

Automatic Verification and Validation of Automatically Generated Simulation-Based Digital Twins for Discrete Material Flow Systems

Author: Daniel Fischer

Supervisor: Prof. Christian Schwede

Program: Research Master Data Science

Institution: Hochschule Bielefeld (HSBI)

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Abstract

This thesis investigates the application of Digital Twins within discrete material flow systems, a key component of Industry 4.0. It reviews the progression from Digital Models and Digital Shadows to fully realized Digital Twins that integrate real-time data, simulation, and control mechanisms. To learn these Digital Twins from data enables companies to reduce twin creation and updating efforts. These gained advantages would be made obsolete if the validation and verification of such twins were performed manually involving experts. To address this problem, this research proposes a data-driven framework for automated verification, validation, and uncertainty quantification of simulation-based digital twins. Leveraging object-centric event logs and advanced machine learning techniques, the framework aims to seamlessly integrate digital simulation with real-world data. This approach ensures that the resulting Digital Twins maintain high fidelity and robustness by continuously benchmarking their performance against operational metrics. The framework is evaluated via a comprehensive case study examining its effectiveness in enhancing process efficiency and predictive precision.

Keywords: Digital Twins, Automated VVUQ, Process Mining, Machine Learning, Discrete Material Flow Systems.

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List of Abbreviations

AGDT Automatically Generated Digital Twin. 1

ASMG Automatic Simulation Model Generation. 1

BNN Bayesian Neural Network. 1

BPMN Business Process Model and Notation. 1

CNN Convolutional Neural Network. 1

CPS Cyber-Physical System. 1

DDDT Data-Driven Digital Twin. 1

DE Deep Ensembles. 1

DES Discrete-Event Simulation. 1

DM Digital Model. 1

DMFS Discrete Material Flow Systems. 1

DS Digital Shadow. 1

DT Digital Twin. 1

E2O Event-to-Object Relation. 1

GP Gaussian Processes. 1

HDT Hybrid Digital Twin. 1

IoT Internet of Things. 1

KPI Key Performance Indicator. 1

LSTM Long Short-Term Memory. 1

MCD Monte Carlo Dropout. 1

ML Machine Learning. 1

O2O Object-to-Object Relation. 1

OCEL Object-Centric Event Log. 1

PM Process Mining. 1

PPC Production Planning and Control. 1

RNN Recurrent Neural Network. 1

SBDT Simulation-Based Digital Twin. 1

V&V Verification and Validation. 1

VVUQ Verification, Validation, and Uncertainty Quantification. 1

XES eXtensible Event Stream. 1

Chapter 1

Introduction

1.1 Initial Situation

Digital Twins (DT) are a key technology at the front of the fourth industrial revolution, often referred to as Industry 4.0. The latter term is characterized by the integration of cyber-physical systems (CPS), the Internet of Things (IoT), and cloud computing to create smart factories aimed at automation and efficiency (Oztemel & Gursev, 2020). Companies pursue this vision by trying to remain competitive through the adoption of innovative technologies that promise enhanced productivity and reduced operational costs. One such technology that supports this transformation is the DT. It can be defined as a virtual representation of physical assets enabling real-time monitoring and optimization (Tao et al., 2018). The DT bridges the connection between the two entities with a bi-directional data flow to exchange information and to influence the behaviour of the physical asset (Grieves, 2014). This technology is central to Industry 4.0, facilitating the physical and digital worlds through real-time data integration, simulation, and optimization (Judijanto et al., 2024).

Although this discipline is rapidly evolving, a unified definition of DT has yet to be established due to the diverse requirements and perspectives across different fields. In engineering, the focus might be on the real-time interaction between physical systems and their digital counterparts, whereas in computer science, the emphasis is often on data integration and simulation capabilities. These varying priorities result in multiple interpretations and applications of the term DT. The concept was first introduced by Michael Grieves in 2002, who defined it as a digital representation of a physical object or system (Grieves, 2014). However, the concept has evolved since, encompassing a broader range of applications and

technologies. In the literature, three terms are used to describe similar characteristics of DT: Digital Model (DM), Digital Shadow (DS), and Digital Twin (DT), see Figure 1.1 (Jones et al., 2020; Zhang et al., 2021).



Figure 1.1: Comparison of Digital Shadow (DS), Digital Model (DM) and Digital Twin (DT) as presented by Kritzinger (2018). This distinction is crucial for understanding validation requirements across different digital representation types.

The Digital Model (DM) represents the most basic form. It involves manual data connections between physical and digital entities. These connections can be temporarily shifted or even disconnected. There is no direct control of the digital object over the physical entity. It is primarily a simple or complex model *describing* the physical object. The data flow must be manually triggered by the modeler, who also interprets the results and controls the DM. The Digital Shadow (DS) is a more advanced version of the DM. It is a digital representation of the physical object that is continuously updated with real-time data, allowing for monitoring, analysis and simulation. While it can predict future states of the physical object based on the current state and historical data, it is not able to influence the physical object without human intervention. The control is, similar to the DM, still in the hands of the modeller. A DS is frequently used for simulation purposes and is sometimes misclassified as a DT in the literature (Kritzinger et al., 2018; Sepasgozar, 2021). The Digital Twin (DT) is the most advanced version of the three, offering a digital representation of the physical object, which is also continuously updated with real-time data. The DT can be used for monitoring, analysis, and *control* purposes. It can predict the future states of the physical object based on the current state and historical data. The DT can also influence the physical object by sending control signals to it. The control is partially or completely in the hands of the DT. The DT thus *can* serve more purpose than modelling or simulating the physical object. It may serve as an autonomous system, updating itself or with minimal human intervention (Kritzinger et al., 2018).

DTs are applied across various sectors, including manufacturing, defence, automotive, service, finance and healthcare (Tao et al., 2018). Manufacturing is particularly notable due to its high potential for process optimization and automation. This thesis focuses on the latter, particularly discrete material flow systems (DMFS). These systems process discrete objects (parts) moving along transportation routes or conveyor lines at regular or irregular intervals, integrating both production and logistics operations (Arnold & Furmans, 2005; Schwede & Fischer, 2024a). A key simplification in their modelling is the abstraction of material flow as a sequence of discrete events, following the principles of discrete-event simulation (DES) (Kovacs & Kostal, 2016; Robinson, 2014). DES is well-suited for analysing complex systems where state changes occur at discrete points in time, such as arrivals, departures, and processing steps (Robinson, 2014).

Historically, DM played a crucial role in the design, planning, and control of DMFS, primarily through applications like material flow simulations, logistic assistance systems, and digital factory implementations (Thiede et al., 2013). However, advancements in both DS and DT have enabled a shift from isolated, use-case-specific models toward complete digital representations that span the entire lifecycle of DMFS (Abdoune et al., 2023). This transition is largely driven by the growing demand for predictive capabilities by stakeholders and automated decision support in manufacturing systems, reflecting the core principles of Industry 4.0 (Frank et al., 2019). A second driver of DT innovation lies in the widely available data from IoT devices and sensors, which enhances model training and real-time adaptation of DTs (Tao et al., 2018).

In practice, the automated data transfer between the digital model and the physical system is not always critical for DMFS management. Unlike in time-sensitive applications, human decision-makers often remain integral to the control loop, meaning that real-time automation is not always necessary (Schwede & Fischer, 2024a). Therefore, for this thesis, DS and DTs will be treated as equivalent concepts.

Beyond replicating the current state and managing historical data, DTs are essential for predicting system behaviour and evaluating potential modifications. The widespread use of DES within digital twins highlights the central role of simulation-based DTs (SBDTs) in DMFS (Lugaresi & Matta, 2021). As Schwede and Fischer emphasize, SBDTs provide decision support for optimizing costs and performance in highly competitive manufacturing environments. While current SBDTs are primarily developed and updated manually by domain experts, emerging research explores how machine learning (ML) can enhance predictive

accuracy and automate model updates by automatically learning model characteristics, reducing costs and development time.

Thus, the progression from digital models to simulation-based DTs reflects an ongoing shift toward data-driven, predictive, and increasingly automated representations of DMFS, enabling more informed decision-making throughout the system's lifecycle (Boschert & Rosen, 2016; Lim et al., 2020).

1.2 Problem

Despite the transformative potential of DTs, their implementation can be challenging. Creating and maintaining accurate DTs require substantial investments in technology and domain knowledge. This investment is wasted if the resulting model fails to accurately represent the physical entity or produces incorrect results. While automatic generation may seem like an elegant solution, it carries risks such as overfitting or biased predictions (Geman et al., 1992). Manufacturing data for training must be rigorously cleaned and preprocessed. Automatically generated DTs must also undergo automatic Validation, Verification, and Uncertainty Quantification (VVUQ) to preserve their cost and time advantages. Manual VVUQ, which relies on humans in the loop, hinders scalability, automatic synchronization with the physical entity, and depends on costly domain knowledge often provided by experts (Bitencourt et al., 2023). These hurdles are significant barriers to automatic learning (Ribeiro et al., 2016; Zhao et al., 2024). As industries integrate DT into their production processes, establishing trust becomes fundamental as well (Arrieta et al., 2020; Trauer et al., 2022). For widespread acceptance among co-workers, stakeholders, and investors, automatic DT creation and VVUQ must demonstrate clear advantages over manual creation and expert-led VVUQ.

Even when DT learning is successfully performed, questions about its correctness, precision, and robustness persist. These concerns are addressed by validation, verification, and uncertainty quantification frameworks (VVUQ) (Sel et al., 2025). Ensuring the validity, reliability, and accuracy of a DT is critical, yet traditional VVUQ approaches rely heavily on manual expert involvement and case-specific reference values (Bitencourt et al., 2023; Hua et al., 2022). This leads to inefficiencies, particularly in the context of automated DT generation, where such manual processes undermine the goal of reducing development effort. Hua et al. even argue that there are no robust and standardized verification and validation methods for DTs. As (Sel et al., 2025) point out, uncertainty quantification is often overlooked, but addresses an important aspect of assess-

ing low noise in explanations. One hurdle to standardized VVUQ frameworks is the lack of a clear definitions for validity and verification in the context of DTs (Bitencourt et al., 2023).

For discrete material flow systems (DMFS), these challenges are even more pressing due to their procedural nature and inherent stochasticity. Rigorous VVUQ is essential to address the risk of manufacturing process failures caused by anomalies, resource constraints, software faults, or human error. This necessity arises because such failures can disrupt the intricate workflows and unpredictable dynamics inherent in DMFS, making reliable performance prediction a priority. When DTs for these systems are generated automatically, traditional validation methods become problematic, as they negate much of the efficiency gains through automation. This creates a fundamental conflict: while automated DT generation reduces initial development and updating efforts, it simultaneously increases the complexity of validation and verification, potentially counteracting its intended efficiency gains.

1.3 Objective

This thesis addresses this conflict by developing a data-driven framework for automated VVUQ of automatically generated, simulation-based DTs which have been learned from data. The focus lies on DMFS due to their practical relevance and dynamical, procedural nature. The research can further be specified by the following research questions (RQ):

- **RQ1:** How can automated validation and verification processes for DTs be efficiently implemented to maintain accuracy?
- **RQ2:** Which data-driven approaches are best suited to identify discrepancies between simulated behaviour and real operational data in discrete material flow systems?
- **RQ3:** To what extent does the developed framework improve the quality and reliability of DTs compared to traditional VV methods?

This thesis proposes that object-centric event logs—commonly used to generate DTs in manufacturing—can also serve as the foundation for an automated, use-case-independent validation and verification framework. Such an approach would preserve the efficiency benefits of automated generation while ensuring that the resulting DTs meet necessary standards. A key aspect of this approach is the development and monitoring of generic, statistically grounded reference

values, which must be quantifiable and have an underlying distribution. The framework will be evaluated using a case study from the discrete material flow domain, providing empirical evidence of its effectiveness in improving model accuracy and efficiency.

1.4 Structure and Methodology

Structure

The thesis is organized into eight chapters. Chapter 2 establishes the theoretical foundation. It begins with broad, domain-specific concepts and progressively narrows the focus to the core topics of this thesis: Automated verification and validation (VVUQ) of simulation-based digital twins (SBDTs) in discrete material flow systems. Section 2.1 introduces material flow planning and simulation, outlining the key elements of production systems, such as processes, resources, and control mechanisms. It also defines key performance indicators (KPIs), essential for evaluating both real and simulated systems, providing the practical context in which DTs operate. Section 2.2 then transitions to the DT concepts. A framework for comparing DTs by Schwede and Fischer (2024a) is presented. Special attention is given to data-driven DTs and their subset, automatically generated digital twins (AGDTs). The section concludes by contrasting AGDTs with classical simulation models, highlighting the challenges posed by automatically generated models. Building on this foundation, Section 2.3 presents the principles of process mining (PM) and event log analysis, focusing on object-centric event logs as a data basis for automated validation. This section demonstrates how PM acts as a bridge between real-world process data and model validation, thus enabling continuous verification of SBDTs. Section 2.4 narrows the focus further to VVUQ in the context of SBDTs, beginning with a historical overview of VVUQ methodologies. It then addresses the specific challenges posed by automatically generated models, such as data dependency and lack of transparency in model creation. The section introduces machine learning-based approaches for VVUQ, particularly classification methods for detecting model deviation. It also explores the current state of VVUQ in corporate practice, emphasizing the need for continuous and automated validation processes.

Chapter 3 outlines the methodology for developing the proposed framework. It begins with a requirements analysis, deriving functional, technical, and data format requirements from theoretical findings. The chapter then elaborates on the data-based validation strategy, machine learning-based validation approach, metrics for model evaluation, and online validation with continuous monitoring.

Chapter 4 presents the implementation of the framework, starting with the architecture and system setup, followed by detailed descriptions of event log processing, simulation integration, and the machine learning pipeline.

Chapter 5 presents the case study results, evaluating the framework's effectiveness in improving DT quality. It describes the application scenario and data basis, the automatically generated DT, validation experiments, and result interpretation. It concludes with a comparison to manual validation methods.

Chapter 6 discusses the implications of the results and provides recommendations for future research. It evaluates the framework in light of the research questions, examines the significance of verification in automatically generated DTs, addresses limitations, and explores implications for research and practice.

Chapter 7 concludes the thesis by summarizing key findings and their implications. It addresses the research questions and hypotheses, discusses the significance of the results, acknowledges limitations, and provides recommendations for future work.

Methodology

The thesis follows a Design Science Research approach (DSR). This approach is characterized by the development of artifacts to solve practical problems (Hevner et al., 2004; Peffers et al., 2007). Artifacts in the sense of DSR are created objects or constructs which address the given problem and contribute to both theory and practice. The artifacts are evaluated in a real-world context to demonstrate their effectiveness. The thesis applies the cyclical DSR model, see figure 1.2.



Figure 1.2: The cyclical design science research model. The model consists of six steps. The problem identification (1) refers to the research gap in automated VVUQ of SBDT. Defining the solution objectives (2) specifies the research gap by formulating questions and hypotheses based on the theoretical foundations. The design and development (3) phase includes the development of the framework. The demonstration (4) phase shows the application of the framework in a case study. The evaluation (5) phase assesses the effectiveness of the framework. The communication (6) phase concludes the research by presenting the results.

The research paradigm of the thesis is deductive-theory critical (Eberhard, 1987). A conceptual VVUQ framework is developed based on existing theoretical foundations, while deriving new requirements through a requirements analysis. The framework is then applied in a case study to evaluate its effectiveness. The research is critical in that it aims to improve the efficiency and effectiveness of VVUQ for automatically generated DTs. Elements of empirical research are included through the case study and the data-driven approach.

Chapter 2

Theoretical Foundation

The following chapter provides a theoretical foundation for the research conducted in this thesis. It introduces the basic concepts of material flow planning and simulation, digital twins, process mining, and verification, validation, and uncertainty quantification (VVUQ). The relevance of these concepts in the context of simulation-based digital twins and their application in corporate practice will also be discussed.

2.1 Discrete Material Flow Systems and Simulation

This section begins with an introduction of the underlying concepts of Discrete Material Flow Systems (DMFS) and Simulation Based Digital Twins (SBDT).

2.1.1 Basic Concepts

Discrete material flow systems cannot be fully understood without first clarifying the principles of Discrete Event Simulation (DES) for Discrete Event Systems. In DES, a system changes its state through *events* that occur at specific, discrete time instances; it is assumed that no changes occur between two successive events. Consequently, the state of the system is completely defined by the values of its descriptive variables at each event occurrence (Varga, 2001). The time at which an event occurs is typically marked by a timestamp, and the scientific observation of such systems is conducted by analysing the discrete *sequence* of events over time (Robinson, 2014).

Simulation, in this context, refers to the process of imitating the operation of a Discrete Event System over time—often through multiple event sequences. This imitation is captured in a model, and the core activities in a simulation involve

constructing and experimenting with this model. A high-quality simulation abstracts the essential features of the system, which requires the modeller to have a sound a priori understanding of what “essential” means in the given context. Although the model can later be refined, its quality is primarily measured by its ability to predict outcomes and offer a diverse range of scenarios (Maria, 1997).

In the context of DMFS, their simulation describes the imitation of material flow systems by breaking down continuous flows into discrete events. Such material flow systems can be characterized as “systems processing discrete objects (parts) that move at regular or irregular intervals along transportation routes or conveyor lines, comprising production and logistic systems” (Arnold & Furmans, 2006; Schwede & Fischer, 2024a). These systems form the backbone of material flow planning and control structures. The central idea of material flow planning and control is to ensure that material requirements—both in terms of quantity and timing—are met during transportation and storage across the various stages of the supply chain (Stommel, 2007). Importantly, the time horizon of interest spans from order placement up to delivery. To summarize, DMFS are often simulated using DES, which abstracts the continuous flow of materials into discrete events. The simulation is carried out using a model. The simulation and modeller are embedded in the context of material flow planning and control, which aims to ensure that material requirements are met across the supply chain. Successfully performed material flow planning and control induce high quality data for simulation and modelling purposes.

2.1.2 Comparing DMFS

Because the simulation of DMFS often involves (discrete) event simulation, events in DMFS need to be further differentiated to be comparable. (Arnold & Furmans, 2006) propose to differentiate DMFS into static and dynamic components.

Static components describe the possible states of the system. Possible states can be the set of possible processes given a part or resource, for example. Dynamic components define the concrete material flow for a certain part or order. Static components include parts, resources and processes (Schwede & Fischer, 2024a). Parts are transformed by processes using resources, sometimes based on orders. Transformation can have an impact on physical properties of the parts (transformation model), spatial position (transition model), the quality of the parts (quality model) and takes time (time model) and uses resources (resource model). Resources have a capacity of handling parts in parallel (resource capac-

ity model) and processes have a predecessor-successors relationship (process model). Dynamic components are used to define the concrete dynamic material flow within the DMFS. There are four components: Order generation, order control, resource control and supply control. Order generation defines the load the system must process. Order control defines how parts are processed, sometimes referred to as routing rules (Milde & Reinhart, 2019). Resource control defines how resources decide to handle processing requests, also sometimes referred to as priority rules. Supply control describes how supply parts are provided (Milde & Reinhart, 2019; Schwede & Fischer, 2024a). See the latter source for a more detailed description of the components.

2.1.3 Production Planning and Control

Successful companies use production planning and control frameworks to describe and optimize their DMFS. After establishing a theoretical foundation and simulation approaches for DMFS, this section thus focusses on Production Planning and Control (PPC) as a critical factor influencing the quality and quantity of data generated by Discrete Event Simulation. PPC is the structured approach to planning, scheduling, controlling and managing all aspects of the manufacturing process. It involves the coordination of resources, processes, and orders to meet production goals. PPC is essential for optimizing production processes, reducing costs, and improving quality. The main functions of PPC include production planning, production scheduling, and production control. Production planning involves determining the production capacity, production goals, and production processes. Production scheduling involves creating a detailed schedule for production activities. Production control involves monitoring and controlling production activities to ensure that production goals are met (Kiran, 2019). Scheduling is usually the last step performed before execution of the plan (Pinedo & Pinedo, 2012).

The integration of PPC with simulation models is crucial because it directly affects the data quality used in DES of DMFS. Effective PPC processes anticipate anomalies in the production cycle, allowing for adjustments that maintain system efficiency and reliability. If successful, these adjustments yield high-quality data that enhance the accuracy of simulation outcomes. (Kiran, 2019).

2.1.4 Key Performance Indicators

Up to this point, DES for SBDT of DMFS has been introduced, outlining the key factors that contribute to a robust simulation. A model differentiation framework

proposed by Schwede and Fischer has been briefly presented to facilitate comparison of SBDT. Furthermore, the critical role of PPC in generating high-quality data for simulation has been discussed. These discussions ignored up till now that, even when SBDT are integrated within well-functioning PPC processes, various SBDT models remain prone to errors and inherent trade-offs that must be addressed by the modeller (Tao et al., 2018).

The goal conflict of the modeller when developing SBDT can be described by the following conflict triangle (Balci, 2012; Robinson, 2014):



Figure 2.1: The goal conflict of the modeller when developing SBDT. Aiming for higher accuracy (validity) often leads to higher computational costs (efficiency) and reduced scalability (applicability). Reaching more efficiency often leads to reduced accuracy and scalability. Aiming for higher scalability often leads to reduced accuracy and efficiency.

Focusing one of the three dimensions—accuracy (validity), efficiency (computation time), and applicability (scalability)—often leads to trade-offs in the other two dimensions. Oftentimes the data itself is not sufficient to make a decision on which trade-off to make. Limited data points may hinder the modeller from reaching high validity. System architecture may block the system from reaching good scalability. Hardware limitations may hinder the modeller from reaching high efficiency. At other times, corporate management may have a preference for one of the dimensions.

