

$$V(k_0) = \sum_{t=0}^{\infty} [\beta^t \ln(1 - \alpha\beta) + \beta^t \alpha \ln k_t]$$

$$= \ln(1 - \alpha\beta) \sum_{t=0}^{\infty} \beta^t + \alpha \sum_{t=0}^{\infty} \beta^t \ln k_t$$

$$= \frac{\alpha}{1 - \alpha\beta} \ln k_0 + \frac{\ln(1 - \alpha\beta)}{1 - \beta} + \frac{\alpha\beta}{(1 - \beta)(1 - \alpha\beta)} \ln(\alpha\beta)$$

$$\begin{aligned} \text{左边} = V(k) &= \frac{\alpha}{1 - \alpha\beta} \ln k + \frac{\ln(1 - \alpha\beta)}{1 - \beta} + \frac{\alpha\beta}{(1 - \beta)(1 - \alpha\beta)} \ln(\alpha\beta) \\ &\triangleq \frac{\alpha}{1 - \beta} \ln k + A \end{aligned}$$

$$\text{右边} = \max_y \{u(f(k) - y) + \beta V(y)\}$$

利用 FOC 和包络条件求解得到 $y = \alpha\beta k^\alpha$ ，代入，求右边。

ElegantLaTeX

$$\text{右边} = \max \{u(f(k) - y) + \beta V(y)\}$$

$$= u(f(k) - g(k)) + \beta \left[\frac{\alpha}{1 - \alpha\beta} \ln g(k) + A \right]$$

FACTORY WON'T COME TO US UNLESS WE GO TO IT.

$$= \ln(1 - \alpha\beta) + \alpha \ln k + \beta \left[\frac{\alpha}{1 - \alpha\beta} [\ln \alpha\beta + \alpha \ln k] + A \right]$$

$$= \alpha \ln k + \frac{\alpha\beta}{1 - \alpha\beta} \alpha \ln k + \ln(1 - \alpha\beta) + \frac{\alpha\beta}{1 - \alpha\beta} \ln \alpha\beta + \beta A$$

$$= \frac{\alpha}{1 - \alpha\beta} \ln k + \ln(1 - \alpha\beta) + \frac{\alpha\beta}{1 - \alpha\beta} \ln \alpha\beta + \beta A$$

$$= \frac{\alpha}{1 - \alpha\beta} \ln k + (1 - \beta)A + \beta A$$

$$= \frac{\alpha}{1 - \alpha\beta} \ln k + A$$

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所以，左边 = 右边，证毕。

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