📮 ongardie / raft.tla

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Branch: master ▼ raft.tla / raft.tla
                                                                                                                    Find file Copy path
🌃 ongardie Fix AppendEntries to only send one entry at a time
                                                                                                                   8098acb on 3 Dec 2014
1 contributor
485 lines (433 sloc) 20.1 KB
       ----- MODULE raft -----
      \ This is the formal specification for the Raft consensus algorithm.
      \*
      \* Copyright 2014 Diego Ongaro.
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      \ International License https://creativecommons.org/licenses/by/4.0/
  8
      EXTENDS Naturals, FiniteSets, Sequences, TLC
      10
      CONSTANTS Server 实际上多个servr,但不用自己指定几个,叫什么名字等
      \ The set of requests that can go into the log
      CONSTANTS Value
 14
      \* Server states.
      CONSTANTS Follower, Candidate, Leader
      \* A reserved value.
      CONSTANTS Nil
      \* Message types:
      CONSTANTS RequestVoteRequest, RequestVoteResponse,
 24
               AppendEntriesRequest, AppendEntriesResponse
      \* Global variables
 28
      \* A bag of records representing requests and responses sent from one server
 30
      \ to another. TLAPS doesn't support the Bags module, so this is a function
      \* mapping Message to Nat.
      VARIABLE messages TLAPS是啥? TLA+ book里面提到了Bags模块,是个multi set 这个变量实际上应该是二维map
      \ A history variable used in the proof. This would not be present in an
      \* implementation.
      \ Keeps track of successful elections, including the initial logs of the
      \ leader and voters' logs. Set of functions containing various things about
      \* successful elections (see BecomeLeader).
      VARIABLE elections
      \ A history variable used in the proof. This would not be present in an
 41
 42
 43
       \ Keeps track of every log ever in the system (set of logs).
 44
      VARIABLE allLogs
 45
 46
                                       下面是每个server一份的变量。用下标方式使用
 47
       \ The following variables are all per server (functions with domain Server).
      \* The server's term number. 这些实际上只有currentTerm, votedFor持久化。其他的在restart后丢失了。参见restart()
 49
 50
      VARIABLE currentTerm
      \* The server's state (Follower, Candidate, or Leader).
      \* The candidate the server voted for in its current term, or
  54
      \* Nil if it hasn't voted for any.
      VARIABLE votedFor
```

```
serverVars == <<currentTerm, state, votedFor>>
 58 \* A Sequence of log entries. The index into this sequence is the index of the
     \* log entry. Unfortunately, the Sequence module defines Head(s) as the entry
 60 \* with index 1, so be careful not to use that!
 61 VARIABLE log
 ^{62} \* The index of the latest entry in the log the state machine may apply.
 63 VARIABLE commitIndex 为什么这个可以不持久化?
 64 logVars == <<log, commitIndex>>
 66 \* The following variables are used only on candidates: 实际上在推选自己当leader期间用
 ^{87} \* The set of servers from which the candidate has received a RequestVote
 68 \* response in its currentTerm.
 69 VARIABLE votesResponded
 70 \* The set of servers from which the candidate has received a vote in its
 71 \* currentTerm.
 72 VARIABLE votesGranted
 73 \* A history variable used in the proof. This would not be present in an
 74 \* implementation.
 75 \* Function from each server that voted for this candidate in its currentTerm
 76 \* to that voter's log.
 77 VARIABLE voterLog
 78 candidateVars == <<votesResponded, votesGranted, voterLog>>
 80 \* The following variables are used only on leaders: 仅仅leader维护的内存变量
 \$1 \* The next entry to send to each follower.
 82 VARIABLE nextIndex
 83 \* The latest entry that each follower has acknowledged is the same as the
 84 \* leader's. This is used to calculate commitIndex on the leader.
 85 VARIABLE matchIndex
 86 leaderVars == <<nextIndex, matchIndex, elections>>
 87
 88 \* End of per server variables.