One solution to balance and quantify these goals can be achieved by defining a set of KPIs. Some may already be available through PPC, some may be calculated from DES data or the DES itself. Optimally, the data warehouse provides relevant views (Cui et al., 2020). Because the SBDT in theory mirrors the DMFS, the KPIs gathered from PPC and the DES should yield identical values. Deviations between the KPIs of the SBDT and the DMFS may indicate errors in

the SBDT or anomalies in the DFMS. The following KPIs are relevant for the evaluation of SBDT:



Figure 2.2: SBDT KPIs differentiated by PPC-based and Infrastructure-based indicators.

The PPC related KPIs may be provided by above mentioned data warehouse, because they are highly relevant in the context of production scheduling and -control. Throughput measures the number of produced parts at the last station in a specified period. It is an indicator for the productivity of the manufacturing system (Imseitif et al., 2019). Lead time is the cumulative time a part travels through the system from start to sink. It is an indicator for the efficiency of the manufacturing system (Pfeiffer et al., 2016). Cycle time measures the same amount like lead time but focusses only on the active production process, excluding transports and waiting times (Griffin, 1993). Setup time measures the time needed to prepare a machine for a new task. It is an indicator for the flexibility of the manufacturing system (Allahverdi & Soroush, 2008). In the given usecase, we aggregate the setup time for all setup processes. All KPIs presented so far can be calculated dynamically when new data has been sent. Later on, they may serve as an alert system for the modeller to detect deviations between the SBDT and the DMFS, see section 2.4.

The infrastructure related KPIs are derived by sensors from the executing system

of the SBDT. Ping time measures the time needed to send a signal from one point to another. It is an indicator for the latency of the infrastructure (Y. Wu et al., 2021). SBDT need to enforce real-time control over the physical entity. The latency thus needs to be as low as possible. In this scenario, one point (sender) is represented by the physical entity and its sensors. The receiving point runs the SBDT. It is advantageous to run the SBDT on Edge to minimize latency- and transmission costs (H. Li et al., 2018). CPU-, memory-, disk- and network usage metrics are indicators for the load of the infrastructure. They are important to detect bottlenecks in the infrastructure (H. Li et al., 2018). The first indicator is usually measured in percent of the maximum CPU capacity. The latter three indicators are usually measured in bytes or bits per second (Granelli et al., 2021). The framework derived in chapter 3 does not incorporate infrastructure-based KPIs.

2.2 Digital Twin: Definition and Concepts

The latter section gave a short introduction into DFMS, DES, its metrics and the corporate processes accompanying the SBDT. Now, we shed light on the DT itself. For a short introduction to the topic, see chapter 1.

Like introduced in the preceding chapter, DT inherent the highest order of modelling fidelity compared to DM or DS. There are different definitions of DT present in the literature (Boschert & Rosen, 2016; Demkovich et al., 2018; Glaessgen & Stargel, 2012; Grieves, 2014; Kritzinger et al., 2018; Negri et al., 2017; Tao et al., 2018; Zehnder & Riemer, 2018; Zheng et al., 2019). Each of them highlights different aspects of the DT. This thesis utilizes the definition by (Grieves, 2014) which highlights the conceptual elements of the twin and its lifecycle focus:

The digital twin concept (...) contains three main parts: A) Physical products in real space, (B) virtual products in virtual space and (C) the two-way connections of data and information that tie the virtual and real products together. (Grieves, 2014)

The physical product is the entity which will be modelled. The virtual product is the DT itself, but also its infrastructure, for example data services making the real-time data flow possible (Tao et al., 2018). The two-way connection is the data flow between the physical and the virtual product. The data flow is bidirectional. Zehnder and Riemer add that the data flow may contain meta data "describing the data source and its context". Also the connection protocol is of

importance here (e.g. MQTT or REST). TCP may be the method of choice as it ensures that the packages arrive in the correct order and without errors (H. Li et al., 2018).

2.2.1 Types of Digital Twins

Now that a unified understanding of DT has been established, this section focuses on how DT may be learned from different sources of information. The following list includes the most relevant types of DT with a focus on different kinds of information sources:

- Simulation-based DT (SBDT) (Lugaresi & Matta, 2021; Martinez et al., 2018)
- Data-driven DT (DDDT) (Friederich et al., 2022; R. He et al., 2019)
- Hybrid Digital Twins (HDT) (Huang et al., 2023; Luo et al., 2020)

SBDTs (Boschert & Rosen, 2016; Lugaresi & Matta, 2021; Martinez et al., 2018) are based on DES. They utilize discrete event simulation (see section 2.1) to create a dynamic representation of the physical system (Pantelides & Renfro, 2013; Schluse & Rossmann, 2016). To incorporate a SBDT into workflows and processes, suitable data structures must be in place beforehand (Boschert & Rosen, 2016). DES may improve the predictive capabilities of the model compared to manual twin creation. DES is able to model causal relationships between the events (Francis et al., 2021). In contrast, the development of a realistic simulation model requires experts and time (Charpentier & Véjar, 2014). If the simulation model fails to capture recent behaviour of the physical entity, a recalibration is mandatory (Friederich et al., 2022). SBDTs are a step forward to speed up the creation and updating processes of DTs.

DDDT rely on the utilization of data to model the physical entity. The data may be gathered from sensors, data warehouses or other sources (later on developed framework summarizes this under the term data sources, see section 3.2). The data is used to train a model which represents the physical entity. The model may be a neural network, a decision tree or another machine learning model. The model is then used to predict future states of the physical entity. The model may be updated with new data to increase its accuracy (Friederich et al., 2022; R. He et al., 2019). For a more detailed description of DDDT including its up- and downsides, see subsection 2.2.2.

HDT combine different sources of information to create a more accurate model

of the physical entity. The sources may be simulation models (see section 2.1), data-driven models (see subsection 2.2.2) or physics-based models. Physics-based models contain information about the physical properties and behaviours of the entity. They do not have to learn these characteristics from the data because this information is made available to the model *a priori* (Aivaliotis et al., 2019; Kapteyn et al., 2022). The simulation based models accompanying the physics-based one obeys characteristics of SBDT, see above. The combination of different sources may make the HDT more robust and a faster learner. HDT unite the advantages of SBDT with the knowledge advantage physics based models have. Unfortunately, they also inherit the disadvantages of SBDT through their simulation character. Physics-based models may also involve heavy involve heavy computational costs and domain expertise (Kapteyn et al., 2022).

2.2.2 Data-Driven Digital Twins

While SBDTs and HDT possess significant computational costs and require domain expertise, DDDT are able to learn from data without the need for a handwritten simulation model. The DDDT *learns* the model. Learning in the context of DDDT is not trivial, several approaches have been proposed in the literature (Francis et al., 2021; Friederich et al., 2022; R. He et al., 2019). Often times Data Science methods come to work. The learning process may be supervised or unsupervised. Supervised learning uses labelled data to train the model (Cunningham et al., 2008). The label can symbolize different values of interest. Unsupervised learning uses unlabelled data to train the model (Barlow, 1989). Often times, the task at hand is to group the data into different categories, see Figure 2.4.4 (Biesinger et al., 2019). The learning process may be online or offline. Offline learning uses the data *once* for training, validation and testing, while online learning continuously updates the model with new data to adapt to changes in the physical system. Online learning is thus able to capture new trends in the data and to foresee concept drift (Tsymbal, 2004). DDDT have to be differentiated from data-driven simulation (Charpentier & Véjar, 2014), which involves human intervention to create highly individual solutions for the physical entity. The key difference is that every characteristic has to be explicitly described in the model by the expert, there are no efforts to let an intelligent algorithm learn these by itself. DDDT may be able to update themselves to new trends in the data by online learning, termed *synchronization* (Reinhardt et al., 2019). Latter has to be differentiated from *updating*, which is a manual process to take corrective action in the logic of the twin itself (Schwede & Fischer, 2024a). An example for updating a DDDT may be the addition of a new feature to the model. An

example for synchronization may be the adaption of the model to new trends in the data. The latter may be done by the model itself, the former has to be done by the modeller. DDDT thus rely less on domain expertise and manual model creation. A suitable model may be able to capture relevant trends in the data and to predict outcomes which describe most of the characteristics of the physical entity. (Francis et al., 2021) propose several elements a DDDT must contain to be termed *data-driven*:

1. **Data Collection:** The relevant entities to be modelled have to be identified. This activity involves data gathering of the identified entities and ensuring a steady data stream to a database. The data may be gathered from sensors, data warehouses or other sources.
2. **Data Validation:** This step involves cleaning and preprocessing the data. The data may contain missing values, outliers or other errors. The data has to be cleaned and preprocessed to ensure a high quality of the model. Plausibility checks may be performed to ensure the data is correct.
3. **Knowledge Extraction:** After the data has been collected and cleaned, events have to be detected. Francis et al. utilize process mining terms in this context, such as event detection and process discovery. The main goal in this step is to find a common ground on which events are of interest. The thesis later dives deeper into Process Mining techniques applied here, see section 2.3.
4. **(Semi-)automatic Simulation Modelling:** The data is used to train a model. This step may use offline or online data as a stream. The model may be a neural network, a decision tree or another machine learning model. The model is then used to predict future states of the physical entity. The model may be updated with new data to increase its accuracy.
5. **Continuous Model Validation:** Interestingly, Francis et al. propose a continuous model validation. In the online learning case, they recommend to use the steady data stream to apply validation techniques continuously, see section 2.4 The validation may be performed by comparing the model predictions with the real data. If the model deviates from the real data, the model may be recalibrated.

DDDTs go one step further than SBDT and minimize the influence of the human in the loop (Francis et al., 2021; Friederich et al., 2022). Faster model development and updating activities are the result. The third reason to automate DT endeavours elaborated by Schwede and Fischer, increasing prediction qual-

ity, rises and falls with the data quality, thus the gathering and preprocessing efforts of the modeller. Extrinsic factors like the number of data points available also play into the equation. If the number of features is greater than the number of samples, the curse of dimensionality hinders a good modelling performance (Köppen, 2000). DDDT should avoid biased or noisy predictions at all costs. The identification of *relevant* events poses the risk of introducing a selection bias, rather a confirmation bias. The modeller may have the tendency to select events which confirm his or her hypothesis. Random sampling may be a solution to this problem, but can destroy sequential information patterns in event sequences. Overall DDDT are a promising approach to model the physical entity. If the right balance between human involvement and automated learning is found, it may be an efficient solution (Francis et al., 2021). Thinking one step ahead, employing data-based VVUQ approaches may also be a step forward. This topic will be discussed in Section ??.

One last discipline, automatic simulation model generation (ASMG), is worth mentioning. ASMG has to be differentiated from DDDT by the effort to automatically generate models, thus DM and DS through DES. Automatic DT generation is not necessarily the goal. It aims to automate the model generation process and tries to eliminate the human in the loop, (Lechevalier et al., 2018; Reinhardt et al., 2019). Automation is achieved by taking into account a diverse range of data sources, including Computer Aided Design data, PPS data, production manuals, process data and programming code, thus reaching a high data variability. The gathered data has to be processed online or offline as well through suitable frameworks or human intervention. Challenges lay in incomplete data (Bergmann, 2014), although the same problems of DDDT also apply here. If the gained data is not mined thoroughly, human intervention is needed again, mitigating automation efforts.

To conclude this section about DT, the thesis summarizes that there are different types of DT differentiated by their source of information retrieval. A lot of work has been done to make the DT creation, updating and prediction process more efficient. By the help of simulation, data and automated model generation, the DT may be created with less time and resources than manually.

2.3 Process Mining and Event Logs

After we introduced the corporate embedding of DTs and their types, the thesis now focusses on process mining (PM) and event logs. PM is a discipline which aims to extract knowledge from event logs. Event logs are the data basis for PM.

The following section introduces the basic concepts of PM and event logs.

2.3.1 Core Concepts

PM is a discipline established 1999 which is interdisciplinary rooted in the field of Data Science and Process Science (Van Der Aalst & van der Aalst, 2016). Data Science can be considered a process agnostic discipline (Van Der Aalst & van der Aalst, 2016) while process science uses models not covering hidden trends in the data. The bridge between both approaches is PM. The goal of PM is to use event data to identify and extract process information (W. van der Aalst, 2012). This information is used to discover (process discovery), monitor (conformance checking) and improve processes (process enhancement) (W. van der Aalst, 2012) by using event logs. Such logs must contain a case ID, an activity name and a timestamp. Additional information like resource information, order information or other context information may be added to the log (W. van der Aalst, 2012). Such logs assume that the process can be captured fully and sequentially.

Table 2.1: A fragment of a manufacturing event log: Each line corresponds to an event. The case ID groups unique events which are identified by an event ID to one group, a trace. The timestamp refers to the time of event occurrence, while the activity describes the event. In this example, additional information like resource name and cost are given as well. Case 1, for example, consists of five events, involving a warehouse, two inspectors, and one machine.

Case id	Event id	Timestamp	Activity	Resource	Cost
1	101	10-01-2025:08.00	receive raw material	Warehouse A	500
	102	10-01-2025:08.30	initial quality check	Inspector Stefan	300
	103	10-01-2025:09.00	cutting process	Machine X	800
	104	10-01-2025:09.45	assembly	Worker Paul	600
	105	10-01-2025:10.30	final inspection	Inspector Eva	400
2	201	11-01-2025:07.45	receive raw material	Warehouse B	500
	202	11-01-2025:08.15	cutting process	Machine Y	800
	203	11-01-2025:09.00	welding	Robot Arm Z	700
	204	11-01-2025:09.45	quality assurance	Inspector David	400
3	301	12-01-2025:06.30	receive raw material	Warehouse C	500
	302	12-01-2025:07.00	initial quality check	Inspector Claudius	300
	303	12-01-2025:07.30	CNC machining	Machine W	900
	304	12-01-2025:08.15	painting	Worker Daniel	500
	305	12-01-2025:09.00	packaging	Worker Johannes	350

Table 2.1 illustrates the PM concepts. The case ID groups unique events which are identified by an event ID to one group, a trace. The timestamp refers to the time of event occurrence, while the activity describes the event. In this example, additional information like resource name and cost are given as well. Cases containing the same events identified by unique event IDs will have different

case IDs (Van Der Aalst & van der Aalst, 2016). Process discovery may try to produce a process model from the event log. The model may be a Petri net, a BPMN model or another process model. The challenge lies not in the recording of every trace present in the event log, rather in finding a generic representation of the most occurring traces. The process model must be generic enough to describe most traces, but specific enough to not get invalidated by future traces which may contain completely different events. Another major building block of this process model is accounting for trace concurrency. When several events may be identified to happen in parallel during the same time window, the model must recognize this. It can be spoken of a classical bias-variance trade-off lend from data science. The process must contain the most frequent traces but has to filter out traces which contain anomalies. Such anomalies like longer time per event due to a fire alarm have to be accounted for. Conformance checking may compare a given process model against a given event log. They are specialized in detecting aforementioned anomalies. A key insight in conformance checking lies in two possible deviations from reality: The given model does not capture the real behaviour (A) or reality differs from the model (B). In the first case, the model is not working as intended. In the second case, the event log is corrupt. The third view on event logs, process enhancement, enables the modeller to use the generated process model to identify bottlenecks. Anomalies identified serve as a good starting point because they reveal errors in the process sequence. The given table offers costs associated to each event ID. This information may be used to create an event benchmark to further optimize the desired "ideal" trace. The first goal of course is to ensure that no mistakes happen during a process.

More generally, PM empowers the modeller to perform VVUQ of an process model, event log or described trace. This concept is captured by the terms *Play-In*, *Play-Out* and *Replay* (Damm & Harel, 2001), see Figure 2.3.

Play-In refers to the creation of a process model out of an event log. Play-Out may be called "sampling" in data science as it generates traces out of the model. DES uses Play-Out to generate new exemplary behaviour, see section 2.1. Here, a process model may be used to play-out (simulate) several traces of the desired events and then use bagging techniques like averaging the durations per event to gain robust KPIs (subsection 2.1.4) and to reduce variance. A biased process model may still generate biased KPIs. Replay uses event log and process model together to check conformance, enriching the model with information captured in the log or to transform a descriptive process model into a prescriptive one (Van Der Aalst & van der Aalst, 2016).

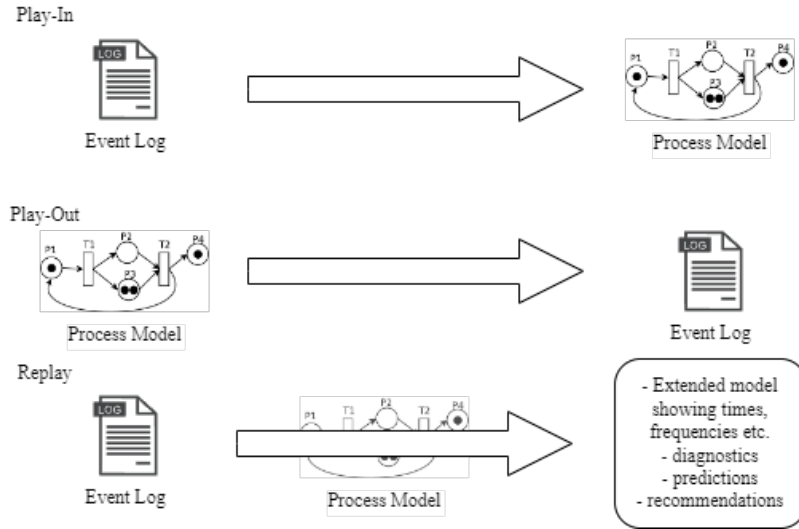


Figure 2.3: The Play-In, Play-Out and Replay concept in the context of process mining. The Play-In phase involves the creation of a process model from an event log. The Play-Out phase involves the creation of an event log from a process model. The Replay phase involves the modification of the process model thorough information gained from the event log.

PM uses different formats to display process models like petri nets and BPMN models, among others (W. van der Aalst, 2012). The thesis at hand focusses on DDDT in the context of simulation. Such data-driven models often come as a black box, thus they can not be rendered by PM models.

2.3.2 Object-Centricness in Process Mining

The problem with traditional PM lies in its single dimensionality of perspective. For each process analysis, a new play-out has to be performed. Interactions between different objects are not captured (W. M. van der Aalst, 2023). One event may be related to different cases (convergence) or from the perspective of a case, there may be several equal activities within a case (divergence) (W. M. van der Aalst, 2019). Recently, object-centric event data (OCED) have been proposed as a new data basis for PM (W. M. van der Aalst, 2019). OCED logs (OCEL) are a generalization of classical event logs. Such traditional event logs use the case ID as a label to group and distinguish events. They assume that the process model describes the start and end of a single object. Each event refers to exactly one object (case) (W. M. van der Aalst, 2023). OCED overthrows these assumptions by assuming that events may relate to multiple objects. To account for this new logic, OCEL coins the terms events, objects, types, attributes and qualifier. Each object has exactly one object type. Several objects may have the same type. An object type can be a description of the function such as machine, customer, supplier or activity descriptions such as invoice, request. Objects are

instances of these types. Events in particular have an event type, termed activity. The same non-uniqueness applies here—many events can have the same type like "processing complaint", "cooking coffee". Each event is described by exactly one type. OCED assumes event atomicity; each event is indivisible. Each event has one timestamp. Compared to traditional PM, events may relate to multiple objects through a qualifier (event to order2O). Such a qualifier may be, considering the event "printing label" and object "printing station", the label to be printed. Objects may be related to multiple objects (order to order2O). O2O relationships are frozen (static) and are assumed to not change. The O2O relationship may be used to describe the order of producing a product. For example, the O2O relation "main pcb to gyroscope" may say that the main pcb has to be produced before the gyroscope. Another O2O relation can be an order, the connection between the customer object and the ordered product. It is worth mentioning that objects can also be related indirectly together through two E2O relations: The E2O relation "producing" may connect the event "machine 1 produces" with the object "gyroscope". The E2O relation "check" may connect the event "machine 1 checks" with the object "main pcb", thus connecting the two objects "gyroscope" and "main pcb" indirectly via two events (W. M. van der Aalst, 2019). E2O relations are dynamic. They may change over time, involving different objects. In the given example, "main pcb" would be checked with "display" instead of "gyroscope".

Events and objects have attributes (keys), possessing values. Event attribute values refer to exactly one event and one event attribute, they are not shared. For example, the cost for one event may have the value 10€. The same logic applies to objects as well, one event attribute value refers to exactly one object and one object attribute. Because several events may have the same type and several objects may have the same type as well, each event- or object type may refer to any number of event or object attributes. They open interpretative possibilities for the modeller by considering them as expected attributes for the event or object type. The given example may be the event type "producing" which may have the event attribute "duration" and "cost". The object type "gyroscope" may have the object attribute "weight" and "size". One may average the different object attribute values of one type cluster to generate object type KPIs. A key specificity of object attribute values lies in the fact that they have a timestamp. Event attribute values do not. Latter information would be redundant because events to already have a timestamp, see above. Event attribute values may have cardinality one per event. N event attributes have n values. This does not apply to object attribute values. They may have multiple values because of their nature to

change over time (W. M. van der Aalst, 2023). This is why each object attribute value has a timestamp. The attribute value is in conclusion unique for a given object during a given time given one attribute. The given example may be the object attribute "weight" of the object "main pcb" which may change over time. The object attribute value "weight" may have the value 100g at time t_1 and 120g at time t_2 .

