

Spec2Vec

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Energy based non-linear
Calibration in NIRS

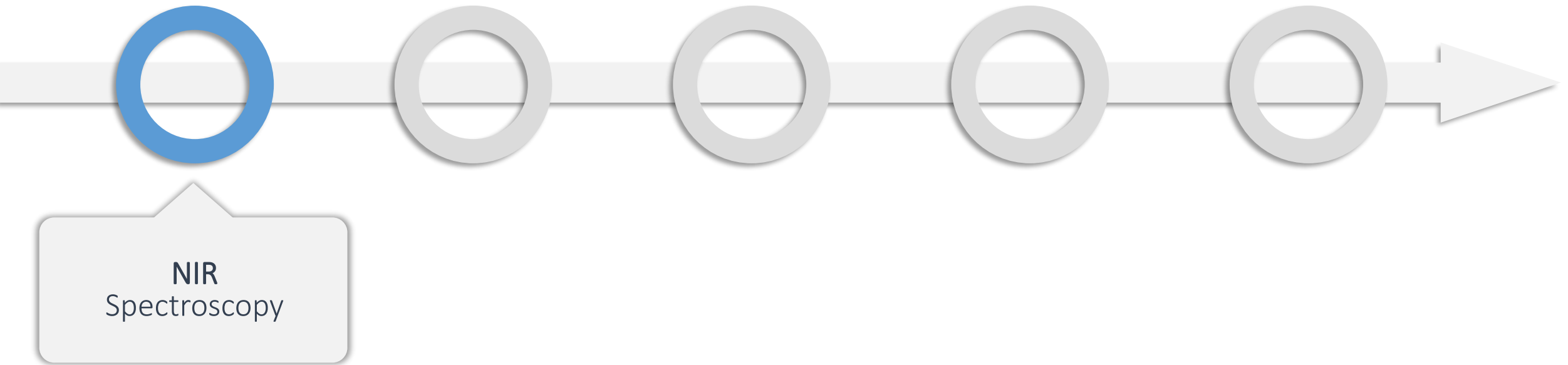
2022-06-21



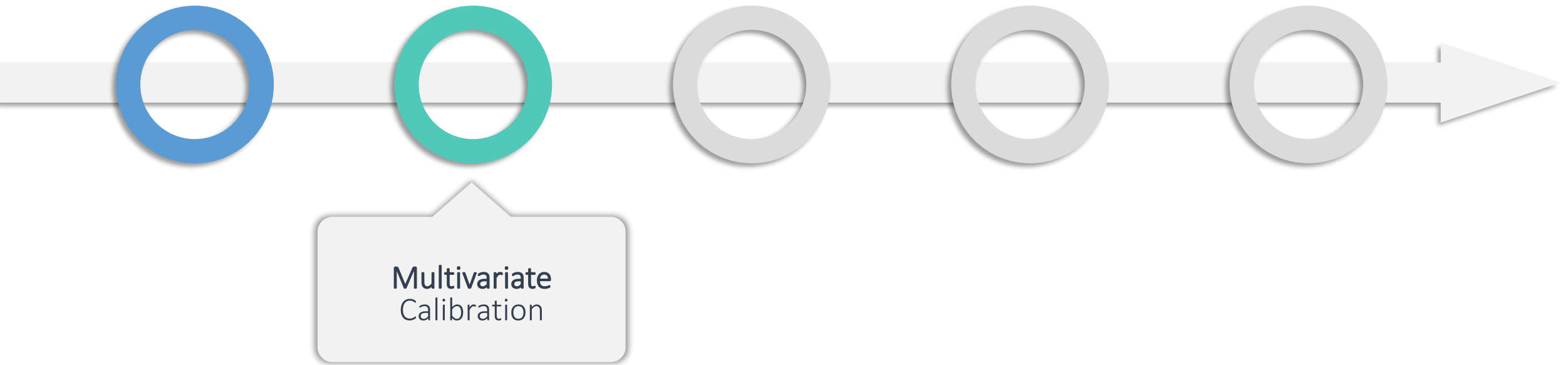
Abstract

The success of multivariate calibration depends on the generalizability of the underlying regression models, for which the spectral features are usually decorrelated in a preliminary step. In order to also allow the application of deep neural networks like transformers, this presentation introduces a powerful approach to highly non-linear decorrelation of spectral features using deep energy based modeling.

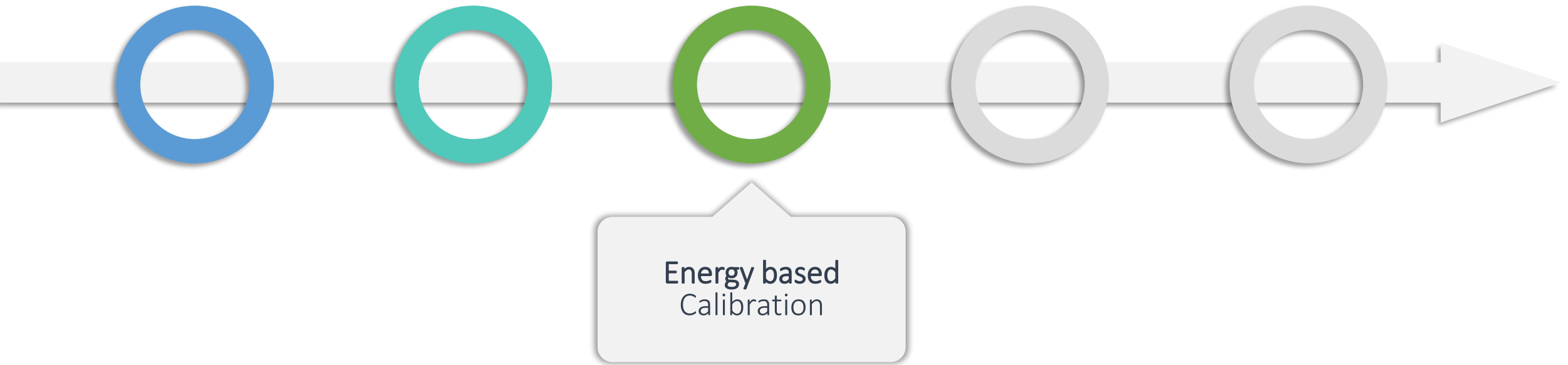
Outline



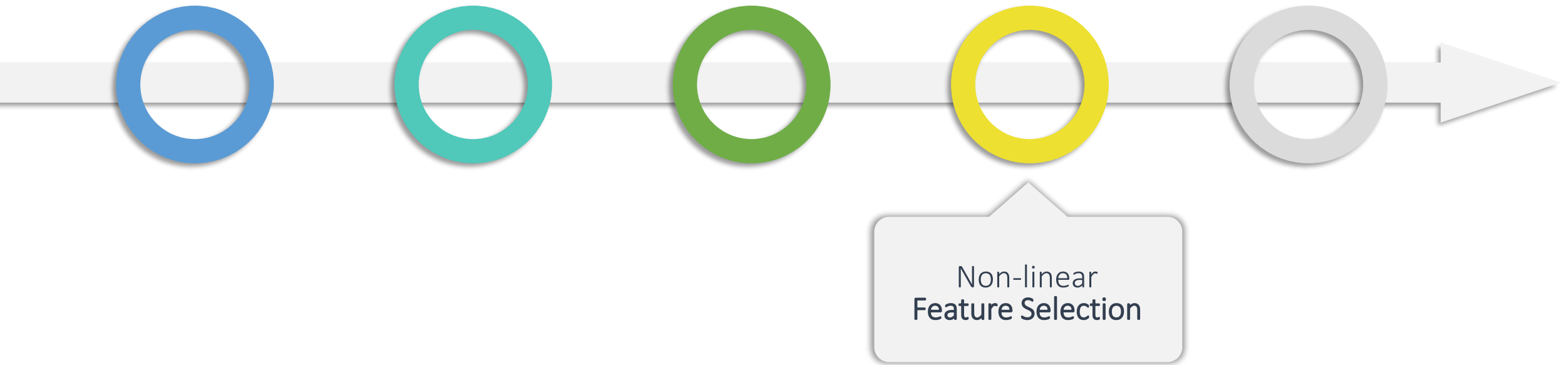
Outline



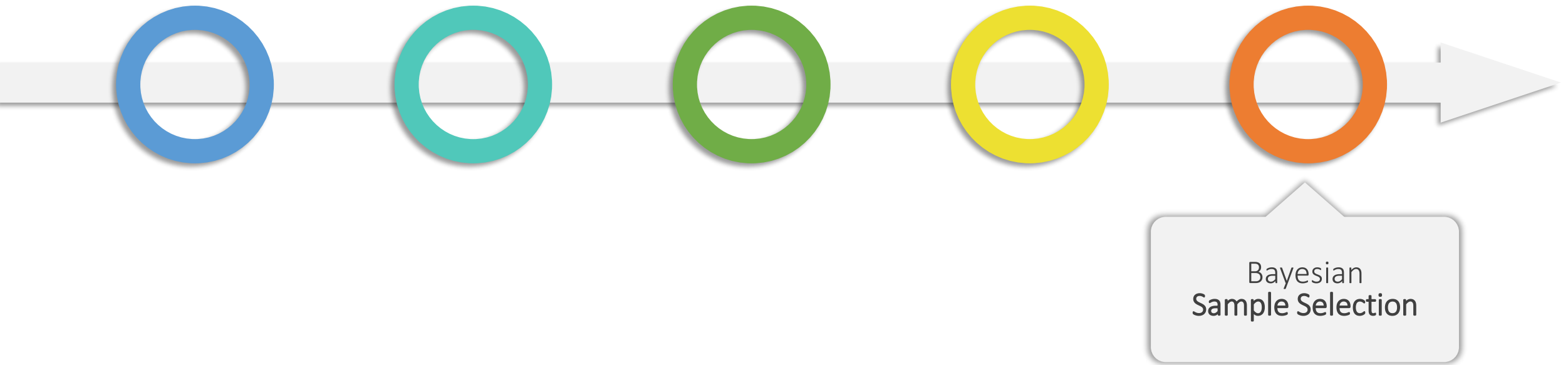
Outline



Outline



Outline



Part 1

NIR Spectroscopy

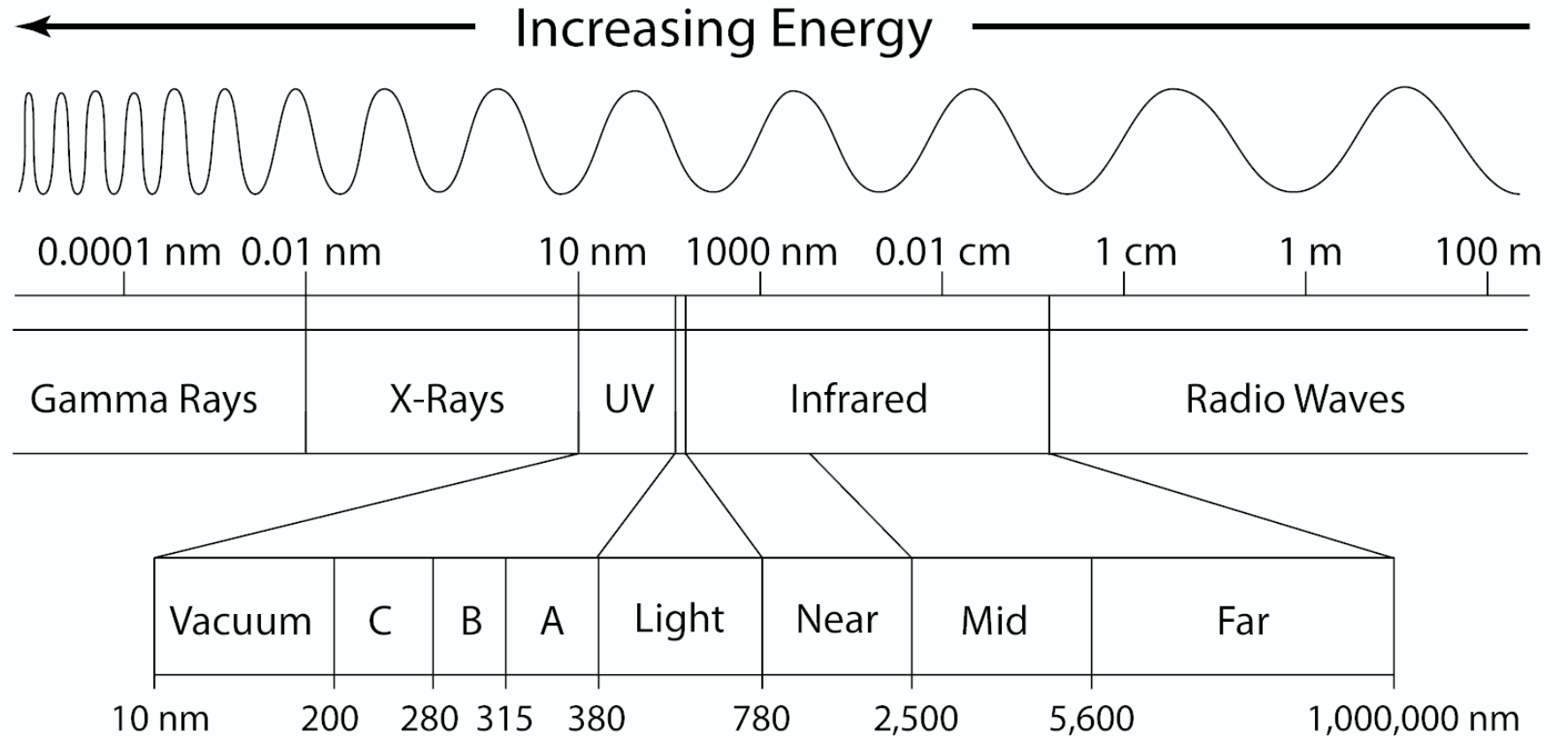


What is **NIR**?

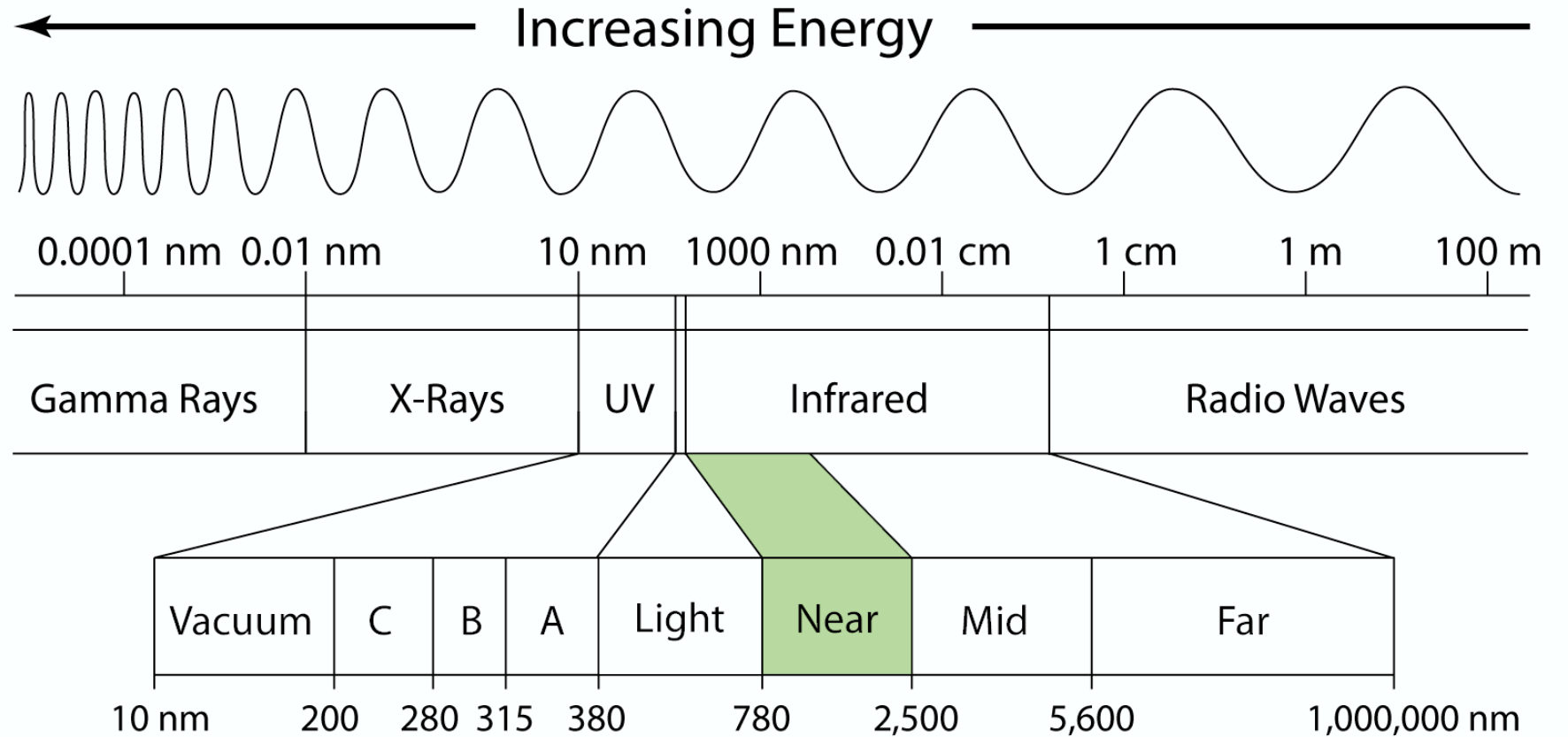


NIR = Near Infrared

Region in the
EM spectrum



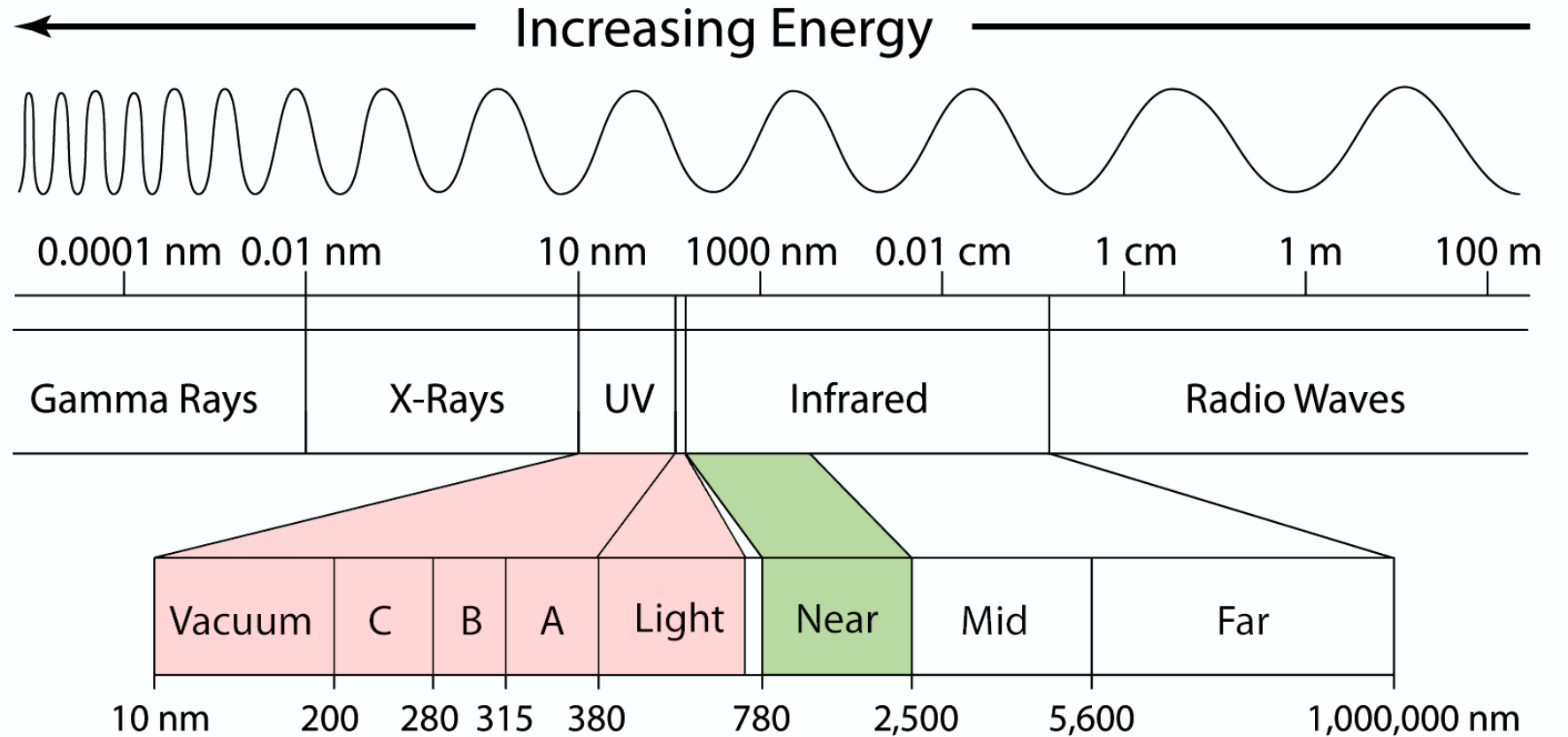
Ranging
from ~780nm
to ~2500nm



Ranging

No Atomic Spectral Lines

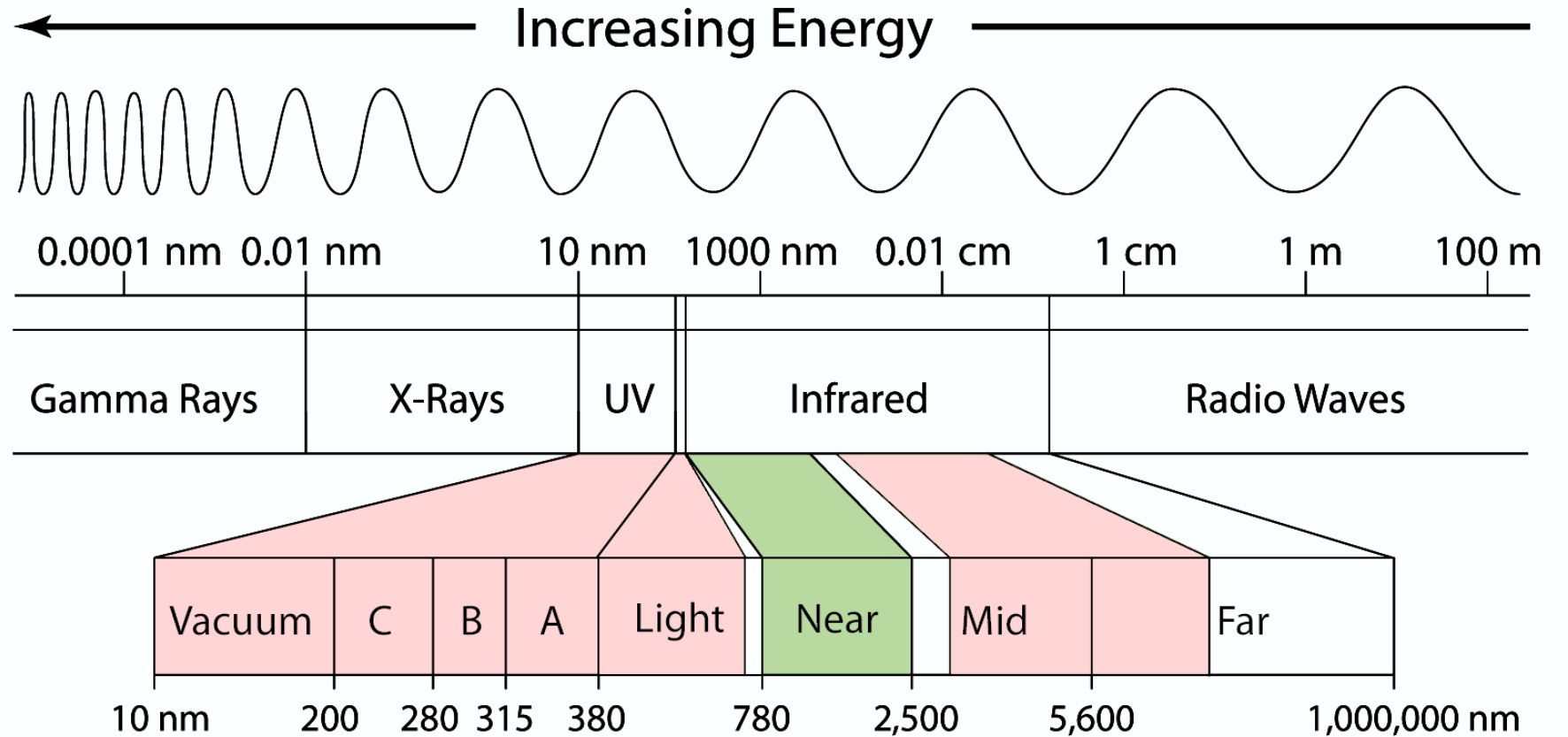
Eigenstates have transitions at typical wavelengths: ~10nm to ~750nm