 89 ----
                                                                         这个是为了表示方便,比如vars'
那些不变的,必须明确说unchanged
 90
 91 \* All variables; used for stuttering (asserting state hasn't changed).
     vars == <<messages, allLogs, serverVars, candidateVars, leaderVars, logVars>>
 92
 94
 95 \* Helpers
 96
    \* The set of all quorums. This just calculates simple majorities, but the only
 97
     Quorum == {i \in SUBSET(Server) : Cardinality(i) * 2 > Cardinality(Server)} 这个定义,只要server个数>=0,还是你能表达原意的
 98
     \ important property is that every quorum overlaps with every other.
 99
100
101 \ The term of the last entry in a log, or 0 if the log is empty.
102 LastTerm(xlog) == IF Len(xlog) = 0 THEN 0 ELSE xlog[Len(xlog)].term
104 \* Helper for Send and Reply. Given a message m and bag of messages, return a
105 \* new bag of messages with one more m in it.
                                    这个\in DOMAIN,与\in不是一码事,啥含义呢? A function f has a domain, written domain f , and it
     WithMessage(m, msgs) ==
                                    assigns to each element x of its domain the value f [x]也就是说,msgs是个函数,m属于这个函数的domain.实际上,就是m可以作为下标使用,或者映射的key使用
       IF m \in DOMAIN msgs THEN
108
            [msgs EXCEPT ![m] = msgs[m] + 1]
       ELSE
110
           msgs @@ (m :> 1)
112 \* Helper for Discard and Reply. Given a message m and bag of messages, return
113 \* a new bag of messages with one less m in it.
114 WithoutMessage(m, msgs) ==
       IF m \in DOMAIN msgs THEN
            [msgs EXCEPT ![m] = msgs[m] - 1] 这样不会减为0么?却没有删除掉!
       ELSE
118
           msgs
120 \* Add a message to the bag of messages.
    Send(m) == messages' = WithMessage(m, messages)
     \* Remove a message from the bag of messages. Used when a server is done
```

```
124 \* processing a message.
125 Discard(m) == messages' = WithoutMessage(m, messages)
     \* Combination of Send and Discard
128 Reply(response, request) ==
        messages' = WithoutMessage(request, WithMessage(response, messages))
130
131 \* Return the minimum value from a set, or undefined if the set is empty.
132 Min(s) == CHOOSE x \setminus in s : \setminus A y \setminus in s : x <= y
133 \* Return the maximum value from a set, or undefined if the set is empty.
134 Max(s) == CHOOSE x \setminus in s : \setminus A y \setminus in s : x >= y
136 ----
137 \* Define initial values for all variables
138
139 InitHistoryVars == /\ elections = {}
                       /\ allLogs = {}
                       /\ voterLog = [i \in Server |-> [j \in {} |-> <<>>]]
141
142 InitServerVars == /\ currentTerm = [i \in Server |-> 1]
                     // state = [i \in Server | -> Follower]
                     /\ votedFor = [i \in Server |-> Nil]
144
145    InitCandidateVars == /\ votesResponded = [i \in Server |-> {}]
                       /\ votesGranted = [i \in Server |-> {}]
147 \* The values nextIndex[i][i] and matchIndex[i][i] are never read, since the
148 \* leader does not send itself messages. It's still easier to include these
149 \ in the functions.
150 InitLeaderVars == /\ nextIndex = [i \in Server |-> [j \in Server |-> 1]]
                    // matchIndex = [i \in Server |-> [j \in Server |-> 0]]
152 InitLogVars == /\ log
                            = [i \in Server |-> << >>]
       /\ commitIndex = [i \in Server |-> 0]
154 Init == /\ messages = [m \in {} |-> 0] 用{},告诉系统,这是个map?
            /\ InitHistoryVars
            /\ InitServerVars
            /\ InitCandidateVars
158
            /\ InitLeaderVars
            /\ InitLogVars
160
161 ----
162 \* Define state transitions
164 \* Server i restarts from stable storage.
165 \* It loses everything but its <u>currentTerm</u>, <u>votedFor</u>, <u>and log</u>.
166 Restart(i) ==
       /\ state'
                          = [state EXCEPT ![i] = Follower]
168
       // votesResponded' = [votesResponded EXCEPT ![i] = {}]
       // votesGranted' = [votesGranted EXCEPT ![i] = {}]
                        = [voterLog EXCEPT ![i] = [j \in {} |-> <<>>]]
170
       /\ voterLog'
       /\ nextIndex'
                          = [nextIndex EXCEPT ![i] = [j \in Server |-> 1]]
       /\ matchIndex'
                          = [matchIndex EXCEPT ![i] = [j \in Server |-> 0]]
       /\ commitIndex' = [commitIndex EXCEPT ![i] = 0]
174
       /\ UNCHANGED <<messages, currentTerm, votedFor, log, elections>>
176 \* Server i times out and starts a new election.