OCEL thus extends traditional PM by accommodating the multi-object nature of complex processes. Unlike classical event logs—which restrict events to a single case—OCEL captures dynamic interactions among multiple objects via E2O relations and static inter-object dependencies through O2O relations. This enriched framework enables a more comprehensive representation of real-world processes, where events may concurrently affect several objects. Timestamped object attribution values enable the modeller to perform temporal analysis and KPI derivation (subsection 2.1.4). Overall, OCED provides a more detailed, semantically rich representation of complex, interconnected processes. (W. M. van der Aalst, 2023).

2.3.3 Process Mining as Enabling Technology

PM uses event logs to develop process models or to enhance existing ones, so these logs may serve as a foundation for VVUQ of models in general. Live twin data often can be exported to the event log format. Several standardizations have been proposed, with the IEEE XES standard being the most widely used (Van Der Aalst & van der Aalst, 2016). The XES standard defines a common format for event logs, enabling the exchange of event data between different software frameworks. The idea lies in exporting twin decisions or live data as event logs and then use PM tools to perform VVUQ. Replay may be used on SBDT simulated traces in comparison with actual event data to reveal mismatches in sequences or timing. For example, the SBDT could have predicted a circular process. Replay can be applied to further analyse this bottleneck. Play-Out can empower the modeller to sample a big amount of exemplary traces to gain KPIs. OCED object attribute values may offer even more insights. PPC systems (subsection 2.1.3) often times deliver even more data to enrich the event log so that VVUQ can be performed easier. If event log extraction out of the SBDT is performed online, VVUQ can be performed on the fly. Both sources of information are incorporated in the framework, see section 3.2.

2.4 VVUQ in the Context of Simulation-Based Digital Twins

The previous sections introduced the concepts of DES, PPC, relevant KPIs, DT, PM and OCED. This section now focusses on VVUQ in the context of SBDT. The thesis at hand uses the term VVUQ to describe the process of verifying, validating and quantifying the uncertainty of a SBDT. Verification and validation has a long history in manufacturing and DES (Bitencourt et al., 2023). (Sel et al., 2025) add uncertainty quantification as a main interest. Their framework is applied in the medical domain, but they mention reasonable arguments regarding efficiency and safety of SBDT in general.¹ Thus, the thesis considers VVUQ instead of merely verification and validation efforts. The following section introduces the basic concepts of VVUQ and its relevance for SBDT.

2.4.1 Development process of VVUQ Concepts

With the uprising of simulation models in the early 1950s (Evans et al., 1967), the need for VVUQ arose unknowingly to the modellers. The usability of such simulations was deemed high as long as the results were promising, increasing trust in the technology (Durst et al., 2017). Blind trust does not validate models. Contrarily, if the results more or less were satisfactory, the model was considered validated (Bonani et al., 2003).

The first effort to define and perform verification was performed by (Machlup, 1955) defining verification as "including the correctness of mathematical and logical arguments, the applicability of formulas and equations (...), the reliability and exactness of observations, the reproducibility of experiments, the explanatory or predictive value of generalizations.". (Naylor & Finger, 1967) further refined this definitions by introducing the idea of "goodness of fit". Latter describes the capability of the model to correctly reflect the modelled system. During the 1970s, researchers like Schlesinger (Schlesinger, 1979) defined validation as achieving a "satisfactory range of accuracy consistent with the application", while Ignall argued for validation against simulations rather than analytical models (Ignall et al., 1978). Sargent's work from 1979 to 1984 proposed methods like user collaboration and independent verification and validation (VV), detailing techniques such as sensitivity analysis and Turing tests (Sargent, 2010). Balci developed a taxonomy and emphasized continuous VV, reflecting the need for ongoing assessment (Balci, 2012).

¹To go into detail, they deem erroneous data through sensor failure, model opacity (subsection 2.4.2) and the speed of model self-adaption as the necessities for UQ.

By 2004, modern VV emerged. Considering model fidelity of today's approaches, (Oberkampff et al., 2004) introduced widely recognized definitions of VV:

Verification is the process of determining that a model implementation accurately represents the developer's conceptual description of the model and the solution to the model.

Validation is the process of determining the degree to which a model is an accurate representation of the real world from the perspective of the intended uses of the model. (Oberkampff et al., 2004)

Verification thus concerns itself with the correctness of the given model (Sargent, 2010), while validation evaluates the quality of explanations quantitatively (Oberkampff et al., 2004). International Organization for Standardization span the concept of validation to computational models, where valid models correctly reflect the users intended functionality. PPC may provide the modeller with relevant KPIs to assess both.

Uncertainty quantification (UQ) is a relatively new field in VV. It aims to quantify the uncertainty of the model and its predictions through the whole lifecycle of the model, including training, inference and prediction (Sel et al., 2025). Uncertainty quantification empowers the modeller to define confidence intervals to correctly emphasize the stochastic nature of the model predictions (Volodina & Challenor, 2021). This is crucial for SBDT, where real-time decisions rely on accurate representations, as (Francis et al., 2021) highlights the need for continuous updates. UQ differentiates *aleatory* uncertainty, which is inherent to the data, and *epistemic* uncertainty, which is due to lack of knowledge (Sel et al., 2025). Aleatory uncertainty may arise due to sensor errors in the physical entity, generating noise. Epistemic uncertainty may arise due to lack of data or knowledge about the physical entity (Thelen et al., 2023). Epistemic uncertainty can be reduced. (Abdoune et al., 2022) provide a comprehensive overview of UQ challenges and potential solutions in the context of SBDT.

For SBDT, VVUQ is not a one-time activity but a continuous process (section 3.2), ensuring digital twins mirror physical systems accurately. This is vital for industries like manufacturing, where decisions based on digital twins have significant implications section 1.2. The historical development of VVUQ, from early verification to integrated UQ, reflects the growing complexity of simulation models. As SBDT become central to decision-making, robust VVUQ practices ensure reliability, linking back to foundational concepts introduced earlier, see subsection 2.2.1. The concepts of VVUQ are embedded in the context of

PM and OCED, which may further assist described endeavours. Especially for UQ, PM offers a rich data source to quantify uncertainty and validate models by providing a *degree of fit* of the given process model.

2.4.2 VVUQ for Automatically Generated Models

AMG stem largely stem from the DES discipline (??), termed automatic simulation model generation, ASMG (Charpentier & Véjar, 2014; Milde & Reinhart, 2019). They may use data-driven techniques which reduce the manual effort to create and update themselves. These models adapt quickly to changing conditions, making them valuable for dynamic environments like manufacturing. However, ensuring their reliability requires specific VVUQ. Because ASMG models often are black boxes, traditional VVUQ methods may not be applicable. The challenge lies in understanding the model's internal logic and ensuring it accurately reflects the physical system. If sophisticated data driven methods have been applied, several *key challenges* arise, hindering successful VVUQ:

- **Model Opacity:** ASMG models often use sophisticated machine learning algorithms like neural networks. Such black-box models are difficult to interpret, making it hard to understand their internal logic. This opacity may hinder VVUQ, as the modeller cannot easily identify errors or biases.
- **Data Dependency:** Data-driven models rely on high-quality data. If the data is biased or noisy, the model's predictions may be inaccurate.
- **Dynamic Model Adaptation:** Models that continuously learn and adapt, such as those employing online learning, require ongoing validation to ensure they remain valid as new data is ingested. This dynamic nature introduces the risk of concept drift (Lu et al., 2018), where the underlying process changes over time, potentially degrading model performance.
- **Quantifying Uncertainty:** Model predictions are stochastic in nature. For applications where precision is crucial, such as in manufacturing, uncertainty needs to be quantified.

To assess these challenges, the thesis defines the following *key requirements* for VVUQ of automatically generated models, especially SBDT:

- **Model Interpretability:** Ensuring the model's internal logic is transparent and understandable, enabling the modeller to identify errors or biases. Developing and employing techniques to make the decision-making processes of automatically generated models more transparent is crucial for

VVUQ. Explainable AI methods, such as SHAP (SHapley Additive exPlanations, (Lundberg & Lee, 2017)) or LIME (Local Interpretable Model-agnostic Explanations, (Ribeiro et al., 2016)), can help shedding light on model behaviour, facilitating verification efforts. This is particularly important for black-box models like deep neural networks, where understanding the reasoning behind predictions is challenging. Often times, it may be easier to use white-box models like decision trees or linear regression models, which are interpretable by design. Such models are often times labelled transparent models. If black-box models are instead chosen, so called *surrogate models* may be used to approximate the black-box model. The surrogate model is a white-box model, which is easier to interpret. This approach is called *post-hoc* explanation (Fischer et al., 2024).

- **Upholding Data Quality:** Implementing procedures to ensure that the data used for model generation and validation is accurate, complete, and representative of the operational environment is vital. This includes data cleaning, preprocessing, and plausibility checks to identify and mitigate issues like missing values, outliers, or biases. For instance, in manufacturing digital twins, sensor data must be validated for accuracy and consistency to ensure reliable model outputs (Rodríguez et al., 2023).
- **Validatable Algorithms:** Besides ensuring model interpretability, the algorithms used for model generation must be validatable. Security risks are a huge concern for companies employing SBDT into their processes (Alcaraz & Lopez, 2022). The algorithms used have to be secure, hardened against attacks. This is especially important for online learning algorithms, which may be vulnerable to adversarial attacks (Balta et al., 2023). Manipulated data may lead to incorrect model predictions, causing severe consequences in safety-critical applications like autonomous driving or medical diagnosis. Ensuring the robustness of the algorithms is crucial for reliable VVUQ.
- **Continuous Validation:** VVUQ processes have to work in real-time to ensure the model remains valid as new data is ingested. This requires continuous monitoring and validation of the model's predictions against real-world data. Techniques like online validation (Francis et al., 2021) can help ensure the model's accuracy and reliability over time. This is particularly important for SBDT, which are designed to adapt to changing conditions and provide real-time insights. Continuous validation ensures the model remains reliable and trustworthy, even as the underlying process

evolves.

- **Integration:** VVUQ processes have to be integrated into existing model- and PPC infrastructure to be able to perform VVUQ on the fly. This requires close collaboration between data scientists, domain experts, and IT specialists to ensure the seamless integration of VVUQ processes into the model lifecycle.
- **Scalability:** VVUQ processes have to be scalable as the underlying model or data evolves over time. This requires the development of scalable VVUQ techniques that can handle large volumes of data and complex models. Of course, the infrastructure must be able to handle the increased computational load.

As noted by Francis et al., the lifecycle SBDT has implications for its VVUQ as well: VVUQ must accompany the SBDT in all phases, from conceptualization to deployment and operation. The key requirements outlined above provide a foundation for developing robust VVUQ processes for automatically generated models, ensuring their reliability and accuracy in real-world applications.

2.4.3 Traditional versus Machine Learning-Based Approaches

VVUQ can be performed using traditional methods or more sophisticated approaches. Traditional verification techniques may include code inspection, unit testing or debugging (Maniaci, 2018). If closed solutions to simulated models are available, they may be used to validate the simulation. Traditional validation techniques involve comparisons between model predictions and real-world data, such as statistical tests or sensitivity analysis. In the context of manufacturing, simple experiments or historical data can be used. The consultation of experts is another possibility (Shao et al., 2023).

Machine Learning-Based VVUQ

Sophisticated approaches may include the use of machine learning (ML) techniques to enhance VVUQ processes. ML can be used to identify patterns in data, detect anomalies, and improve model predictions. In addition to supervised and unsupervised learning shortly introduced in subsection 2.2.2, semi-supervised learning and reinforcement learning are two other approaches. Supervised learning may be employed where labels regarding the validity or non-validity of an OCEL (see subsection 2.3.2) are given. Unsupervised learning may provide such labels as learned categories if they are missing or may assist with finding common patterns in the data. Unsupervised techniques are context-agnostic and

assume no patterns in the data, see Hastie et al. for the reverse problem of encoding a priori information in unsupervised algorithms. Semi-supervised learning combines labelled and unlabelled data to improve model performance. It somehow forms a middle ground where lots of unlabelled data is available and is then grouped by the algorithm. The scarce data is then used in the holdout set to perform testing (Learning, 2006). Reinforcement learning is not commonly applied in VVUQ of SBDT. ML techniques are often referred to as "oracles" when used for VVUQ because of their key challenge of opacity subsection 2.4.2.

Challenges in Data Preparation and Feature Selection

Before discussing the application of ML techniques in VVUQ, several problems hindering successful application of ML in VVUQ are identified. The first problem is data quality (X. Wu et al., 2025). Data quality may degrade the performance and reliability of ML-based VVUQ approaches. Firstly, *missing values* in the dataset can hinder the training process and potentially introduce biases. To account for this, imputation strategies or simply removing defect rows may be a solution (Gudivada et al., 2017). The modeller has to keep in mind that this may corrupt the VVUQ process. Secondly *outliers*, which are data points that deviate significantly from the rest, create a challenge as they might represent real trends in the data (and thus containing valuable edge cases for VVUQ) or simply be erroneous entries, requiring care of the modeller. Thirdly *noise* can superimpose the underlying patterns that ML algorithms aim to learn, reducing the accuracy and generalization ability of the VVUQ models (Liu et al., 2020). Such noise may be random, for example by measuring environmental influence, or systematic, for example emitted by erroneous sensors. The first kind of noise can be reduced by smoothing or filtering.

Inconsistent data is another mistake to avoid in data gathering. It may arise from deviations in formats, units or representations of the same information. It can lead to confusion for ML algorithms and require standardization and cleaning (Mahanthappa & Chandavarkar, 2021). Duplicate data entries may also generate false trends in the data. Imbalance introduced by duplicates or measurement errors can bias the model in predicting only the majority class when a classification problem is at hand. Beyond data quality, the modeller has to make sure that the data is representative and bias-free. The training data used for VVUQ models must accurately reflect the operational environment. Biases can arise through human intervention or environmental influence (Liu et al., 2020). Finally, the way data is split into training, testing, and validation sets is important for avoiding overfitting. Here, the model memorizes the training data and fails

to generalize to unseen data.

After ensuring data quality, the modeller has to consider suitable features for the given problem. Features are columns in the dataset describing characteristics of the data points (rows) through values. OCEL provide a relatively strict feature set in which the modeller has to operate. This has the advantage that several of the upper challenges may be eliminated because the data can be exported through a standardized interface. Successful VVUQ methods may require additional features nonetheless. Only the most relevant features may be selected (Géron, 2022). Feature engineering describes the endeavour of creating new features through combining existing features or through a new data gathering process. The incorporation of features in model training is coined feature selection. In the given use case, an adaptive feature a feature selection based on twin components may be useful, see subsection 2.1.2.

Classification Methods for the Detection of Model Deviations

Extensive work has been done on the topic of ML-based deviation detection. Such deviations are called "anomalies" and the process is termed "anomaly detection" (Kharitonov et al., 2022). Anomalies are data points that deviate significantly from the majority of the data. They can be classified into three categories: point anomalies, contextual anomalies and collective anomalies (Chandola et al., 2009). Point anomalies are single data points that differ significantly from the rest of the dataset. Contextual anomalies are data points that are normal in one context but anomalous in another. They appear less often than point anomalies and have less statistical weight. Collective anomalies are groups of data points that are anomalous when considered together but may not be anomalous individually. Anomalies are of special interest in the context of VVUQ, as they can indicate potential issues with the model or the data, see subsection 2.1.4.

Anomaly detection and VVUQ share common goals of identifying deviations from expected behaviour and ensuring the reliability of models. The two fields can benefit from each other, as VVUQ can provide a framework for evaluating the performance of anomaly detection algorithms, while anomaly detection techniques can enhance VVUQ processes by identifying potential issues in models or data. Several algorithms exist to detect anomalies, including statistical methods, clustering-based methods, and supervised learning methods. If the data is sufficiently labelled and preprocessed, supervised methods are promising. Algorithms such as Support Vector Machines (SVM), Neural Networks (NN), Decision Trees, and Random Forests can learn from this labelled data to classify new

model outputs or behaviours as either normal or divergent. However, a common challenge in anomaly detection scenarios is the issue of class imbalance, where instances of normal behaviour are more common than the occurrences of deviations. This imbalance needs to be carefully addressed during model training to prevent the classifier from being biased towards the majority class. Clustering-based unsupervised methods detect anomalies through grouping similar data points together. Algorithms like K-Means, DBSCAN, and Hierarchical Clustering can be used to identify clusters of normal behaviour, with anomalies being those points that do not belong to any cluster. They measure the distance between data points to cull anomalous points as reaching far outside of a group of common data points. Often times the assigned groups can be plotted, yielding further insights in the nature of the detected anomalies. Statistical methods, on the other hand, rely on the assumption that the data follows a certain distribution. They identify anomalies based on statistical properties such as mean, variance, and standard deviation (Chandola et al., 2009).

Metrics for Model Quality Assessment

Another important aspects of assessing model quality is through metrics. The following section introduces the most common metrics used in VVUQ of SBDT. The introduction is supported by an exemplary OCEL:

Table 2.2: A fragment of a manufacturing OCEL with type annotations. Each row represents an event with associated process execution details. The columns are annotated as follows: `process_execution_id` (int), `order_id` (int), `start_time` (datetime), `end_time` (datetime), `part_id` (int), `process_type` (int), `process_id` (int), `resource_id` (int), and `is_valid` (bool).

<code>process_execution_id</code>	<code>order_id</code>	<code>start_time</code>	<code>end_time</code>	<code>part_id</code>	<code>process_type</code>	<code>process_id</code>	<code>resource_id</code>	<code>is_valid</code>
0	2529	2020-04-22 14:21:07	2020-04-22 14:21:31	-1	0	0	0	True
1	2529	2020-04-22 14:23:35	2020-04-22 14:23:58	-1	1	1	1	True
2	2529	2020-04-22 14:21:09	2020-04-22 14:21:33	-1	0	0	0	True
3	2529	2020-04-22 14:23:36	2020-04-22 14:23:58	-1	1	1	1	True
4	2529	2020-04-22 14:21:11	2020-04-22 14:21:35	-1	0	0	0	True
5	2529	2020-04-22 14:23:36	2020-04-22 14:23:58	-1	1	1	1	True
6	2529	2020-04-22 14:21:13	2020-04-22 14:21:37	-1	0	0	0	True
7	2529	2020-04-22 14:23:36	2020-04-22 14:23:58	-1	1	1	1	True
8	2529	2020-04-22 14:21:15	2020-04-22 14:21:39	-1	0	0	0	True
9	2529	2020-04-22 14:23:37	2020-04-22 14:23:58	-1	1	1	1	True
10	2529	2020-04-22 14:21:18	2020-04-22 14:21:41	-1	0	0	0	True
11	2529	2020-04-22 14:23:37	2020-04-22 14:23:57	-1	1	1	1	False
12	2529	2020-04-22 14:21:20	2020-04-22 14:21:44	-1	0	0	0	False
13	2529	2020-04-22 14:23:37	2020-04-22 14:23:57	-1	1	1	1	False
14	2529	2020-04-22 14:21:22	2020-04-22 14:21:46	-1	0	0	0	False
15	2529	2020-04-22 14:23:38	2020-04-22 14:23:57	-1	1	1	1	False

Accuracy

Accuracy quantifies the overall correctness of the classification model. It represents the ratio of correctly classified instances to the total number of instances in the dataset (Fahrmeir et al., 2016).

$$\text{Accuracy} = \frac{\text{Number of Correct Predictions}}{\text{Total Number of Predictions}} = \frac{TP + TN}{TP + TN + FP + FN} \quad (2.1)$$

where TP denotes the count of true positives, TN represents true negatives, FP shows false positives, and FN indicates false negatives.

This metric offers a high-level overview of the model's performance by indicating the proportion of predictions that align with the actual classes. Accuracy can be a misleading metric when dealing with imbalanced datasets (Fahrmeir et al., 2016). In manufacturing, where the occurrence of invalid processes might be significantly lower than valid ones, a high accuracy score could be achieved by a model that predominantly predicts the majority class, failing to effectively identify the critical minority class of invalid processes. Therefore, relying only on accuracy might not provide a complete or accurate assessment of the model's utility in identifying process anomalies.

Precision

Precision, also known as the positive predictive value, focuses on the quality of the positive predictions made by the model. It measures the proportion of instances that the model predicted as positive which were indeed positive.

$$\text{Precision} = \frac{TP}{TP + FP} \quad (2.2)$$

A high precision score shows that when the model predicts a manufacturing process as 'valid' (assuming 'valid' is the positive class), it is highly likely to be genuinely valid. This is particularly important in manufacturing quality control to minimize the occurrence of false alarms, which can lead to unnecessary interruptions in the production line and increased operational costs (Kharitonov et al., 2022). A model with high precision ensures that interventions based on its predictions are more likely to be warranted, thereby enhancing the efficiency of the quality assurance process.

Sensitivity

Recall, also referred to as sensitivity or the true positive rate (TPR), assesses the model's ability to identify all the actual positive instances within the dataset. It measures the proportion of actual positive instances that were correctly classified as positive by the model (Fahrmeir et al., 2016).

$$\text{Recall} = \frac{TP}{TP + FN} \quad (2.3)$$

In the context of manufacturing, a high recall for the 'valid' class is crucial for ensuring that the model effectively detects the majority of the truly valid processes. Failing to identify an valid process (a false negative) can have significant consequences, potentially leading to the production of defective goods that may incur costs related to rework, scrap, or customer dissatisfaction (Kharitonov et al., 2022). Therefore, a model with high recall minimizes the risk of overlooking critical quality issues in the manufacturing process.

