

(1 point) In general, what can be said about the vector product  $x \times (x \times y)$ ?

- ☒ A. the result is orthogonal to  $x$   
☐ B. the result is orthogonal to  $y$   
☐ C. the result is orthogonal to  $x$  and  $y$   
☐ D. the result is parallel to  $x$   
☐ E. the result is parallel to  $y$   
☐ F. the result is not parallel to  $x$  or to  $y$

(1 point) Find the vector in  $\mathbb{R}^3$  from point  $A = (x, y, z)$  to  $B = (6, -4, 3)$ .

$\vec{AB} =$   [help \(vectors\)](#)

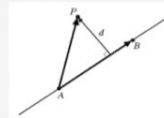
(1 point) From the list below, select the vector that is NOT orthogonal (perpendicular) to:

$$\begin{bmatrix} \cos \theta \\ \sin \theta \\ 1 \end{bmatrix}$$

- ☒ A.  $\begin{bmatrix} -\sin \theta \\ \cos \theta \\ 0 \end{bmatrix}$   
☐ B.  $\begin{bmatrix} -\cos \theta \\ -\sin \theta \\ 1 \end{bmatrix}$   
☐ C.  $\begin{bmatrix} \sin \theta \\ -\cos \theta \\ 0 \end{bmatrix}$   
☐ D.  $\begin{bmatrix} 0 \\ -1 \\ \sin \theta \end{bmatrix}$   
☐ E.  $\begin{bmatrix} \sin \theta \\ \cos \theta \\ 0 \end{bmatrix}$

(1 point)

The distance  $d$  of a point  $P$  to the line through points  $A$  and  $B$  is the length of the component of  $\overline{AP}$  that is orthogonal to  $\overline{AB}$ , as indicated in the diagram.



So the distance from  $P = (4, -3)$  to the line through the points  $A = (-4, 1)$  and  $B = (0, 4)$  is

.

(1 point) If  $\vec{v} \times \vec{w} = 2\vec{i} + 2\vec{j} + \vec{k}$ , and  $\vec{v} \cdot \vec{w} = 3$ , and  $\theta$  is the angle between  $\vec{v}$  and  $\vec{w}$ , then

(a)  $\tan \theta =$

(b)  $\theta =$

(1 point) Let  $\mathbf{a} = (6, -7, -3)$  and  $\mathbf{b} = (-2, -9, 4)$  be vectors.

(A) Find the scalar projection of  $\mathbf{b}$  onto  $\mathbf{a}$ .

Scalar Projection:

(B) Decompose the vector  $\mathbf{b}$  into a component parallel to  $\mathbf{a}$  and a component orthogonal to  $\mathbf{a}$ .

Parallel component: (  ,  ,  )

Orthogonal Component: (  ,  ,  )

(1 point) Find two vectors  $\vec{v}_1$  and  $\vec{v}_2$  whose sum is  $\langle -3, 2, -5 \rangle$ , where  $\vec{v}_1$  is parallel to  $\langle 4, 4, -2 \rangle$  while  $\vec{v}_2$  is perpendicular to  $\langle 4, 4, -2 \rangle$ .

$\vec{v}_1 =$   and

$\vec{v}_2 =$   .

(1 point) Are the following statements true or false?

1. If  $\vec{v}$  and  $\vec{w}$  are any two vectors, then  $||\vec{v} + \vec{w}|| = ||\vec{v}|| + ||\vec{w}||$ .

2.  $(\vec{i} \times \vec{j}) \cdot \vec{k} = \vec{i} \cdot (\vec{j} \times \vec{k})$ .

3. For any scalar  $c$  and any vector  $\vec{v}$ , we have  $||c\vec{v}|| = c||\vec{v}||$ .

4. The value of  $\vec{v} \cdot (\vec{v} \times \vec{w})$  is always zero.