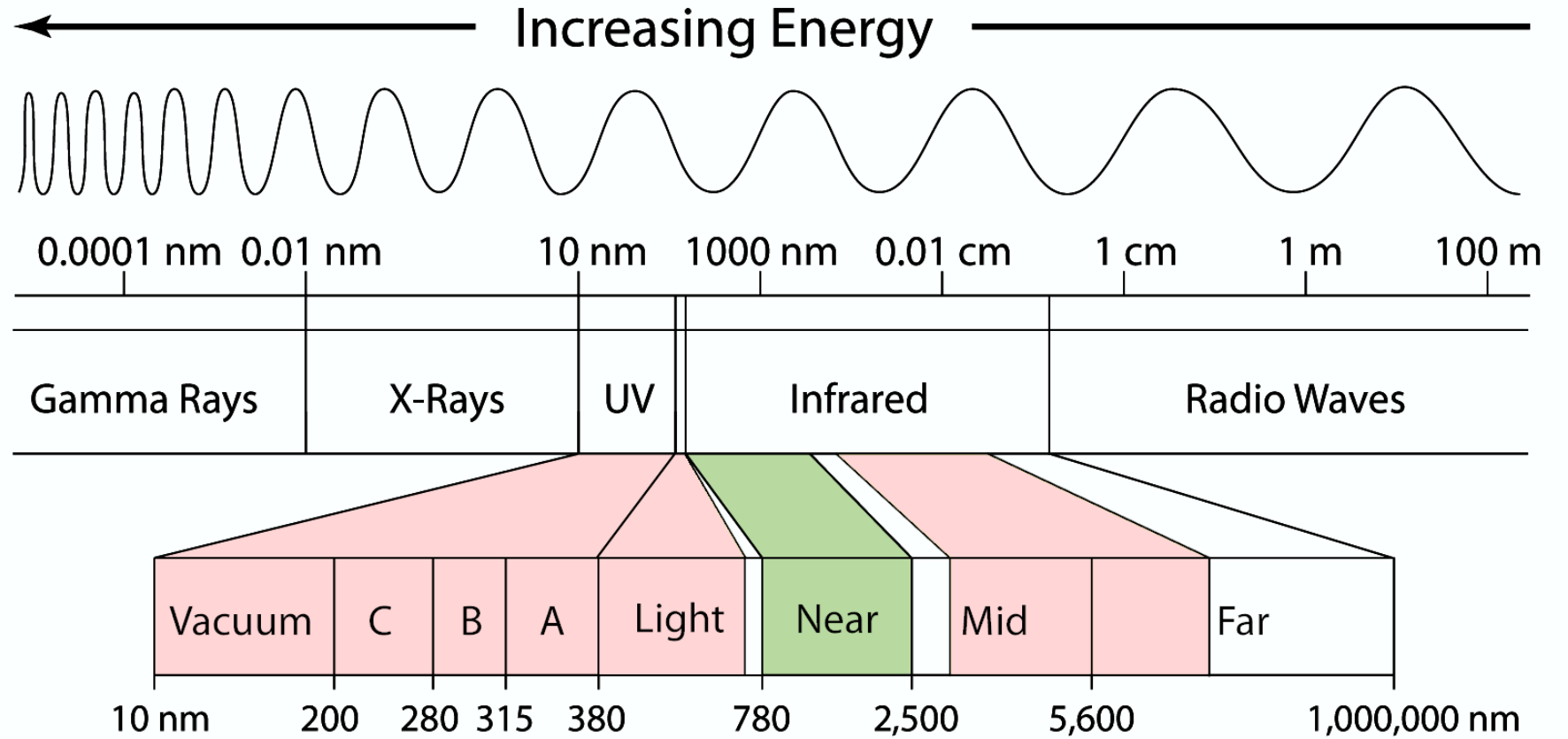
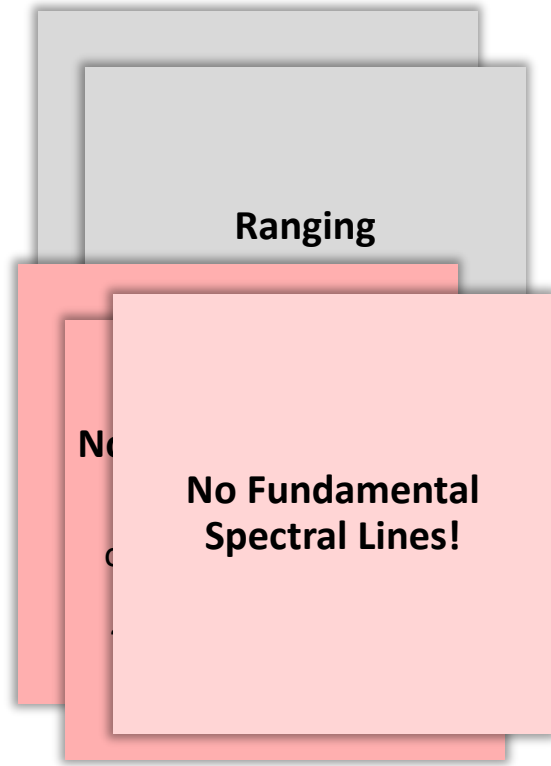


Ranging

**No
Molecule Vibrations**

Eigenfrequencies
of bonds are typically at
wavelengths:
~3000nm to ~30000nm



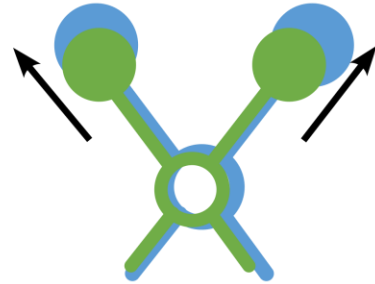


Ranging

Vibrational Overtones

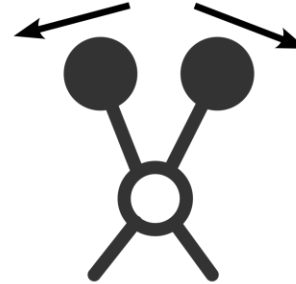
Vibration modes provide higher modes. *2nd* modes are about 10-100x weaker than fundamental modes

Stretching Vibrations



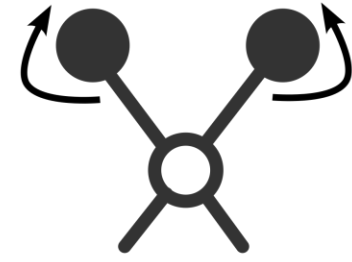
Symmetric Stretching

XY-Bending Vibrations

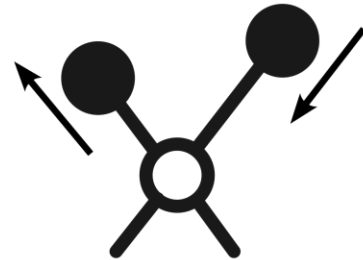


Scissoring

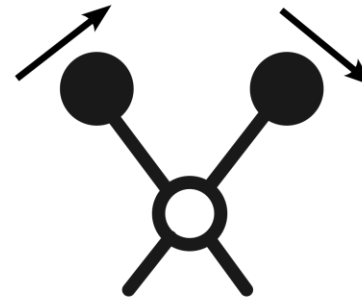
XZ-Bending Vibrations



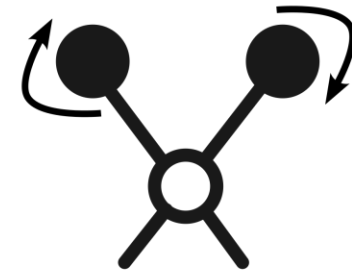
Wagging



Asymmetric Stretching



Rocking



Twisting

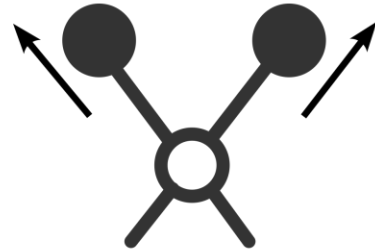


Ranging

Combination Modes

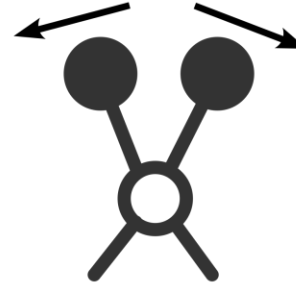
12 possible pairwise combinations of fundamental modes with highly unspecific (broad) bands

Stretching Vibrations



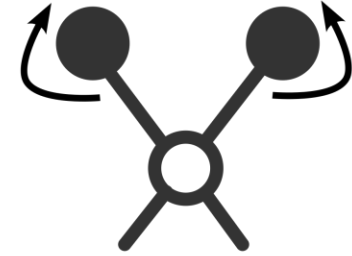
Symmetric Stretching

XY-Bending Vibrations



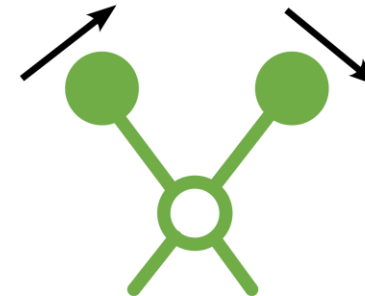
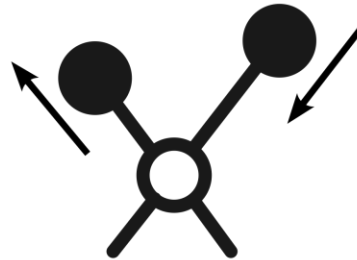
Scissoring

XZ-Bending Vibrations

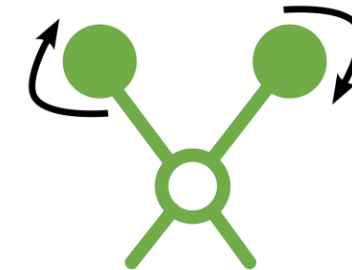


Wagging

Asymmetric Stretching



Rocking



Twisting



What can be concluded
about **NIR**?

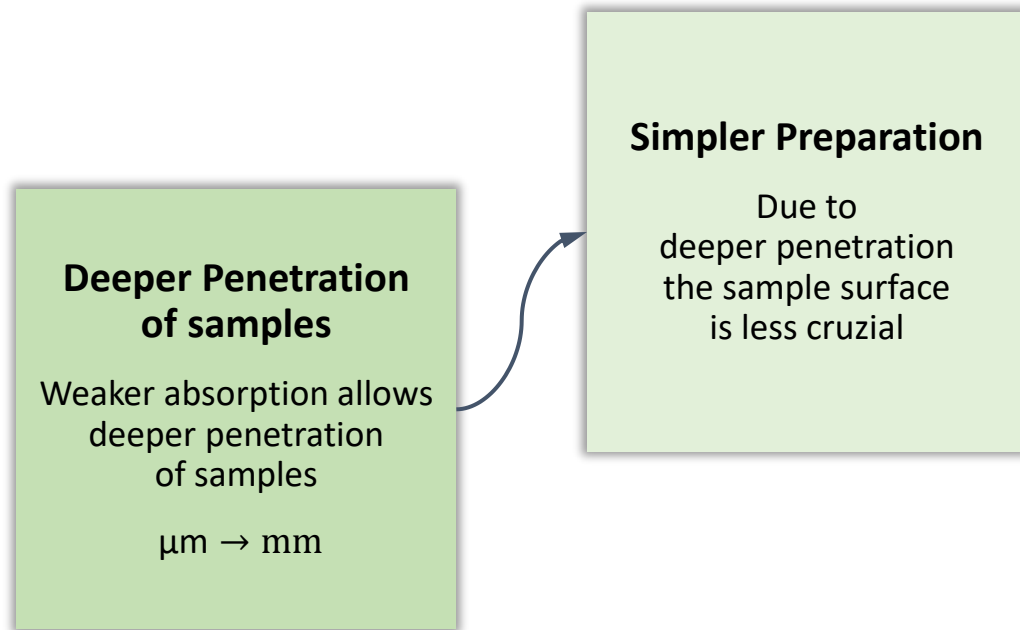


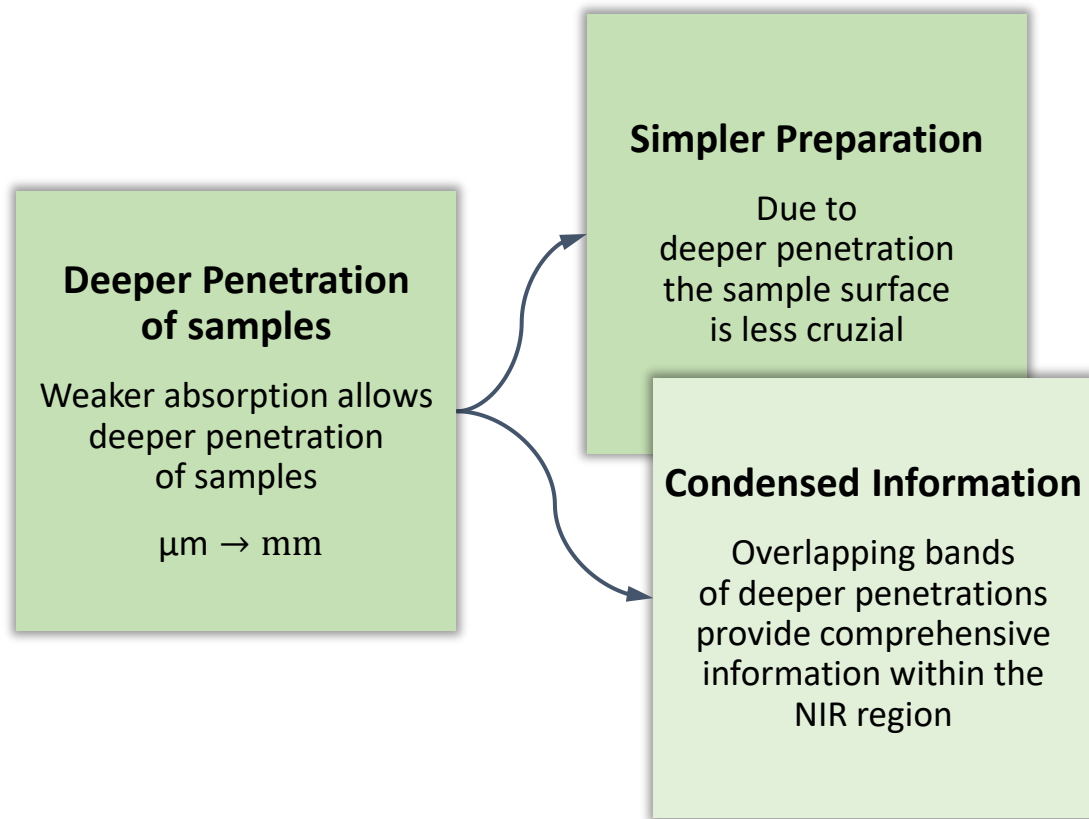
Deeper Penetration of samples

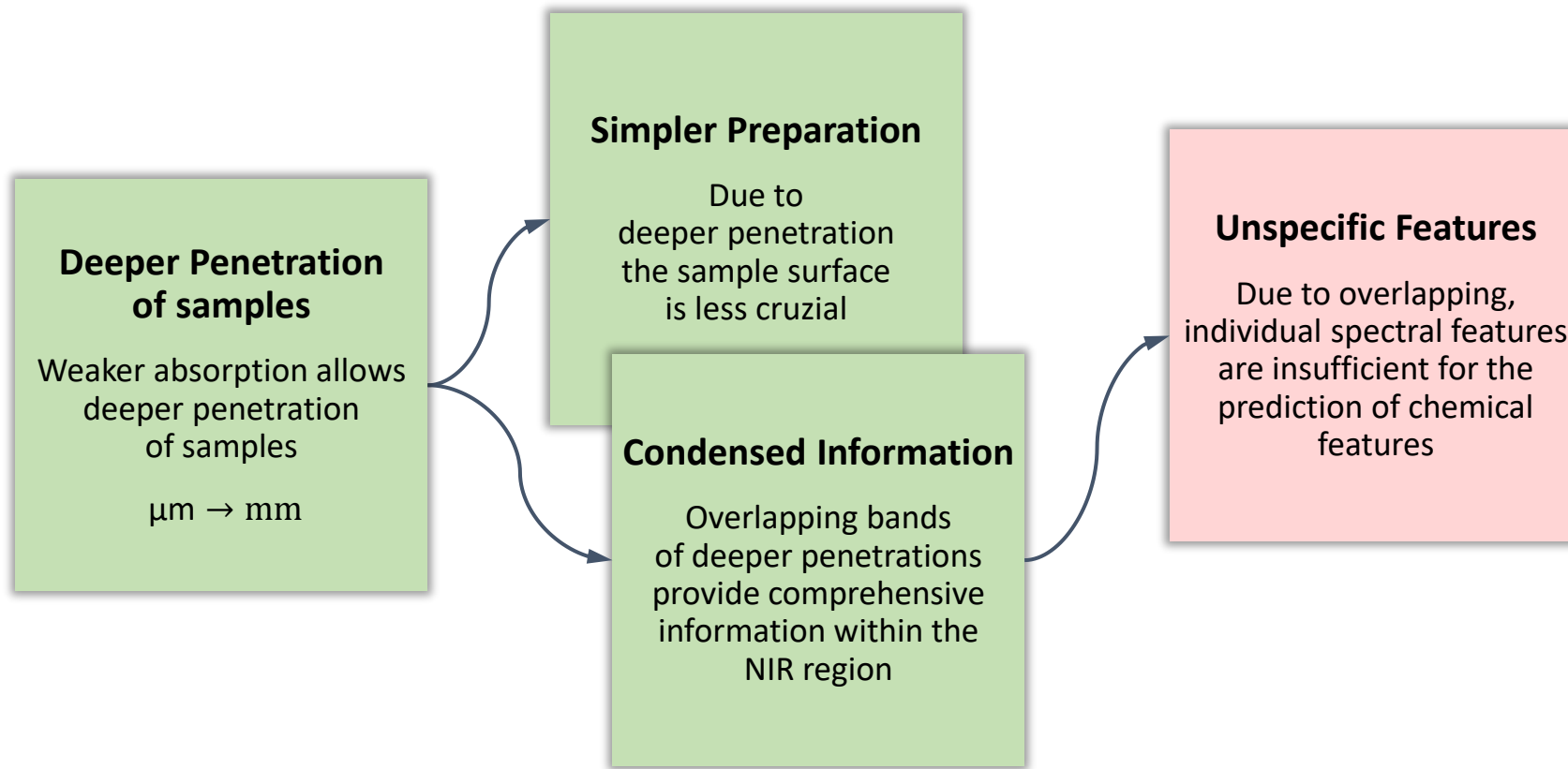
Weaker absorption allows
deeper penetration
of samples