Timeout(i) == /\ state[i] \in {Follower, Candidate} Leader, 不会发生超时? 关键是发现也没啥用,已经是leader
178
                  /\ state' = [state EXCEPT ![i] = Candidate]
                  /\ currentTerm' = [currentTerm EXCEPT ![i] = currentTerm[i] + 1]
                  \* Most implementations would probably just set the local vote
                  \* atomically, but messaging localhost for it is weaker.
                  // votedFor' = [votedFor EXCEPT ![i] = Nil]
                 /\ votesResponded' = [votesResponded EXCEPT ![i] = {}]
                 /\ votesGranted' = [votesGranted EXCEPT ![i] = {}]
185
                 /\ voterLog' = [voterLog EXCEPT ![i] = [j \in {} |-> <<>>]]
                  /\ UNCHANGED <<messages, leaderVars, logVars>>
187
188 \* Candidate i sends j a RequestVote request.
189 RequestVote(i, j) ==
       190
         /\ j \notin votesResponded[i]
```

```
/\ Send([mtype
                               -> RequestVoteRequest,
                 mterm
                               |-> currentTerm[i],
                  mlastLogTerm |-> LastTerm(log[i]),
                  mlastLogIndex |-> Len(log[i]),
                  msource
                              |-> i,
                              |-> j])
                  mdest
198
         \* Leader i sends j an AppendEntries request containing up to 1 entry.
      \* While implementations may want to send more than 1 at a time, this spec uses
     \ just 1 because it minimizes atomic regions without loss of generality.
     AppendEntries(i, j) ==
         /\ i /= j
         /\ state[i] = Leader
         /\ LET prevLogIndex == nextIndex[i][j] - 1
                prevLogTerm == IF prevLogIndex > 0 THEN
                                 log[i][prevLogIndex].term
                              ELSE
210
                \* Send up to 1 entry, constrained by the end of the log.
                lastEntry == Min({Len(log[i]), nextIndex[i][j]})
                entries == SubSeq(log[i], nextIndex[i][j], lastEntry)
214
            IN Send([mtype
                                  -> AppendEntriesRequest,
                                  -> currentTerm[i],
                    mterm
                    mprevLogIndex |-> prevLogIndex,
                    mprevLogTerm | -> prevLogTerm,
218
                    mentries
                                  -> entries,
                    \* mlog is used as a history variable for the proof.
220
                    \ It would not exist in a real implementation.
                                  -> log[i],
                    mlog
                    mcommitIndex |-> Min({commitIndex[i], lastEntry}),
                                  |-> i,
                    msource
                    mdest
                                  |-> j])
         /\ UNCHANGED <<serverVars, candidateVars, leaderVars, logVars>>
      \* Candidate i transitions to leader.
      BecomeLeader(i) ==
         /\ state[i] = Candidate
         // votesGranted[i] \in Quorum
                       = [state EXCEPT ![i] = Leader]
         /\ state'
         // nextIndex' = [nextIndex EXCEPT ![i] =
                             [j \in Server |-> Len(log[i]) + 1]]
234
         /\ matchIndex' = [matchIndex EXCEPT ![i] =
                             [j \in Server |-> 0]]
         /\ elections' = elections \cup
                                        -> currentTerm[i],
                             {[eterm
                               eleader |-> i,
                               elog
                                        -> log[i],
240
                               evotes |-> votesGranted[i],
241
                               evoterLog |-> voterLog[i]]}
242
         /\ UNCHANGED <<messages, currentTerm, votedFor, candidateVars, logVars>>
      \ Leader i receives a client request to add v to the log.
      ClientRequest(i, v) ==
                                如果发的不是leader,直接无视了?不告诉它leader是谁?
