Assignment: Checkerboard classification problem

David Bertoldi – 735213 email: d.bertoldi@campus.unimib.it

Department of Informatics, Systems and Communication

University of Milano-Bicocca

Abstract—In this brief work we trained a FNN in order to classify points in a check pattern.

1 Inspecting the data

The data provided consists of an set of points $X \in \{(x_1, x_2) | 10 \le x_1, x_2 \le 20\}$ and a set of binary labels $y \in \{0, 1\}$. The points in X follow a uniform distribution with mean $\mu = 14.97$ and variance $\sigma = 8.3$; the 0s and 1s in y are quite uniformly distributed with a mean of $\mu = 0.498$.

If we map each point $i \in X$ with the i^{th} element of y and assign for each element of y a different color we get a *check pattern* over the points of X, partitioning the 4000 points in 6 columns and 6 rows. The result can be observed in Figure 1

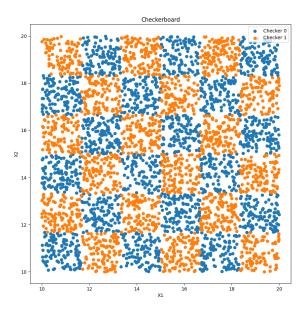


Figure 1: Visualization of the dataset

2 Preparing the data

Before using the data we want to standardize features by removing the mean and scaling to unit variance. Standardiza-

tion of a dataset is a common requirement for many machine learning estimators: they might behave badly if the individual features are not standard normally distributed. That's why we want to remove the mean μ and scale σ to unit variance.

In order to do so, we use the StandardScaler from sklearn.preprocessing package. After this operation we have $\mu=1.4\cdot 10^{-9}$ (very close to 0) and $\sigma=1$, which is exactly what we wanted.

3 Building the network and training

3.1 Data split

The dataset does not provide a set of points to be used for validation and testing. So we split the dataset into three partitions: 72% of points are used for the training, 18% for validation and 10% for testing. Having less points used for training had proved to perform worse.

3.2 Network

The network chosen is a Feed-Forward Neural Network with non-linear activation functions. We tried two approaches: tanh and LeakyReLU. The first one seemed to be right choice because it is possible to emulate the check pattern with the following formula:

$$sin(y) \leq cos(x)$$

and since the definition of tanh(x) can be derived from cos(ix) and sin(ix), there could had been some facilitation on using such activator. Unfortunately, despite the good results, LeakyReLU performed better and for this reason we used it as a definitive one.

Because we are trying to classify points between two classes, the output function is a sigmoid.

Finally, the network architecture is composed by 4 hidden dense layers of rispectively 200, 150, 100 and 50 nodes. Each node uses LeakyReLU as activator function with $\alpha=0.1$. The output node computes the sigmoid logistic function so that the output ranges between 0 and 1.

3.3 Training

The choice of the optimizer was among SGD, RMSProp and Adam. We tried all of them and chose Adam with learning

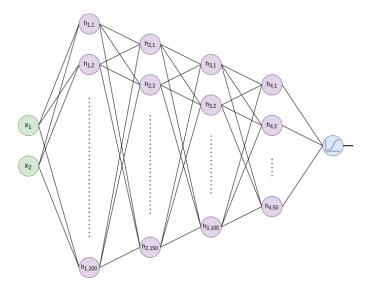


Figure 2: The neural network with 4 dense hidden layers

rate of 0.001, $\beta_1 = 0.9$ and $\beta_2 = 0.999$ because it seemed to escape better from local minima, converging faster and giving better accuracy.

Because we are treating a binary classification problem, we used the $binary\ crossentropy$ loss function. Figure 3 shows how the decision boundaries evolve over the test dataset every 10 epochs.

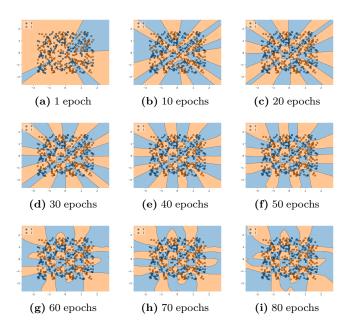


Figure 3: Evolution of decision boundaries during the training

measure Figure 4 and Figure 5 plots the trend of the loss function and its accuracy over the validation set. The first one measures the absolute difference between the model's prediction and the actual value.

The second one represents the ratio between the number of correct predictions to the total number of predictions; it is preferable over the precision because accuracy treats all classes with the same importance while precision measures the model's accuracy only in classifying a sample as positive.