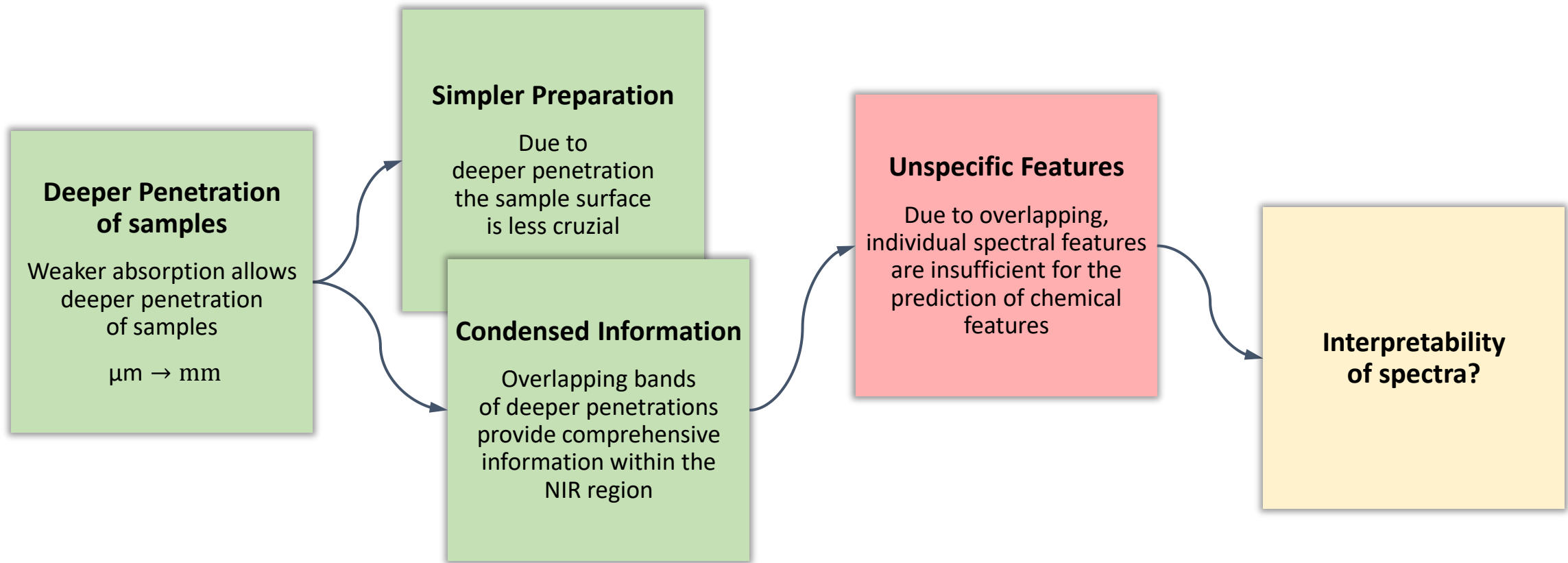
$\mu\text{m} \rightarrow \text{mm}$











Part 2

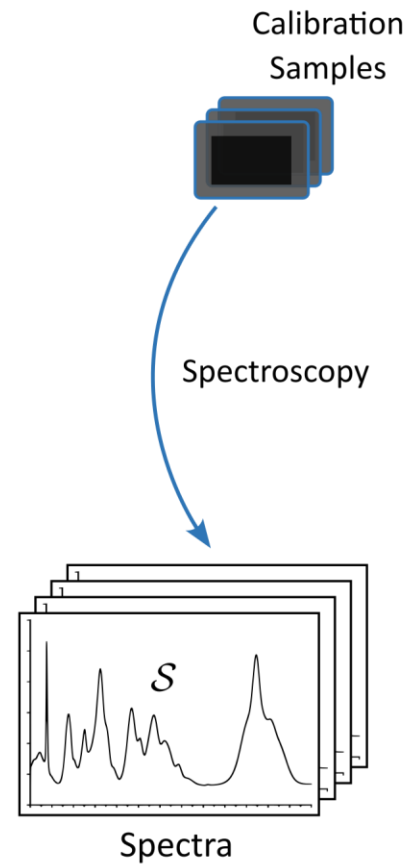
Multivariate Calibration



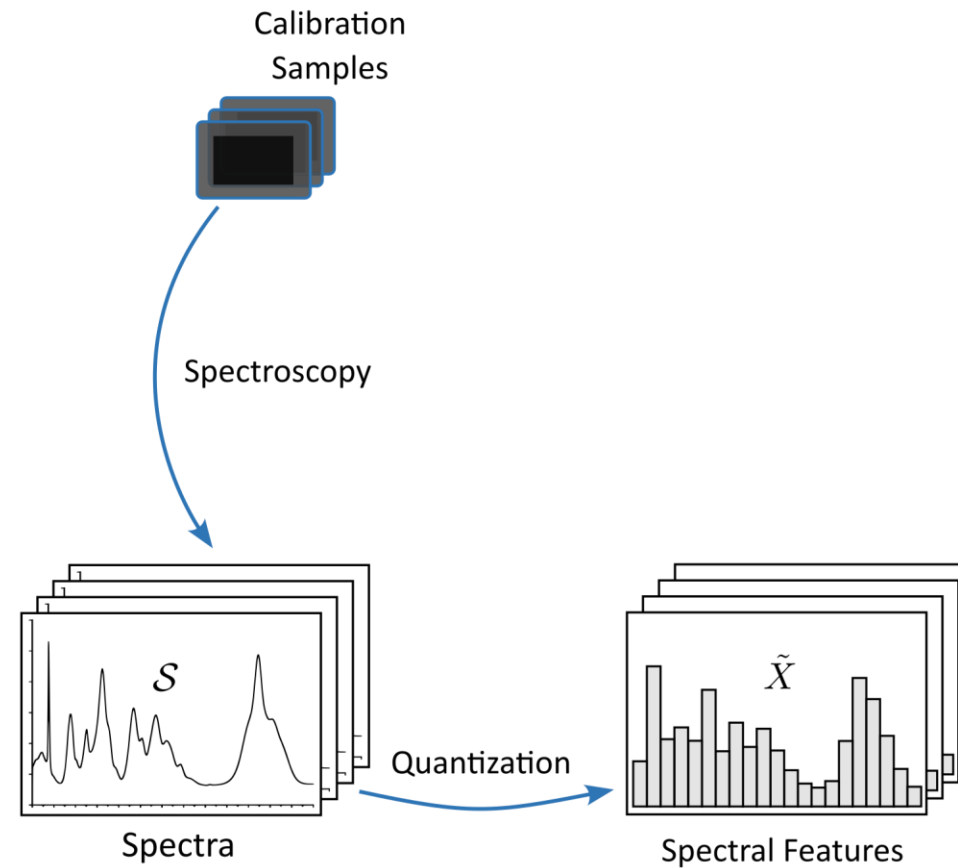
What is the **General Setup**?



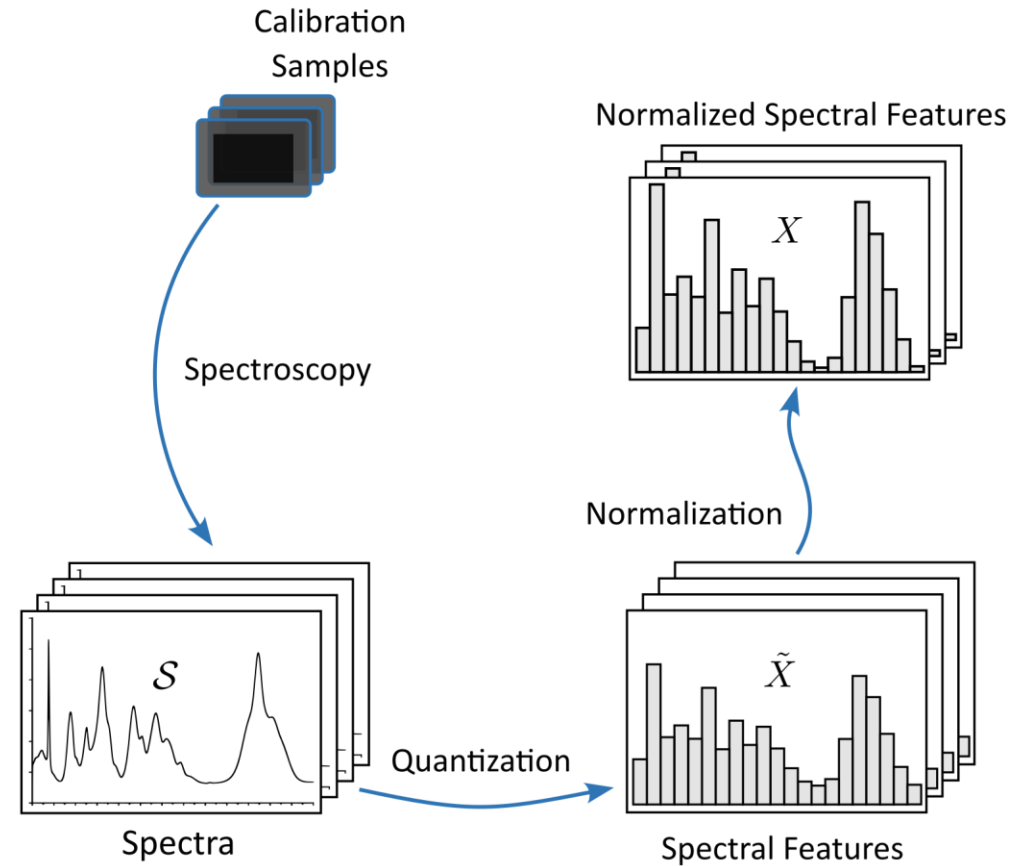
1. Spectroscopy



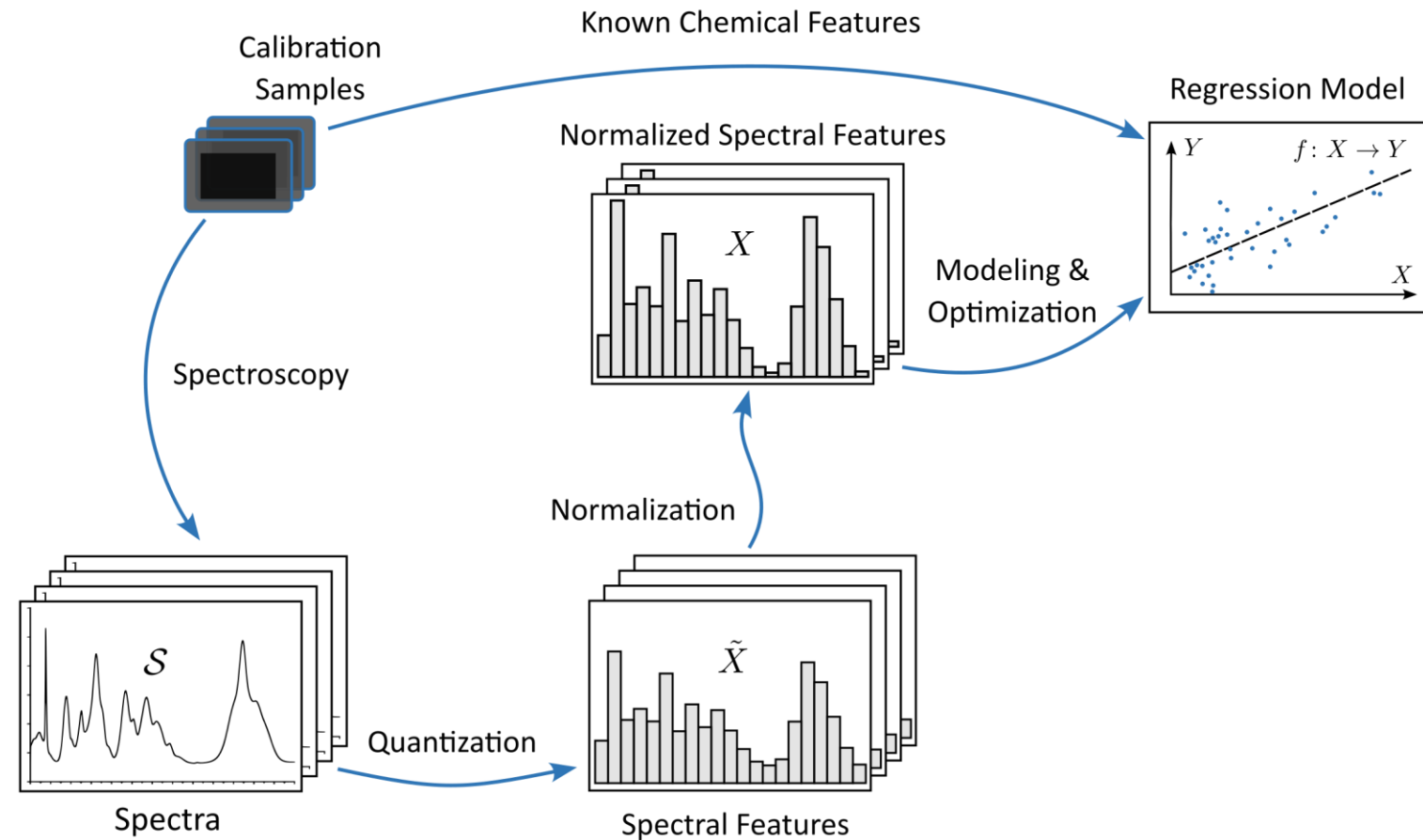
1. Spectroscopy
2. Quantization



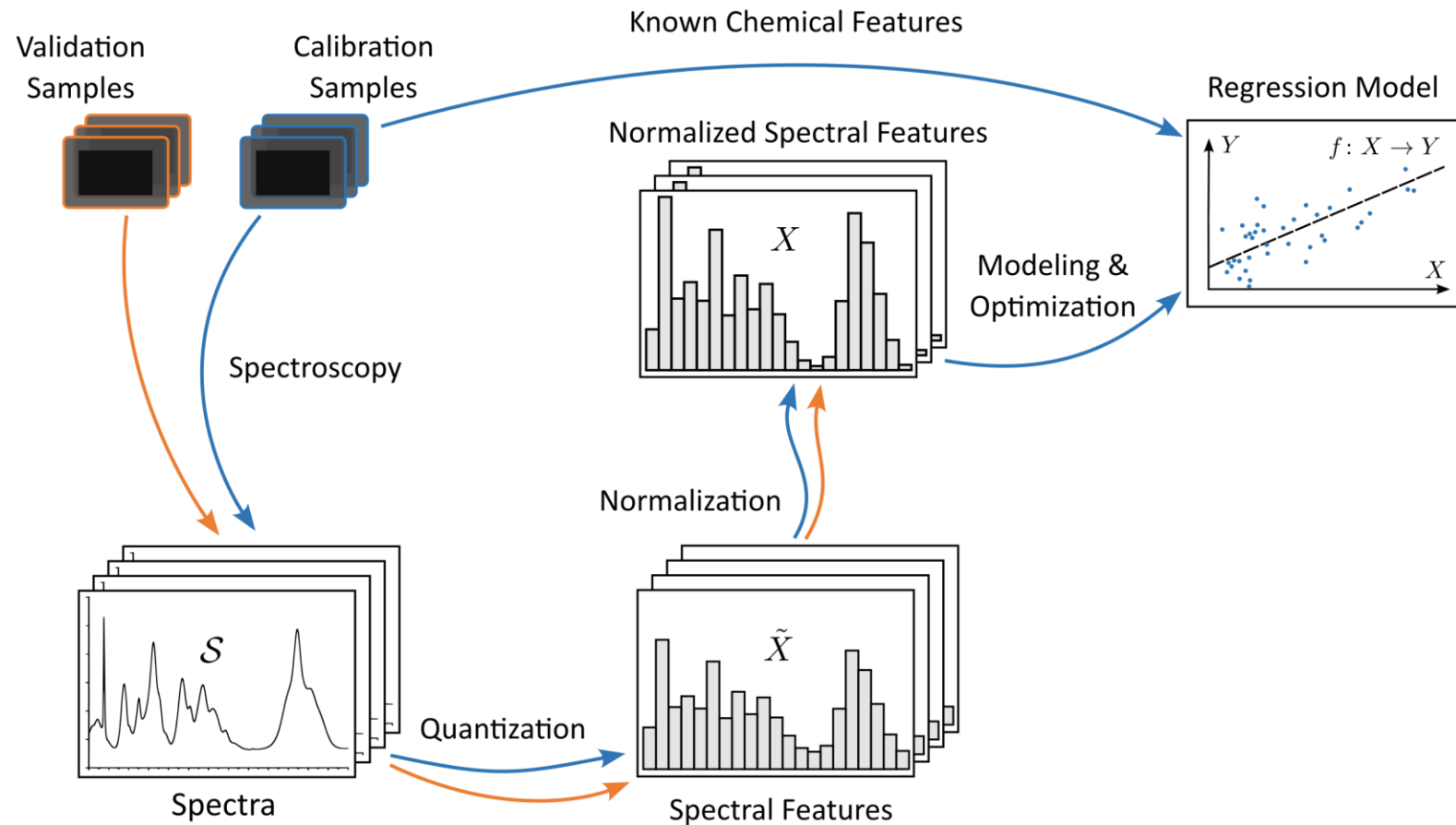
1. Spectroscopy
2. Quantization
3. Normalization



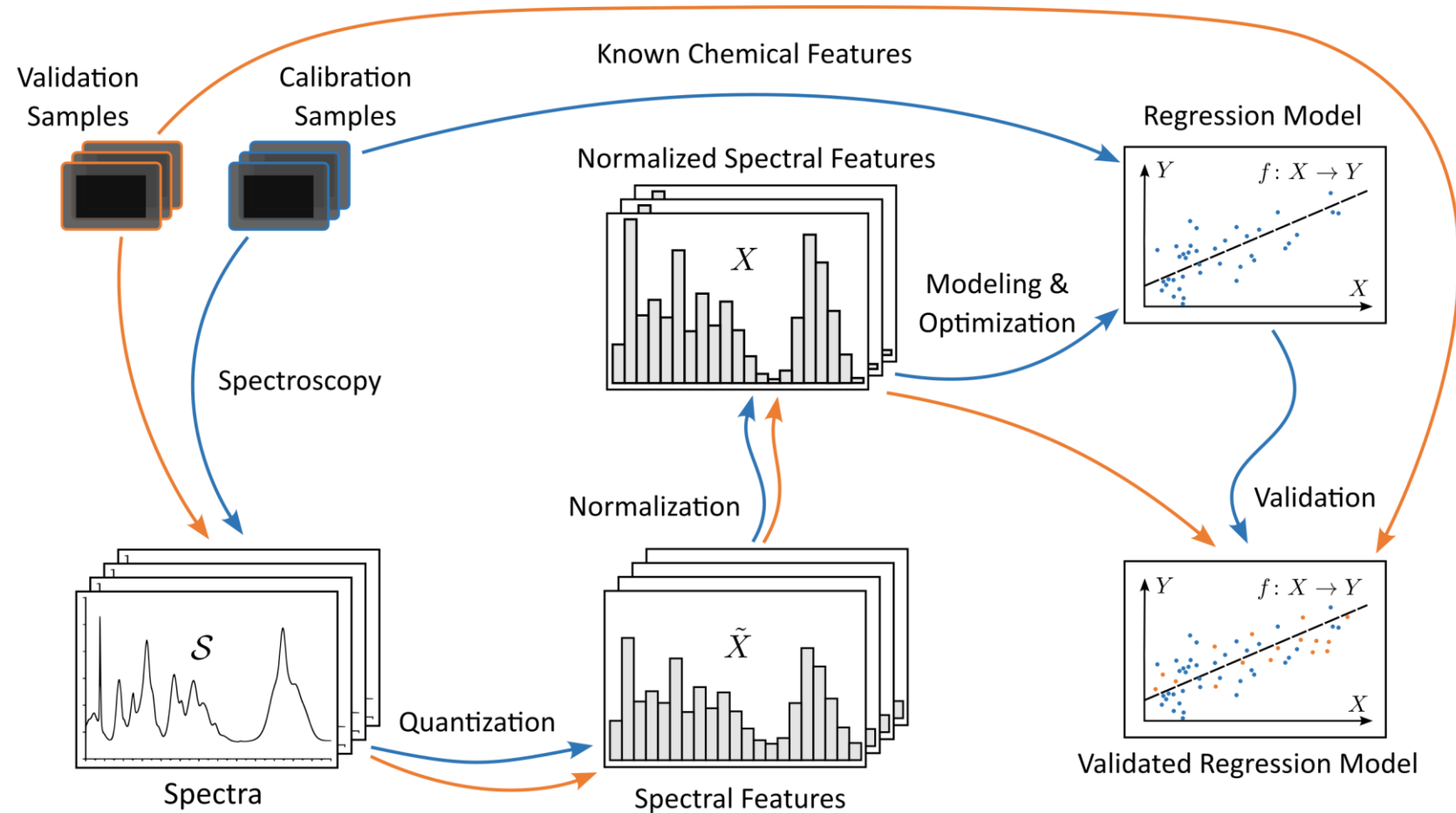
1. Spectroscopy
2. Quantization
3. Normalization
4. Modeling & Optimization



1. Spectroscopy
2. Quantization
3. Normalization
4. Modeling & Optimization
5. Validation



1. Spectroscopy
2. Quantization
3. Normalization
4. Modeling & Optimization
5. Validation



What are the tools in
Statistical Modeling?



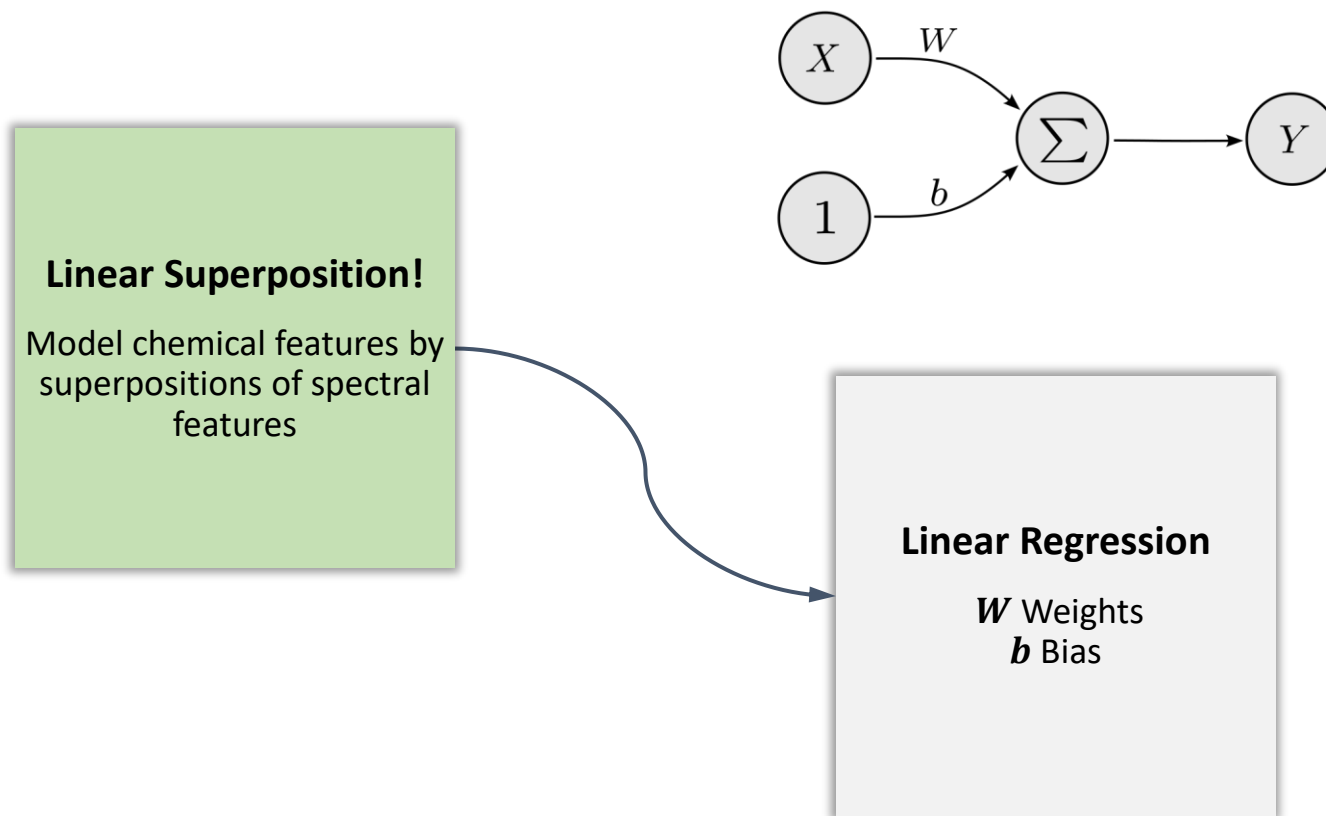
Approach 1: *Multiple Linear Regression*

Linear Superposition!