         /\ state[i] = Leader
         // LET entry == [term |-> currentTerm[i], 里面有term信息
                         value |-> v]
                                               log',只有server i的log变了,其他server的log不变
                newLog == Append(log[i], entry)
            IN log' = [log EXCEPT ![i] = newLog]
                                                                 IN的含义: (let def in expr,只对这个表达式有效)
         /\ UNCHANGED <<messages, serverVars, candidateVars,
                       leaderVars, commitIndex>>
     \* Leader i advances its commitIndex. leader自身,不含其他
254
     \ This is done as a separate step from handling AppendEntries responses,
     \ in part to minimize atomic regions, and in part so that leaders of
     \* single-server clusters are able to mark entries committed.
258
     AdvanceCommitIndex(i) ==
         /\ state[i] = Leader
```

```
/\ LET \* The set of servers that agree up through index.
                 Agree(index) == \{i\} \setminus \{k \in Server : \}
                                              matchIndex[i][k] >= index}
                 \ The maximum indexes for which a quorum agrees
                 agreeIndexes == \{index \setminus in 1..Len(log[i]) :
                                     Agree(index) \in Quorum}
                 \* New value for commitIndex'[i]
                 newCommitIndex ==
268
                    IF /\ agreeIndexes /= {}
                      /\ log[i][Max(agreeIndexes)].term = currentTerm[i]
270
                    THEN
                       Max(agreeIndexes)
                    ELSE
                        commitIndex[i] 条件不符合,则根本没变
274
             IN commitIndex' = [commitIndex EXCEPT ![i] = newCommitIndex]
          /\ UNCHANGED <<messages, serverVars, candidateVars, leaderVars, log>>
278 \* Message handlers
279
     \* i = recipient, j = sender, m = message
280
281 \* Server i receives a RequestVote request from server j with
    \* m.mterm <= currentTerm[i].</pre>
283
      HandleRequestVoteRequest(i, j, m) ==
                                                              TLA+ book里面有"Let expression"
          LET logOk == \/ m.mlastLogTerm > LastTerm(log[i])
                      // /\ m.mlastLogTerm = LastTerm(log[i])
286
                         // m.mlastLogIndex >= Len(log[i])
287
              grant == /\ m.mterm = currentTerm[i]
                      /\ log0k
                      // votedFor[i] \in {Nil, j} 这个感觉与论文中的反了?==>实际上, UpdateTerm已经修改了server的term,就比mterm大。

■ CurrentTerm[i]     但是这个感觉比较奇怪,这些//,是不是一个原子操作?
          IN /\ m.mterm <= currentTerm[i]</pre>
            // \/ grant // votedFor' = [votedFor EXCEPT ![i] = j] grant为true , 执行后面这个。替代了if..else
                \/ ~grant /\ UNCHANGED votedFor
            /\ Reply([mtype
                                  -> RequestVoteResponse,
                                   -> currentTerm[i],
                      mvoteGranted |-> grant,
                       \* mlog is used just for the `elections' history variable for
                       \ the proof. It would not exist in a real implementation.
                                   |-> log[i],
                       msource
                                   |-> i,
                                   |-> j],
                       m)
302
             /\ UNCHANGED <<state, currentTerm, candidateVars, leaderVars, logVars>>
303
      \* Server i receives a RequestVote response from server j with
      \* m.mterm = currentTerm[i].
306
      HandleRequestVoteResponse(i, j, m) ==
307
          \* This tallies votes even when the current state is not Candidate, but
          \ they won't be looked at, so it doesn't matter.
309
         // m.mterm = currentTerm[i]
         // votesResponded' = [votesResponded EXCEPT ![i] =
                                    votesResponded[i] \cup {j}]
         /\ \/ /\ m.mvoteGranted
               /\ votesGranted' = [votesGranted EXCEPT ![i] =
                                       votesGranted[i] \cup {j}]
               // voterLog' = [voterLog EXCEPT ![i] =
                                   voterLog[i] @@ (j :> m.mlog)]
            \/ /\ ~m.mvoteGranted
               /\ UNCHANGED <<votesGranted, voterLog>>
          /\ Discard(m)
          /\ UNCHANGED <<serverVars, votedFor, leaderVars, logVars>>
      \* Server i receives an AppendEntries request from server j with
      \* m.mterm <= currentTerm[i]. This just handles m.entries of length 0 or 1, but</pre>
      \ implementations could safely accept more by treating them the same as
324
      \ multiple independent requests of 1 entry.
