

AG Tema 2

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1 Introduction

This report takes a closer look at what are the particularities of the genetic algorithms. We will firstly discuss general aspects, and then compare results of a genetic algorithm with our previously analyzed heuristic algorithms: Hill-climber and Simulated Annealing. The three algorithms will try to solve the Minimization Problem on four functions (Rastrigin, Schwefel, Rosenbrock and Sphere). These results will be represented by a number of comparative tables and graphs that will then allow us to obtain a conclusion about genetic algorithms.

1.1 Problem

If we look at some of the heuristic algorithms (HillClimbing, for instance) we will notice that while their approach is indeed one that is randomized, the way they tackle finding the optimum is rather by trying out systematic changes to our current solution. This is a great improvement from the deterministic way of doing things, of course, because now we don't have to consume a large amount of resources to compute the output to our problem. But if these algorithms have a small part that resemble deterministic methods, could we go even further and randomize the process more? The answer is yes, by using genetic algorithms. By having a fully-heuristic way to search for a solution we now start to analyze its different parameters and particularities, and how each influences the final solution.

2 Method

2.1 Pseudocode

The pseudocode for GA is shown below:

```
begin  
t := 0  
generate P(t)
```

```

evaluate P(t)
while (not STOP_CONDITION()) do begin:
  mutate P(t)
  crossover P(t)
  select P(t + 1) from P(t)
  t := t + 1
end

```

2.2 Description

Genetic algorithms resemble the HC and SA algorithms, and that is obvious when we look at their structure. We have the initialization and a loop in which we modify the candidates slightly and compare them.

The representation for the solution to this problem is a bitstring that represents a real number in the interval of the chosen function.

In the initialization part we have to choose a random solution, and for that we give each gene a probability of 50% of choosing each of the two possible values. We choose this probability as an assurance that whatever problem we have, we can start closer to it by initializing values that are (virtually) in the middle area.

2.3 The particularities of the GA algorithm

The algorithm consists in three major procedures: mutation, crossover and selection.

2.4 Mutation

The mutation procedure allows every gene in a chromosome to change, though this chance is small (1%). The mutation gene comes first in this algorithm because it is the only procedure that actually changes the information that the population carries. We can see that in a test with no mutation the variation from one population to another is slower than that in a normal run, and that could be explained like this: if we imagine the “optimal” genes that the chromosomes are carrying as units on a distribution graph, the overall “optimality” of the population does not actually change, as the number of good genes do not change in the crossover or selection procedure. Only by mutation it is that we can gain optimal genes and thus changing the distribution. To offer an example in which we can identify these optimal genes we can look at the minimization problem of the Rastrigin function: in this case the global minimum is 0.0, thus the optimal genes we are looking for are the ones that have a numeric value of 0.

While it is true that we can talk about optimal genes only when they are in

combination with the other genes, it is also a fact that the “winning” chromosome has a range of neighbors that resemble its particular “distribution” that we have talked earlier. So we can approach the optimal solution by matching its number of favorable genes.

2.5 Crossover

The crossover procedure is also an important part of the algorithm. We have already talked about tweaking our solution chromosome to obtain a certain number of “optimal” genes. But it is more often that we will find solutions in which the genes would be more fitting in other places: for a chromosome with $n * l$ genes, the total number of genes can vary by only this amount, $n * l$, while if we would like to compute all possible permutations of the genes in the chromosome we would reach a number of $2^{n * l}$, which is exponentially higher. We understand now why running the algorithm without this functionality would take ages to reach the solution, and the reason is this rearrangement of information in the population.

Now it is true that crossing-over is done between the chromosomes, that means that the crossover procedure also changes the number of good genes in chromosomes and it would appear to have less to do with the rearrangement of information, but it is essentially what it is used for in this algorithm, and we have two arguments for that. Firstly, at the start, the distribution of optimal genes is virtually the same for each chromosome, when we are switching parts between two of them, we are essentially changing the arrangement of those genes. It is true though, that in the late part of the algorithm, when we switch large parts of the chromosomes, we are changing the distribution considerably, though the actions that happen at this stage are considered less impactful than those in the beginning. Secondly, the switching between chromosomes, because it is done randomly and often between chromosomes (one chromosome is more often to be crossed-over with another than mutated, because of the probabilities of the two procedures) in most cases leads to a chromosome switching small chunks of genes in itself.

2.6 Selection

The selection procedure is the part of the algorithm that actually dictates the course of the algorithm. We say this because, while the mutation and crossover power the solving mechanism for genetic algorithms, this procedure is the part that particularizes and adapts this mechanism to the given problem. This is not only because the selection procedure offers a semi-evaluation of the current population, but also because it is the place where the programmer can use his insight to mold the finding of particular solutions.