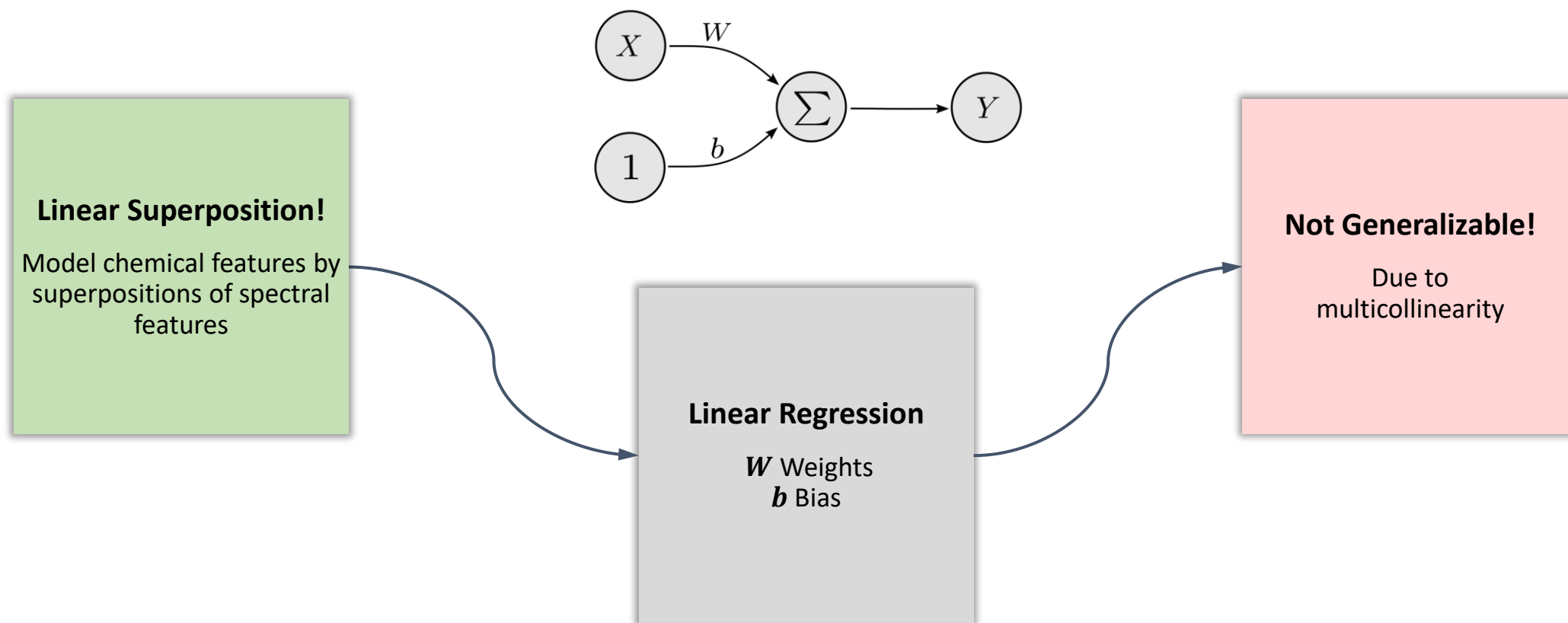
Model chemical features by
superpositions of spectral
features



Approach 1: Multiple Linear Regression



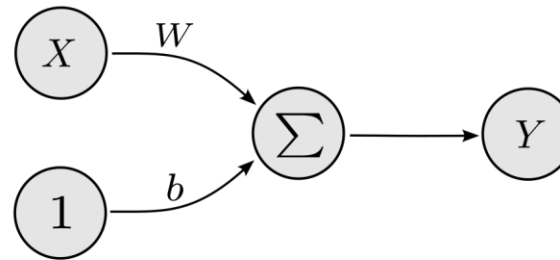
Approach 1: Multiple Linear Regression



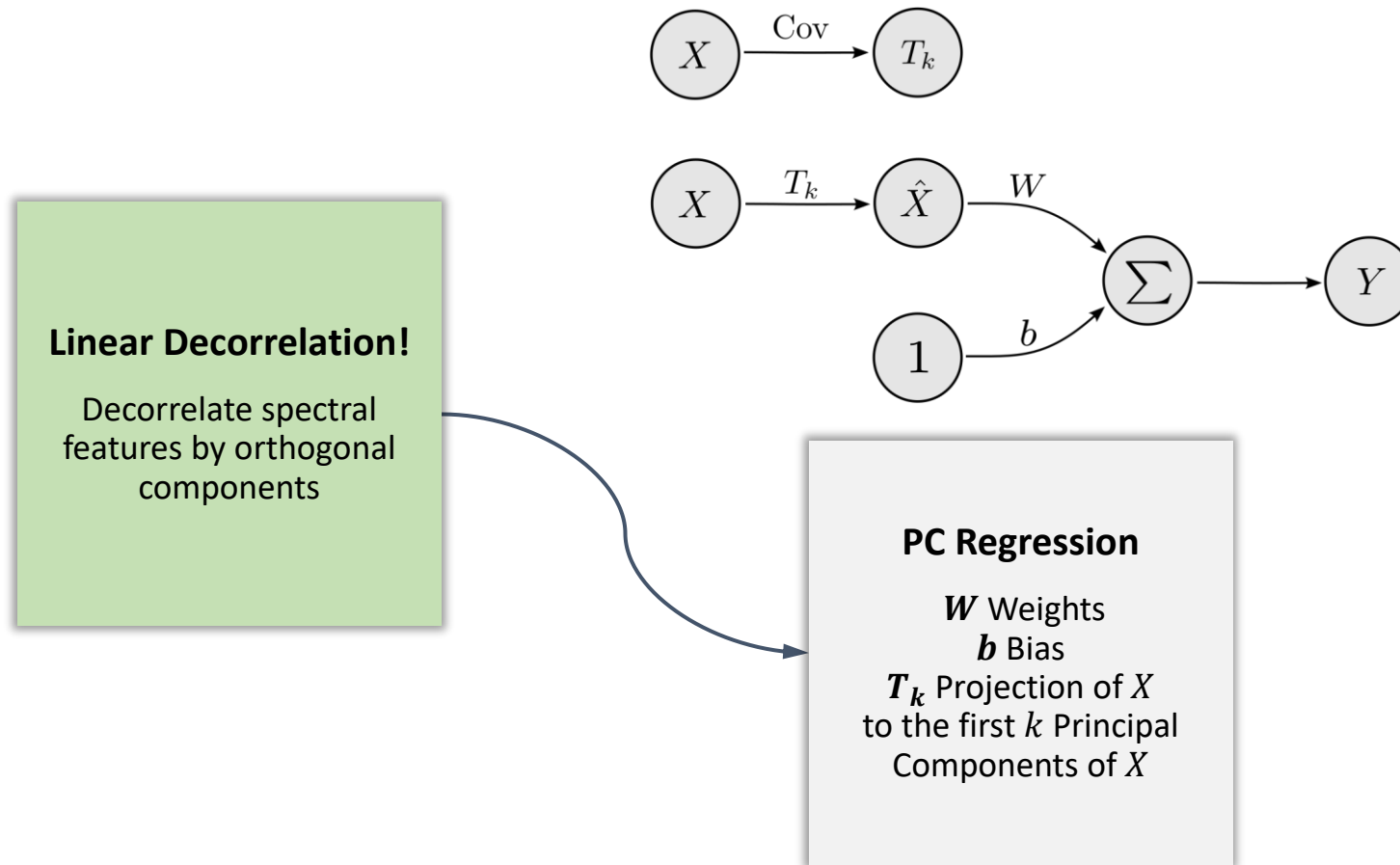
Approach 1: *Multiple Linear Regression*

Linear Decorrelation!

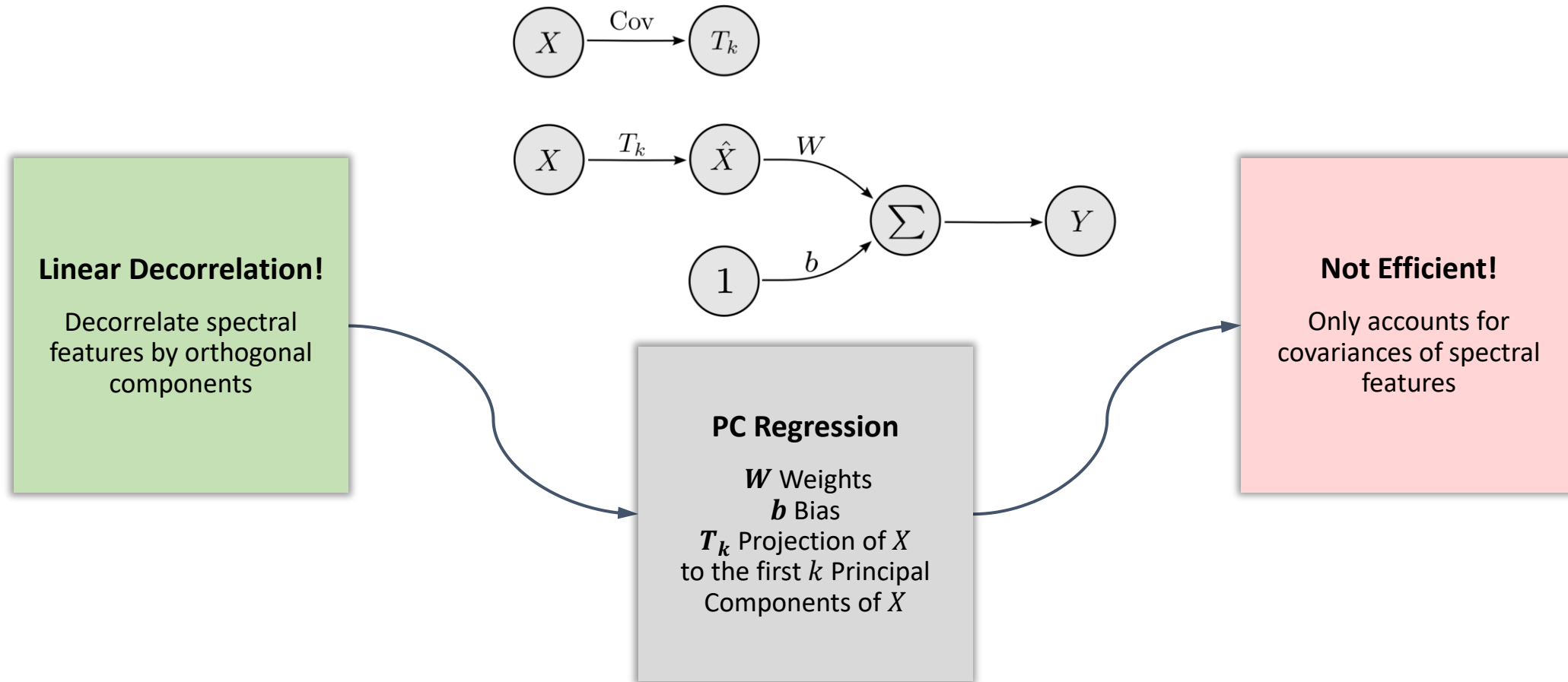
Decorrelate spectral
features by orthogonal
components



Approach 2: Principal Component (PC) Regression



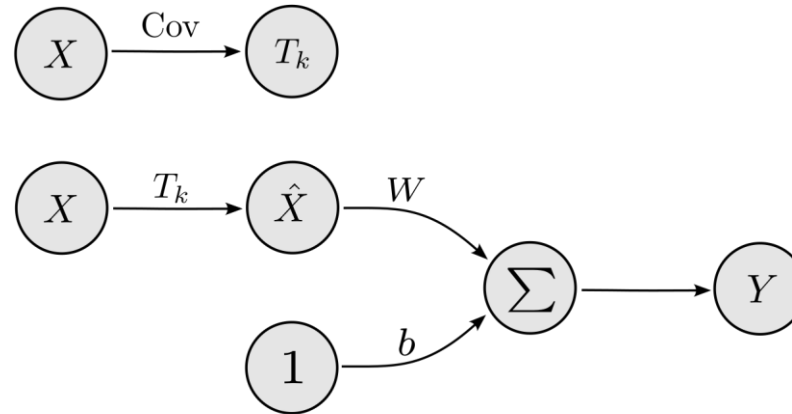
Approach 2: Principal Component (PC) Regression



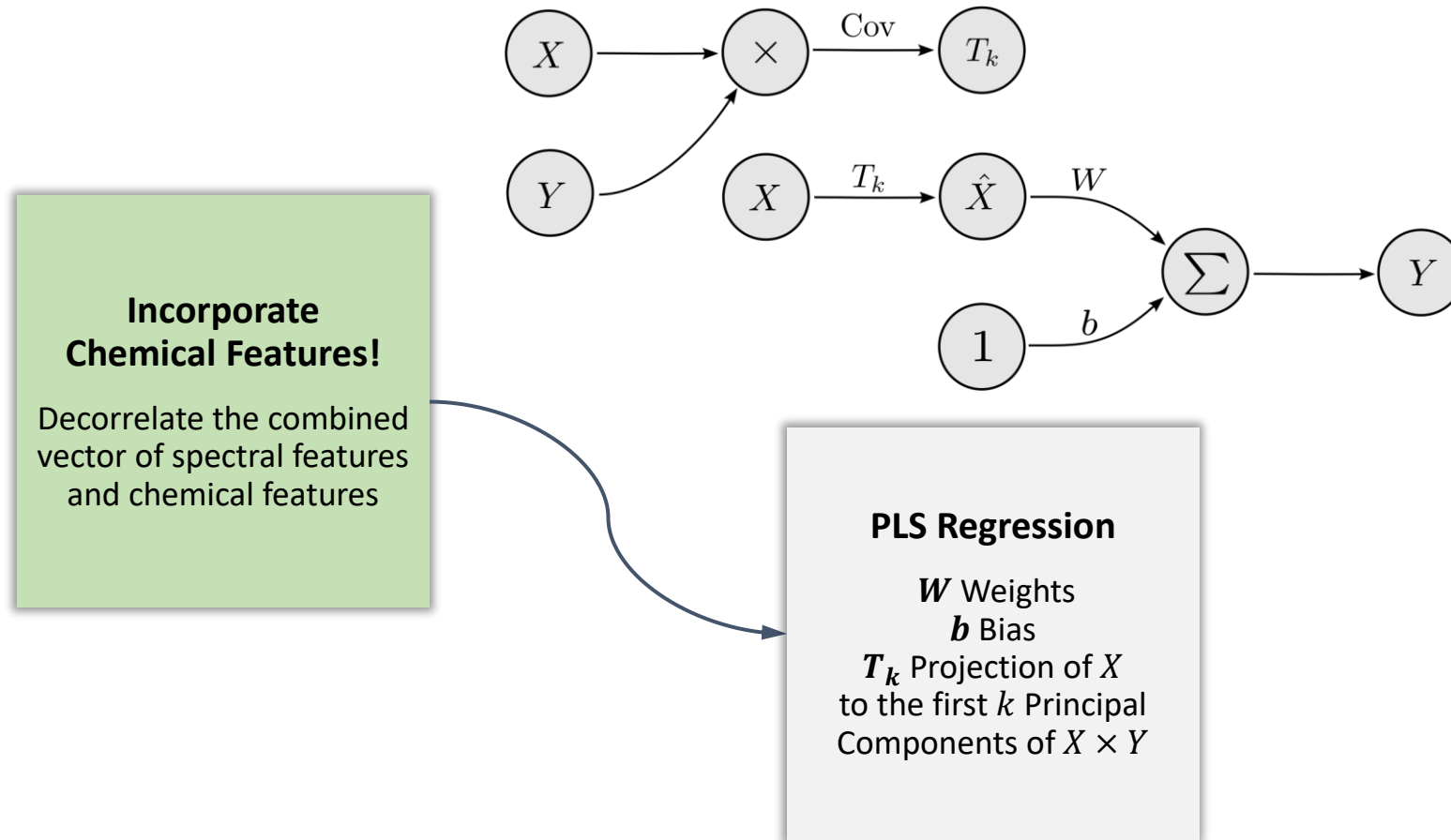
Approach 2: *Principal Component (PC) Regression*

Incorporate Chemical Features!

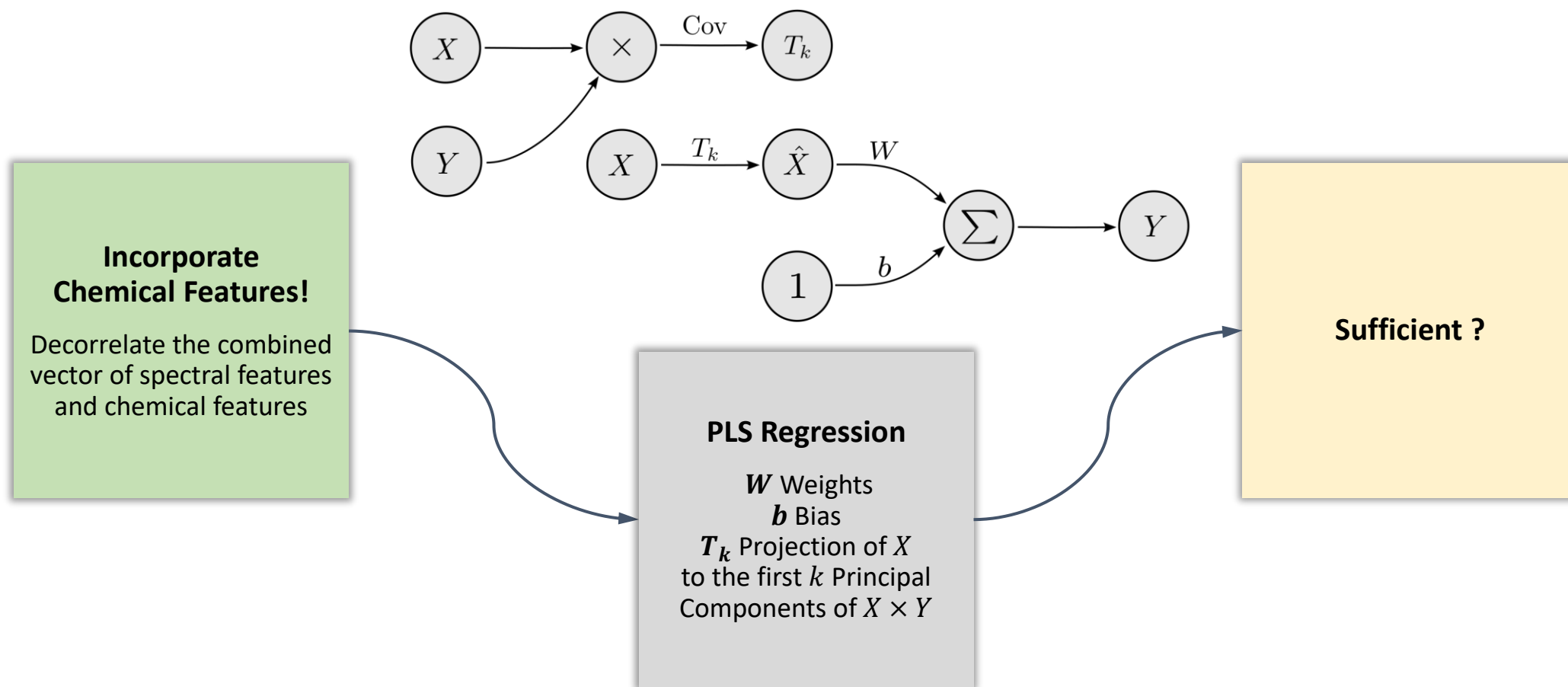
Decorrelate the combined
vector of spectral features
and chemical features



Approach 3: Partial Least Squares (PLS) Regression



Approach 3: *Partial Least Squares (PLS) Regression*



What can be concluded
about **Multivariate Calibration**?



Samples are rare!