      HandleAppendEntriesRequest(i, j, m) ==
          LET logOk == \/ m.mprevLogIndex = 0
```

```
\/ /\ m.mprevLogIndex > 0
                         // m.mprevLogIndex <= Len(log[i])</pre>
                         // m.mprevLogTerm = log[i][m.mprevLogIndex].term
          IN /\ m.mterm <= currentTerm[i]</pre>
            /\ \/ /\ \* reject request
                     // m.mterm < currentTerm[i]</pre>
                     // // m.mterm = currentTerm[i]
                        /\ state[i] = Follower
                        /\ \lnot log0k
                                            -> AppendEntriesResponse,
                  /\ Reply([mtype
                                            -> currentTerm[i].
                            mterm
                                            |-> FALSE.
                            msuccess
                                          |-> 0,
                            mmatchIndex
341
                                            |-> i.
                            msource
                                            |-> j],
                            mdest
                            m)
                  /\ UNCHANGED <<serverVars, logVars>>
               // \* return to follower state
346
                  // m.mterm = currentTerm[i]
                  /\ state[i] = Candidate
348
                  // state' = [state EXCEPT ![i] = Follower]
                  /\ UNCHANGED <<currentTerm, votedFor, logVars, messages>>
350
               \/ \* accept request
                  // m.mterm = currentTerm[i]
                  /\ state[i] = Follower
                  /\ log0k
354
                  /\ LET index == m.mprevLogIndex + 1
                     IN \/ \* already done with request
356
                            /\ \/ m.mentries = << >>
                               /\ log[i][index].term = m.mentries[1].term
                               \* This could make our commitIndex decrease (for
                               \* example if we process an old, duplicated request),
                               \* but that doesn't really affect anything.
                                                                          根据什么决定修改commitIndex? 而且还是捎带?
                            /\ commitIndex' = [commitIndex EXCEPT ![i] =
                                                   m.mcommitIndex]
                            /\ Reply([mtype
                                                      -> AppendEntriesResponse,
                                      mterm
                                                      |-> currentTerm[i],
                                      msuccess
                                                      -> TRUE,
                                                     -> m.mprevLogIndex +
                                      mmatchIndex
                                                          Len(m.mentries),
                                                      |-> i,
                                      msource
                                      mdest
                                                      |-> j],
                                      m)
                            /\ UNCHANGED <<serverVars, logVars>>
                        \/ \* conflict: remove 1 entry
                            /\ m.mentries /= << >>
                            /\ Len(log[i]) >= index
                            /\ log[i][index].term /= m.mentries[1].term
                            /\ LET new == [index2 \in 1..(Len(log[i]) - 1) |->
                                               log[i][index2]]
                               IN log' = [log EXCEPT ![i] = new]
                            /\ UNCHANGED <<serverVars, commitIndex, messages>>
                        \/ \* no conflict: append entry
                            /\ m.mentries /= << >>
                            /\ Len(log[i]) = m.mprevLogIndex
                            /\ \log' = [\log EXCEPT ![i] =
                                           Append(log[i], m.mentries[1])]
                            /\ UNCHANGED <<serverVars, commitIndex, messages>>
             /\ UNCHANGED <<candidateVars, leaderVars>>
      \* Server i receives an AppendEntries response from server j with
     \* m.mterm = currentTerm[i].
      HandleAppendEntriesResponse(i, j, m) ==
          // m.mterm = currentTerm[i]
          /\ \/ /\ m.msuccess \* successful
               /\ nextIndex' = [nextIndex EXCEPT ![i][j] = m.mmatchIndex + 1]
               // matchIndex' = [matchIndex EXCEPT ![i][j] = m.mmatchIndex]
```

```
\/ /\ \lnot m.msuccess \* not successful
               /\ nextIndex' = [nextIndex EXCEPT ![i][j] =
                                    Max({nextIndex[i][j] - 1, 1})]
               /\ UNCHANGED <<matchIndex>>
400
          /\ Discard(m)
401
          \verb|/\setminus UNCHANGED| << server Vars, candidate Vars, log Vars, elections>>
402
403
     \* Any RPC with a newer term causes the recipient to advance its term first.
