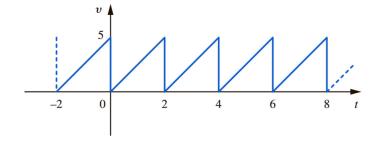
EE1002 Principles of Electrical Engineering Assignment 1

- If $z = \frac{a+3j}{1-2j}$, where $a \in R$ (" \in " means "belong to", and " $a \in R$ " means that a belongs to a real number.)
- If z is a real number, find a. a)
- If z is a purely imaginary number, find a.

2.

- If $\frac{\bar{z}}{1+j} = 2+j$ where \bar{z} is the complex conjugate of z. Find the complex number z.
- b) If $z_1 = \frac{y+3j}{1+xj}$ $(x, y \in R)$ is a real number and $z_2 = (xy+j)^2$. Find the complex conjugate of z_2 .
- c) If $z = \frac{1+7j}{2-i} = a + jb$, find a, b, and |z| (modulus of z).
- Use Table 1 to find y', given 3.
- $v = t^2$
- $y = t^{-3}$
- $y = \ln t$ $y = t^{1/2}$ d)
- e)
- $y = e^{3t}$ f)
- g)
- $y = \frac{1}{e^{5t}}$ $y = \sin(2t + 3)$ h)
- $y = \tan(\frac{t}{2} + 1)$ i)
- $y = \arcsin(t + \pi)$ i)
- Find the derivatives of the following functions:
- $y = 4x^3 5x^2$ a)
- $y = 3\sin(5x) + 2e^{4x}$
- $y = 3\sin(3x) + 2c$ $y = 2e^{3x} + 17 4\sin(2x)$ $y = \frac{1}{x^3} + \frac{\cos 5x}{2}$ $y = \frac{2x^3}{3} + \frac{e^{4x}}{2}$
- e)
- $y = \sqrt{x} + \ln(\sqrt{x})$ [Hint: $\sqrt{x} = x^{1/2}$, and use the formula $\ln a^b = b \ln a$]
- 5. Consider the saw-tooth waveform shown in the following figure. Calculate the average value of this waveform over a complete period.



- Calculate the r.m.s. value of $f(t) = A\sin(\omega t + \varphi)$. (Hint: The period is given by $T = 2\pi/\omega$.) 6.
- Evaluate the following integrals.

a)
$$\int_0^a x^2 \sqrt{a^2 - x^2} \, dx$$

b)
$$\int_{-1}^{1} \frac{x dx}{\sqrt{5-4x}}$$

a)
$$\int_{0}^{a} x^{2} \sqrt{a^{2} - x^{2}} dx$$
b)
$$\int_{-1}^{1} \frac{x dx}{\sqrt{5 - 4x}}$$
c)
$$\int_{-\pi}^{4} \frac{dx}{\sqrt{x + 1}}$$
 (Hint: You may let $t = \sqrt{x}$)
d)
$$\int_{-\pi}^{\pi} x^{4} \sin x dx$$

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$$\int_{-\pi}^{\pi} x^4 \sin x dx$$

Find the general solution of

(a)
$$\frac{dx}{dt} = 2x$$

(a)
$$\frac{dx}{dt} = 2x$$
(b)
$$(1+t)\frac{dx}{dt} = 3$$
(c)
$$\frac{dy}{dx} = y^2 \cos x$$

(c)
$$\frac{dy}{dx} = y^2 \cos x$$

Find the general solution of

(a)
$$\frac{d^2y}{dx^2} + 3\frac{dy}{dx} - 10y = 0$$

(b)
$$\frac{d^2y}{dx^2} + 4y = 0$$

(c)
$$y'' + 8y' + 16y = 0$$

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Find the general solution of the following differential equation by using the integrating factor technique:

$$x\frac{dy}{dx} - y = x^2 \cos^3 x$$

11. Show that the following expression is equal to a constant. What is the value of this constant?

$$\frac{2\cos^2 a - 1}{2\tan\left(\frac{\pi}{4} - a\right)\sin^2\left(\frac{\pi}{4} + a\right)}$$

- A signal is given by $y(x) = A \sin(x + \phi)$ $(A > 0; 0 < \phi < \pi), x \in R$. It passes through the point $M(\frac{\pi}{3}, \frac{1}{2})$. The maximum value of y(x) is equal to 1.
- (1) Find A and ϕ .

(2) If
$$y(\alpha) = \frac{3}{5}$$
, $y(\beta) = \frac{12}{13}$, $\alpha, \beta \in \left(0, \frac{\pi}{2}\right)$, find $y(\alpha - \beta)$.