The requirement to extract chemical features by **wet-lab** experiments makes reference samples rare



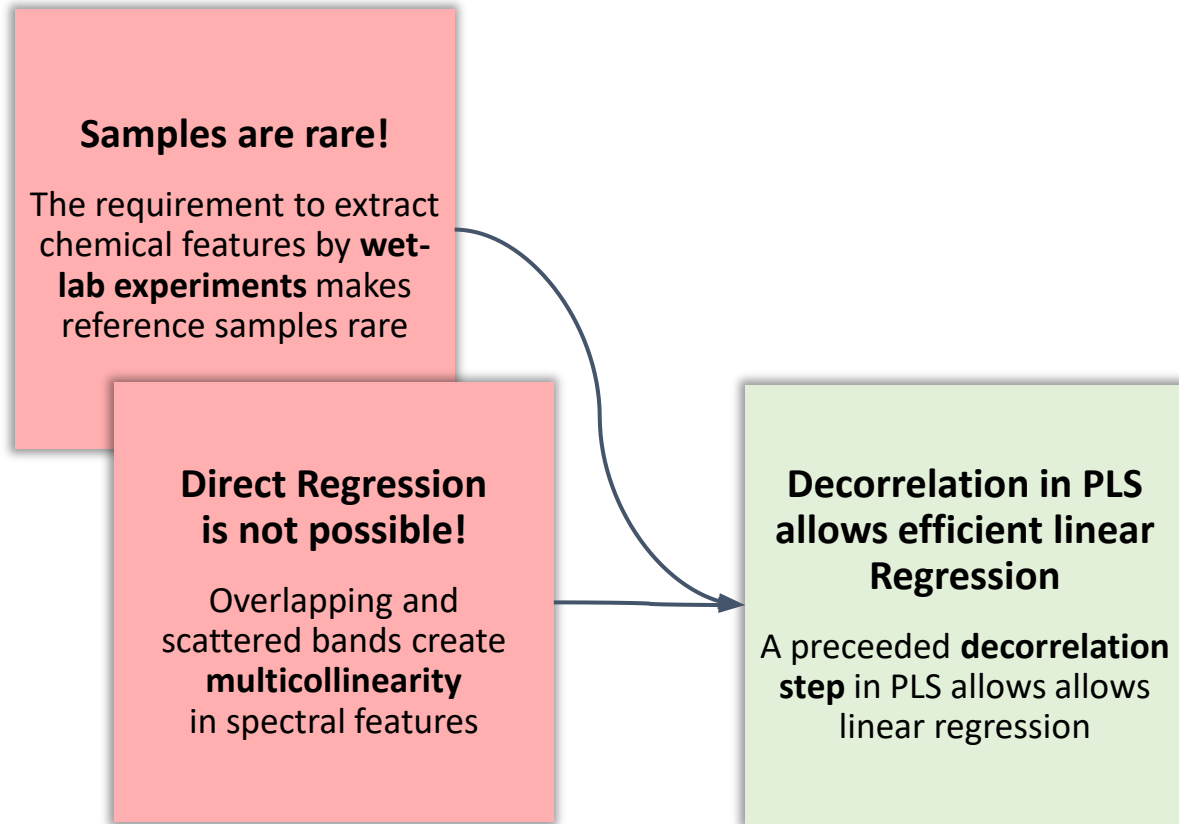
Samples are rare!

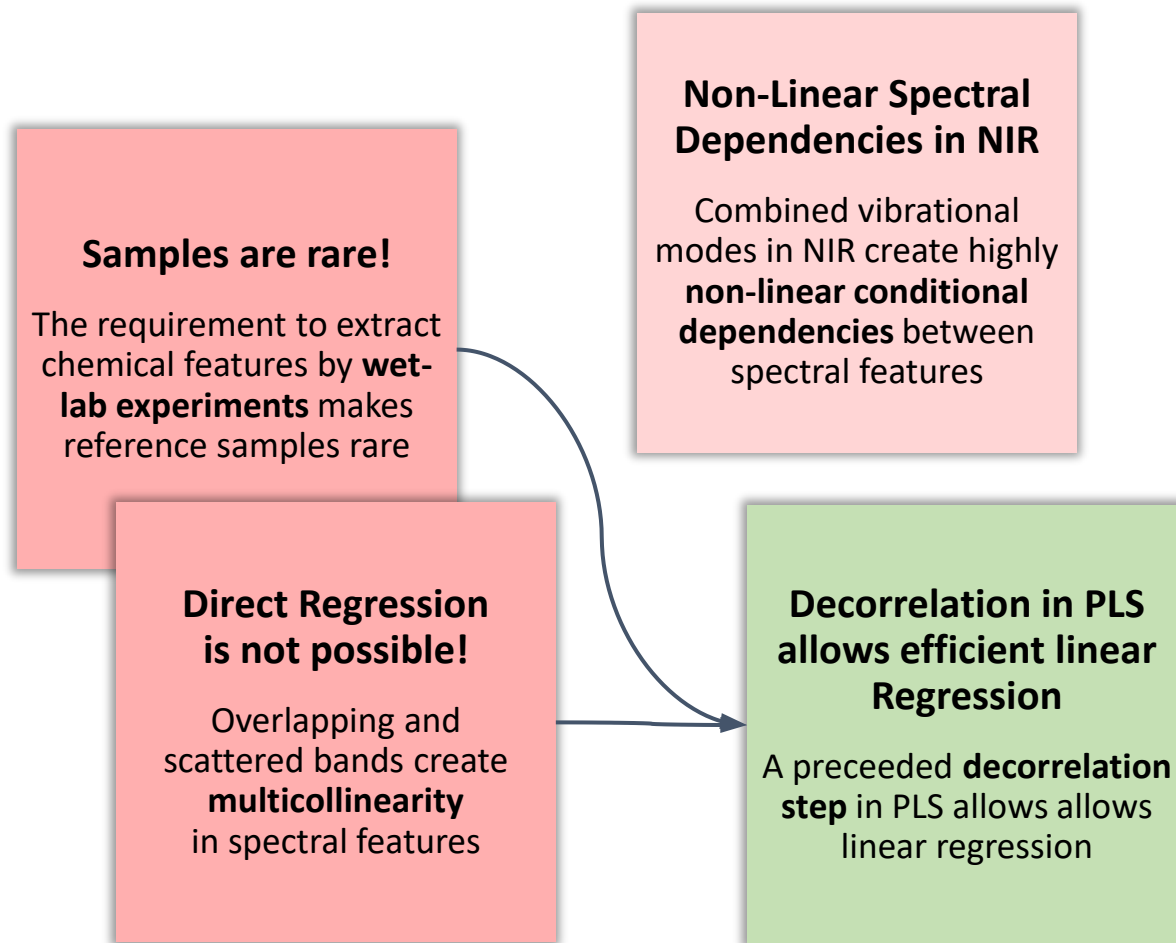
The requirement to extract chemical features by **wet-lab experiments** makes reference samples rare

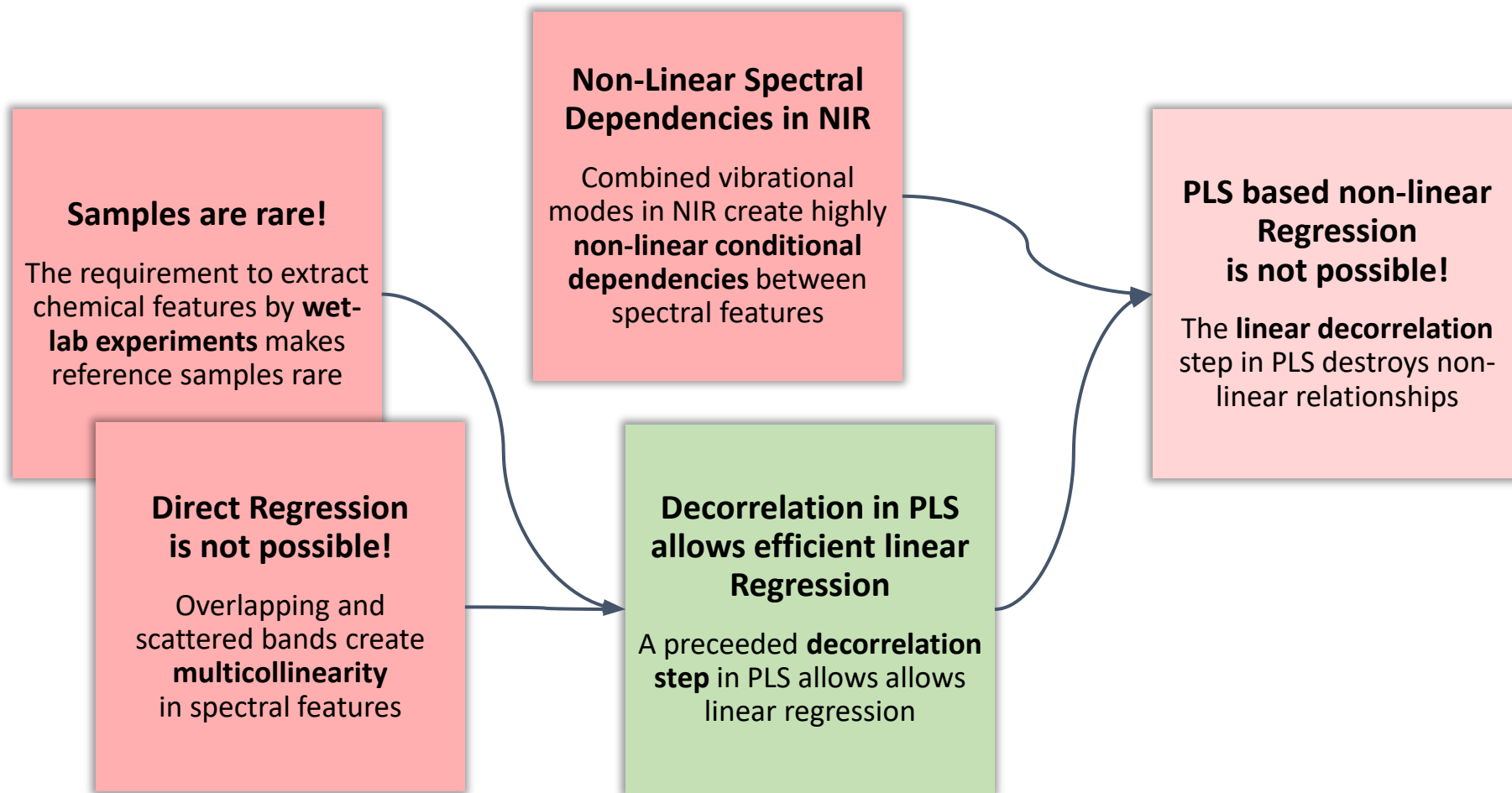
Direct Regression is not possible!

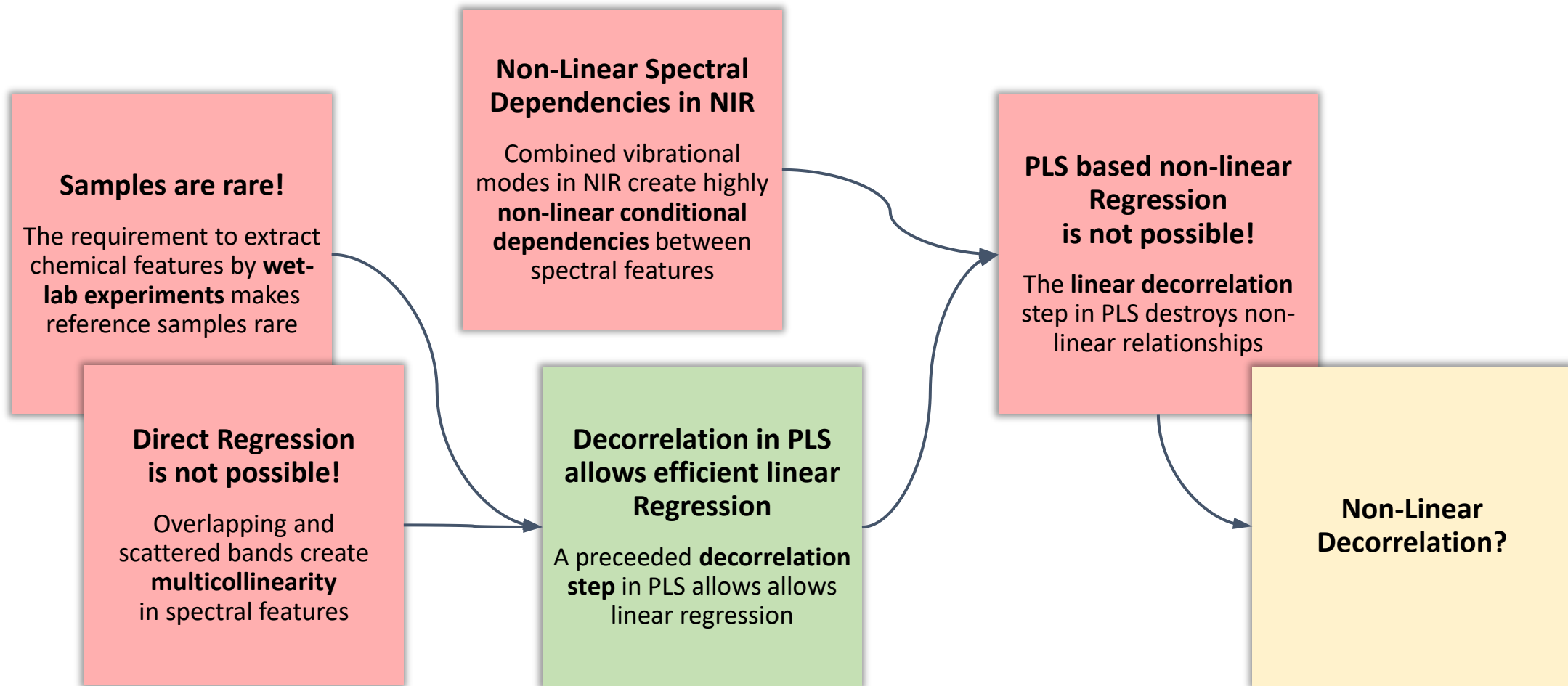
Overlapping and scattered bands create **multicollinearity** in spectral features











Part 3

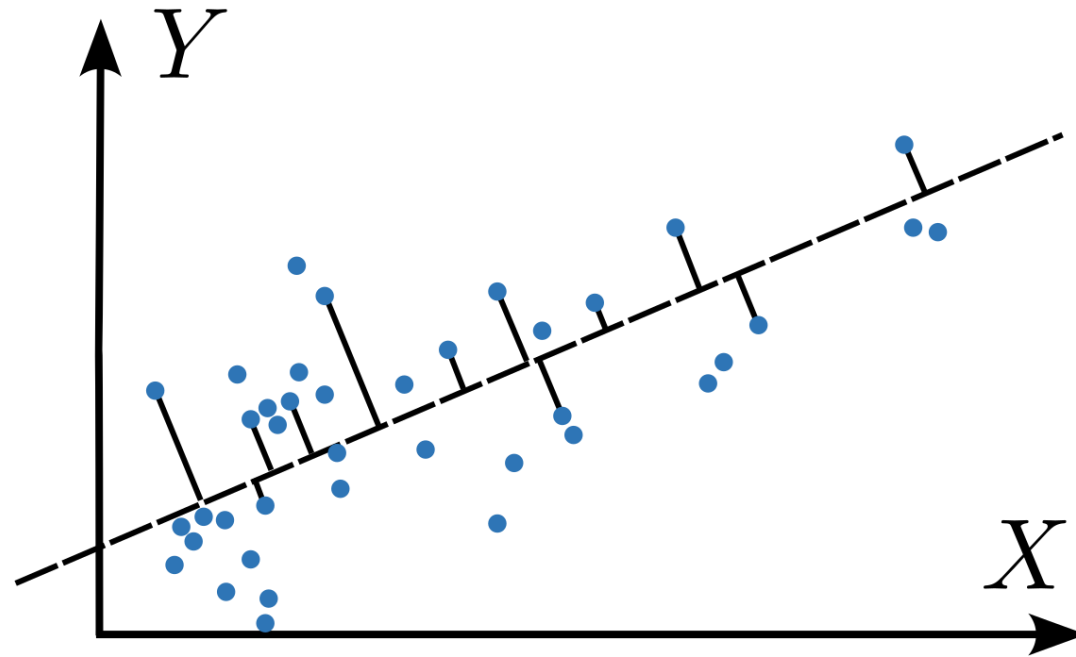
Energy based Calibration



What is **non-linear Decorrelation?**

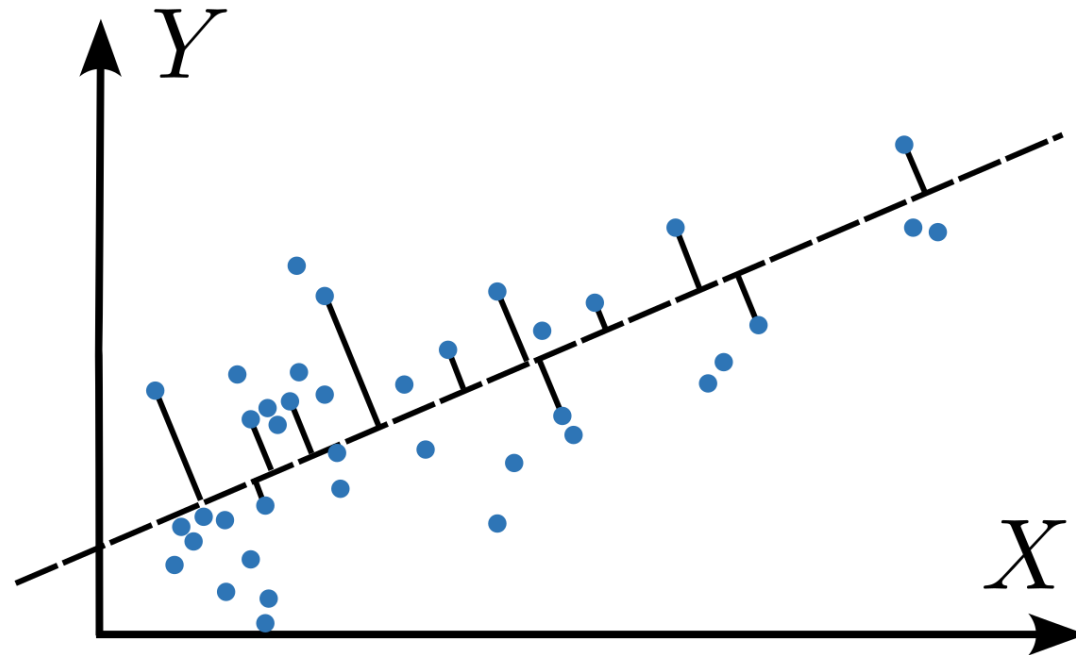


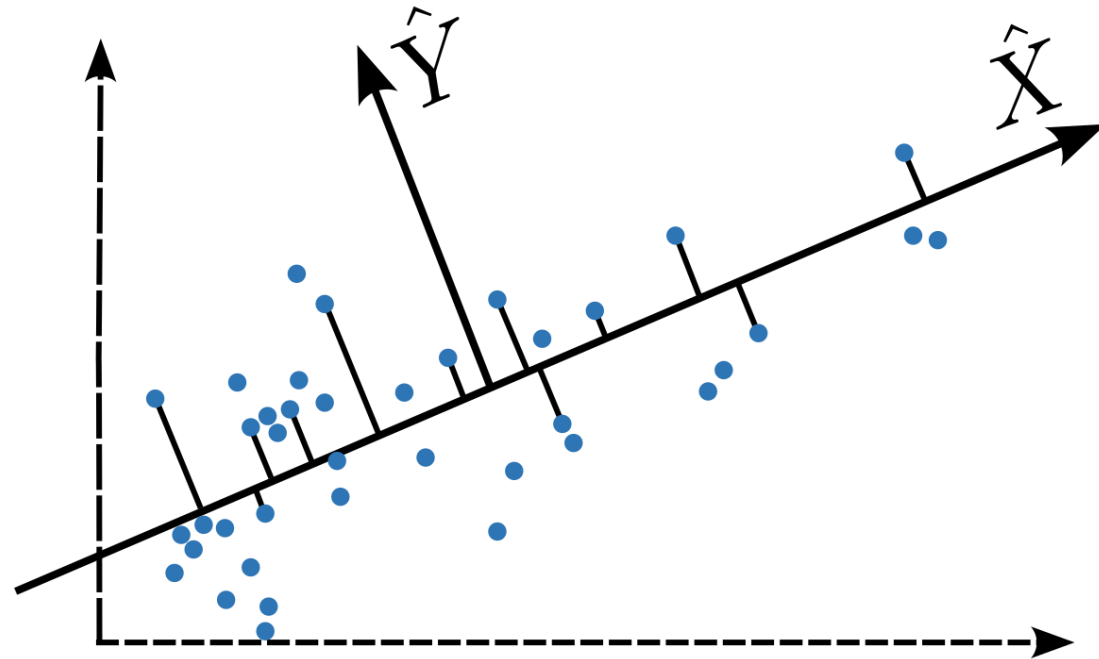
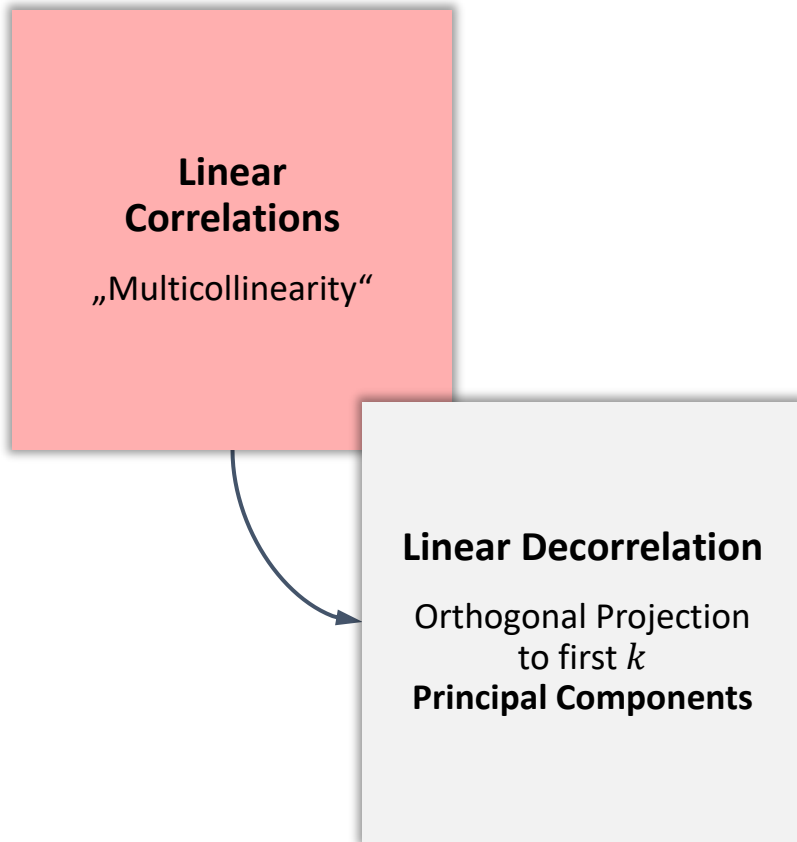
**Linear
Correlations**
„Multicollinearity“

