta x &= v_0 \Delta t + \frac{1}{2} a \Delta t^2 \\ -80 &= 20 t - 4.9 t^2\end{aligned}$$

quadratic

Graphing Free Fall

Dropped ($v_0 = 0$ down is + direction)



Thrown up & returns to same height
(up is +)

