

(1 point) Evaluate the integrals that converge, enter 'DNC' if integral Does Not Converge.

$$\int_0^{+\infty} \frac{1}{(x+2)\sqrt{x}} dx = \text{DNC}$$

(1 point) Determine whether each of the following integrals is proper, improper and convergent, or improper and divergent.

? 1. $\int_0^{19} \frac{1}{\sqrt[3]{x-9}} dx$

? 2. $\int_{-\infty}^{\infty} \sin(5z) dz$

? 3. $\int_{-\infty}^{\infty} \frac{t}{t^2+6} dt$

? 4. $\int_{-6\pi}^{33\pi} \sin(\theta) \arctan(\theta) d\theta$

? 5. $\int_9^{19} \ln(x-9) dx$

? 6. $\int_{-\pi/9}^{19\pi/2} \tan^2(5x) dx$

? 7. $\int_5^{\infty} \frac{1}{\sqrt{t^2-25}} dt$

? 8. $\int_1^{\infty} se^{5s^2} ds$

(1 point) The improper integral $\int_{-\infty}^{\infty} x dx$ is

- ☐ A. divergent by comparison to $\int_{-\infty}^{\infty} xe^{-x} dx$.
- ☐ B. convergent since it equals $\lim_{t \rightarrow \infty} \int_{-t}^t x dx = \lim_{t \rightarrow \infty} \left(\frac{t^2}{2} - \frac{(-t)^2}{2} \right) = 0$.
- ☐ C. divergent since $\int_{-\infty}^0 x dx$ is convergent and $\int_0^{\infty} x dx$ is divergent.
- ☐ D. divergent since both integrals $\int_{-\infty}^0 x dx = -\infty$ and $\int_0^{\infty} x dx = +\infty$ are divergent.
- ☐ E. divergent by comparison to $\int_{-\infty}^{\infty} \sqrt{x} dx$.
- ☐ F. convergent since it equals $\lim_{a \rightarrow -\infty} \int_a^0 x dx + \lim_{b \rightarrow \infty} \int_0^b x dx = -\infty + \infty = 0$.
- ☐ G. convergent since the area to the left of $x = 0$ cancels with the area to the right of $x = 0$.

(1 point) Evaluate the integrals that converge, enter 'DNC' if integral Does Not Converge.

$$\int_8^{+\infty} \frac{3}{x^2-1} dx = 3\ln(63)/16$$