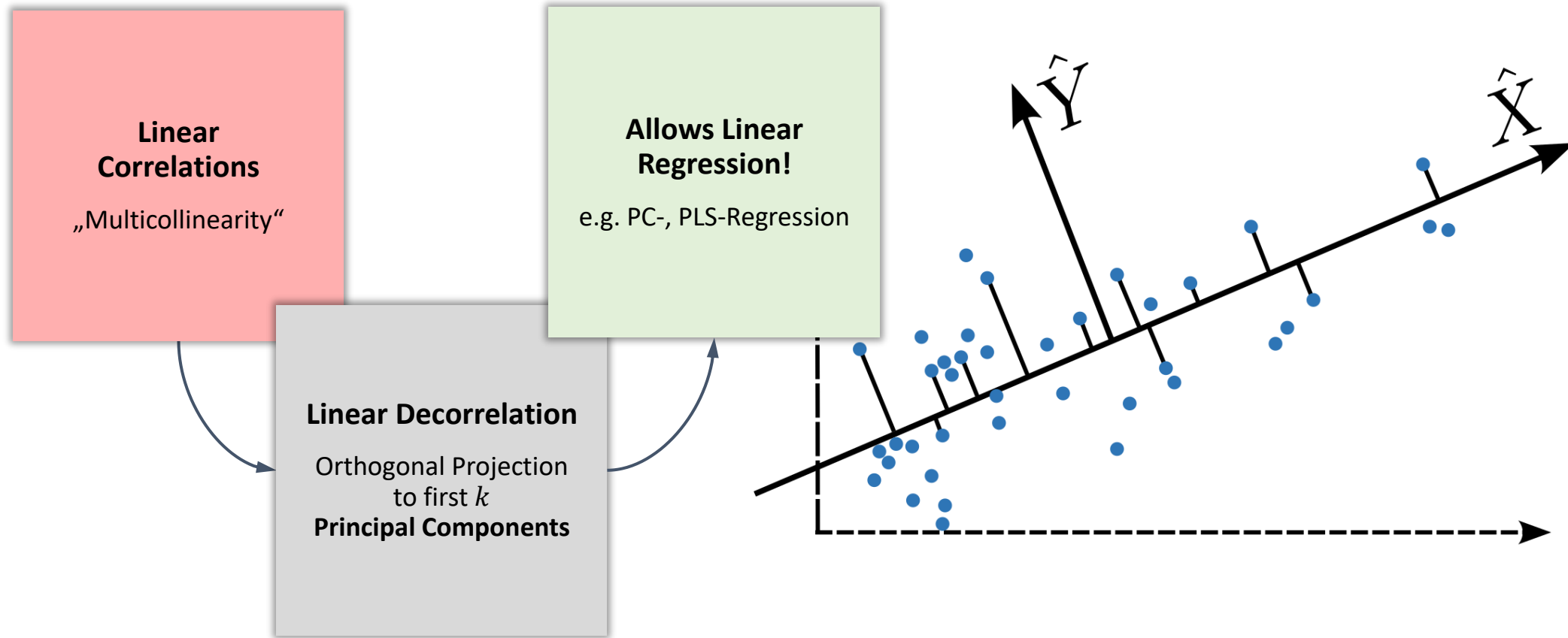


**Linear
Correlations**
„Multicollinearity“

Linear Decorrelation
Orthogonal Projection
to first k
Principal Components

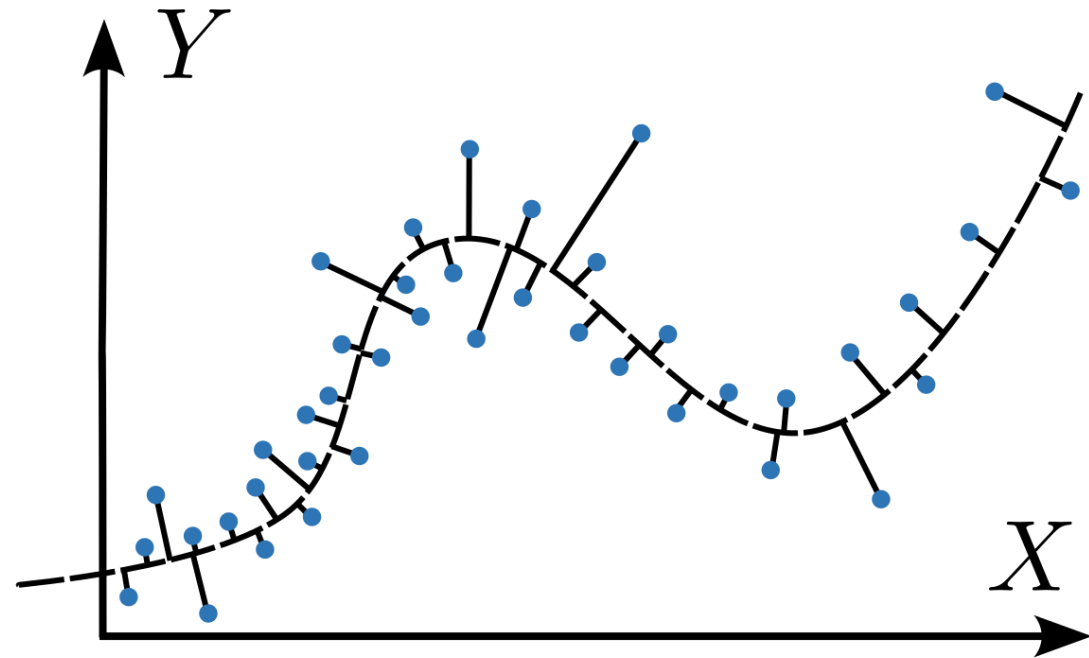


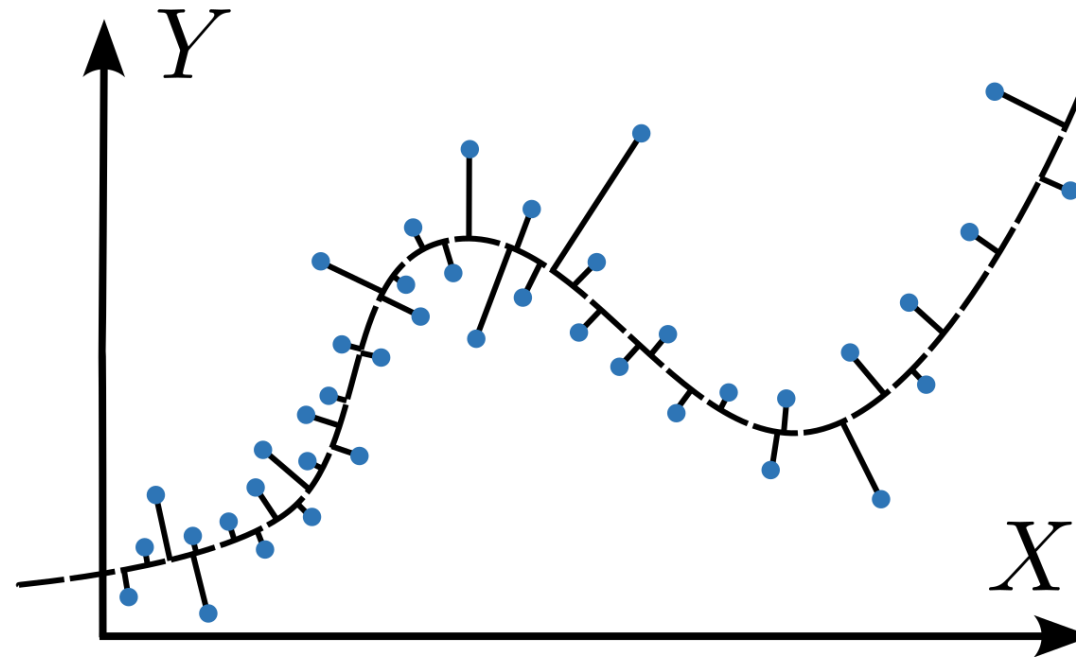
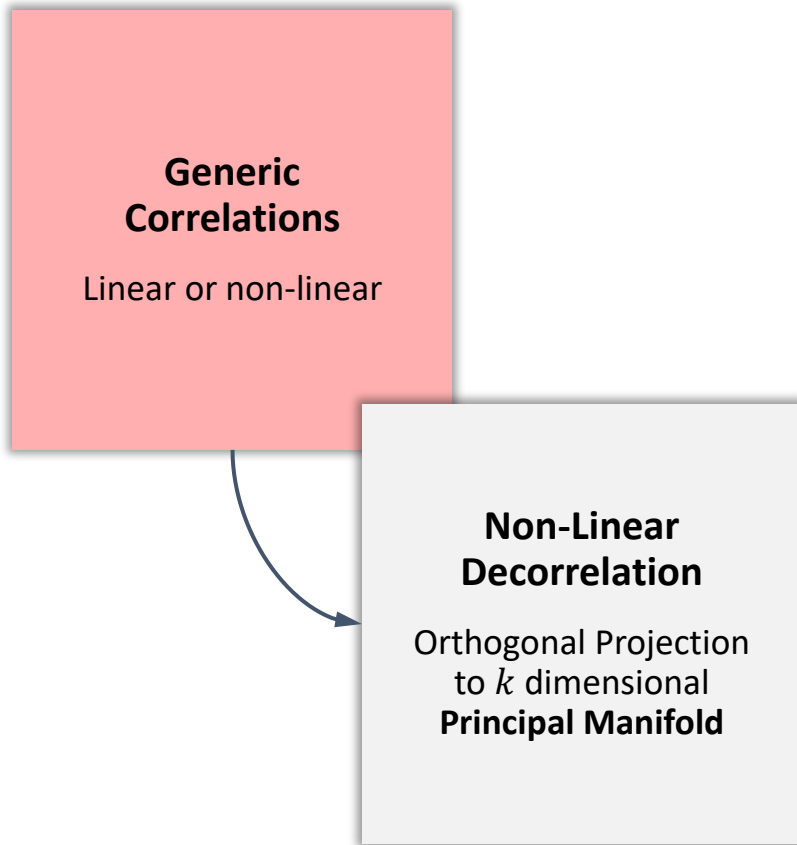


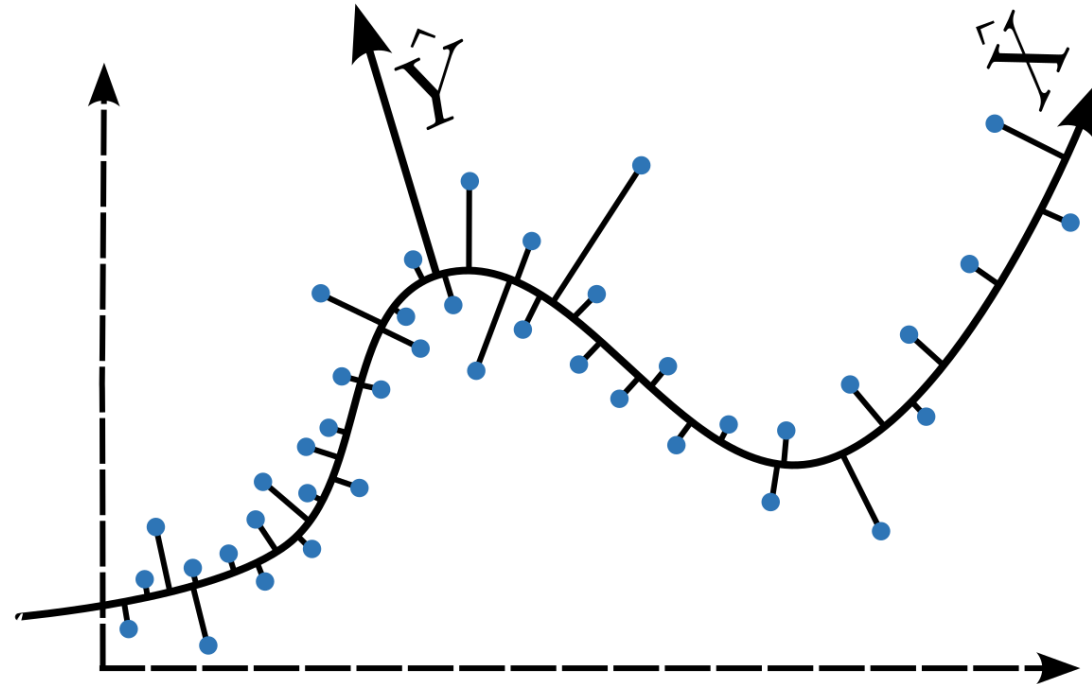
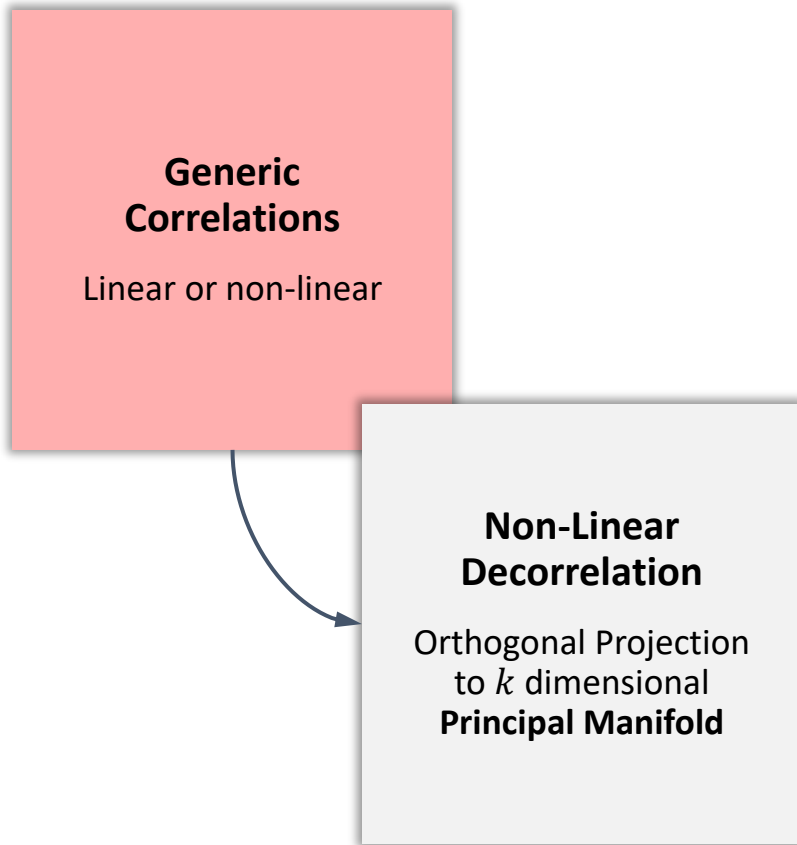


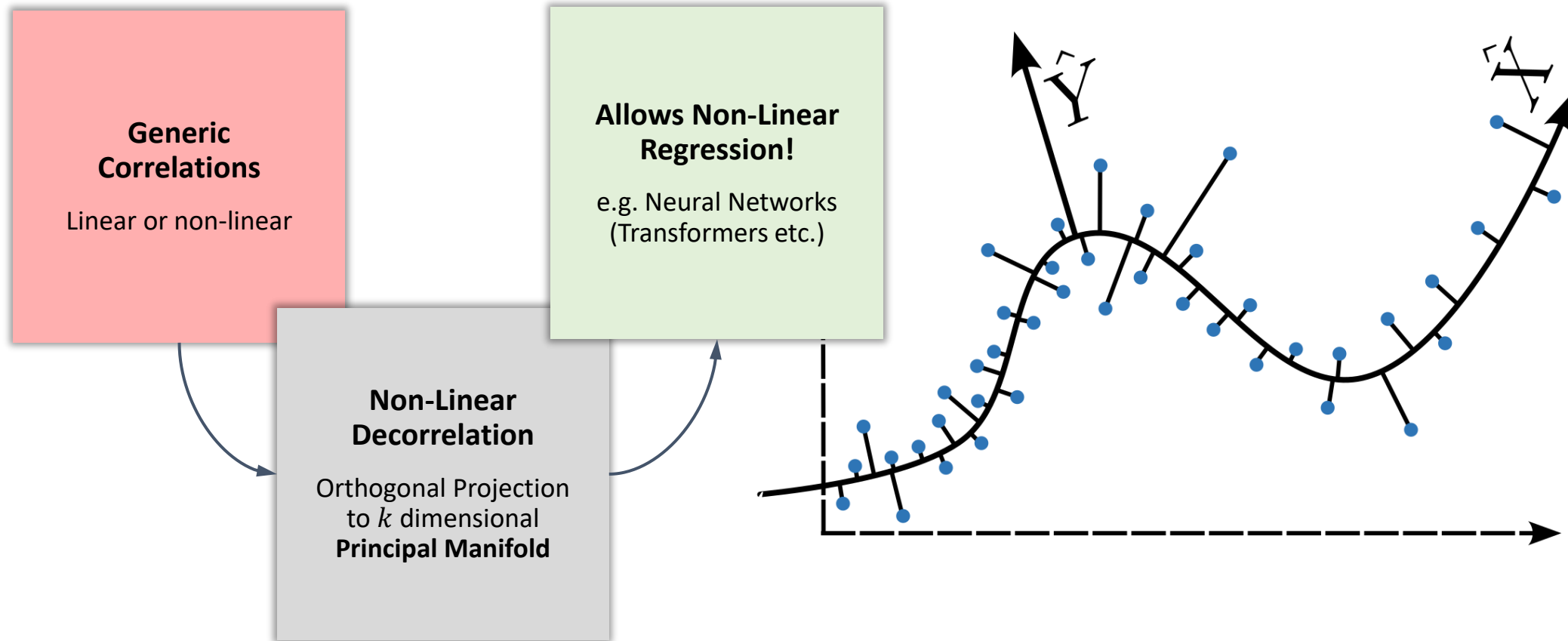
Generic Correlations

Linear or non-linear









How to model **non-linear Decorrelation?**



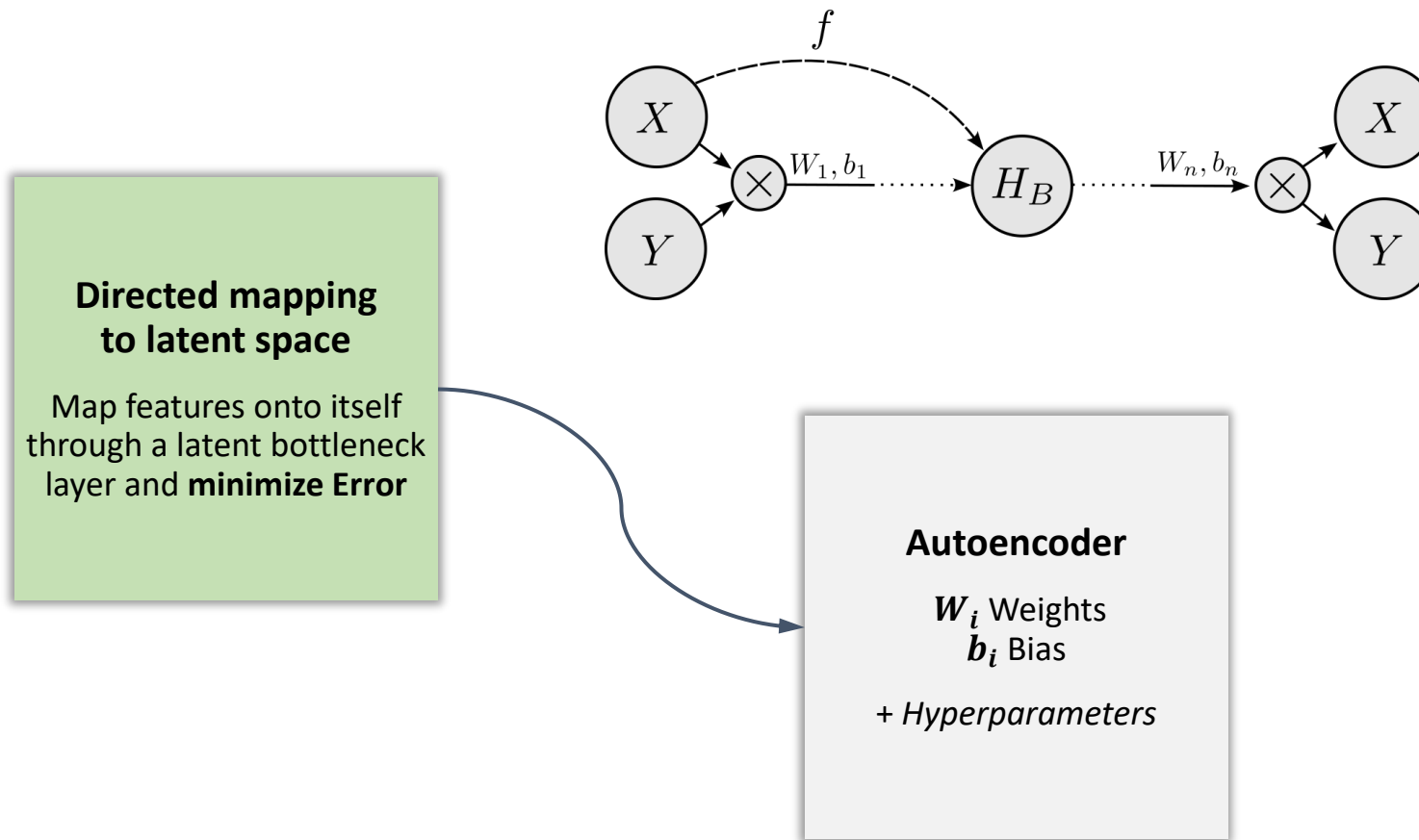
Approach 1: *Directed Graphical Model*

Directed mapping to latent space

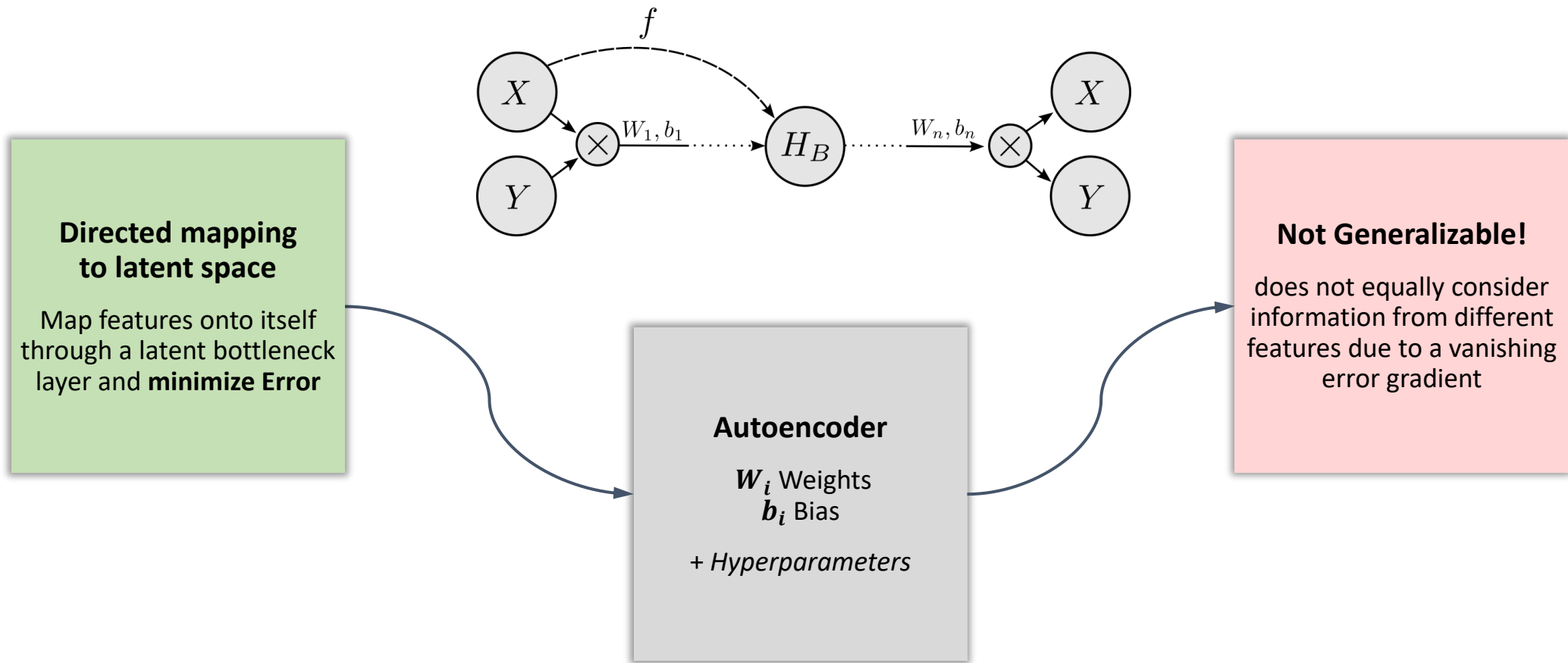
Map features onto itself
through a latent bottleneck
layer and **minimize Error**