F1-Score

The F1-score provides a balanced measure of the classification model's performance by calculating the harmonic mean of precision and recall. This metric is particularly useful when dealing with datasets that contain an imbalance in the class distribution.

$$\text{F1-score} = 2 \times \frac{\text{Precision} \times \text{Recall}}{\text{Precision} + \text{Recall}} = \frac{2TP}{2TP + FP + FN} \quad (2.4)$$

By considering both the precision (the accuracy of positive predictions) and the recall (the ability to find all positive instances), the F1-score offers a single metric that summarizes the trade-off between these two important aspects of a classifier's performance. In manufacturing's quality prediction, where achieving a balance between accurately identifying invalid processes and minimizing false alarms is often a key objective, the F1-score serves as a valuable tool for assessing the overall effectiveness of the model. It is especially beneficial when the costs associated with false positives and false negatives are relatively similar, or when a general measure of good performance across both precision and recall is desired.

Confusion Matrix

A confusion matrix is a specific type of contingency table that provides a detailed breakdown of the performance of a classification model by displaying the counts of true positives, true negatives, false positives, and false negatives. For a binary classification problem, such as predicting whether a manufacturing process is valid or not, the confusion matrix typically takes the form of a 2x2 table (Fahrmeir et al., 2016).

Table 2.3: Confusion Matrix for Binary Classification

Actual Class	Predicted Class	
	Positive (True)	Negative (False)
Positive (True)	True Positive (TP)	False Negative (FN)
Negative (False)	False Positive (FP)	True Negative (TN)

This matrix offers a granular view of the model's predictive behaviour, allowing for a thorough analysis of the different types of errors it makes. True positives represent the cases where the model correctly predicted a positive outcome (e.g., a valid process was correctly identified). True negatives indicate instances where the model correctly predicted a negative outcome (e.g., an invalid process was correctly identified). False positives occur when the model incorrectly predicts a positive outcome for a negative instance (e.g., an invalid process was wrongly flagged as valid). Conversely, false negatives arise when the model incorrectly predicts a negative outcome for a positive instance (e.g., a valid process was missed and classified as invalid). Analysing the confusion matrix for the 'is_valid' prediction in the context of manufacturing can reveal crucial information about the model's tendencies, such as whether it is more prone to generating false alarms or to missing actual defects, which has direct implications for the design and implementation of quality control strategies.

While the primary focus based on the example data is on classification, the model might also be employed for regression tasks in manufacturing, such as predicting continuous variables like throughput times or resource utilization levels. In such scenarios, the following regression metrics are crucial for evaluating the model's predictive accuracy.

Mean Squared Error (MSE)

Mean Squared Error (MSE) quantifies the average of the squared differences between the values predicted by the model and the actual observed values.

$$\text{MSE} = \frac{1}{n} \sum_{i=1}^n (y_i - \hat{y}_i)^2 \quad (2.5)$$

where y_i represents the actual value of the target variable for the i -th instance, \hat{y}_i is the corresponding predicted value, and n is the total number of data points in the dataset.

MSE is a widely used metric that provides a measure of the overall prediction

error. The squaring of the differences means that larger errors contribute more significantly to the final MSE value, making it particularly sensitive to outliers in the predictions. In the context of manufacturing, if the model were predicting throughput time, a high MSE would indicate that, on average, the squared difference between the predicted and actual throughput times is large, suggesting a lower accuracy in the model's predictions (Fahrmeir et al., 2016).

Mean Absolute Error (MAE)

Mean Absolute Error (MAE) measures the average of the absolute differences between the predicted and actual values.

$$\text{MAE} = \frac{1}{n} \sum_{i=1}^n |y_i - \hat{y}_i| \quad (2.6)$$

MAE offers a more direct and interpretable measure of the average magnitude of the errors in the model's predictions. Unlike MSE, MAE treats all errors equally, without giving disproportionate weight to larger errors (Fahrmeir et al., 2016). In manufacturing applications, such as predicting resource utilization, MAE would represent the average absolute percentage point difference between the model's predictions and the actual utilization rates, providing a clear indication of the typical size of the prediction errors.

Mean Absolute Percentage Error (MAPE)

Mean Absolute Percentage Error (MAPE) calculates the average percentage error between the predicted and actual values.

$$\text{MAPE} = \frac{1}{n} \sum_{i=1}^n \left| \frac{y_i - \hat{y}_i}{y_i} \right| \times 100\% \quad (2.7)$$

MAPE is particularly useful when the scale of the target variable varies, as it provides an error measure in relative terms. The percentage error is often easier to understand and communicate than absolute errors, especially in a business or operational context. For example, if the network were predicting the percentage of defective parts produced, MAPE would indicate the average percentage by which the model's predictions deviate from the actual defect rates, offering a valuable perspective on the model's performance in predicting proportional outcomes.

Performance Evaluation using ROC Curves and AUC

For binary classification tasks, such as the prediction of 'is_valid' status in manufacturing processes, Receiver Operating Characteristic (ROC) curves and the Area Under the Curve (AUC) provide a evaluation of the model's performance.

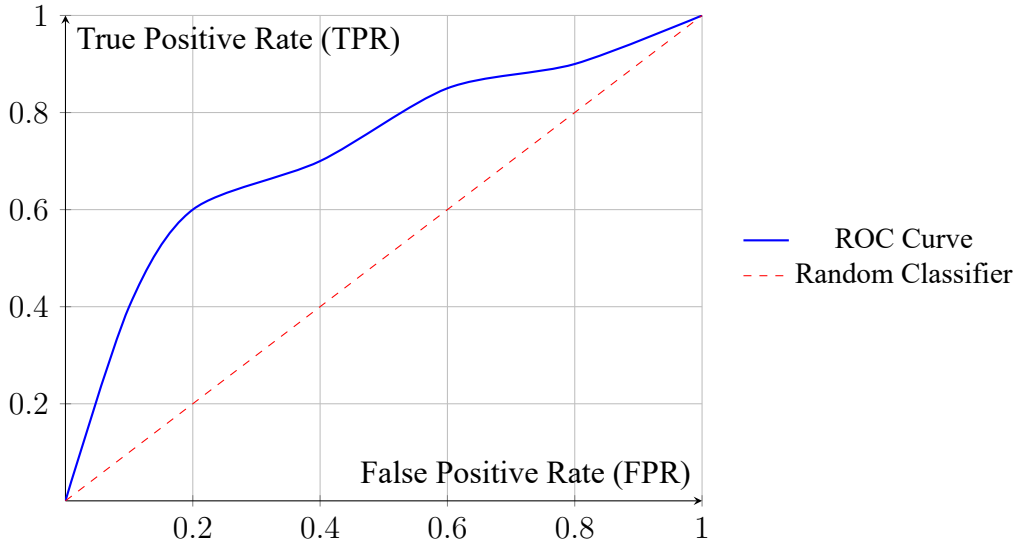


Figure 2.4: Example ROC Curve

$$\text{AUC} = \int_0^1 \text{TPR}(\text{FPR}) d\text{FPR} \quad (2.8)$$

An ROC curve is a graphical representation that plots the true positive rate (TPR or recall) against the false positive rate (FPR) at various classification thresholds. By examining the curve, one can visualize the trade-off between the model's sensitivity (its ability to correctly identify positive instances) and its specificity (its ability to correctly identify negative instances) across different decision points. The value of AUC ranges from 0 to 1. An AUC of 1 indicates a perfect classifier, while an AUC of 0.5 suggests a performance no better than random guessing. In the context of predicting 'is_valid' in manufacturing, a higher AUC for the network would signify that the model is better at distinguishing between valid and invalid processes, regardless of the chosen classification threshold. This is particularly valuable when the class distribution is imbalanced, as ROC and AUC provide a more robust evaluation compared to metrics like accuracy that can be skewed by the majority class.

Now that the basic concepts of VVUQ and the metrics used to assess model quality have been introduced, the next section will delve into the specific models employed in this work. The focus will be on the ResNet Bi-LSTM Multi-Head

attention network, which is designed to automatically generate VBVVQ models for SBDT. This model leverages the strengths of LSTM networks and attention mechanisms to effectively handle sequential data and improve prediction accuracy.

Bidirectional LSTM Networks for Sequence-Based Anomaly Detection

The Foundation: Recurrent Neural Networks (RNNs)

The following section describes the model types on which the automatic VBVVQ is based. The model types are introduced in a bottom-up fashion, starting with the most basic model type and building up to the more complex models. The first model type is the Recurrent Neural Network (RNN), which is the basis for the Long Short-Term Memory (LSTM) networks. The LSTM networks are then used in a bidirectional fashion, which is the basis for the ResNet Bi-LSTM Multi-Head attention network. Because the OCEL data is sequential in nature, the RNNs are used to model the sequential data. The LSTM networks are used to overcome the limitations of the RNNs, and the bidirectional LSTM networks are used to improve the performance of the LSTM networks. The ResNet Bi-LSTM Multi-Head attention network is then introduced as a more advanced model that combines the strengths of both LSTM and attention mechanisms.²

Recurrent Neural Network (RNN) were the first novel networks to handle sequential data. Unlike feedforward neural networks that process each input independently, RNNs are specifically designed to handle sequences by maintaining an internal memory, known as the hidden state, which summarizes past information (Géron, 2022). As sequential data $\{x_1, x_2, \dots, x_T\}$ is fed into the network step by step (indexed by t), the RNN processes each element x_t while simultaneously updating its hidden state h_t . This hidden state acts as the network's memory, retaining information from previous time steps. It can be thought of as the long-term memory of the network.

The core computation within an RNN at time step t involves calculating the new hidden state h_t based on the current input x_t and the previous hidden state h_{t-1} .

²Throughout this section, specific mathematical notation conventions are used. Vectors, such as inputs, hidden states, cell states, outputs, and biases, are written by bold lowercase letters (e.g., x, h, c, y, b). Matrices, primarily representing weights, are represented by uppercase letters (e.g., W, U). The symbol σ denotes a generic non-linear activation function, while σ_h and σ_y specifically refer to activation functions in the hidden and output layers. Commonly used specific activation functions like hyperbolic tangent and softmax are written as \tanh and softmax . Element-wise multiplication is indicated by the symbol \odot .

This relationship is typically defined as:

$$\mathbf{h}_t = \sigma_h(W_{xh}\mathbf{x}_t + W_{hh}\mathbf{h}_{t-1} + \mathbf{b}_h) \quad (2.9)$$

where W_{xh} is the weight matrix connecting the input to the hidden layer, W_{hh}



Figure 2.5: Unfolded architecture of a Recurrent Neural Network (RNN) over time, illustrating the computation of the hidden state \mathbf{h}_t according to Equation 2.9.

is the weight matrix for the recurrent connection from the previous hidden state to the current hidden state, \mathbf{b}_h is the bias vector for the hidden layer, and σ_h is a non-linear activation function, commonly the hyperbolic tangent (tanh) or ReLU. The initial hidden state \mathbf{h}_0 is typically initialized to zeros or learned.

The output \mathbf{y}_t at time step t can then be computed from the hidden state:

$$\mathbf{y}_t = \sigma_y(W_{hy}\mathbf{h}_t + \mathbf{b}_y) \quad (2.10)$$

Here, W_{hy} is the weight matrix from the hidden layer to the output layer, \mathbf{b}_y is the output bias vector, and σ_y is an activation function appropriate for the task, for example softmax for classification tasks.

A crucial characteristic of RNNs is parameter sharing: the weight matrices (W_{xh} , W_{hh} , W_{hy}) and biases (\mathbf{b}_h , \mathbf{b}_y) are the same across all time steps $t = 1, \dots, T$. This allows the model to generalize learned patterns regardless of their position in the sequence and significantly reduces the number of parameters to learn. Conceptually, this process is often understood by thinking of the network as being "unfolded" over time, creating a deep feedforward-like structure where each layer corresponds to a time step but utilizes shared weights (Medsker, Jain, et al., 2001).

Depending on the task, RNNs can be structured differently, such as many-to-one (sequence input, single output—sentiment analysis), one-to-many (single input, sequence output—image captioning), or many-to-many (sequence input, sequence output—machine translation).

In contrast their conceptual elegance, standard RNNs face challenges when learning dependencies over long sequences. During training using Backpropagation Through Time (BPTT), gradients are propagated backward through the unfolded network representation. The repeated multiplication involving the recurrent weight matrix W_{hh} (specifically, its Jacobian matrix containing the first derivatives) can cause gradients to either shrink exponentially towards zero (vanishing gradients) or grow uncontrollably (exploding gradients) (Hochreiter, 1998). Vanishing gradients hinder the model's ability to capture long-range dependencies, as updates to weights connecting distant past inputs become negligible. Exploding gradients can lead to numerical instability during training (Philipp et al., 2017).

Long Short-Term Memory Networks (LSTMs)

To address the vanishing gradient problem and effectively learn long-range dependencies, Long Short-Term Memory Networks (LSTMs) were introduced (Hochreiter & Schmidhuber, 1997). LSTMs employ a more sophisticated internal structure within each recurrent unit, often called an LSTM cell.

The key innovation of the LSTM cell is the introduction of a *cell state*, c_t , which acts as an information conduit, allowing information to flow through time with potentially minimal modification. The long-term preservation is a key distinction from the RNN, where the hidden state gets overwritten. The flow of information into, out of, and within the cell state is regulated by three specialized gating mechanisms: the forget gate, the input gate, and the output gate. These gates use sigmoid activation functions (σ), which output values between 0 and 1, representing the proportion of information allowed to pass.



Figure 2.6: Visual representation of the LSTM cell computations detailed in Equations 2.11-2.16. The diagram shows how inputs (x_t) and (h_{t-1}) interact with the forget gate (f_t), input gate (i_t), candidate state (\tilde{c}_t), and

Source: Own illustration based on (Géron, 2022).

At each time step t , given the input \mathbf{x}_t , the previous hidden state \mathbf{h}_{t-1} , and the previous cell state \mathbf{c}_{t-1} , the LSTM cell performs the following computations:

1. **Forget Gate (\mathbf{f}_t):** Decides which information to discard from the previous cell state \mathbf{c}_{t-1} .

$$\mathbf{f}_t = \sigma(W_f \mathbf{x}_t + U_f \mathbf{h}_{t-1} + \mathbf{b}_f) \quad (2.11)$$

2. **Input Gate (\mathbf{i}_t):** Determines which new information from the input and previous hidden state should be stored in the cell state. This involves two parts:

- The input gate layer decides which values to update:

$$\mathbf{i}_t = \sigma(W_i \mathbf{x}_t + U_i \mathbf{h}_{t-1} + \mathbf{b}_i) \quad (2.12)$$

- A candidate cell state $\tilde{\mathbf{c}}_t$ is created with potential new values, typically using a tanh activation:

$$\tilde{\mathbf{c}}_t = \tanh(W_c \mathbf{x}_t + U_c \mathbf{h}_{t-1} + \mathbf{b}_c) \quad (2.13)$$

3. **Cell State Update (\mathbf{c}_t):** The old cell state \mathbf{c}_{t-1} is updated to the new cell state \mathbf{c}_t . This involves element-wise multiplication (\odot) to forget parts of the old state (via \mathbf{f}_t) and add parts of the new candidate state (via \mathbf{i}_t).

$$\mathbf{c}_t = \mathbf{f}_t \odot \mathbf{c}_{t-1} + \mathbf{i}_t \odot \tilde{\mathbf{c}}_t \quad (2.14)$$

4. **Output Gate (\mathbf{o}_t):** Determines what part of the (filtered) cell state \mathbf{c}_t should be outputted as the new hidden state \mathbf{h}_t .

$$\mathbf{o}_t = \sigma(W_o \mathbf{x}_t + U_o \mathbf{h}_{t-1} + \mathbf{b}_o) \quad (2.15)$$

$$\mathbf{h}_t = \mathbf{o}_t \odot \tanh(\mathbf{c}_t) \quad (2.16)$$

In these equations, W_* , U_* represent the respective weight matrices for connections from the input and the previous hidden state, and \mathbf{b}_* are the bias vectors.

The gating mechanisms allow LSTMs to selectively remember or forget information over long durations. The cell state's update mechanism, involving addition and element-wise multiplication controlled by gates often close to 1 (especially the forget gate), facilitates a more stable gradient flow compared to the repeated

matrix multiplications in simple RNNs. This characteristic, sometimes associated with the Constant Error Carousel (CEC) concept (Hochreiter & Schmidhuber, 1997), effectively mitigates the vanishing gradient problem. LSTMs have become a standard tool for various sequence modelling tasks, including time series prediction and machine sequences (Al-Selwi et al., 2024).

Bidirectional LSTMs (Bi-LSTMs)

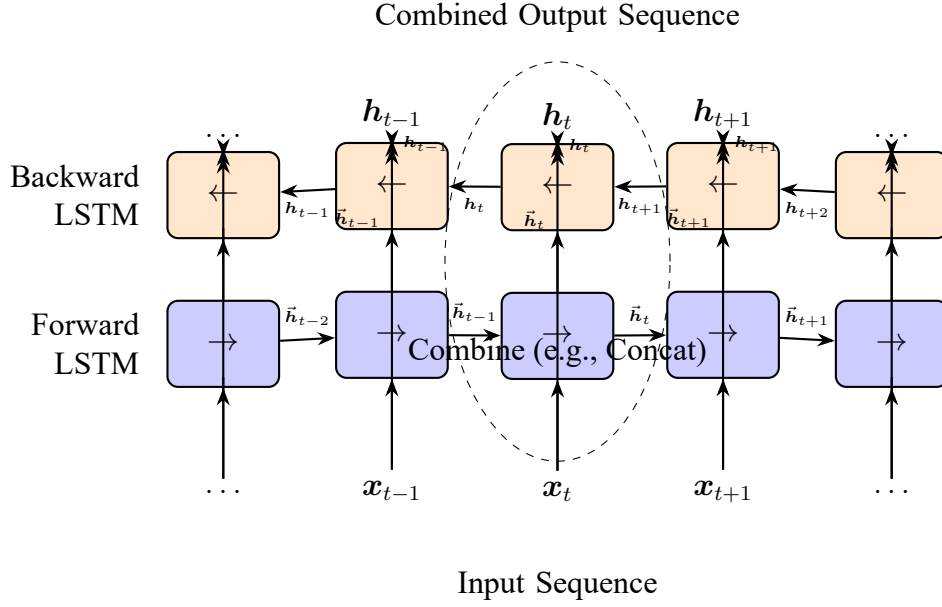


Figure 2.7: Architecture of a Bidirectional LSTM (Bi-LSTM), processing the input sequence (x_t) both forwards (generating \vec{h}_t) and backwards (generating \vec{h}_t). The final hidden states \vec{h}_t are produced by combining information from both directions (e.g., via concatenation according to Equation 2.17).

While standard LSTMs process sequences chronologically, capturing dependencies on past inputs, many tasks benefit from considering context from both past and future elements. For example, understanding why a specific machine task is performed requires knowledge about the task performed afterwards. Bidirectional LSTMs (Bi-LSTMs) address this by processing the input sequence in both forward and backward directions (Schuster & Paliwal, 1997).

A Bi-LSTM consists of two separate LSTM layers:

1. A **forward LSTM** processes the input sequence $\{x_1, \dots, x_T\}$ from $t = 1$ to T , producing a sequence of forward hidden states $\{\vec{h}_1, \dots, \vec{h}_T\}$. The computation for \vec{h}_t follows the standard LSTM equations (2.11) through (2.16).
2. A **backward LSTM** processes the input sequence in reverse order, from $t = T$ down to 1, producing a sequence of backward hidden states $\{h_1, \dots, h_T\}$.

The computation for \mathbf{h}_t uses a separate set of LSTM parameters and processes the sequence $\{\mathbf{x}_T, \dots, \mathbf{x}_1\}$.

At each time step t , the final hidden state representation \mathbf{h}_t combines the information from both directions. A common method is concatenation:

$$\mathbf{h}_t = [\vec{\mathbf{h}}_t; \mathbf{h}_t] \quad (2.17)$$

where $[\cdot]$ denotes vector concatenation. Other combination methods like summation or averaging are also possible. This combined state \mathbf{h}_t contains information about the input \mathbf{x}_t informed by both its preceding and succeeding context within the sequence.

Bi-LSTMs have proven highly effective in tasks requiring contextual understanding, such as Named Entity Recognition or sentiment analysis (Al-Selwi et al., 2024). However, they are computationally more expensive than unidirectional LSTMs due to the doubled network structure.

Residual Networks (ResNets)

As neural networks became deeper to model more complex functions, researchers encountered the *degradation problem*: simply stacking more layers could lead to higher training error, even though a deeper network should theoretically be able to represent the functions learned by a shallower one (K. He et al., 2016). This issue, distinct from overfitting, indicated difficulties in optimizing very deep networks.

Residual Networks (ResNets) were introduced to overcome this challenge. The core idea is to reframe the learning process by having layers learn a *residual function* with respect to their input, rather than learning the desired underlying mapping directly. This is achieved using *residual blocks* containing skip connections (or shortcut connections).

Consider a block of layers aiming to learn a mapping $\mathcal{H}(\mathbf{x})$. A residual block instead learns a residual function $\mathcal{F}(\mathbf{x}) = \mathcal{H}(\mathbf{x}) - \mathbf{x}$. The output \mathbf{y} of the residual block is then computed as:

$$\mathbf{y} = \mathcal{F}(\mathbf{x}, \{W_i\}) + \mathbf{x} \quad (2.18)$$

Here, \mathbf{x} is the input to the block, $\mathcal{F}(\mathbf{x}, \{W_i\})$ represents the function learned by the stacked layers within the block (parameterized by weights $\{W_i\}$), and the $+\mathbf{x}$ term is the identity skip connection. This formulation makes it easier for the

network to learn an identity mapping (if optimal) by simply driving the weights in \mathcal{F} towards zero.

