

哈希表，恰k个在第一个槽的概率

$$\begin{aligned}Q_k &= \binom{n}{k} \left(\frac{1}{n}\right)^k \left(1 - \frac{1}{n}\right)^{n-k} \\&\leq \binom{n}{k} \frac{1}{n^k} \\&= \frac{n!}{(n-k)!n^k} \frac{1}{k!} \\&= \frac{n(n-1)\cdots(n-k+1)}{n^k} \frac{1}{k!} \\&\leq \frac{1}{k!} \\&\leq \frac{e^k}{k^k} \quad \left(\text{Stirling's approximation: } k! \geq \left(\frac{k}{e}\right)^k\right)\end{aligned}$$

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