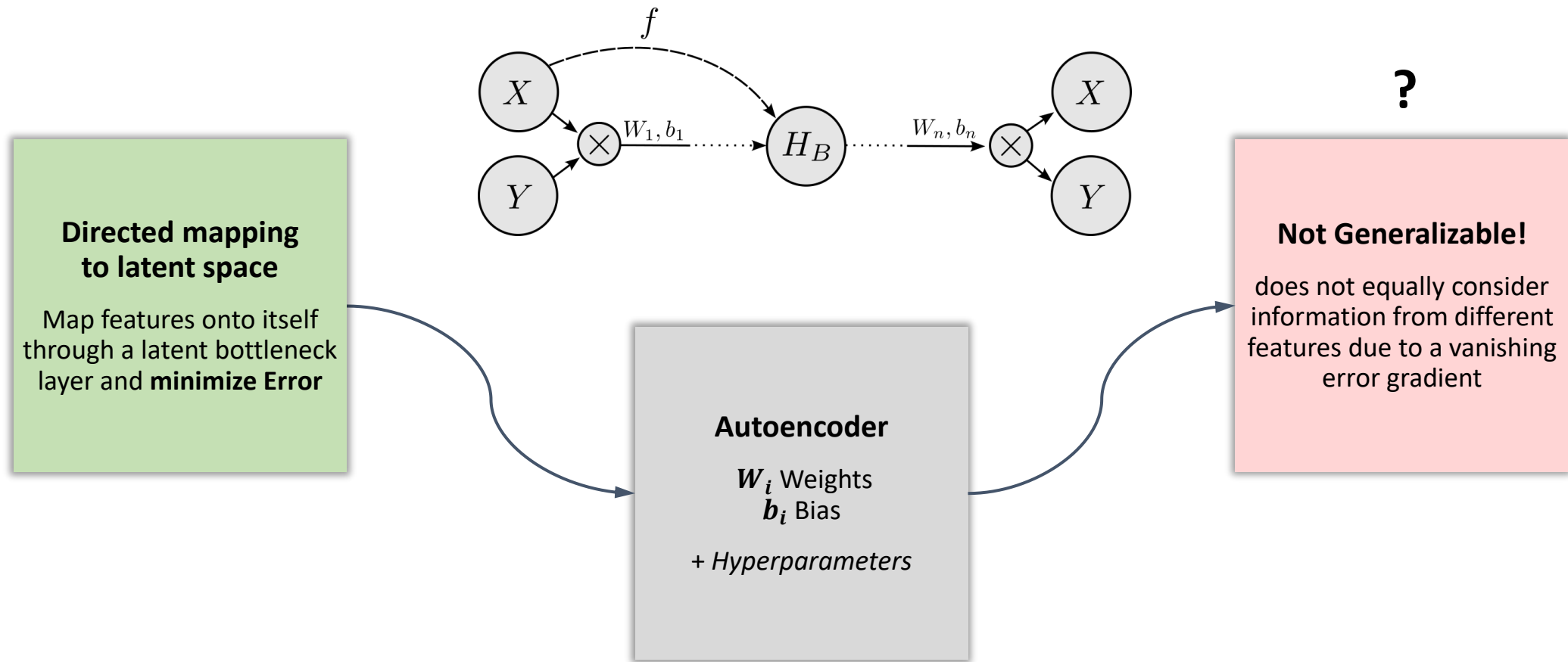
Approach 1: Directed Graphical Model



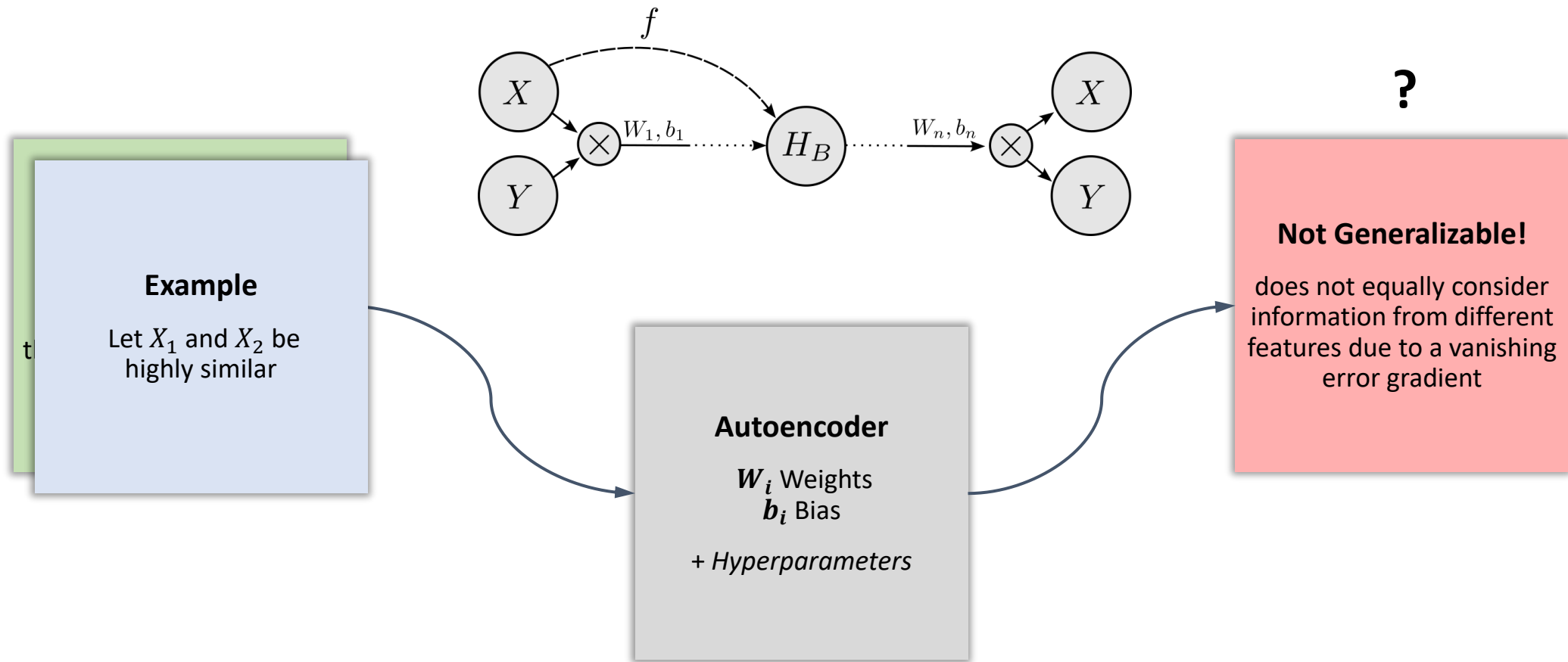
Approach 1: Directed Graphical Model



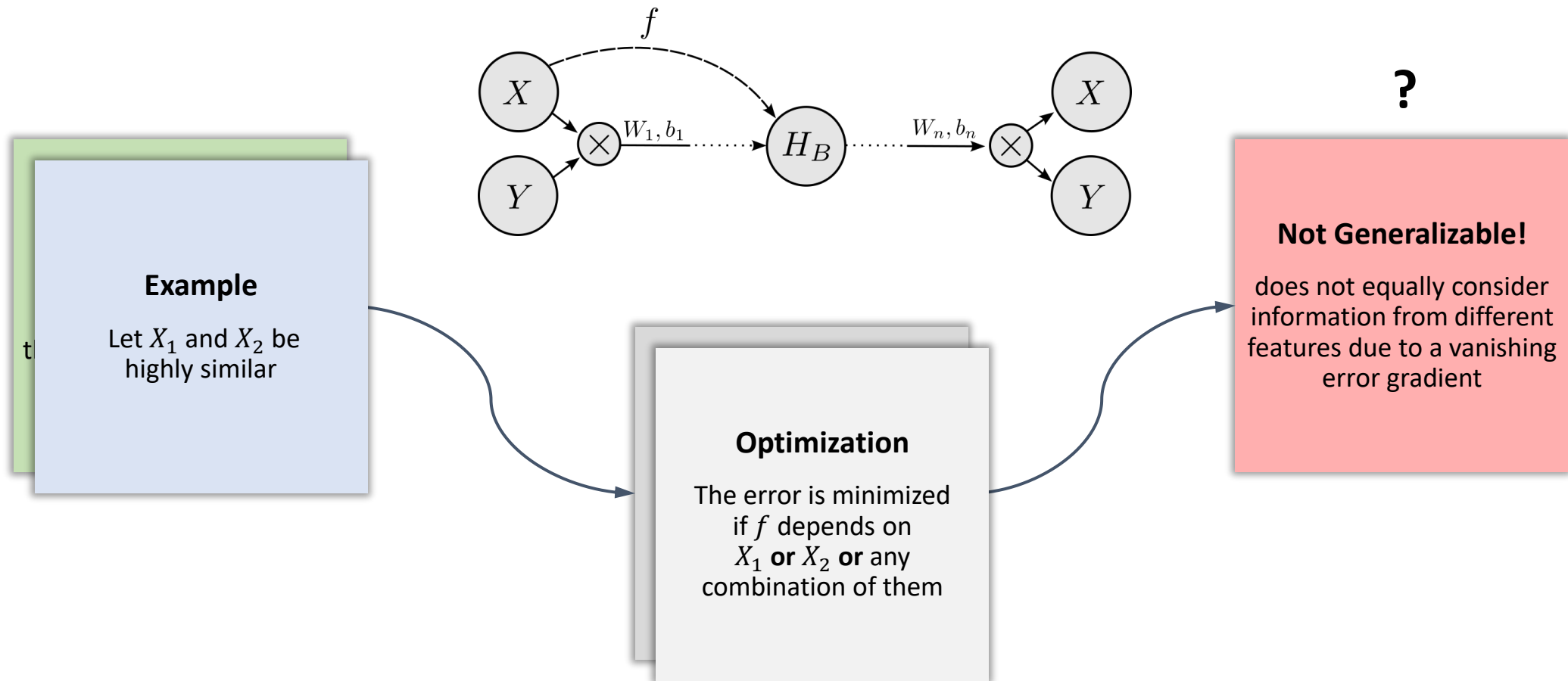
Approach 1: Directed Graphical Model



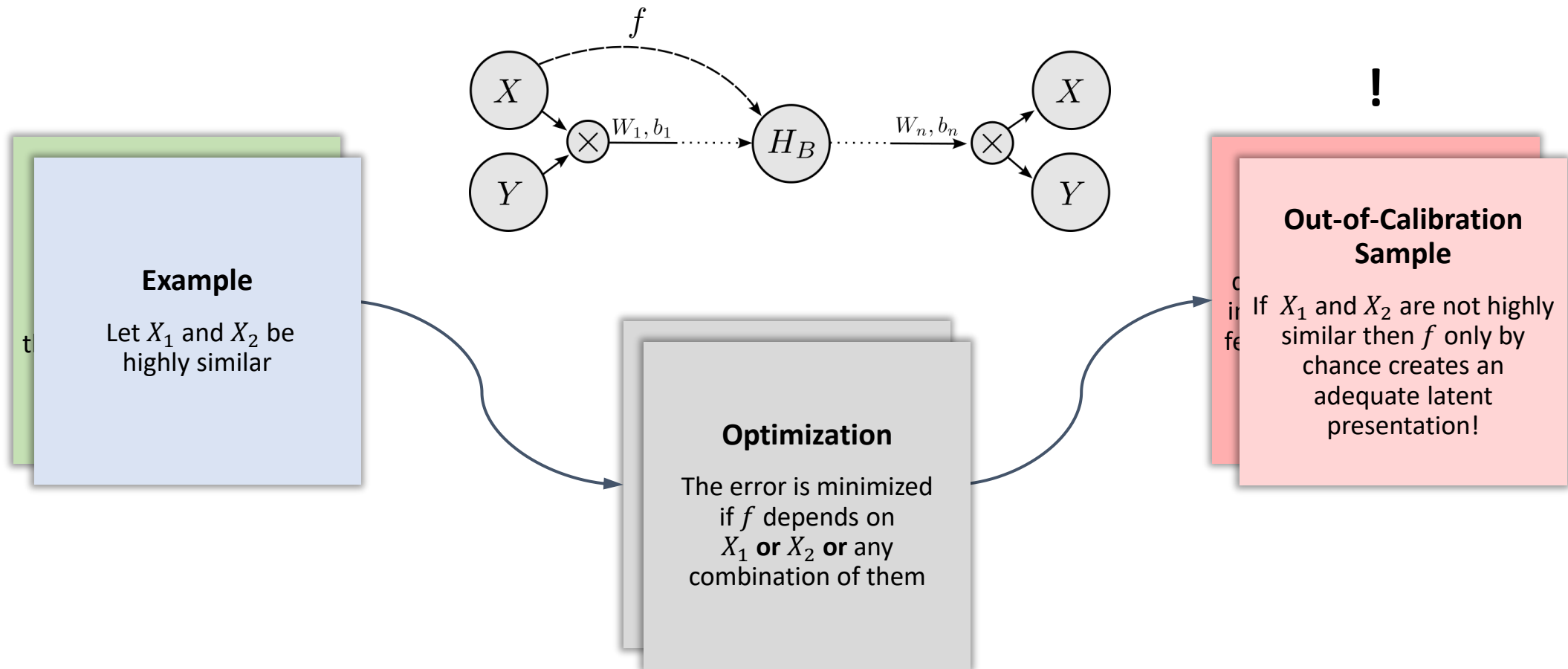
Approach 1: Directed Graphical Model



Approach 1: Directed Graphical Model



Approach 1: Directed Graphical Model



Approach 1: *Directed Graphical Model*



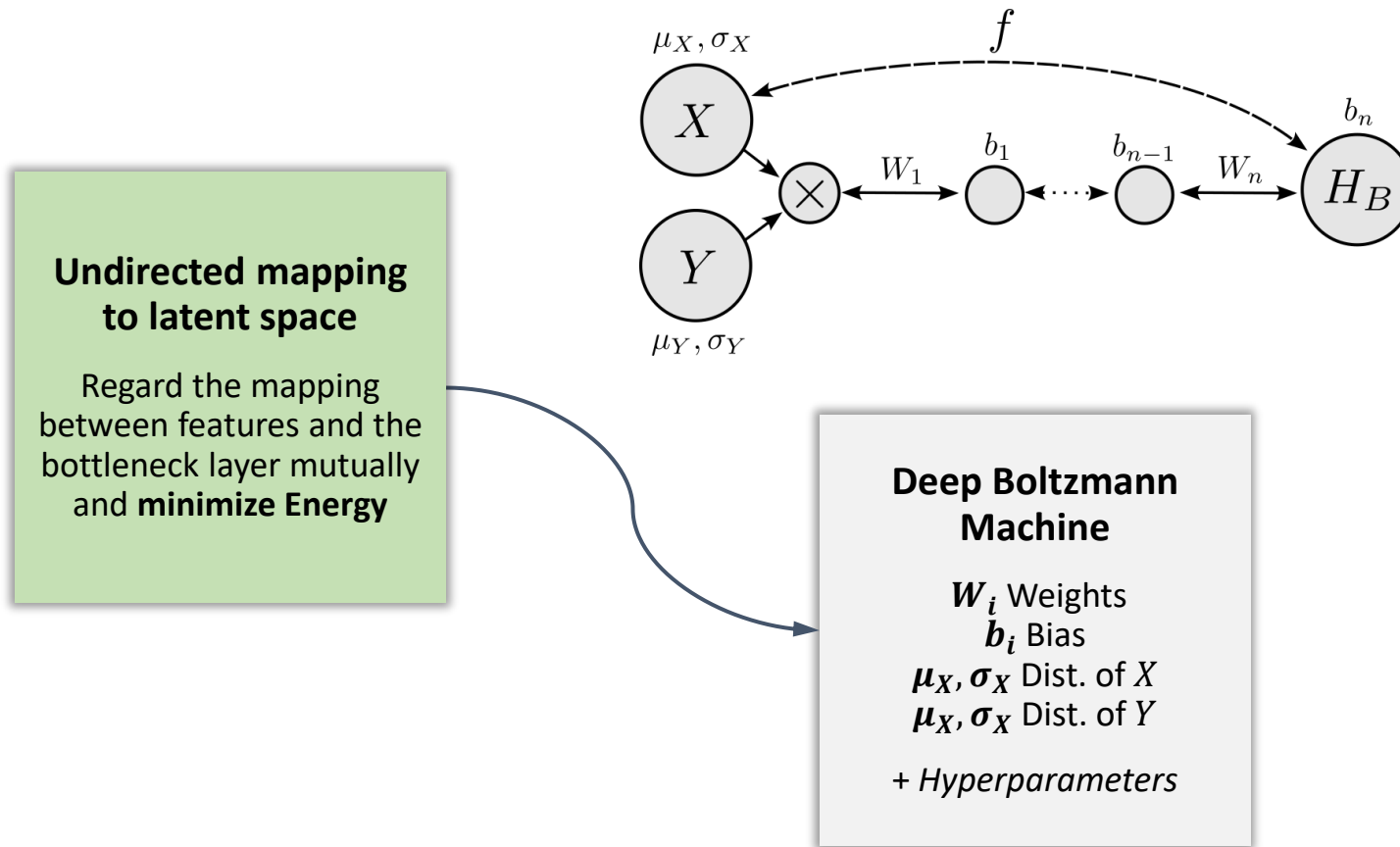
Approach 2: *Undirected Graphical Model*

Undirected mapping to latent space

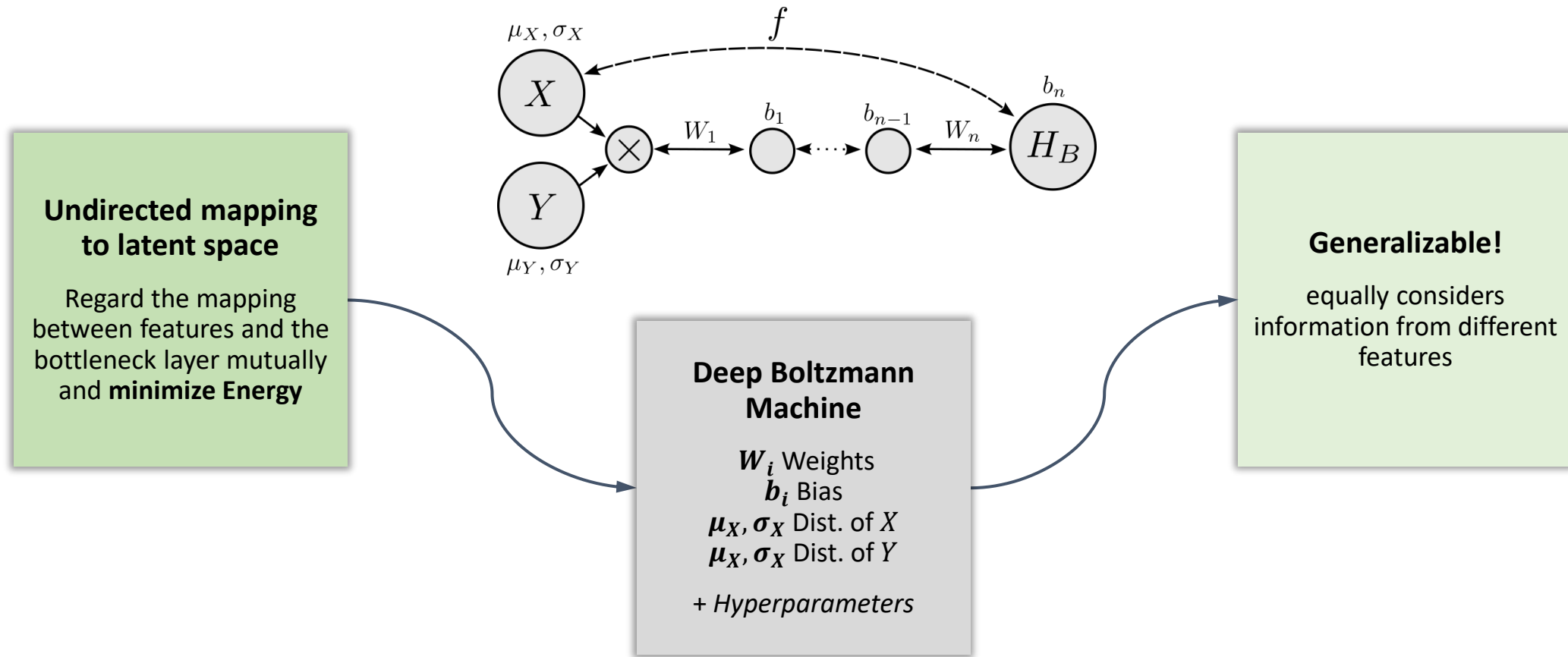
Regard the mapping
between features and the
bottleneck layer mutually
and **minimize Energy**