These skip connections provide alternative pathways for gradient propagation during backpropagation. Gradients can flow directly through the identity connections, bypassing the layers in \mathcal{F} . This significantly alleviates the vanishing gradient problem in very deep networks, allowing for the successful training of models with hundreds or even thousands of layers (K. He et al., 2016).

While originally developed for computer vision, the principle of residual connections can be applied to other architectures, including sequential models. Incorporating ResNet-like connections within or around (Bi-)LSTM layers can potentially stabilize training and allow for deeper sequential architectures, enabling the capture of more intricate temporal patterns without suffering from degradation.

Multi-head Attention Mechanism

In sequence modelling, particularly with long sequences, not all parts of the input are equally relevant for making a prediction at a given time step. Attention mechanisms allow a model to dynamically focus on the most pertinent parts of the input sequence (Chorowski et al., 2014). A significant advancement is *self-attention*, where the mechanism relates different positions of a single sequence to compute its representation (Vaswani et al., 2017).

Self-attention operates on a set of input vectors, typically representing tokens or time steps in a sequence. For each input vector, three representations are derived through learned linear transformations: a query (q), a key (k), and a value (v). The attention mechanism computes the output as a weighted sum of the values, where the weight assigned to each value is determined by the compatibility (often measured by dot product) between its corresponding key and the query.

The most common form is *Scaled Dot-Product Attention*, calculated for a set of queries Q , keys K , and values V (where Q, K, V are typically matrices stacking the q, k, v vectors):

$$\text{Attention}(Q, K, V) = \text{softmax} \left(\frac{QK^T}{\sqrt{d_k}} \right) V \quad (2.19)$$

Here, QK^T computes the dot products between all query-key pairs. The result is scaled by $\sqrt{d_k}$, where d_k is the dimension of the keys, to prevent the dot products from becoming too large and pushing the softmax function into regions with

very small gradients. The softmax function normalizes these scores into attention weights, which sum to 1. Finally, these weights are multiplied by the Value matrix V to produce the output, effectively highlighting the values corresponding to the most relevant keys for each query.

Multi-Head Attention enhances this mechanism by performing the attention calculation multiple times in parallel, each with different, learned linear projections of the original Q, K, V . This allows the model to jointly attend to information from different representation subspaces at different positions (Vaswani et al., 2017).

Let the number of heads be h . For each head $i \in \{1, \dots, h\}$, the input Q, K, V are projected using learned weight matrices W_i^Q, W_i^K, W_i^V :

$$\text{head}_i = \text{Attention}(QW_i^Q, KW_i^K, VW_i^V) \quad (2.20)$$

The outputs of all heads are then concatenated and projected one final time using another learned weight matrix W^O :

$$\text{MultiHead}(Q, K, V) = \text{Concat}(\text{head}_1, \dots, \text{head}_h)W^O \quad (2.21)$$

This multi-head structure allows each head to potentially focus on different types of relationships (e.g., short-range vs. long-range dependencies, different syntactic or semantic features), leading to a richer representation. Multi-head attention is a cornerstone of the transformer architecture (Vaswani et al., 2017) and is increasingly combined with other models like LSTMs.

The Integrated Architecture for Anomaly Detection

The theoretical components described above – (Bi-)LSTMs, residual connections, and multi-head attention – can be integrated. For the challenge of anomaly detection in sequential manufacturing process data within the context of Simulation-Based Digital Twins (SBDT), an architecture combining these elements offers significant advantages.

The proposed model utilizes Bi-LSTM layers as the core sequence processing units to capture the temporal dynamics inherent in manufacturing operations, leveraging their ability to model long-range dependencies as described in Section Equation 2.4.3 and Equation 2.4.3. To potentially enable deeper Bi-LSTM stacks and stabilize training, residual connections, inspired by ResNet principles (Section Equation 2.4.3), can be incorporated within or between these layers.



Following the Bi-LSTM layers, a multi-head attention mechanism (Section Equation 2.4.3) is applied to the sequence of hidden states generated by the Bi-LSTMs. This allows the model to adaptively weigh the importance of different time steps or features in the sequence when making a final prediction. By focusing on the most salient parts of the process history, the attention mechanism can enhance the model's ability to distinguish between normal and anomalous patterns. The multi-head approach enables simultaneous focus on diverse aspects potentially indicative of anomalies.

The final output of the attention layer is typically passed through further feed-forward layers to produce the anomaly classification (e.g., a probability score indicating deviation from normal behaviour). This integrated architecture aims to leverage the strengths of each component: Temporal modelling from Bi-LSTMs, improved trainability from residual connections, and context-aware focusing from multi-head attention.

This architecture directly relates to the VVUQ of SBDTs. Accurate anomaly classification serves as a form of validation for the DTs representation of normal process behaviour. Furthermore, analysing the attention weights (derived from Equation Equation 2.19) can provide insights into which process steps or features the model considers most indicative of anomalies, aiding in the verification and interpretation of both the model and the manufacturing process itself. While not explicitly detailed here, uncertainty quantification could be explored by examining the model's output confidence for different detected anomalies. The subsequent chapter will delve deeper into modern VVUQ techniques within the SBDT context.

2.4.4 Modern VVUQ in the Context of SBDT

ML-based VVUQ approaches heavily rely on data. In the preceding sections, the thesis introduced several interfaces which may serve as suitable data sources. PM/OCED may provide event logs for VVUQ approaches —ML approaches can ingest those. PPC systems may provide additional data to enrich the event log. This section will shed light on a systematic literature review (SLR) on VV in the context of DTs. After summarizing the main findings, several VV approaches with increasing sophistication are presented. The section closes with a discussion of the most promising approaches.

(Bitencourt et al., 2023) conducted a SLR on VV in the context of DT —a relatively new field. They did not consider uncertainty quantification in their SLR. As (Hua et al., 2022) note, there are no structured and established frameworks

for validating DTs. This statement holds for all sectors where DTs are applied. The SLR analysed 269 papers. They applied the 4R framework by (Osho et al., 2022) to describe the capabilities of the analysed twin frameworks. The 4R framework consists of the four dimensions *Representation*, *Replication*, *Reality* and *No DT*. The SLR found that most frameworks (49%) rather developed a DM or DS. Another 26% of DT were only able to *represent* the physical entity. Highly sophisticated DT were the exception, not the rule. Considering this trend, VV may not be a topic researchers are interested in at first sight. (Bitencourt et al., 2023) identified a trend throughout the years of increasing modelling capabilities of the considered DT. Up to the year 2023, the trend is still increasing. They identify more data sources as the main driver for this trend. From the 269 papers, 47% have been applied in the manufacturing domain. Of all classified DT, one key insight is that most authors performed at least one form of VV.



Figure 2.9: Donut chart showing the distribution of VV methods in the context of DT.

DTs ranking in the *reality* category where most often verified and validated. The authors deduct that because of the increasing complexity of the model, VV may become a stressing topic. (Nie et al., 2023) propose a multi-agent and cloud-edge orchestration framework leveraging Digital Twin and IIoT to optimize distributed manufacturing resources. Their framework integrates a Convolutional Neural Network (CNN) with a bidirectional Long Short Term Memory (LSTM) module to perform scheduling and self-adaptive strategies for intelligent, real-time production control. They compare their network with an earlier adopted algorithm and its result to perform VV. Quantifying the validity, they use Mean Squared Error (MSE) and Mean Absolute Error (MAE), see ?? (Lv et al., 2023) defined target scenarios and boundaries to verify their DT for fault diagnosis of a drilling platform. They defined intervals for the metrics to be valid. Validation

was performed by conducting a case study. Latter can be termed qualitative validation because the factual similarity of the case study against the DT has been assessed. Regarding their verification approach, they go one step further than (Nie et al., 2023) by defining control intervals. This is somewhat automatic verification, but still requires human intervention when the values leave the defined intervals. (Chen et al., 2023; Mykoniatis & Harris, 2021) both performed visual inspection to verify their DT. Both used cameras or other visual inspection tools to compare the DT results with reality. (Chen et al., 2023) used thermal cameras to conduct temperature scans and compared the results with temperature prediction of the twin. (Mykoniatis & Harris, 2021) used video recordings to validate their twin behaviour, but consulted KPIs to further validate their twin. Both approaches use aids for measurements and visual inspection. The measurements still have to be conducted and compared manually. Some authors performed statistical VV, although the measurements were not automated. (Wang et al., 2023) compared historical data with the twin data and calculated the mean absolute percentage error of both datasets, subsection 2.4.3. For validation they relied on conducting a case study, thus not fully automating VV. (Min et al., 2019) performed verification using PPC KPIs, automating the VV process even further. Their validation included using a validation set and measuring a set of metrics including error of fit and accuracy. This approach can be considered the first step towards a fully automated VVUQ process. (Bitencourt et al., 2023) conclude that the majority of the analysed papers performed VV manually, with only a few authors automating the process. They also note that most authors did not consider uncertainty quantification in their work. And indeed, most work was performed in only conducting verification (31%) where case studies were the method of choice (Eunike et al., 2022; Jia et al., 2023; Kumbhar et al., 2023; Leng et al., 2020, 2022). Case studies were also often applied where only validation tool place (35%) (Alam et al., 2023; Dobaj et al., 2022; Kherbache et al., 2022; Latsou et al., 2023; Leng et al., 2021; Negri et al., 2019). The SLR shows that VV is a topic of interest in the context of DT, but most authors still rely on manual methods. The trend towards more sophisticated DTs and the increasing complexity of models will likely drive further research in this area. The SLR also highlights the need for more automated and standardized VV processes, especially in the context of uncertainty quantification. Very few authors performed fully automated VVUQ for DT. The ones who did will now be discussed in more detail.

K-Nearest Neighbours (KNN) for Digital Twin Accreditation in Manufacturing

The k-Nearest Neighbours (KNN) algorithm, a lazy learning approach grounded in measuring feature similarity, can be used for the accreditation of manufacturing digital twins (dos Santos, Montevechi, et al., 2024). KNN classifies new data points by identifying the majority class among the K nearest neighbours in the training dataset. The determination of "being close" relies on various distance metrics. Most commonly, the Euclidean distance (see subsection 7.5.3) is used. Selecting an appropriate value for K is crucial for balancing the model's bias and variance. A small K can lead to overfitting, while a large K may provide no insights at all. It is not an eager learner like DT or NN because it does not learn a model from the training data. Instead, it stores the training data and makes predictions based on the stored data. This characteristic makes KNN particularly suitable for scenarios where the underlying distribution of the data is unknown or complex. The algorithm's simplicity and interpretability make it a popular choice for various classification tasks, including those in manufacturing contexts.



Figure 2.10: KNN algorithm. The algorithm classifies a new data point based on the majority class of its K nearest neighbours in the training dataset. Euclidean distance metric has been used to determine the distance between data points.

In the given figure, we see the lazy learning approach of KNN near completion. The star-formed point has to be assigned to class one or two. Based on the count of points in the near region of the unassigned point, the algorithm will decide class two. The approach by (dos Santos, Montevechi, et al., 2024) integrates

KNN with p-charts for the concurrent validation of SBDT (dos Santos, Campos, et al., 2024). This involves monitoring the DTs output over time and using KNN to classify its behaviour. Subsequently, p-charts are employed to statistically monitor the proportion of anomalies detected by KNN. The X-axis represents the discretized time t , the Y-axis represents the proportion of anomalies detected by the KNN. P-charts normally show a relative proportion of nonconforming items in a sample (Acosta-Mejia, 1999). (Dos Santos, Montevechi, et al., 2024) enriched their chart with an upper control limit (UCL) and lower control limit (LCL) which stand for acceptable statistical boundaries. This approach is similar to (Nie et al., 2023) who also defined control intervals. If the p-value exceeds the boundaries, the twin may deviate from real behaviour. This method offers the advantage of real-time monitoring. However, it is sensitive to the choice of the hyperparameter K and can be computationally expensive for large datasets (dos Santos, Montevechi, et al., 2024). The presence of outliers and noisy data can also impact the accuracy of KNN, and its performance may decrease in high-dimensional spaces. The authors utilized metrics such as accuracy, precision, recall and F1-Score (subsection 2.4.3. They also used cross validation for increasing robustness of the prediction. By varying values for K , an optimal split may be found. Recalling the different kinds of anomalies from subsection 2.4.3, KNN is able to capture point anomalies and contextual anomalies. Collective anomalies are not captured by KNN, as they are not able to learn from the data.

P-Chart for Digital Twin Anomaly Monitoring (using KNN results)



Figure 2.11: Example P-Chart showing the proportion of anomalies detected by KNN over time for Digital Twin accreditation, with Upper (UCL) and Lower (LCL) control limits. A point outside the limits (like at $t=7$) suggests potential deviation.

Time Series Classification for Fault Localization

Time series classification techniques also play an important role in detecting and classifying anomalies within manufacturing digital twin systems (Lugaresi et al., 2023). These techniques involve training classifiers on simulation data generated by the digital twin to identify and categorize faults in the real physical system (Dihan et al., 2024). A case study involving a scale-model gantry crane demonstrates the application of time series classification for this purpose (Mertens & Denil, 2024). Other techniques in this domain often involve deep learning models such as CNN, Recurrent Neural Networks (RNN), and LSTM networks. These models perform well at automatically extracting relevant features from time series data (Cao et al., 2023), outperforming traditional rule-based or statistical methods in complex scenarios. Time series classification offers the benefits of automated anomaly detection and classification, with the potential for early fault prediction. However, a key challenge is the need for sufficient labelled data for training these models (Zemskov et al., 2024), and real-time performance is often a critical requirement.

Uncertainty Quantification for Digital Twin Validation

VV is an important aspect of SBDT, but uncertainty quantification (UQ) is equally crucial. UQ aims to quantify the uncertainty associated with the predictions made by the digital twin, providing insights into the reliability and confidence of its outputs (Sel et al., 2025). Certainty in predictions creates trust in the application, a desirable property of SBDT when used in practice (Dwivedi et al., 2023). State of the art approaches to tackle uncertainty are Bayesian Neural Networks (BNN) (C. Li et al., 2017), Monte Carlo Dropout (MCD), Deep Ensembles (DE) and Gaussian Processes (GP). BNNs are able to quantify epistemic and aleatoric uncertainty (see ??). They are a type of neural network that introduce uncertainty into its predictions by treating the weights and biases as probability distributions rather than fixed values. Thus, each weight has a mean and a variance parameter for quantifying its uncertainty. During inference, samples are drawn from this distribution to *learn* its characteristics. This allows the model to capture uncertainty in the data and make probabilistic predictions (C. Li et al., 2017). MCD, DE and GP train surrogate models (see subsection 2.4.2) to approximate the uncertainty in the model's predictions.

MCD is a technique that uses dropout (Srivastava et al., 2014) during both training and inference phases to approximate the uncertainty in the model's predictions, unlike traditional dropout which is only used during training. By randomly

dropping out neurons during inference with a chosen probability p , MCD generates multiple predictions, which then are averaged and can be used to estimate uncertainty. The key insight here is that effectively, the sampling happens from a dozen different NN because of their different weight configurations. We thus reach ensemble-learner like accuracy without the computational cost of training multiple complete models like in DE. DE involves training multiple models with different initializations and architectures, and then combining their predictions to obtain a more robust estimate of uncertainty (Rahaman et al., 2021). The difference between DE and MCD lies in statistically independent NNs, meaning they do not share statistical interaction processes. Furthermore, they are initialized randomly, whereas MCD networks share the same weight initialization. MCD and DE both provide good estimates for uncertainty, but it is recommended to apply both techniques after rigorous fine-tuning of the DNN architecture (Kamali et al., 2024). GPs are a non-parametric Bayesian approach that models the underlying function as a distribution over functions (Bilionis & Zabaras, 2012). They provide a measure of uncertainty in their predictions by estimating the variance and mean of the predicted outputs (Burr et al., 2025).

Overall VVUQ for SBDT is conducted with varying efforts. There is not a lot of research on fully automated VVUQ processes. The SLR by (Bitencourt et al., 2023) shows that most authors still rely on manual methods, if VVUQ has been performed at all. The trend towards more sophisticated DTs and the increasing complexity of models will likely drive further research in this area. The SLR also highlights the need for more automated and standardized VVUQ processes, especially in the context of uncertainty quantification. Very few authors performed fully automated VVUQ for DT. The ones who did were presented in this section.

Approaches not applied in VVUQ yet

This section closes with considering diverse promising approaches not yet applied in concurrent VVUQ of SBDT, which could address the limitations identified in existing methods.

The Local Outlier Factor (LOF) is a distance-based approach which identifies data points with high variance, thereby detecting outliers potentially connected to rare events or concept drift (Alghushairy et al., 2020). Density-based methods, including Density-Based Spatial Clustering of Applications with Noise (DBSCAN), identify anomalies as data points placed in low-density regions (Çelik et al., 2011). These methods can effectively distinguish between clusters of normal

behaviour and deviations that fall outside these typical regions. The Isolation Forest algorithm offers an efficient approach for high-dimensional data by isolating anomalies through random data partitioning, where anomalies, being rare by nature, tend to be isolated more quickly than normal data points (Xu et al., 2017). One-Class Support Vector Machines (OCSVM) learn a boundary that capture the normal data, identifying any instances falling outside this region as anomalies (K.-L. Li et al., 2003). This method is especially useful when only data representing normal SBDT behaviour is readily available, allowing the model to learn the manifold of "normal" operations and flag any future deviations. NN-based methods, particularly autoencoders (AE) (Zhou & Paffenroth, 2017), can be trained on normal SBDT data to learn a compressed representation and then reconstruct the original data. Anomalies typically exhibit higher errors when the AE tries to reconstruct the default behaviour, making them detectable. These methods are capable of learning complex, non-linear patterns in SBDT behaviour and are effectively identify subtle deviations. Furthermore, semi-supervised techniques can enhance deviation detection by leveraging a small amount of labelled anomaly data in comparison with a larger set of normal data. ■

This chapter established the theoretical foundation for the research presented in this thesis. It began by introducing DMFS and their simulation using DES, differentiating static and dynamic components. The discussion highlighted the connection between PPC and data quality. KPIs were identified as critical tools for balancing the inherent trade-offs between model accuracy, computational efficiency, and scalability—an omnipresent challenge in SBDT section 1.2.

The chapter then explored the concept of DT, SBDT, DDDT, and HDT. Each type was analysed for its strengths and limitations, with SBDT relying on DES for dynamic representation, DDDT using machine learning for automated adaptation, and HDT combining domain knowledge with data-driven insights. PM was mentioned as a useful tool for DT validation, particularly through object-centric event logs (OCEL), which provide a multi-dimensional perspective on process interactions. OCEL's ability to capture complex, concurrent relationships between objects and events positions it as a powerful tool for enhancing traditional PM techniques.

Finally, the chapter addressed VVUQ as essential processes for ensuring the reliability of SBDT. Traditional VVUQ methods, such as statistical tests were compared with modern machine learning approaches, including KNN and BNN. This highlights the need for continuous, automated VVUQ frameworks capable of handling the dynamic nature of SBDT. Key challenges such as model opacity,

data dependency, and uncertainty quantification were identified as critical areas for future research. Key requirements for successful VVUQ were developed.

These theoretical components —DMFS modelling, DT architectures, PM/OCEL integration, and advanced VVUQ techniques —form the foundation for this thesis. The next chapter will present the methodology employed to develop a framework for VVUQ of SBDT, addressing the challenges and opportunities identified in this chapter. The goal of the framework is to enhance the reliability and accuracy of SBDT in real-world applications.

Chapter 3

Framework Design

This chapter develops the methodological approach for automatically performing VVUQ for automatically generated SBDT in the manufacturing domain. The foundational methodology uses data-driven frameworks and applies ML techniques to verify and validate the SBDT. The following chapter structure derives requirements besides the identified key requirements given in subsection 2.4.2, categorizes them and presents a conceptual blueprint. It is based on the theoretical findings from Chapter 2 and designed to ensure that the VVUQ process is systematic, reproducible, and adaptable to different use cases.

3.1 Requirements Engineering

A thorough analysis of the requirements for the proposed VVUQ framework is essential. (Sindhgatta & Thonse, 2005) distinguishes between functional (FR, (Van Lamsweerde, 2001)) and non-functional requirements (NFR, (Glinz, 2005)). Functional requirements define the specific functions and features that the system must provide, while non-functional requirements specify the quality attributes, constraints, and performance criteria that the system must meet. Additionally, technical requirements (TR) and operational requirements (OR) may also be considered. TR specifies the technical specifications of the system which are necessary to meet the functional requirements (Chikh & Aldayel, 2012), while OR outlines the operational constraints and conditions under which the system must operate (INCOSE, 2023).

The following Figure 3.1 summarizes the key requirements identified in subsection 2.4.2 and adds requirements which have been derived from the theoretical findings in Chapter 2.

Functional Requirements	Real-Time Data Integration
	Automatic VVUQ
	Anomaly Detection
	Adaptive Recalibration
	Alert System
Non-Functional Requirements	Performance Monitoring
	Dynamic Scalability
	Resilience against Uncertainty
	Safety
	Interoperability
	Ease of Use
	Continuous Optimization
	Continuous Learning
Technical Requirements	Scalable Architecture
	Data Compatibility
	Hardware Requirements
	Historical Data
	Meta Data
	Labelled Data
Operational Requirements	Data Quality
	Data Stewardship
	Certifications and Monitoring
	Continuous Maintenance
	Runtime Environment

Figure 3.1: Key Requirements for the VVUQ framework differentiated by FR, NFR, TR, and OR.

