MA1300 Self Practice # 12

1. (P402, #49, 50; P418, #3, 12; P419, #49, 52; P460, #25, 26, 29; P468, #33, 35) Find the derivative of the function.

(a).
$$y = \cos\left(\frac{1 - e^{2x}}{1 + e^{2x}}\right)$$
,
(b). $f(t) = \sin^2\left(e^{\sin^2t}\right)$,
(c). $f(x) = \sin(\ln x)$,
(d). $h(x) = \ln\left(x + \sqrt{x^2 - 1}\right)$,
(e). $y = x^{\sin x}$,
(f). $y = (\sin x)^{\ln x}$,
(g). $y = \sin^{-1}(2x + 1)$,
(h). $g(x) = \sqrt{x^2 - 1}\sec^{-1}x$,
(i). $y = \cos^{-1}(e^{2x})$,
(j). $h(x) = \ln(\cosh x)$,
(k). $y = e^{\cosh(3x)}$.

2. (P477, #25, 32; P478, #38, 57) Find the limit. Use l'Hospital's Rule where appropriate. If there is a more elementary method, consider using it. If l'Hospital's Rule doesn't apply, explain why.

(a).
$$\lim_{x \to 0} \frac{e^x - 1 - x}{x^2},$$
(b).
$$\lim_{x \to 0} \frac{\cos mx - \cos nx}{x^2},$$
(c).
$$\lim_{x \to 0} \frac{e^x - e^{-x} - 2x}{x - \sin x},$$
(d).
$$\lim_{x \to 0} (1 - 2x)^{1/x}.$$