

Algorithms Lab HS22
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cadmo.ethz.ch/education/lectures/HS22/algolab

Exercise - Even pairs

You are part of a team to develop a new kind of pseudorandom number generator (PRNG). To gauge how good your algorithm is at producing random sequences of bits, you are running several different statistical tests.

For example, if x_0, \ldots, x_{n-1} was a truly random sequence of bits, then it would have the property that the sum $x_i + \cdots + x_j$ is even for about half of the pairs $0 \le i \le j < n$ (and odd for the other half).

To check whether this is the case, if x_0, \ldots, x_{n-1} are generated by your PRNG, you need to be able to count the number of pairs $0 \le i \le j < n$ for which the sum is even.

Input The first line of the input contains the number $t \le 30$ of test cases. Each of the t test cases is described as follows.

- It starts with a line that contains an integer n, such that $1 \le n \le 5 \cdot 10^4$.
- The following line contains n integers $x_0 \dots x_{n-1}$, separated by a space, such that $x_i \in \{0, 1\}$, for all $i \in \{0, \dots, n-1\}$.

Output For each test case output a single line containing the number of pairs $0 \le i \le j < n$ such that the sum $x_i + \cdots + x_j$ is even.

Points There are three groups of test sets, worth 100 points in total.

- 1. For the first group of test sets, worth 40 points, you may assume that $1 \le n \le 200$.
- 2. For the second group of test sets, worth 40 points, you may assume that $1 \le n \le 5000$.
- 3. For the third group of test sets, worth 20 points, there are no additional assumptions.

Corresponding sample test sets are contained in testi.in/out, for $i \in \{1, 2, 3\}$.

Sample Input	Sample Output
2	4
4	6
0 1 1 1	
3	
0 0 0	