Source: Own illustration.

Real-time data integration enables continuous synchronization between physical processes and the digital twin through real-time data streams. This is crucial for ensuring that the digital twin accurately reflects the current state of the physical system. The latency in this regard has to be minimized (H. Li et al., 2018). Of course, one FR has to be the Automatic VVUQ of the SBDT with its functional capabilities anomaly detection (Pang et al., 2021), uncertainty quantification (Sel et al., 2025), and adaptive recalibration to new physical states. The framework should also include an alarm management system that generates alerts and recommendations for action in the event of anomalies or validation errors. This is essential for ensuring that operators can respond quickly to potential issues and maintain the integrity of the system. The performance evaluation of the framework should be automated and include key performance indicators (KPIs) such as F1-Score, MAE, and synchronization accuracy see subsection 2.4.3.

The NFRs include dynamic scalability, which allows the framework to handle large amounts of data and complex models in real time (Leskovec et al., 2020). This is essential for ensuring that the system can adapt to changing conditions and requirements also defined by evolving technical requirements or new demands of the stakeholders. The framework should also be robust against uncertainties, meaning it should be able to tolerate noise, incomplete data, and model uncertainties like concept drift. Security is another important NFR, as the framework must ensure the confidentiality and integrity of sensitive data. Interoperability with existing systems is also crucial for successful integration into existing workflows. The user-friendliness of the framework is important for ensuring

that operators can easily monitor real-time data, visualize anomalies, and understand uncertainty metrics. Finally, continuous learning capabilities are essential for enabling the anomaly detection network to adapt to changing processes over time.

The TR includes a scalable architecture that can be deployed in cloud or edge environments to process real-time data streams. The framework should support heterogeneous data formats, including sensor data and IoT streams. The integration of the ResNet BiLSTM network into the data pipeline is essential for efficient anomaly detection. The framework should also include modules for uncertainty quantification, such as Monte Carlo simulations and Gaussian processes. Hardware requirements should be defined to ensure sufficient storage and computing capacity for deep learning and real-time processing. Finally, the framework should support protocols such as OPC UA, MQTT, and RESTful APIs for system integration. Several data sources and stewardship are required to ensure the quality of the data used for VVUQ. This includes real-time data streams, historical data for training and baseline comparisons, metadata for context information, labelled anomaly datasets for training the ResNet BiLSTM network, and data quality standards for noise filtering, consistency checking, and gap handling.

The OR incorporate several key aspects that ensure the effective operation of the framework. Data stewardship ensures that the data quality follows high standards throughout the whole process. Continuous monitoring, for example logging, maintenance procedures and a flexible runtime environment close the list of identified requirements.

3.2 An Automated VVUQ Framework for Automatically Generated SBDTs

The framework consists of five interconnected layers that form a closed-loop system with continuous data flow, validation and improvement. At the start, diverse data sources such as PPC systems, DES outputs, PM, expert knowledge, sensor networks, and CRM feedback provide the raw inputs, which are centralized in a data lake with structured views managed by a data warehouse. The data warehouse enriches the incoming data with engineering features. The DL collects and integrates this data, preprocesses it through cleaning, normalization and feature extraction. The DL performs a subset of the actions of the data warehouse, but tailors the data specifically for the SBDT. This structured approach



Figure 3.2: Framework for VVUQ of SBDDT in the manufacturing domain. The framework starts with the data sources which all lead into the data lake. The data warehouse provides the Data Layer (DL) with different views. The DL further enriches the data to feed it into the Twin Layer (TL). The TL contains the DT and the physical entity. The TL is connected to the VVUQ Layer (VVUQL). It incorporates the ResNet BiLSTM network for VVUQ of the twin. It can trigger alarms and recommendations for action. The VVUQL is connected to the Decision Support Layer (DSL) which provides different data analysis and visualization tools. The DSL is responsible for the short-term decision making to manage the VVUQ process. The DSL is connected to the user interface (UI) which provides the user with a dashboard for monitoring and controlling the system. The DSL can request new data from the Data Sources. It also is connected to the Continuous Improvement Process layer (CIP) which is responsible for the long-term decision making.

Source: Own illustration.

meets real-time integration and quality requirements considered above.

Within the TL, the physical entity and its SBDT are in connection through a bi-directional data flow that ensures real-time synchronization. Evidently this framework does not allow DS or DM, because the closed-loop structure would be interrupted here. Complementing this, the VVUQ Layer is dedicated to the automatic VVUQ processes. This layer forms the core of the solution designed to answer how automated VVUQ can be efficiently implemented while maintaining accuracy (section 1.3) and determining which data-driven approaches are best suited for this task (section 1.3). It ensures that the SBDT represents both the conceptual model and the physical entity, using advanced methods such as a ResNet Bi-LSTM Attention Model. The choice of this specific deep learning architecture represents the framework's proposed answer to identifying the most suitable data-driven approaches for detecting discrepancies between simulated behaviour and real operational data (section 1.3). Furthermore, this DL approach, which processes historical and real-time data, provides robust anomaly detection capabilities, triggers recalibration when necessary, and validates outputs against actual measurements, thus fulfilling adaptive recalibration and anomaly detection requirements.

Translating these technical evaluations into corporate processes and recommendations is the role of the DSL. This layer synthesizes the VVUQ assessments into prioritized *short-term* decision recommendations, monitors KPIs, identifies data gaps, and manages alerts. By serving as the interface between technical processes and operational decision-making, it ensures that manufacturing personnel receive insights. The CIP layer further enhances the system by monitoring performance, detecting concept drift, scheduling model retraining based on accumulated data, and generating KPI reports. The CIP layer manages *long-term* feedback. Through an "Adapt Twin" process, this layer feeds insights back into the TL, ensuring that the digital twin evolves in connection with changes in the physical entity.

3.3 Online Validation and Continuous Feedback Loop

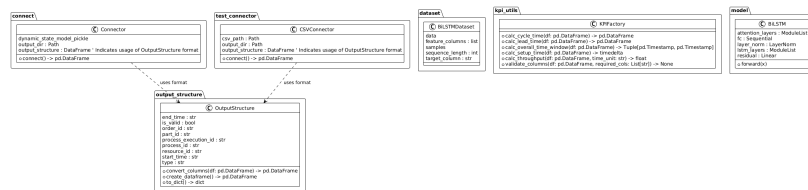
The entire framework operates as a closed-loop system characterized by continuous data collection from diverse sources, real-time synchronization between physical and digital entities, ongoing validation of simulation outputs against physical measurements, and a systematic flow of decision recommendations and alerts. This architecture ensures interoperability by providing standardized interfaces between layers and existing manufacturing systems while maintain-

ing the flexibility to adapt to various manufacturing contexts. The framework transforms VVUQ from a periodic technical assessment into an ongoing process that enhances DT quality and decision support capabilities. By meeting comprehensive functional, non-functional, technical, and operational requirements, this framework not only improves the accuracy and effectiveness of simulation-based digital twins but also facilitates their practical application as decision support tools in modern manufacturing environments. Stakeholder feedback and personnel suggestions are integrated into the framework through the DSL and CIP layers, ensuring that the system evolves in response to changing needs and conditions. This approach fosters a culture of continuous improvement and innovation, ultimately enhancing the overall performance and reliability of simulation-based digital twins in manufacturing.

Implementation

4.1 Architecture and System Setup

The implementation follows a modular architecture. It can process both streams and batches of manufacturing data.



Source: Own figure.

- **Data Connectors:** In the given code, two classes `InputStructure` and `OutputStructure` are responsible for reading and writing data. The `InputStructure` class reads raw data from the twin simulation, while the `OutputStructure`

class writes the processed data into the OCEL format developed for this framework, see section 4.2. The mapping logic is returned as well. The connector assigns IDs for different parts, resources, and processes. The IDs are used to identify the different components in the manufacturing process. This is a requirement for OCED. The mapping is returned as JSON files for each category, respectively.

- **KPIFactory:** Contains utility functions to calculate a diverse set of KPIs for PPC evaluation of the process.
- **Baseline Model:** Implements a baseline model for comparison with the ResNet-BiLSTM-Attention model. This model serves as a reference point to evaluate the performance of the more complex architecture.
- **PyTorch DataSet and DataLoader:** Handles the conversion of raw data into a format suitable for the ResNet-BiLSTM-Attention model.
- **ResNet-BiLSTM-Attention:** The core model that combines ResNet and BiLSTM architectures with attention mechanisms to learn from the data.

4.1.2 Tech Stack and Setup

The implementation is built with Python 3.12 (van Rossum & Foundation, 1991), using the following frameworks and libraries:

- **PyTorch:** Powers the deep learning components, chosen for its dynamic computational graph that facilitates complex architecture development and debugging (Contributors, 2016).
- **Pandas & NumPy:** Handle data manipulation, transformation, and numerical operations (N. Developers, 2006; P. D. Team, 2008).
- **Scikit-learn:** Provides implementation of the baseline model and evaluation metrics (S.-l. Developers, 2007).
- **Matplotlib & Graphviz:** Generate visualizations of model architecture and performance (Hunter & Team, 2003; G. D. Team, 2000).
- **UV Package Manager:** Ensures reproducible dependency management with exact version pinning (A. Developers, 2024).

Besides well established packages, PyTorch was preferred over TensorFlow due to its flexibility and ease of use, especially for research purposes. The implementation is designed to be modular and extensible, allowing for future enhance-

ments and adaptations to different manufacturing environments. The system is designed to run on a standard workstation with a multi-core CPU and an optional GPU for accelerated training. The given framework utilizes CUDA (NVIDIA Corporation, 2025) for GPU acceleration, which significantly speeds up the training process. The system is capable of processing large datasets efficiently, making it suitable for real-time applications in manufacturing environments.

4.2 Data Preprocessing

After laying out the architecture and system setup, this section focuses on the data preprocessing steps necessary for preparing the input data for the baseline model.

4.2.1 OCEL Format

Both models used in this thesis require the input data to be in the OCEL format, see subsection 2.3.2. The columns are inspired by the twin comparison model by (Schwede & Fischer, 2024a). For the given framework, the format is expected as input in the following format:

The terms are consistent with the upper cited framework. For the model components, following features may be considered:

1. **Time Model:** duration, start_time, end_time and further engineered features.
2. **Transition Model:** process_id, resource_id, end_time.
3. **Transformation Model:** part_id.
4. **Quality Model:** Exclusion of quality information in the given model.
5. **Resource Model:** resource_id, process_id, part_id.
6. **Resource Capacity Model:** resource_id; Note: Insufficient data available for detailed capacity modelling.
7. **Process Model:** process_id, part_id, resource_id.

This table does not forbid adding relational logic by the modeller. For example, each ID may be a foreign key to another table. Each row in the OCEL represents a single event instance. This schema aligns with OCED principles (subsection 2.3.2) by explicitly linking each recorded event instance (process_execution_id per timestamp) to the multiple object instances (order_id, part_id, resource_id,

Table 4.1: Detailed structure, data types, and description of the processed manufacturing OCEL.

Column Name	Data Type	Description
process_execution_id	int	Unique identifier for the specific process recorded.
order_id	Index (int/str)	Identifier for the overall manufacturing order this event belongs to.
start_time	Timestamp [UTC]	The precise timestamp marking the beginning of the event, adjusted to UTC.
end_time	Timestamp [UTC]	The precise timestamp marking the end of the event, adjusted to UTC.
duration	float (seconds)	The calculated duration of the event (end_time - start_time) in total seconds.
part_id	int	Identifier for the specific part or component being processed or handled during the event.
resource_id	int	Identifier for the machine, station, or other resource involved in the event.
process_id	int	Identifier indicating the type of process step or operation performed (e.g., milling, assembly).
type	str	A textual description or category classifying the type of event recorded.
is_valid	bool	Boolean flag indicating whether the recorded event sequence or outcome is considered valid (e.g., based on model prediction or predefined rules).

`process_id`) involved in its execution. This inherent multi-object relationship within each event record is important for modelling complex process dependencies. The structure empowers the representation of complex control flows often found in manufacturing. Parallel execution paths (AND-split) can be inferred by identifying events associated with different resources or process steps occurring *within* overlapping time intervals (`start_time`, `end_time`) but related to shared object instances, such as a common `order_id`. Alternative paths and process variants (EXCLUSIVE OR-split) are explicitly captured through the diversity of event sequences observed across different process instantiations (e.g., grouped by `order_id`); the log records exactly which path or sequence of activities occurred for each instance. The object-centric nature enriches this analysis by providing context (e.g., the specific `part_id` or `resource_id` involved) that can explain why a particular variant or choice was executed. The OCEL retains its sequential linear character by grouping it by `order_id` and sorting ascending related to `end_time`. This allows for the reconstruction of the process flow. The use-case in chapter 5 will engineer further features from the OCEL format.

Because conciseness of the data structure was a requirement, the OCEL format is not fully compliant with the OCED standard (W. M. van der Aalst, 2023). The OCEL format used in this thesis is rather simplified. Specifically, this simplification means the schema does not include distinct tables for object instances and their types, explicit modelling of static O2O relationships (subsection 2.3.2) or the capability to store timestamped attributes associated directly with objects rather than events. Despite these omissions the implemented structure retains the core OCED principles. The goal is rather to *learn* these relationships from the data itself.

4.3 Model Implementation

After the basic OCEL format is established, the next step is to implement the models. The implementation consists of two main components: a baseline model and the black-box model. The baseline model serves as a reference point for evaluating the performance of the more complex architecture. The ResNet-BiLSTM-Attention model is designed to learn from the data and make predictions based on the features extracted from the OCEL format, as well as the baseline model does. The key distinction lies in interpretability: while the DT baseline (white-box) enables direct rule extraction, the ResNet-BiLSTM-Attention (black-box) trades explainability for sequential pattern capture. In the course of the experiments, the baseline model can serve as a VVUQ tool by itself. Data leakage

may be diagnosable by analysing the results of the `DecisionTreeClassifier`. Furthermore, model components can be analysed by themselves through adaptive feature selection during training. If the classifier was able to learn well on the dataset, the model component may be present in the dataset and thus the SBDT was able to encode this information in the data. The ResNet-BiLSTM-Attention model is a black-box model, which means that the decision-making process is not easily interpretable. The `DecisionTreeClassifier` will thus from now on often be referred to as 'white-box model' or 'baseline model'. The ResNet-BiLSTM-Attention model will be referred to as 'black-box model'. The implementation of both models is described in detail in the following sections.

The general modelling decision is as follows: The models receive a binary classification task. The task is to predict whether the process execution is 'valid' or not. Validity in the sense is also including verification and uncertainty quantification. If the row or process is not valid ('accurate'), the modeller has to further identify the root cause. The models thus serve as a diagnostic tool to conduct more deep analysis. UQ is achieved by measuring the metrics of both models. Verification is achieved by the manual efforts of the modeller¹. The `is_valid` column in the OCEL format serves as the target variable. The models are trained on a subset of the data, and their performance is evaluated on a separate test set. The models are compared based on various metrics, including accuracy, precision, recall, and F1-score. The goal is to determine which model performs better in terms of predicting the validity of process executions. Both models are compared using the same metrics described in subsection 2.4.3. The models are trained and evaluated using the same dataset, ensuring a fair comparison. The results are presented in chapter 5. The data has been sorted by `end_time` and grouped by `order_id` to ensure that the white-box model has a chance to learn sequential patterns as well. By nature, decision tree classifiers are not able to learn sequential patterns. The ResNet-BiLSTM-Attention model is able to. For the train-test split, a random split is used. Despite sequential nature, random splitting was prioritized to mitigate temporal bias from incomplete process traces (Morita et al., 2022). Temporal bias refers to wrongly guessed correctness of patterns which are induced by choosing wrong cut-off points for splits.

¹Of course, this undermines our efforts to present a fully automatic VVUQ framework. A lot of time is saved in the timespan when no validity breach is detected. This is the main advantage of this approach.

4.3.1 Whitebox Baseline Model

As a baseline model, a white-box model is implemented to provide a reference point for the performance of the ResNet-BiLSTM-Attention model. The white-box model is based on a simple decision tree classifier, which is interpretable and easy to understand. This model serves as a benchmark for evaluating the performance of the more complex ResNet-BiLSTM-Attention model. For the concrete implementation, the `DecisionTreeClassifier` from the `sklearn.tree` module is used (S.-I. Developers, 2007).

4.3.2 ResNet BiLSTM Multi-Head Self-Attention Network

As a primary 'challenger' model, the ResNet-BiLSTM-Attention model is implemented, see Equation 2.4.3. This model combines the strengths of residual networks (ResNet) and bidirectional long short-term memory networks (BiLSTM) with multi-head self-attention mechanisms. The model is implemented using the PyTorch modules `torch.nn`, `torch.functional` and `torch.optim` (Contributors, 2016). Before the data is ingested by the network, specific `DataSet` and `DataLoader` classes are implemented to handle the data. The `DataSet` class is responsible for loading the data and transforming it into a format suitable for the model. The `DataLoader` class is responsible for batching the data and shuffling it during training.

The architecture of the ResNet-BiLSTM-Attention model is shown in Figure 4.2. The `torch.nn` module integrates Bidirectional Long Short-Term Memory (BiLSTM) layers with Multi-Head Self-Attention and Residual Connections. The model architecture consists of several layers, including convolutional layers, BiLSTM layers, and attention mechanisms.

1. **Input/Configuration:** The model is initialized with hyperparameters defining its structure: `input_size` (number of input features, D), `hidden_size` (dimensionality of LSTM states, H), `num_layers` (number of stacked LSTM/Attention blocks, N), and `attention_heads` (number of parallel attention heads, A).
2. **BiLSTM Layers:** The core consists of N stacked BiLSTM layers (`nn.LSTM` with `bidirectional=True`). Each layer processes the input sequence in both forward and backward directions, capturing dependencies from past and future context. The output dimensionality of each BiLSTM layer is $2H$. Dropout is applied between layers for regularization.
3. **Multi-Head Self-Attention:** Following each BiLSTM layer, a `nn.MultiheadAttention`



Figure 4.2: ResNet-BiLSTM-Attention architecture. The model consists of a ResNet block, followed by a BiLSTM layer and a multi-head self-attention mechanism. The output is then passed through a fully connected layer for classification.

Source: Own Torchview illustration.

layer is applied. It performs self-attention on the BiLSTM output sequence, allowing the model to weigh the importance of different time steps relative to each other within the sequence.

4. **Layer Normalization & Residual Connections:** `nn.LayerNorm` is applied after the attention mechanism within each block to stabilize activations. A residual connection adds the input to this block to the output before a final ReLU activation, facilitating gradient flow in deeper networks.
5. **Sequence Pooling:** After the final LSTM/Attention block, the output sequence (shape: $Batch \times SequenceLength \times 2H$) is aggregated across the sequence dimension using temporal mean pooling (`torch.mean`), resulting in a single fixed-size vector (shape: $Batch \times 2H$) representing each input sequence.
6. **Final Classifier:** A feed-forward network (`nn.Sequential`) processes the pooled representation. It typically includes one or more linear layers with ReLU activations and Dropout for regularization, culminating in a final linear layer producing a single output logit.
7. **Output Activation:** A sigmoid function (`torch.sigmoid`) is applied to the final logit to produce a probability score between 0 and 1, suitable for binary classification.
8. **Weight Initialization:** Linear layers within the network are initialized using Kaiming Normal initialization (`nn.init.kaiming_normal_`), a standard practice often beneficial for layers followed by ReLU activations.

For training, the model has to be set to inference mode using the `train_model()` method. The model is trained using the Adam optimizer `torch.optim.Adam` ?? (Kingma & Ba, 2014) to update model weights based on calculated gradients. The loss function used is binary cross-entropy subsection 7.5.9 `nn.BCELoss`. It quantifies the difference between the predicted probabilities and the true binary labels. The learning rate is not fixed, rather a learning rate scheduler `torch.optim.lr_scheduler.ReduceLROnPlateau` is used to adjust the learning rate during training based on the performance on a monitored metric (e.g., training or validation loss). The model is trained for a specified number of epochs, and the training loop iterates over the training dataset in mini-batches. In each epoch, the model performs forward and backward passes to compute loss and gradients, updating model parameters using the optimizer. Training loss is typically tracked per epoch.

4.4 Model Evaluation

Based on the reference in subsection 2.4.3, the evaluation of the models is performed using various metrics. To achieve this, the model is switched to evaluation mode, `model.eval()`, to ensure deterministic behaviour. This disables dropout layers so that all neurons are used for the forward pass to achieve predictions. Gradient calculations are disabled through `torch.no_grad()`. BatchNorm layers now use their learned estimates of mean and variance parameters to process the data. During evaluation mode, the model processes the test set batch per batch, yielding output probabilities. These are compared against the true labels. The evaluation metrics are implemented in the `evaluate_model()` method. The evaluation metrics include a classification report, confusion matrix Table 2.3, accuracy Equation 2.1, precision Equation 2.2, recall Equation 2.3, F1-score Equation 2.4 and ROC AUC score Equation 2.8. The metrics are calculated using the `sklearn.metrics` module. The evaluation metrics are used to compare the performance of the baseline model and the ResNet-BiLSTM-Attention model as well as the standalone performance on the holdout set. The evaluation metrics are also used to diagnose the models and identify potential issues with respect to the bespoke adaptive feature selection procedure. For the assignment of the label 'valid' or 'invalid', a threshold of 0.9 is used. This value is higher than the usual threshold of 0.5. This means that if the predicted probability is greater than or equal to 0.9, the process execution is classified as 'valid'. If the predicted probability is less than 0.9, the process execution is classified as 'invalid'. Setting the boundary so high is a conservative approach. It ensures that only the most confident predictions are classified as 'valid'. This is important for the VVUQ framework, as it aims to identify potential issues in the process execution. The threshold can be adjusted based on the specific requirements of the application and the desired trade-off between precision and recall. The 0.9 validity threshold reflects manufacturing VVUQ's low tolerance for false positives Equation 2.2.