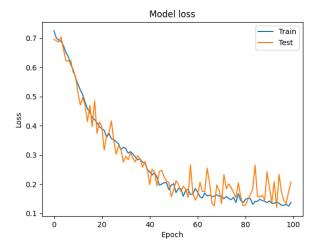


Figure 4: Loss

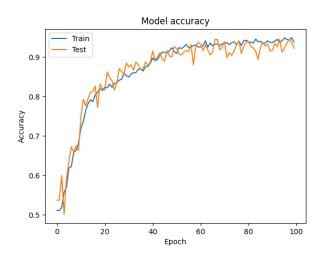


Figure 5: Accuracy

4 Analysis

As we can see from Figure 3, as the accuracy of the model increases, it is clear that the model fails to recognize the *check* pattern itself. Even if it is true that the accuracy reaches a score of 93%, the model overfits the data and could not generalize the pattern beyond the region occupied by training data. This means that a point in (9,17) is classified by the model as orange checker instead of blue. Figure 6 shows a simplified trend in model's prediction if we increase the number of epochs.

5 Alternative problem

The following problem is a variation of the previously presentend one. What is changing is the number of samples (from 4000 to 1000) and the number of checkers (from 36 to 400). This means that the frequency of samples is much more rare while leaving almost unchanged means and variation ($\mu=15.09, \sigma=8.64$).

Figure 7 shows the new problem and it is impossible for the human brain to recognize the *checker pattern*. The checkers

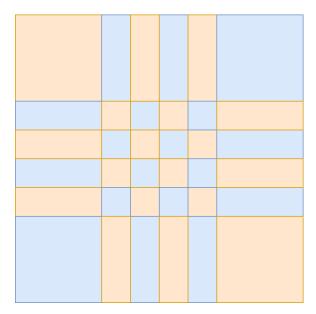


Figure 6: Trend of the decision boundaries of the model

are too thin and the data is not enough in order to recognize any pattern.

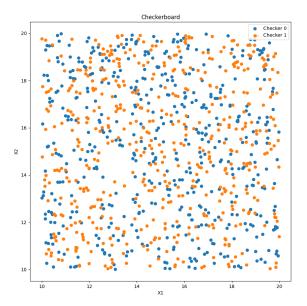


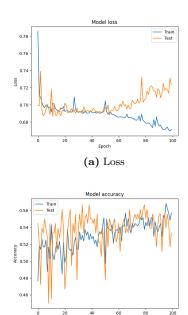
Figure 7: Visualization of the dataset of the alternative problem

The model, without any surprise, performs much worse: the maximum accuracy is $\sim 55\%$, the loss remains quite high and it never converges (Figure 8)

Figure 9 shows how the model could not find any pattern, changing quite frequently its decision boundaries

6 Other experiments

In this section we briefly documented the experiments with other optimizers: SGD and RMSprop. Even if their results where good, they converged slower than Adam.



(b) AccuracyFigure 8: Loss and accuracy plots of the alternative problem

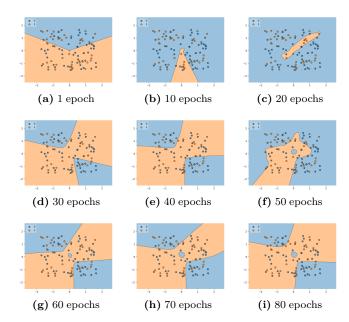


Figure 9: Evolution of decision boundaries during the training of the alternative problem

RMSprop converges better than SGD but it has difficulties on escaping local minima, having the loss function over test data to be more swinging (Figure 10).

SGD converges slower than RMSprop but seems to be slighty better in escaping local minima (Figure 12).

References

- 1] NVIDIA Developer: Turing tuning guide,
- https://docs.nvidia.com/cuda/turing-tuning-guide/index.html
- Fletcher, J. G. (January 1982). An Arithmetic Checksum for Serial Transmissions. IEEE Transactions on Communications. COM-30 (1): 247–252. doi:10.1109/tcom.1982.1095369

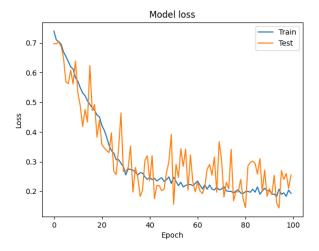


Figure 10: Loss of RMSprop

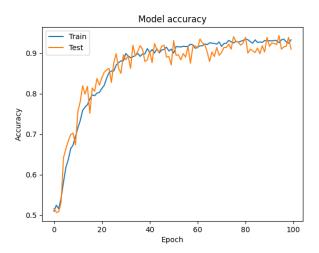


Figure 11: Accuracy of RMSprop

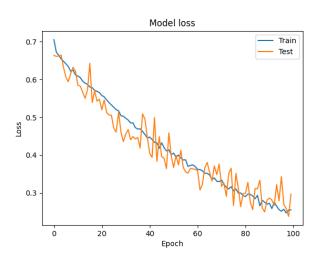


Figure 12: Loss of SGD

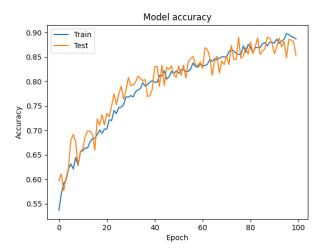


Figure 13: Accuracy of SGD