404 UpdateTerm(i, j, m) ==
405
         /\ m.mterm > currentTerm[i]
406
         // currentTerm' = [currentTerm EXCEPT ![i] = m.mterm]
407
                           = [state EXCEPT ![i] = Follower]
         /\ state'
         /\ votedFor'
                          = [votedFor EXCEPT ![i] = Nil]
408
409
            \* messages is unchanged so m can be processed further.
410
         /\ UNCHANGED <<messages, candidateVars, leaderVars, logVars>>
411
412 \* Responses with stale terms are ignored.
413 DropStaleResponse(i, j, m) ==
414
         // m.mterm < currentTerm[i]</pre>
415
         /\ Discard(m)
416
         /\ UNCHANGED <<serverVars, candidateVars, leaderVars, logVars>>
417
418 \* Receive a message.
419 Receive(m) ==
420
        LET i == m.mdest
421
            j == m.msource
422
         IN \* Any RPC with a newer term causes the recipient to advance
423
            \* its term first. Responses with stale terms are ignored.
                                             执行的原子单位是什么? UpdateTerm会不会执行完了,后面的操作都不执行,中间插入了别的操作?
424
            \/ UpdateTerm(i, j, m)
425
            \/ /\ m.mtype = RequestVoteRequest
426
               /\ HandleRequestVoteRequest(i, j, m)
427
            \/ /\ m.mtype = RequestVoteResponse
428
             /\ \/ DropStaleResponse(i, j, m)
429
                  \/ HandleRequestVoteResponse(i, j, m)
430
            \/ /\ m.mtype = AppendEntriesRequest
431
               /\ HandleAppendEntriesRequest(i, j, m)
            \/ /\ m.mtype = AppendEntriesResponse
433
               /\ \/ DropStaleResponse(i, j, m)
434
                  \/ HandleAppendEntriesResponse(i, j, m)
436 \* End of message handlers.
437
438 \* Network state transitions
439
440 \* The network duplicates a message
441
      DuplicateMessage(m) ==
443
          /\ UNCHANGED <<serverVars, candidateVars, leaderVars, logVars>>
445
     \* The network drops a message
446
      DropMessage(m) ==
447
        /\ Discard(m)
         /\ UNCHANGED <<serverVars, candidateVars, leaderVars, logVars>>
450
451 \* Defines how the variables may transition.
452 Next == /\ \/ \E i \in Server : Restart(i)
453
                \/ \E i \in Server : Timeout(i)
                \/ \E i,j \in Server : RequestVote(i, j)
455
                \/ \E i \in Server : BecomeLeader(i)
456
                \/ \E i \in Server, v \in Value : ClientRequest(i, v)
457
                \/ \E i \in Server : AdvanceCommitIndex(i)
458
                \/ \E i,j \in Server : AppendEntries(i, j)
459
                \/ \E m \in DOMAIN messages : Receive(m)
460
                \/ \E m \in DOMAIN messages : DuplicateMessage(m)
461
                \/ \E m \in DOMAIN messages : DropMessage(m)
462
                \* History variable that tracks every log ever:
463
             /\ allLogs' = allLogs \cup {log[i] : i \in Server}
```

```
464
465 \* The specification must start with the initial state and transition according
466 \* to Next.
                                  //TODO: 这里没有没有让系统保证什么条件一定成立,Liveness或者theorem,这样运行的意义?
到底在保证什么?例如paxos例子的voting module中,有很多。
起码需要保证,各个server,同位置的log,是相同的。
467 Spec == Init \ \ [][Next]_vars
468
469 -----
470
471 \* Changelog:
472 \*
473 \* 2014-12-02:
^{475} \* intended. Since SubSeq is inclusive, the upper bound of the range should
476 \* have been nextIndex, not nextIndex + 1. Thanks to Igor Kovalenko for
477 \* reporting the issue.
478 \* - Change matchIndex' to matchIndex (without the apostrophe) in
479 \* AdvanceCommitIndex. This apostrophe was not intentional and perhaps
480 \* confusing, though it makes no practical difference (matchIndex' equals
481~\ensuremath{\mbox{\sc Name}} matchIndex). Thanks to Hugues Evrard for reporting the issue.
482 \*
483 \* 2014-07-06:
484 \* - Version from PhD dissertation
```