The evaluation logic presented so far applies to batch data. The idea of the black-box model and concurrent VVUQ lies in processing stream data, preferably in chunks equal to the `sequence_length` of one batch of the network during the evaluation phase. Pandas (P. D. Team, 2008) provides the `chunksize` parameter to read the data in chunks. The `chunksize` parameter can be set to the `sequence_length` of the model. The model is then evaluated on each chunk of data. The evaluation metrics are calculated for each chunk updated in real time for PPC and direct reporting. This can be applied on the white-box model

as well. For the black-box model, this implementation may be achieved using specific `DataLoader` classes. For concurrent evaluation, UCL and LCL can be set. If they are exceeded, the model will raise an alert. This approach is inspired by the p-chart approach used by (dos Santos, Montevechi, et al., 2024).

If desired, the learned parameters of the model can be saved to a file using the `torch.save()` method. This allows the trained model to be loaded later for inference or further analysis without repeating the training process. The model can be saved in two different formats: the entire model or just the state dictionary. The state dictionary contains all the parameters of the model, while the entire model includes the architecture and parameters. The state dictionary is preferred for saving models, as it is more flexible and allows for easier loading of models with different architectures.

Chapter 5

Testing

The thesis now focusses on the application of the implemented features and methods in a real-world scenario. The goal is to demonstrate the practical applicability of the developed concepts and to validate the theoretical findings presented in the previous chapters.

5.1 Application Scenario and Data Basis

5.1.1 Application Scenario

The framework has been applied on the Internet of Things-Factory (IOT) in Gütersloh, Germany (for Applied Data Science, 2024). It is a cyber-physical system (CPS) (Baheti & Gill, 2011) mimicking industry-relevant processes in a smaller scale for research students. It consists of several stations that are partly interconnected via an assembly line or a delivery service conducted by automatic guided vehicles (AGVs). The factory is modular, so processes can be discovered module-wise in isolation. All modules are working on edge but are connected to a cluster to control it. The factory works without any personnel in theory. The main process also evaluated here is circular, meaning that the product is assembled and can be disassembled in a loop. The factory is shown in Figure 5.1.

The robot cells are responsible for performing transformation operation like assembling additional parts or testing functions.

The factory produces an exemplary product, consisting of a back part, a breadboard for several parts and a front panel. The parts to put on the breadboard are a display, gyroscope, an analog board and a weather station.

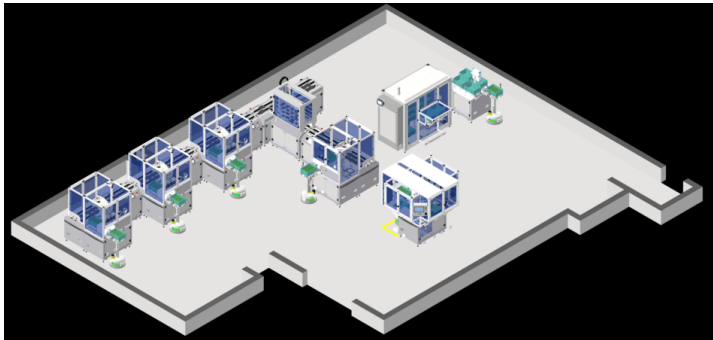


Figure 5.1: Overview of the IOT factory. It consists of three production stations from left to right, which are followed by a sorting station and a packaging station. The stations are interconnected by an assembly line. Isolated from the assembly part, two AGVs are used to transport parts between the warehouse station (upper right) and another flexible workstation (right).

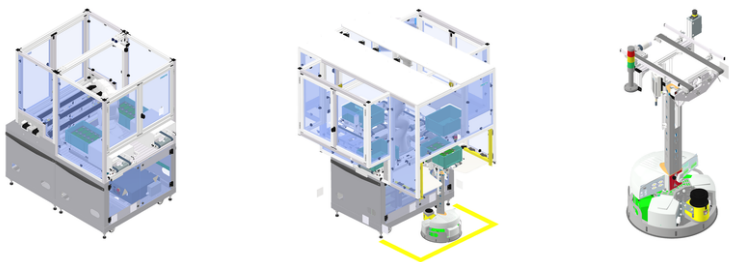


Figure 5.2: Two robot cells. The first cell is the main actor in this exemplary production process. Cell two is not part of the observed process here. The third image shows an AGV which transports boxes with assembled and disassembled parts to the stations.











	IoT main PCB
	IoT Gyrostep
	IoT Weatherstation / Weatherstation
	IoT analog PCB / 0-50V analog
	IoT Display
	IoT back black
	IoT front black
	IoT front blue
	IoT front red
	IoT front grey

Figure 5.3: The product consists of a back part, a breadboard and a front panel. The breadboard is used to put on several parts, such as a display, gyroscope, analog board and a weather station.

The only colour produced at the moment is black. Not all parts can be put on the breadboard and there are several parts which conflict in size and location on the breadboard. The ground-truth assembly rules look as follows: PRÜFEN UND ANPASSEN

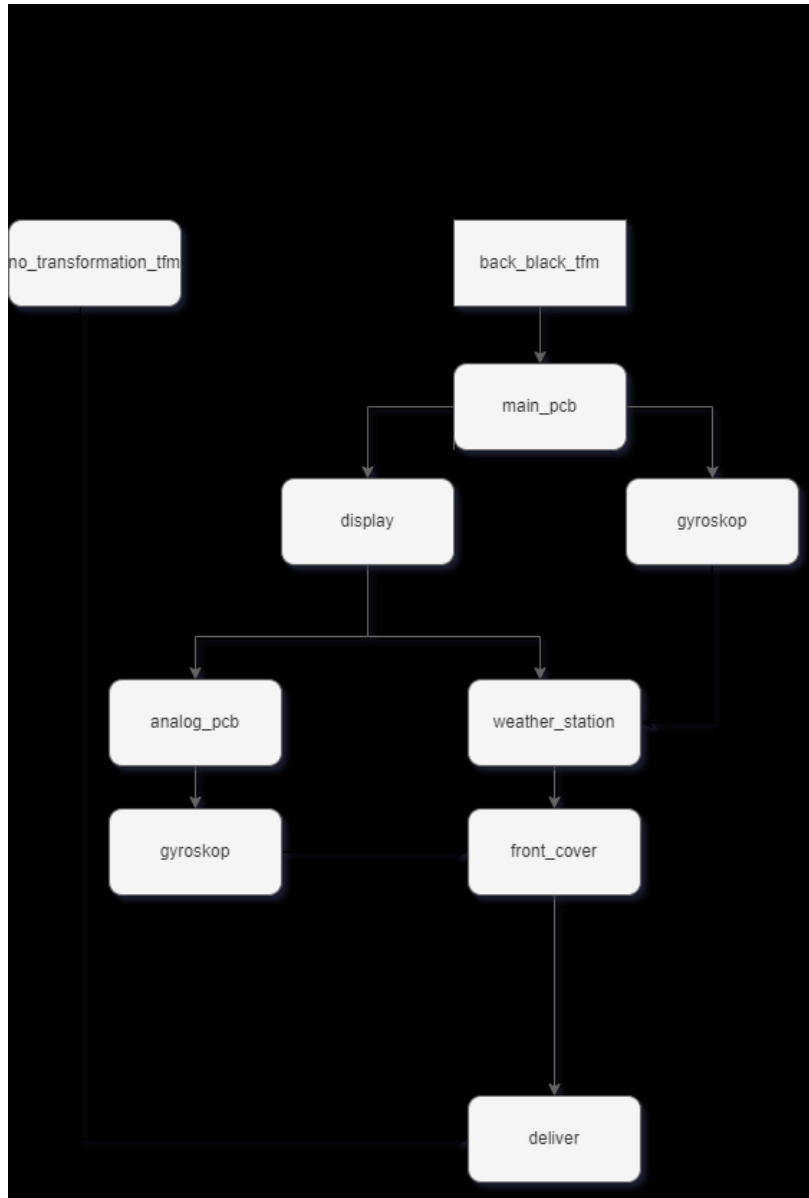


Figure 5.4: Three variants are possible. No transformation is also a possibility.

Back and front cover are necessary parts and are assembled every time. The main part `main_pcb` is also obligatory. It is placed at the beginning. Following that, the display or gyroscope can be assembled. If the display has been chosen, only the analog board or the weather station can be assembled. The weather station takes too much space on the breadboard for the gyroscope to be placed. If the analog board has been placed, the gyroscope is of course possible. The product is finished by placing the front cover and delivering the product to the

sink.

During the production, the factory gathers data via sensors. The data is saved in a database and can be used for further analysis.

Finally, the sequential order of the production process is as follows:

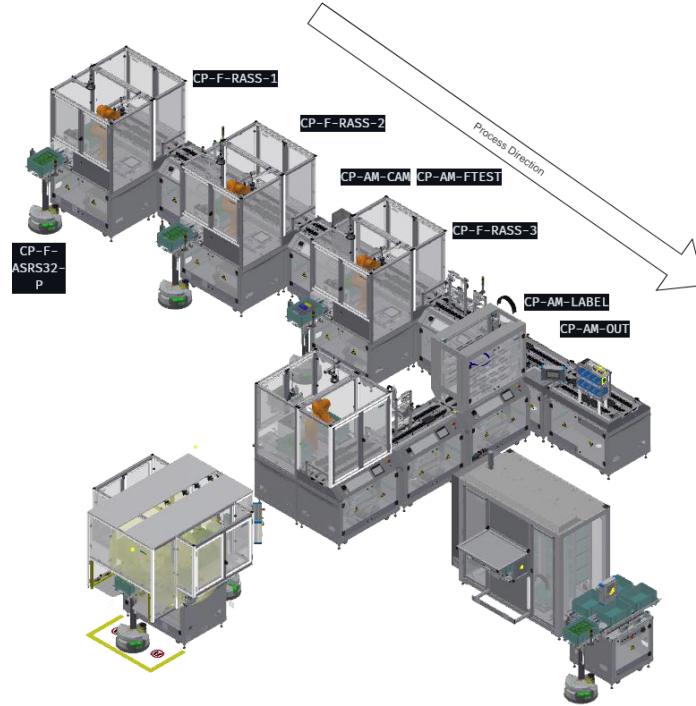


Figure 5.5: The blueprint with transitions between resources.

5.1.2 Data Basis

SBDT Dataset

The dataset gathered from the SBDT is referred to as `sim_data`. The OpenFactoryTwin (see section 5.2) provides a method to deserialize the simulated orders and save them in a CSV file. The dataset then gets converted to the OCEL structure. For this endeavour, a separate connector logic has to be implemented in every use case. See `src/connector/ofact` for the connector here.

The connector's output follows a standardized structure defined by the `OutputStructure` class, which ensures consistency across different data sources. The connector first deserializes the dynamic state model from a pickle file, accessing the full simulation state. Only actual process executions (as opposed to planned ones) are retained for further processing, identified by the "ACTUAL" flag in their event type. The connector creates mapping dictionaries for various categorical attributes following the OCED standard:

- **Part ID Mapping:** Uses domain expertise to identify part types from process names, normalizing text (lowercase, no whitespace) to match against a predefined list of possible parts. This list contains possible parts from Figure 5.3.
- **Process Type Categorization:** Assigns process steps to expert-defined categories such as "machine," "feature," "endproduct," "test," and "transport" based on keywords in process names. These types have been assigned by the modeller and are of free choice. See Table 4.1.
- **Process ID Mapping:** Creates unique integer identifiers for each distinct process description based on enumeration.
- **Resource ID Mapping:** Generates unique identifiers for each resource involved in the process executions based on enumeration.
- **Temporal Data Extraction:** The connector extracts start and end times for each process execution.

Process executions are associated with their respective order IDs, establishing the connection between individual process steps and the orders they belong to. All extracted information is then consolidated into a standardized DataFrame structure with properly typed columns as defined in the `OutputStructure` class. The connector also includes a validation step to ensure that the generated DataFrame adheres to the expected structure and data types, raising an error if any discrepancies are found.

A key aspect of the connector's functionality is the integration of domain knowledge into the data transformation process. Instead of relying solely on the raw data structure, the connector employs expert-defined categorizations and normalization procedures to ensure semantic consistency in the transformed data.

For example, the part identification logic uses a predefined list of potential parts (such as "GYROSCOPE," "MAIN PCB," "FRONT COVER," etc.) and searches for these terms within process descriptions. Similarly, the process type categorization uses domain-specific groupings like "machine," "feature," and "test" based on keywords found in process names. This domain knowledge integration ensures that the transformed data maintains the semantic richness required for meaningful validation and comparison between simulated and real-world processes.

The `sim_data` rows will receive the label 0 for `is_valid`, because we want the black-box model to learn to distinguish between real and simulated data to perform VVUQ. This way we can

Factory Dataset

The dataset has been gathered from the database of the IoT Factory. In the code it is referred to as *real_data*.

The dataset contains 18057 rows and 4696 orders from a timespan of 22.04.2020 to 14.05.2024. There are no duplicate rows. Each row describes a unique operation step in an order. Roughly 40 percent of the rows contain missing values, which have been filled with zeros. The data has been mined from a MariaDB SQL database of the IoT Factory. Several tables have been aggregated to form the dataset. Without additional tables, no information about workplans, resources and operation numbers would be available. The dataset is filtered for promising trajectories of meaningful and intact process executions. The filter considers data between the 20.04.2020 and 22.04.2022, 02.05.2022 and 19.07.2022, 02.11.2022, 11.11.2022, 23.01.2022 and March 2023, each data inclusively.

The dataset contains the following columns:

- **WPNo**: The workplan number of the specific workplan.
- **StepNo**: The step number of the specific workplan. The workplan is divided in sequential steps enumerated by this number.
- **ONo**: The order number of the specific order. Each order has a unique number.
- **OPos**: The order position of the specific order. The order position is the position of the order in the workplan.
- **Description**: The description of the specific step in spoken language.
- **OpNo**: The operation number of the specific operation. Each operation has a unique number.
- **NextStepNo**: The next step number of the specific step. This is the step that follows the current step.
- **FirstStep**: The first step of the specific workplan.
- **ErrorStepNo**: The error step number of the specific step. This is the step that is executed in case of an error.

- **Start:** The start time of the specific step.
- **End:** The end time of the specific step.
- **OPNoType:** The operation number type of the specific operation.
- **ResourceID:** The resource ID of the specific resource.
- **ErrorStep:** Is this step an error step (yes/no)?
- **ErrorRetVal:** The error return value of the specific step.
- **Active:** Is this step active (yes/no)?
- **op_desc:** The operation description of the specific operation.
More specific than the description.
- **ResourceName:** The name of the specific resource.
- **resource_desc:** The description of the specific resource.
- **workplan_desc:** The description of the specific workplan.
- **workplantype_desc:** The description of the specific workplan type.
- **case_id:** The case ID of the specific case.
- **Description_Encoded:** The description of the specific step
ordinally encoded.

The operations performed can be seen in the following:

1. **Release a part on stopper 1:** The AGV delivered the box with the parts to be manufactured to the first station. The box is travelling over the assembly line to the first station where the first part is released.
2. **Place cover to assembly place:** The first part is placed on the assembly place. The cover is placed on top of the part as the first piece of the product.
3. **Assemble part from box on RASS1 - MAIN PCB:** The main PCB is assembled on the cover. This is the first configured part of the product. The main PCB is the breadboard of the product.
4. **Switch on PCB:** The main PCB is switched on. This is necessary to activate it.

5. **Assemble part from box on RASS1 - DISPLAY:** The display is assembled on the main PCB. This is the second configured part of the product. The display is one optional part of the product. This factors out one product variant, see ??.
6. **Move part to pallet on belt:** The product is moved to the pallet on the belt for further processing.
7. **Measure a part (analog):** The product is measured. This is necessary to ensure the quality of the product for later steps.
8. **Assemble part from box on RASS2 - ANALOG:** The analog part is assembled on the product. This is the third configured part of the product. The analog part is also one optional part of the product.
9. **Assemble part from box on RASS2 - GYROSCOPE:** The gyroscope is assembled on the product. This is the fourth configured part of the product. The gyroscope is also one optional part of the product.
10. **Move part to pallet on belt:** The product is moved to the pallet on the belt for further processing.
11. **Check analog:** The analog part is checked. This is necessary to ensure the quality of the product for later steps.
12. **Check gyroscope:** The gyroscope is checked. This is necessary to ensure the quality of the product for later steps
13. **Assemble part from box on RASS3 - FRONT COVER:** The front cover is assembled on the product. This is the last configured part of the product. The front cover is the last part of the product.
14. **Move part to pallet on belt:** The product is moved to the pallet on the belt for further processing.
15. **Test connection to IoT main PCB:** The connection to the IoT main PCB is tested. This is necessary to ensure the quality of the product for later steps.
16. **Test the function of the touch display:** The touch display is tested. This is necessary to ensure the quality of the

product for later steps.

17. **Test the analog input/output shield:** Analog PCB is tested.

18. **Test the historical gyroscope data:** The gyroscope is tested.

19. **Print Label:** The label is printed. The label contains information about the product configuration, the time manufactured and the serial number.

20. **Deliver Part:** The final product is delivered to the sink.

Per step, several resources are involved. The following table shows the utilized resources per step:

Table 5.1: Steps and Resources Used

Process Step Name	Resource Name
Release a part on stopper 1	CP-F-ASRS32-P
Place cover to assembly place	CP-F-RASS-1, CP-F-RASS-2, CP-F-RASS-3
Assemble part from box on RASS1 - MAIN PCB	CP-F-RASS-1
Switch on PCB	CP-F-RASS-1
Assemble part from box on RASS1 - DISPLAY	CP-F-RASS-1
Move part to pallet on belt	CP-F-RASS-1, CP-F-RASS-2, CP-F-RASS-3
Measure a part (analog)	CP-AM-MEASURE
Assemble part from box on RASS2 - ANALOG	CP-F-RASS-2
Assemble part from box on RASS2 - GYROSCOPE	CP-F-RASS-2
Move part to pallet on belt	CP-F-RASS-1, CP-F-RASS-2, CP-F-RASS-3
Check analog	CP-AM-CAM
Check gyroscope	
Assemble part from box on RASS3 - FRONT COVER	CP-F-RASS-3
Move part to pallet on belt	CP-F-RASS-1, CP-F-RASS-2, CP-F-RASS-3
Test connection to IoT main PCB	CP-AM-FTEST
Test the function of the touch display	CP-AM-FTEST
Test the analog input/output shield	CP-AM-FTEST
Test the historical gyroscope data	CP-AM-FTEST
Print Label	CP-AM-LABEL
Deliver Part	CP-AM-OUT

This process has been identified as the ground-truth process. The

process is circular, meaning that the product is assembled and can be disassembled in a loop. The process is also modular, meaning that the product can be assembled in different configurations. The process is also flexible, meaning that the product can be assembled in different ways.

Concatenation of Datasets

Several preprocessing steps had to be performed to account for the fact that the SBDT simulated only one variant of the product: 'analog', 'cover', 'display', 'gyroscope', 'pcb' and the involved machines. This yielded the necessity to make both datasets congruent to each other. The following steps were performed:

- The `sim_data` dataset was aligned for the same time period as the `real_data` dataset. The SBDT chose the time of order as the production time. In the modelling phase, when adaptive feature selection had been performed to identify if the SBDT was able to learn the Time Model, only *relative* time features were chosen which were developed in ??.
- The `real_data` dataset was filtered for the same process steps as the `sim_data` dataset. This means that only the process steps which are present in the `sim_data` dataset were kept, producing only one product variant. This has also been applied on the `partid`, `the processt type` and `resourceid` columns. The IDs based on enumeration had to
- Both datasets have been cleaned and entries containing invalid IDs were removed. This means that all entries which are not present in the mapping dictionaries were removed. The mapping dictionaries are generated by the connector and contain only valid IDs per definition.
- Only a subset of all performed processes was included (in detail, all `processid ≤ 26`. These processes all have the

The `real_data` dataset was then concatenated with the `sim_data` dataset. The concatenation was done by appending the `sim_data` dataset to the `real_data` dataset. The resulting dataset contains all process steps from both datasets. The resulting dataset is referred to as `final_data`. The unification before concatenation was necessary

to ensure that no logical flaws are present in the data.

The `final_data` dataset finally after preprocessing as described contains 1978 rows and 56 orders with 24 features. The following section elaborates how these features were generated.