In a general sense in a selection we keep the best chromosomes and filter out the candidates that are under-performing, only keeping some that might lead to

an optimum. There should be a certain balance between the best-chosen candidates and the potential candidates, for if we choose only optimal candidates, we might reach a narrow number of attraction basins that would not contain the global minima. On the other hand, if we choose a large number of possible yet not optimal candidates we hinder our process of finding the solution in a short amount of time. The selection procedure is composed mainly of a fitness function (or pressure function), which represents the particularities of the solution to the given problem. By evaluating each candidate we can reach the exact pool of chromosomes we consider suitable to find the optimum. The other element that is introduced in the selection process is the current state of the population – by knowing the values that our current candidates hold we can favor those that are either common or rare, based on what we want to achieve.

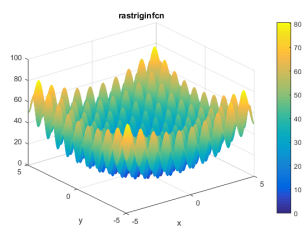
2.7 Implementation of selection

In the implementation of this paper we have used such a selection, in which we favored the best values and overlooked the worst, and also keeping a steady value for those in the middle. Our goal is to select a chromosome with the value randomly chosen based on a distribution of values to become a member of a new population. Besides implementing a standard approach to selecting values with a Wheel of Fortune procedure, we strived to select a value that was not necessarily as much-met as it was good. This proved to be rather good choice, because it broke one of the disadvantages of the canonical method: in the normal selection there was the possibility that similar candidates would have a combined percentage greater than those of better solutions and therefore be chosen more often. This is often happening either because of duplicates or close values. With this method the optimal values have a greater chance to be selected and the under-performing ones are rather ignored.

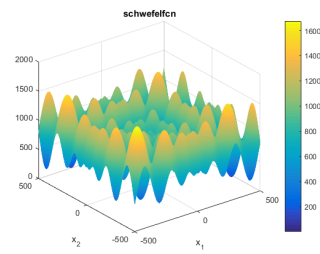
3 Experiment

All of the three algorithms: Genetic Algorithm, Hill climbing and Simulated Annealing are anytime algorithms: they can return a valid solution even if they are interrupted at any time before it ends. For each function, the 3 algorithms ran 30 times (without the inner loops) on 5,10 and 30 dimensions each. For a function an analysis took about 5 minutes.

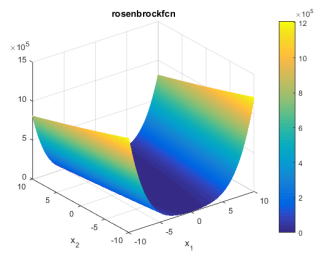
MRT = MeanRunTime in seconds RT = RunTime in minutes



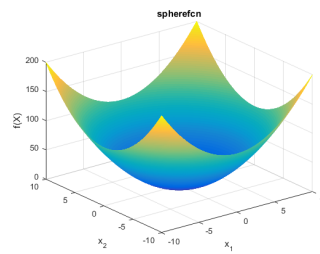
(a) Rastrigin Function



(b) Schwefel Function



(c) Rosenbrock Function



(d) Sphere Function

Figure 1: The 4 functions

3.1 Rastrigin

Genetic Algorithm on Rastrigin has produced the following results:

Dim.	Mean	Max	Min	Median	MRT(sec.)	RT(min.)	StdDev
5	0.08239	1.23582	0.00000	0.00000	4.88224	2.44112	0.30827
10	1.19463	2.47165	0.00000	1.23582	9.55004	4.77502	0.81248
30	17.01436	22.38879	9.01019	17.94064	29.04039	14.52020	3.10018

Hillclimbing-best on Rastrigin has produced the following results:

Dim.	Mean	Max	Min	Median	MRT(sec.)	RT(min.)	StdDev
5	6.59833	7.54576	6.30998	6.30998	0.02402	0.01201	0.52267
10	19.58638	23.98059	12.84137	20.84383	0.19925	0.09962	4.23800
30	49.00509	61.54694	35.68955	49.51379	5.24325	2.62163	6.46535

Simulated Annealing on Rastrigin has produced the following results:

Dim.	Mean	Max	Min	Median	MRT(sec.)	RT(sec.)	StdDev
5	3.67282	6.94417	1.14883	3.74431	3.00664	1.50332	1.28280
10	10.27761	16.72864	7.56243	10.02213	3.00603	1.50301	2.27522
30	48.10074	58.08957	35.60556	48.89670	3.00605	1.50302	6.38749

3.2 Schwefel

Genetic Algorithm on Schwefel has produced the following results:

Dim.	Mean	Max	Min	Median	MRT(sec.)	RT(sec.)	StdDev
5	0.06637	0.20776	0.00000	0.10352	6.97189	3.48595	0.05644
10	0.21616	0.31348	0.10547	0.20923	17.37879	8.68939	0.07493
30	297.19870	506.46094	62.54395	310.91553	41.29582	20.64791	114.51190

Hillclimbing-best on Schwefel has produced the following results:

Dim.	Mean	Max	Min	Median	MRT(sec.)	RT(sec.)	StdDev
5	292.29132	387.63892	237.09009	237.09009	0.03423	0.01711	72.54864
10	634.09524	981.04395	306.35840	627.99341	0.29534	0.14767	199.48108
30	1973.12520	2515.98828	1482.08496	2016.91064	7.11674	3.55837	260.33367

Simulated Annealing on Schwefel has produced the following results: //aici

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Dim.	Mean	Max	Min	Median	MRT(sec.)	RT(sec.)	StdDev
5	264.56776	475.01636	27.87842	260.91876	3.00609	1.50304	104.52989
10	707.11108	1101.05273	333.41235	696.53076	3.00621	1.50310	197.38461
30	2773.79717	3372.21582	2042.97070	2846.76074	3.00604	1.50302	293.09082

3.3 Sphere

Genetic Algorithm on Sphere has produced the following results:

Dim.	Mean	Max	Min	Median	MRT(sec.)	RT(sec.)	StdDev
0.00000	0.00000	0.00000	0.00000	5.06041	2.53020	0.00000	
10	0.00000	0.00000	0.00000	0.00000	11.37833	5.68916	0.00000
30	0.00006	0.00012	0.00004	0.00006	31.03870	15.51935	0.00002

Hillclimbing-best on Sphere has produced the following results:

Dim.	Mean	Max	Min	Median	MRT(sec.)	RT(sec.)	StdDev
5	0.00120	0.00120	0.00120	0.00120	0.00657	0.00329	0.00000
10	0.01244	0.02840	0.00320	0.00320	0.03107	0.01554	0.01214
30	0.10668	0.44200	0.01440	0.06220	0.95315	0.47657	0.10734

Simulated Annealing on Sphere has produced the following results:

Dim.	Mean	Max	Min	Median	MRT(sec.)	RT(sec.)	StdDev
5	0.41735	1.16289	0.04203	0.34125	3.00601	1.50301	0.25495
10	1.33097	2.40128	0.59801	1.28658	3.00602	1.50301	0.50278
30	5.24496	7.87754	2.37124	5.32371	3.00604	1.50302	1.19954

3.4 Rosenbrock

Genetic algorithm on Rosenbrock has produced the following results:

Dim.	Mean	Max	Min	Median	MRT(sec.)	RT(sec.)	StdDev
5	2.28845	3.75156	0.22253	2.28204	5.34209	2.67105	1.04807
10	7.51159	8.33795	4.35584	7.93529	12.23295	6.11648	0.88948
30	28.24058	29.71366	25.24927	28.29572	31.88165	15.94082	0.79304
128.69940							

Hillclimbing-best on Rosenbrock has produced the following results:

Dim.	Mean	Max	Min	Median	MRT(sec.)	RT(sec.)	StdDev
5	134.72946	134.72946	134.72946	134.72946	0.00561	0.00281	0.00000
10	94.63492	137.28891	20.58109	137.28891	0.04732	0.02366	56.06301
30	172.91218	517.54858	30.81817	137.38277	1.22030	0.61015	128.69940

Simulated Annealing on Rosenbrock has produced the following results:

Dim.	Mean	Max	Min	Median	MRT(sec.)	RT(sec.)	StdDev
5	58.39948	362.91174	3.50077	6.40541	3.00601	1.50301	90.77307
10	257.32415	1946.52673	11.80267	130.76601	3.00602	1.50301	374.07534
30	3671.87897	8397.09570	162.17835	3656.89038	3.00619	1.50309	2447.80553

From these results we can observe that in most cases, a larger number of dimensions leads to a more erroneous solution, and a larger number of iterations (and the observation before about time) leads to a better solution. For more dimensions we might need to do more iterations to get an equally better result.

4 Conclusions

We can see that using a Genetic Algorithm is a far better solution than HillClimbing and Simulated Annealing, though they produce close results. Out of the three GA is though the slowest, but it provides good results.

References

BenchMarking Functions
<http://benchmarkfcns.xyz>

Wikipedia
 Global optimization
https://en.wikipedia.org/wiki/Global_optimization#Deterministic_methods

Mating pool
https://en.wikipedia.org/wiki/Mating_pool

For contributing with the idea for the selection process to prioritise better solutions.