Feature Engineering

5.2 Automatically Generated Digital Twin

The simulation is conducted using an updated version of the Open Factory Twin (ofact) (Schwede et al., 2024). The dataset was fed in the twin after preprocessing steps were made. For the simulation, the entire time horizon of the dataframe was used and a state model was generated. To achieve this, the IoT factory had to be subsumed under the vocabulary of the twin. The ofact twin has great similarity to the framework by Schwede and Fischer (2024b). There are the following aspects in the twin which needed to be filled with information of the factory (see `small.xlsx` sheets from left to right as well):

- **Plant:** The overall entity of production. The plant name used here was `iot_factory`.
- **EntityType:** All entities have to be defined here. This ranges from the parts, resources and AGVs to the factory itself. For a complete list see the excel document `small.xlsx` on the second sheet.
- **Resource:** Because we model the resources more specifically, we did not use this functionality.
- **StationaryResource:** Stationary resources are static and can not move. In our case, we modelled an artificial obstacle to simulate production problems if wanted. This was not relevant here.
- **Storage:** Storage units contain parts. They are used to traverse the parts through the factory. In this context, I modelled the sink, a box and a carrier unit which contains the parts to be assembled.
- **Warehouse:** This is a static storage unit where the parts are stored in boxes until they are processed. In this case, this

is the 'Hochregallager' of the factory.

- **WorkStation:** Workstations (or assembly stations in an older version of ofact) are resources which perform processes on parts. In our use case, these are the RASS stations, measurement-, cam-, function test- and labelling station.
- **ConveyorBelt:** There is one belt where the storage units traverse through the factory.
- **NonStationaryResource:** There are no non-stationary resources.
- **ActiveMovingResource:** There are no active moving resources.
- **PassiveMovingResource:** The product carrier, box and sink are modelled as passive moving resources.
- **Process:** Contains processes and value added processes (VAP). VAP are adding features to parts and modify it. There are n VAP for n features (like gyroscope, weather station and more). Additional processes for activities like taking a photo of the product through the cam station are also added here.
- **ProcessController:** This controller summarizes all processes to come and connects them.
- **ResourceModel:** Resource groups are formulated for activities like montage, identifying to attach the relevant parts to these resources. This way, main resources and parts are getting matched.
- **ProcessTimeModel:** Each part receives a time simple time distribution to account for its production time.
- **QualityModel:** Each part receives a bernoulli distribution to account for its quality. In the dataset, no quality information existed.
- **TransitionModel:** This model connects possible origins to possible destinations, to that the traversal of the parts can be modelled correctly. Each part and additional processes are relevant here.
- **TransformationModel:** This model contains the building rules from Section ??.

- **Time:** Process execution plans get a starting time here.
- **Part:** Parts are connected to their EntityType here. There is also information attached where the part is stored or situated in.
- **Sales:** Lists the features and feature cluster. This matches the building rules. Parts have to be defined as features here.
- **CustomerGeneration:** Customer generation logic.
- **Customer:** List of customers.
- **Orders:** The orders with their requested features.

5.3 VVUQ Experiments

5.4 Results and Interpretation

5.5 Comparison with Manual Validation Methods

Chapter 6

Discussion

- 6.1 Evaluation of the Developed Framework**
- 6.2 Significance of Verification in Automatically Generated Digital Twins**
- 6.3 Limitations of Automated Validation**
- 6.4 Implications for Research and Practice**

Chapter 7

Conclusion and Outlook

7.1 Summary of the Key Findings

7.2 Methodological and Theoretical Insights

7.3 Outlook

7.4 Recommendations for Practical Application

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7.5 Mathematical Foundations

This appendix provides formal definitions and illustrations for the core mathematical functions and operations referenced in the theoretical foundations chapter (Section 2.4.3 onwards), as well as other relevant mathematical concepts and techniques commonly encountered in machine learning, deep learning, optimization, and data handling that are pertinent to the methods employed in this thesis.

7.5.1 Basic Notation and Operations

As established at the beginning of the chapter, vectors are denoted by bold lowercase letters (e.g., \mathbf{z}) and matrices by uppercase letters (e.g., W). Vectors are assumed to be column vectors unless otherwise specified.

Matrix-Vector Multiplication:

Given a matrix $W \in \mathbb{R}^{m \times n}$ and a vector $\mathbf{x} \in \mathbb{R}^n$, their product is a vector $\mathbf{y} = W\mathbf{x} \in \mathbb{R}^m$, where the i -th element is calculated as:

$$y_i = \sum_{j=1}^n W_{ij}x_j \quad (7.1)$$

Vector Addition:

Given two vectors $\mathbf{y}, \mathbf{b} \in \mathbb{R}^m$, their sum is a vector $\mathbf{z} = \mathbf{y} + \mathbf{b} \in \mathbb{R}^m$, computed element-wise:

$$z_i = y_i + b_i \quad (7.2)$$

Element-wise (Hadamard) Product:

Given two vectors $\mathbf{a}, \mathbf{b} \in \mathbb{R}^m$, their Hadamard product is a vector $\mathbf{c} = \mathbf{a} \odot \mathbf{b} \in \mathbb{R}^m$, computed element-wise:

$$c_i = a_i \cdot b_i \quad (7.3)$$

This operation is notably used in LSTM cells to apply gate activations (Section 2.4.3).

Vector Concatenation:

Given two vectors $\mathbf{a} \in \mathbb{R}^{d_a}$ and $\mathbf{b} \in \mathbb{R}^{d_b}$, their concatenation $\mathbf{c} = [\mathbf{a}; \mathbf{b}]$ results in a vector $\mathbf{c} \in \mathbb{R}^{d_a+d_b}$ formed by stacking the elements of \mathbf{b} below the elements of \mathbf{a} . This is used in Bi-LSTMs (Equation 2.17) and Multi-Head Attention (Equation 2.21).

Matrix Transpose:

The transpose of a matrix $A \in \mathbb{R}^{m \times n}$, denoted $A^T \in \mathbb{R}^{n \times m}$, is obtained by swapping its rows and columns:

$$(A^T)_{ij} = A_{ji} \quad (7.4)$$

This is used in the Scaled Dot-Product Attention formula (Equation 2.19).

7.5.2 Activation Functions

Activation functions introduce non-linearity into neural network models, allowing them to learn complex patterns. They are typically applied element-wise to the output of a linear transformation $z = Wx + b$.

Sigmoid Function (σ):

The standard sigmoid function maps any real input to the range $(0, 1)$. It is defined as:

$$\sigma(z) = \frac{1}{1 + e^{-z}} \quad (7.5)$$

Due to its output range, it is commonly used for gating mechanisms in LSTMs (Equations 2.11, 2.12, 2.15) and for producing probabilities in binary classification outputs. A plot is shown in Figure 7.1.

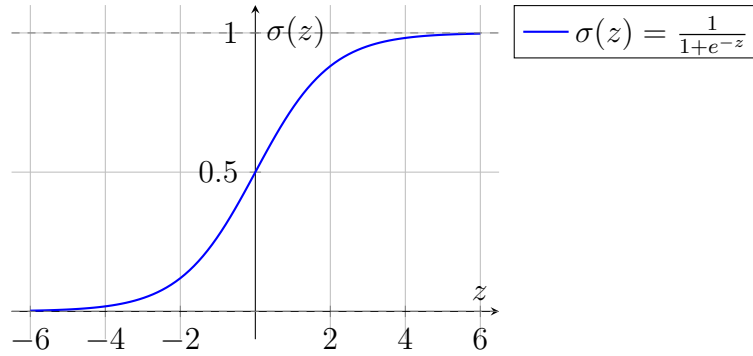


Figure 7.1: The Sigmoid activation function.

Hyperbolic Tangent Function (\tanh):

The hyperbolic tangent function maps any real input to the range $(-1, 1)$. It is defined as:

$$\tanh(z) = \frac{e^z - e^{-z}}{e^z + e^{-z}} = 2\sigma(2z) - 1 \quad (7.6)$$

It is frequently used as the main activation function for hidden states in RNNs and LSTMs (e.g., Equations 2.9, 2.13, 2.16). See Figure 7.2.

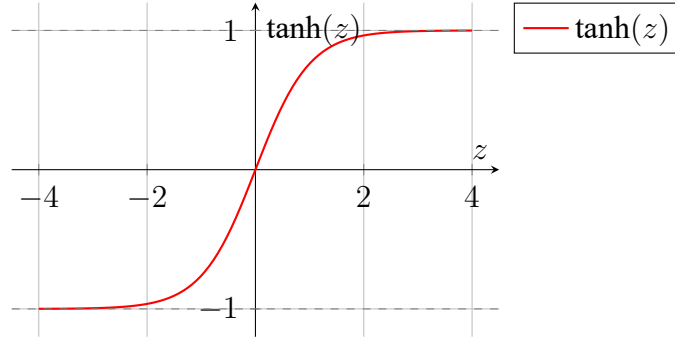


Figure 7.2: The Hyperbolic Tangent (tanh) activation function.

Rectified Linear Unit (ReLU):

The ReLU function outputs the input directly if it is positive, and zero otherwise. It is defined as:

$$\text{ReLU}(z) = \max(0, z) \quad (7.7)$$

ReLU is widely used in deep learning due to its simplicity and effectiveness in mitigating the vanishing gradient problem for positive inputs. It is used within the model presented in this thesis (Section 2.4.3 refers to the code using it). See Figure 7.3.

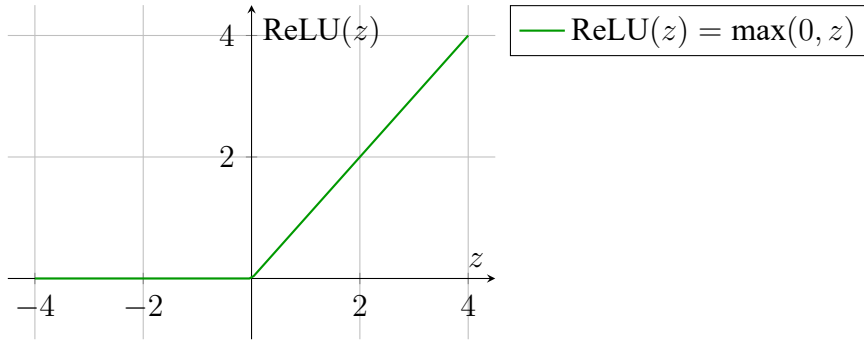


Figure 7.3: The Rectified Linear Unit (ReLU) activation function.

Softmax Function:

The softmax function converts a vector of K real numbers $\mathbf{z} = (z_1, \dots, z_K)$ into a probability distribution consisting of K probabilities. The function is applied to the entire vector and the i -th element of the output vector is calculated as:

$$\text{softmax}(\mathbf{z})_i = \frac{e^{z_i}}{\sum_{j=1}^K e^{z_j}} \quad \text{for } i = 1, \dots, K \quad (7.8)$$

The outputs are non-negative and sum to 1 ($\sum_{i=1}^K \text{softmax}(z)_i = 1$).

Softmax is commonly used in the output layer of multi-class classification models and plays a crucial role in normalizing scores into attention weights in the Attention mechanism (Equation 2.19).

7.5.3 Distance and Similarity Metrics

These metrics quantify the difference or similarity between vectors, which is fundamental in many machine learning tasks like clustering, nearest neighbour search, and evaluating embedding spaces. Let $\mathbf{a}, \mathbf{b} \in \mathbb{R}^d$ be two vectors of dimension d .

Euclidean Distance (L2 Distance):

The most common distance measure, representing the straight-line distance between two points in Euclidean space. It is the L2 norm of the difference between the vectors:

$$d_{\text{Euclidean}}(\mathbf{a}, \mathbf{b}) = \|\mathbf{a} - \mathbf{b}\|_2 = \sqrt{\sum_{i=1}^d (a_i - b_i)^2} \quad (7.9)$$

Manhattan Distance (L1 Distance):

Measures the distance by summing the absolute differences of the vector components. It corresponds to the distance travelled along axes at right angles (like navigating city blocks). It is the L1 norm of the difference:

$$d_{\text{Manhattan}}(\mathbf{a}, \mathbf{b}) = \|\mathbf{a} - \mathbf{b}\|_1 = \sum_{i=1}^d |a_i - b_i| \quad (7.10)$$

Cosine Similarity:

Measures the cosine of the angle between two non-zero vectors, indicating their orientation similarity irrespective of their magnitude. It ranges from -1 (exactly opposite) through 0 (orthogonal) to 1 (exactly the same direction). It is calculated using the dot product and

vector magnitudes (L2 norms):

$$\text{CosineSimilarity}(\mathbf{a}, \mathbf{b}) = \frac{\mathbf{a} \cdot \mathbf{b}}{\|\mathbf{a}\|_2 \|\mathbf{b}\|_2} = \frac{\sum_{i=1}^d a_i b_i}{\sqrt{\sum_{i=1}^d a_i^2} \sqrt{\sum_{i=1}^d b_i^2}} \quad (7.11)$$

Cosine similarity is widely used for comparing high-dimensional vectors, such as text document embeddings or feature vectors, where magnitude might be less important than orientation. Note that while similarity increases as the value approaches 1, Cosine Distance is sometimes defined as $1 - \text{CosineSimilarity}(\mathbf{a}, \mathbf{b})$.

7.5.4 Attention Mechanism Components

The Scaled Dot-Product Attention mechanism (Equation 2.19) relies on several fundamental operations beyond the Softmax function:

Dot Product Similarity:

The compatibility between a query \mathbf{q} and a key \mathbf{k} (both typically vectors of the same dimension d_k) is often computed using the dot product $\mathbf{q} \cdot \mathbf{k} = \mathbf{q}^T \mathbf{k}$. As noted above, this is closely related to Cosine Similarity but does not normalize for vector magnitudes. For matrices Q and K containing multiple queries and keys as rows, the matrix product QK^T computes all pairwise dot products efficiently.

Scaling:

To counteract the effect of large dot product values when the dimension d_k is high, the scores QK^T are scaled down by dividing by $\sqrt{d_k}$ before applying the softmax function. This helps maintain a stable gradient flow during training.

7.5.5 Normalization Techniques

Normalization layers help stabilize training, speed up convergence, and sometimes improve generalization by standardizing layer inputs.

Layer Normalization (LayerNorm):

Layer Normalization normalizes the inputs across the features for *each individual data sample* in a batch, making its computation independent of the batch size. For an input vector \mathbf{x} representing

the features for one sample at a specific layer, LayerNorm computes:

$$\text{LayerNorm}(\mathbf{x}) = \gamma \odot \frac{\mathbf{x} - \mu_{\text{sample}}}{\sqrt{\sigma_{\text{sample}}^2 + \epsilon}} + \beta \quad (7.12)$$

Here, μ_{sample} and σ_{sample}^2 are the mean and variance calculated across the feature dimension(s) of the single input sample \mathbf{x} . γ (scale) and β (shift) are learnable affine transformation parameters of the same dimension as \mathbf{x} , and ϵ is a small constant added for numerical stability. LayerNorm is frequently used in RNNs and Transformers (including the model implemented in this work) where batch statistics might be less stable or meaningful.

Batch Normalization (BatchNorm):

(Included for contrast, delete if not relevant) Batch Normalization normalizes inputs across the *batch dimension* for each feature separately. It calculates the mean μ_{batch} and variance σ_{batch}^2 for each feature across all samples in the current mini-batch. While highly effective in CNNs, its dependence on batch statistics can be less suitable for sequence models with variable lengths or small batch sizes compared to LayerNorm.

7.5.6 Pooling Strategies for Sequences

Pooling layers are used to aggregate information across the time or sequence dimension, often to produce a fixed-size representation from variable-length sequence outputs for downstream tasks like classification. Given a sequence of hidden states $H = [\mathbf{h}_1, \mathbf{h}_2, \dots, \mathbf{h}_T]$, where each $\mathbf{h}_t \in \mathbb{R}^d$:

Mean Pooling:

Calculates the element-wise average of the hidden state vectors across the sequence dimension:

$$\mathbf{h}_{\text{mean_pool}} = \frac{1}{T} \sum_{t=1}^T \mathbf{h}_t \quad (7.13)$$

The resulting vector $\mathbf{h}_{\text{mean_pool}} \in \mathbb{R}^d$ represents the average activation over the sequence. This strategy is used in the implemented model

to summarize the output sequence before the final classification layer.

Max Pooling:

Calculates the element-wise maximum of the hidden state vectors across the sequence dimension:

$$(\mathbf{h}_{\text{max_pool}})_j = \max_{t=1\dots T} (\mathbf{h}_t)_j \quad \text{for } j = 1, \dots, d \quad (7.14)$$

The resulting vector $\mathbf{h}_{\text{max_pool}} \in \mathbb{R}^d$ captures the strongest activation for each feature dimension across the sequence.

7.5.7 Weight Initialization

Initializing the weight parameters of a neural network appropriately is crucial for effective training, helping to prevent issues like vanishing or exploding gradients.

Kaiming (He) Initialization:

Proposed by He et al. (K. He et al., 2015), this method is primarily designed for layers followed by Rectified Linear Unit (ReLU) activations. It accounts for the non-linearity of ReLU. For Kaiming Normal initialization (used in the implemented model via ``kaiming_normal``), $\text{weights} W$ are drawn from a normal distribution $\mathcal{N}(0, \text{std}^2)$, where:

$$\text{std} = \sqrt{\frac{2}{\text{fan_in}}} \quad (7.15)$$

Here, ``fan_in`` is the number of input units to the weight tensor. A variant considers the non-linearity slope a of leaky ReLU (where $a = 0$ for standard ReLU).

Xavier (Glorot) Initialization:

Proposed by Glorot and Bengio (Glorot & Bengio, 2010), this method aims to keep the variance of activations and gradients roughly constant across layers, particularly effective for symmetric activations like tanh or sigmoid. For Xavier Normal initialization, $\text{weights} W$ are drawn from $\mathcal{N}(0, \text{std}^2)$, where:

$$\text{std} = \sqrt{\frac{2}{\text{fan_in} + \text{fan_out}}} \quad (7.16)$$

fan_{out} is the number of output units. Uniform versions also exist for both Kaiming and Xavier initialization.

7.5.8 Optimization Algorithms and Refinements

Optimization algorithms iteratively update model parameters θ to minimize a loss function $J(\theta)$.

Stochastic Gradient Descent (SGD):

A fundamental algorithm that updates parameters based on the gradient of the loss computed on a small batch (or single sample) of data at iteration k .

$$\theta_{k+1} = \theta_k - \eta \nabla J(\theta_k; \mathbf{x}^{(i)}; \mathbf{y}^{(i)}) \quad (7.17)$$

where η is the learning rate and $\nabla J(\dots)$ is the gradient computed on a mini-batch $(\mathbf{x}^{(i)}, \mathbf{y}^{(i)})$. Variants include momentum or Nesterov momentum.

Adam Optimizer:

An adaptive learning rate optimization algorithm that computes individual adaptive learning rates for different parameters using estimates of first and second moments of the gradients (Kingma & Ba, 2014). It often converges faster than basic SGD. The update rules involve computing biased moment estimates $(\mathbf{m}_t, \mathbf{v}_t)$, bias-corrected estimates $(\hat{\mathbf{m}}_t, \hat{\mathbf{v}}_t)$, and then updating parameters:

$$\theta_{t+1} = \theta_t - \frac{\eta}{\sqrt{\hat{\mathbf{v}}_t} + \epsilon} \hat{\mathbf{m}}_t \quad (7.18)$$

Adam is used for training the model in this work.

Learning Rate Scheduling:

Techniques used to adjust the learning rate η during training, which can improve convergence and final model performance.

- *ReduceLROnPlateau*: Monitors a specified metric (e.g., validation loss). If the metric does not improve for a defined number of 'patience' epochs, the learning rate is reduced by a multiplicative 'factor'. This strategy is employed in the training procedure of this thesis.

- *Step Decay*: Reduces the learning rate by a fixed factor every specified number of epochs.
- *Cosine Annealing*: Gradually decreases the learning rate following a cosine curve shape over a specified number of epochs or iterations.

7.5.9 Loss Functions

Loss functions quantify the difference between the model's predictions and the true target values, guiding the optimization process.

Binary Cross-Entropy (BCE):

Used for binary classification tasks where the model outputs a probability \hat{p}_i for the positive class (true label $y_i \in \{0,1\}$). It is the loss function used in the model training for this thesis.

$$\text{BCE} = -\frac{1}{N} \sum_{i=1}^N [y_i \log(\hat{p}_i) + (1 - y_i) \log(1 - \hat{p}_i)] \quad (7.19)$$

7.5.10 Regularization Techniques

Regularization techniques are used to prevent overfitting by adding constraints or penalties to the model or its training process.

L2 Regularization (Weight Decay):

Adds a penalty to the loss function proportional to the squared magnitude of the model weights θ .

$$J_{reg}(\theta) = J(\theta) + \frac{\lambda}{2} \|\theta\|_2^2 = J(\theta) + \frac{\lambda}{2} \sum_i \theta_i^2 \quad (7.20)$$

where λ is the regularization strength. This encourages smaller weights.

Dropout:

During training, randomly sets a fraction of neuron activations (outputs) to zero at each forward pass before the subsequent layer (Srivastava et al., 2014). This prevents units from overly co-adapting and can be interpreted as training an ensemble of thinned networks.

The dropout rate (e.g., 0.3 in the implemented model) specifies the probability of an element being zeroed out. At test time, dropout is turned off, and sometimes the outputs of the kept units are scaled down by the dropout rate (though often handled implicitly by libraries or absorbed into subsequent layers). Dropout is used in both the LSTM layers and the final fully connected block in the implemented model.

7.5.11 Data Handling for Sequences

Sequence Padding:

Neural networks typically require inputs within a batch to be tensors of uniform shape. Since sequential data (like manufacturing process steps or natural language sentences) often has varying lengths, techniques are needed to handle this during batch processing. Padding involves augmenting shorter sequences within a batch with special padding values (often zero) until they reach the length of the longest sequence in that batch. This results in rectangular tensors suitable for processing. The `collate_fn` used in the data loading pipeline for this thesis is

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