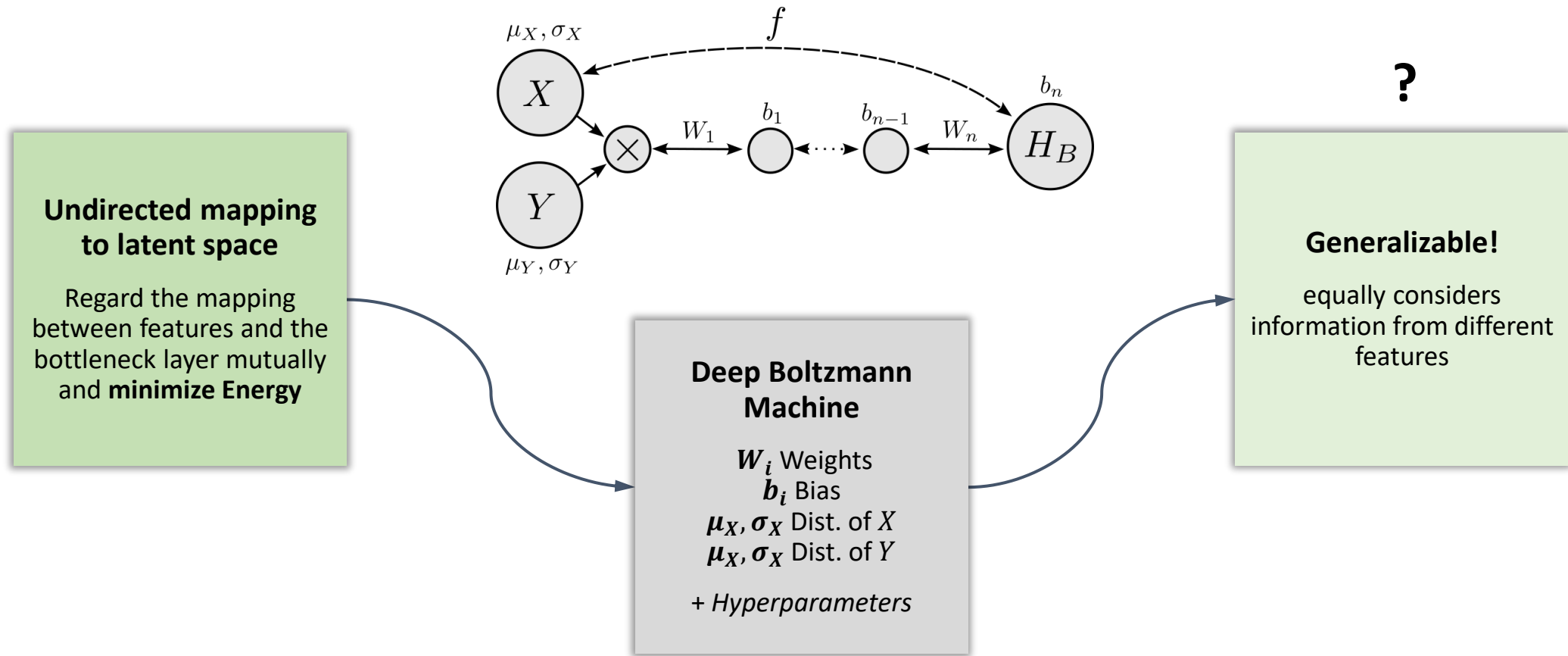
Approach 2: Undirected Graphical Model



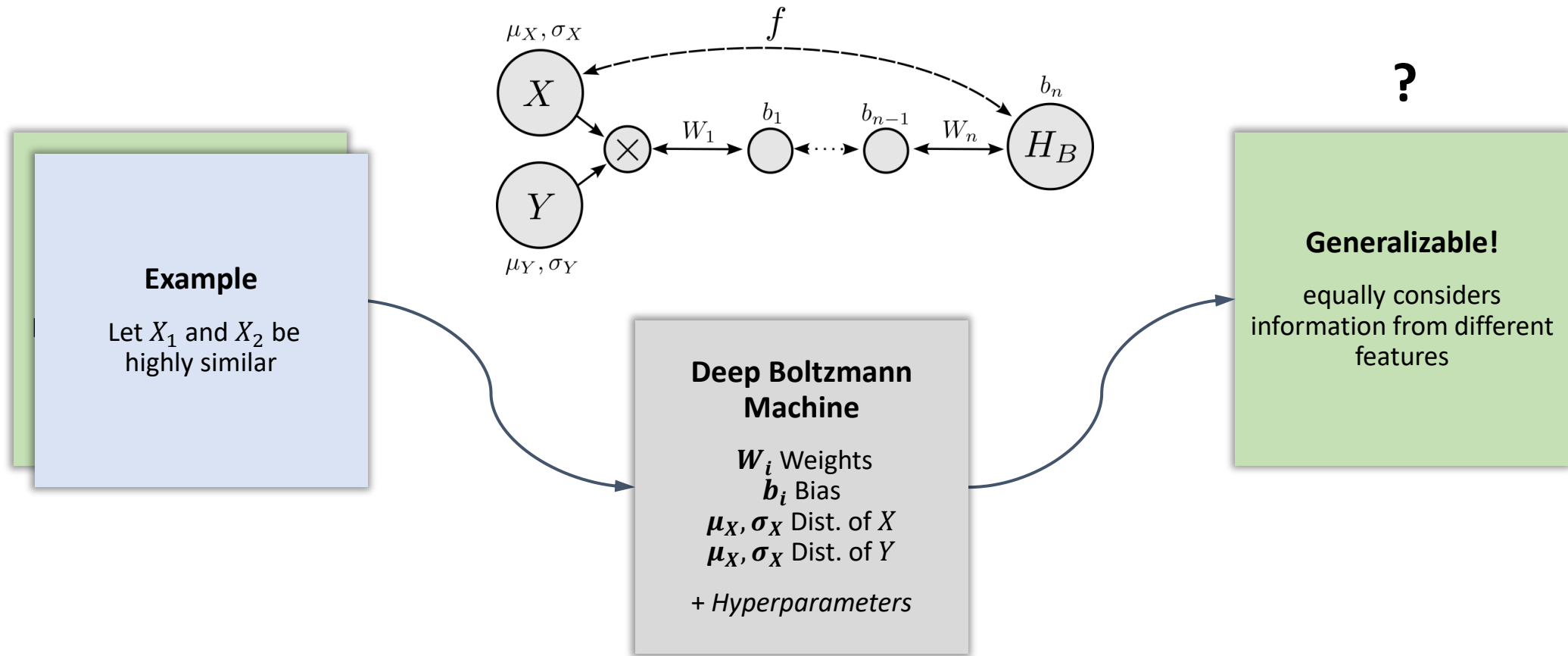
Approach 2: Undirected Graphical Model



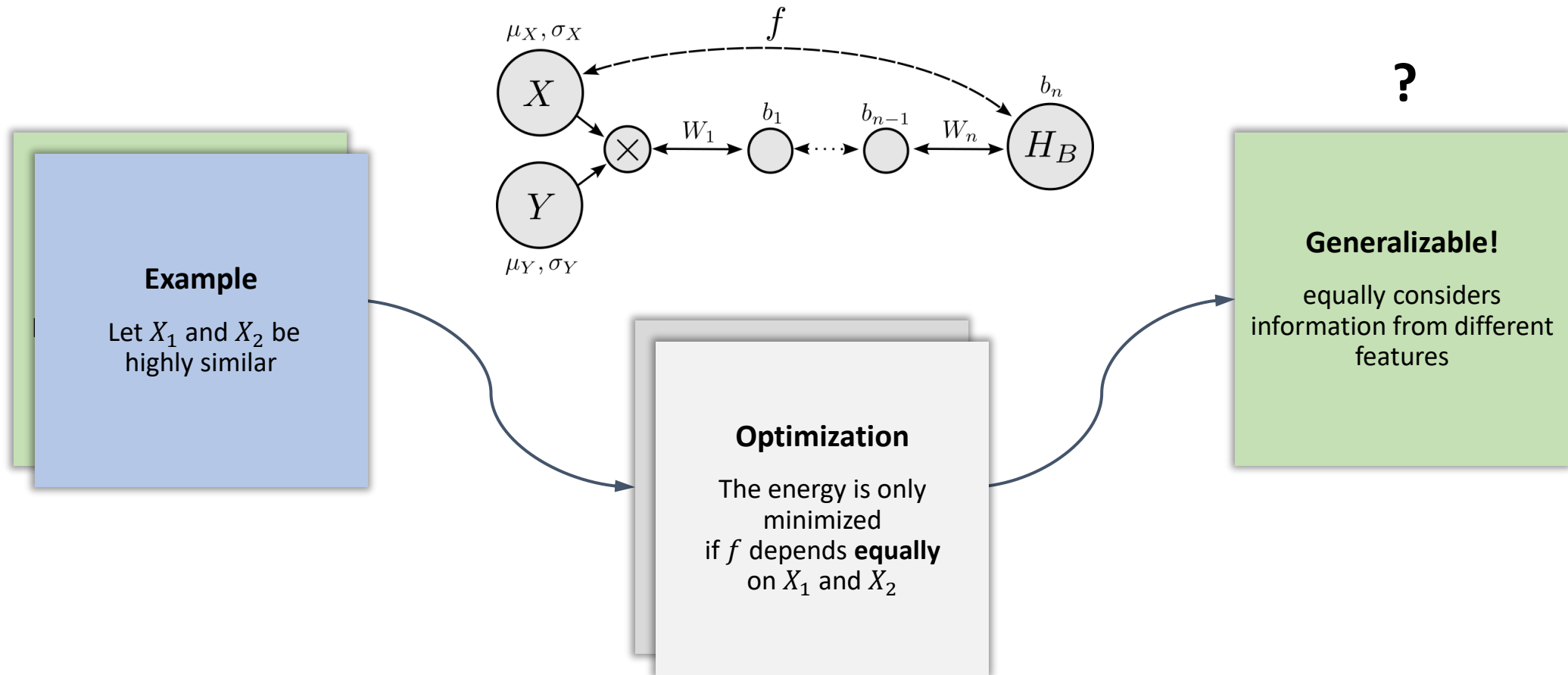
Approach 2: Undirected Graphical Model



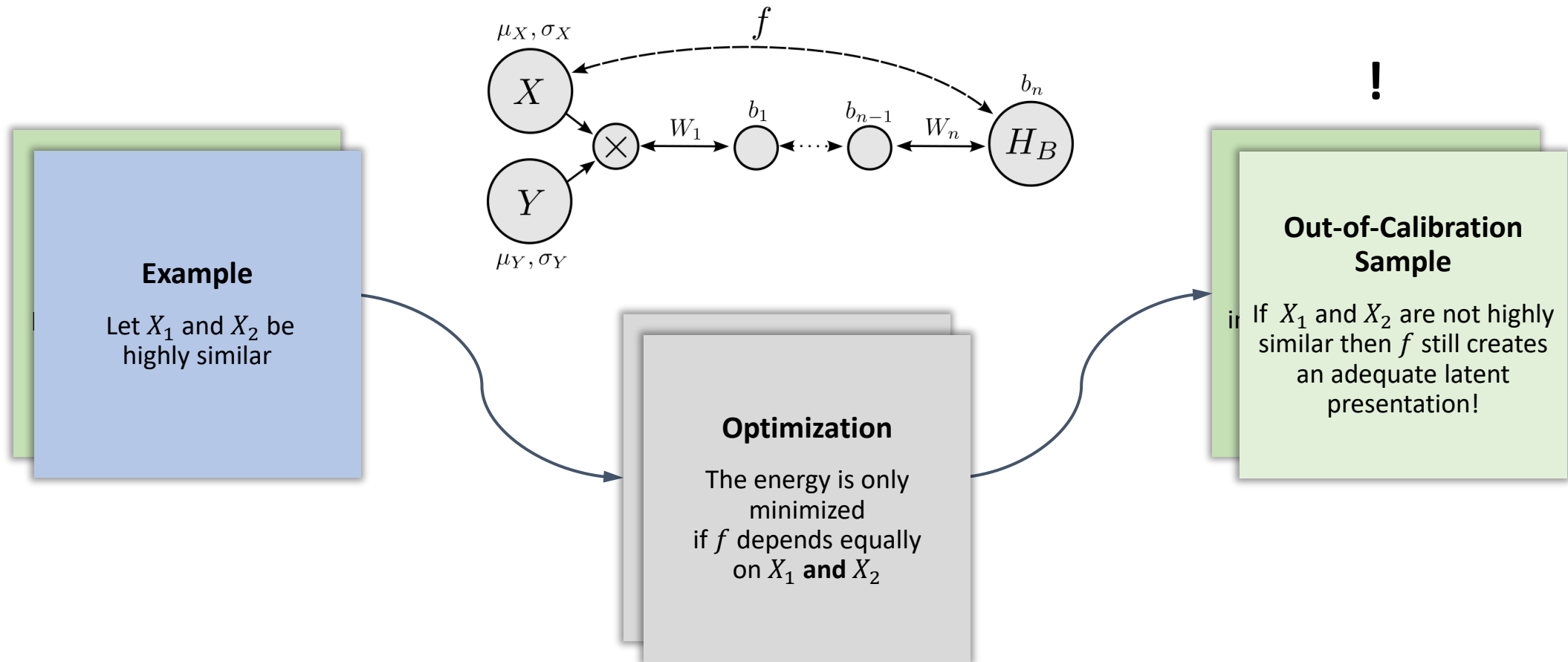
Approach 2: Undirected Graphical Model



Approach 2: Undirected Graphical Model



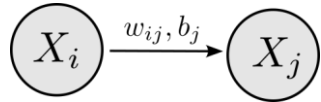
Approach 2: Undirected Graphical Model



What is **Energy based Modeling?**



Regression Model

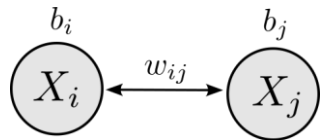


Directed Connections

Weights model
one direction:

$$w_{ij}$$

Energy based Model



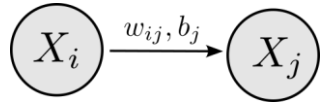
Undirected Connections

Weights model
both directions:

$$w_{ij} = w_{ji}$$



Regression Model



Directed Connections

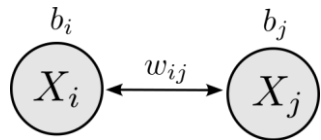
Weights model one direction:

$$w_{ij}$$

Minimizes Error

Parameters minimize the error between targets and predictions

Energy based Model



Undirected Connections

Weights model both directions:

$$w_{ij} = w_{ji}$$

Minimizes Energy

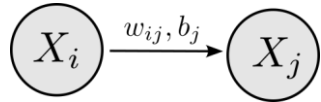
Parameters minimize the pairwise energies of connected vertices:

Pos. Corr.: $w_{ij} > 0$

Neg. Corr.: $w_{ij} < 0$



Regression Model



Directed Connections

Weights model one direction:

$$w_{ij}$$

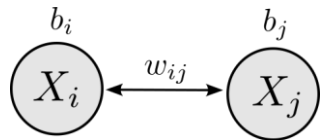
Minimizes Error

Parameters minimize the error between targets and predictions

Calculates Predictions

Predictions **of targets** are directly calculated

Energy based Model



Undirected Connections

Weights model both directions:

$$w_{ij} = w_{ji}$$

Minimizes Energy

Parameters minimize the pairwise energies of connected vertices:

Pos. Corr.: $w_{ij} > 0$

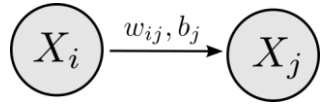
Neg. Corr.: $w_{ij} < 0$

Approximates Predictions

Predictions of **all variables** are approximated by a Markov Chain using Gibbs Sampling



Regression Model



Directed Connections

Weights model one direction:

$$w_{ij}$$

Minimizes Error

Parameters minimize the error between targets and predictions

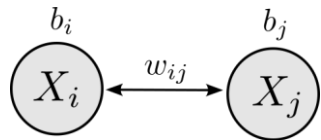
Calculates Predictions

Predictions **of targets** are directly calculated

Optimizes Prediction Function

Gradient Descent in the Errorlandscape approximates the prediction function

Energy based Model



Undirected Connections

Weights model both directions:

$$w_{ij} = w_{ji}$$

Minimizes Energy

Parameters minimize the pairwise energies of connected vertices:

Pos. Corr.: $w_{ij} > 0$

Neg. Corr.: $w_{ij} < 0$

Approximates Predictions

Predictions of **all variables** are approximated by a Markov Chain using Gibbs Sampling

Optimizes Joint Distribution

Gradient Descent in the Energylandscape approximates the joint distributon

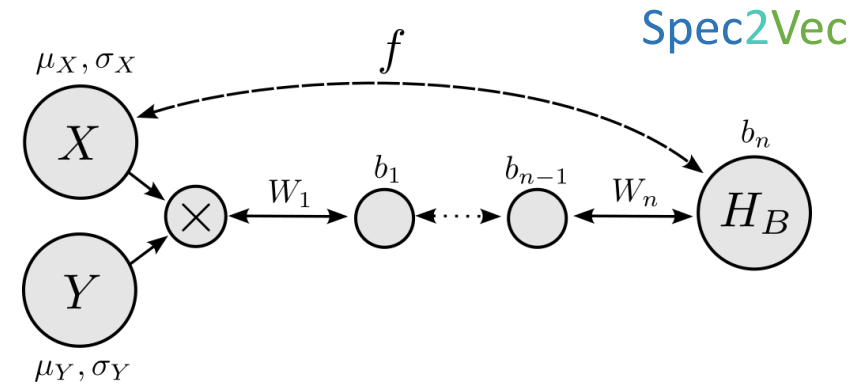
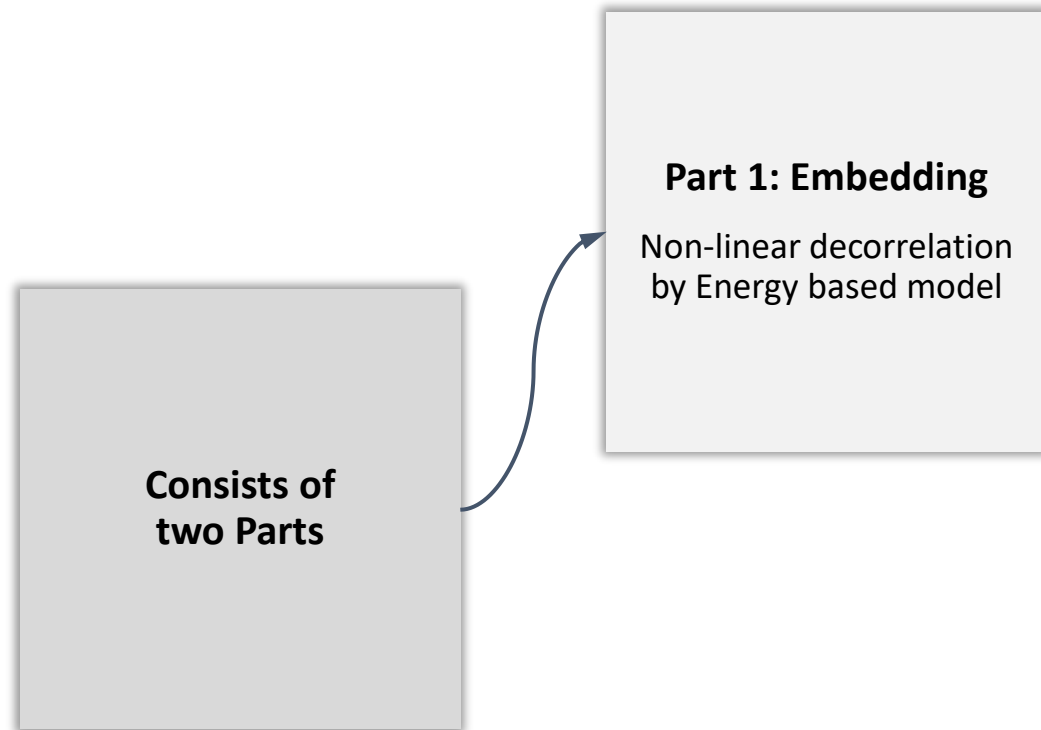


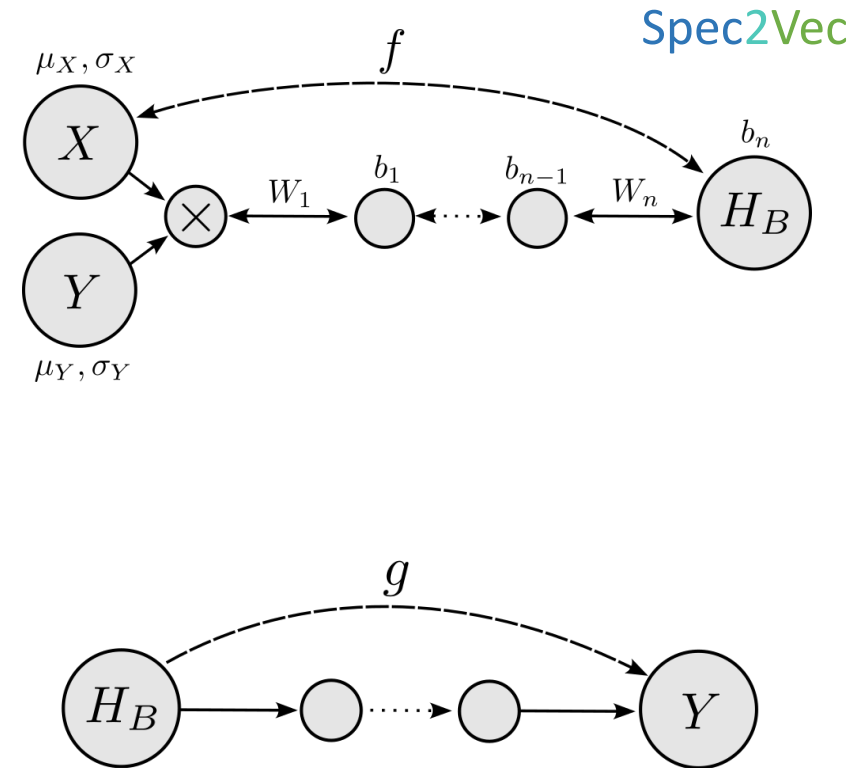
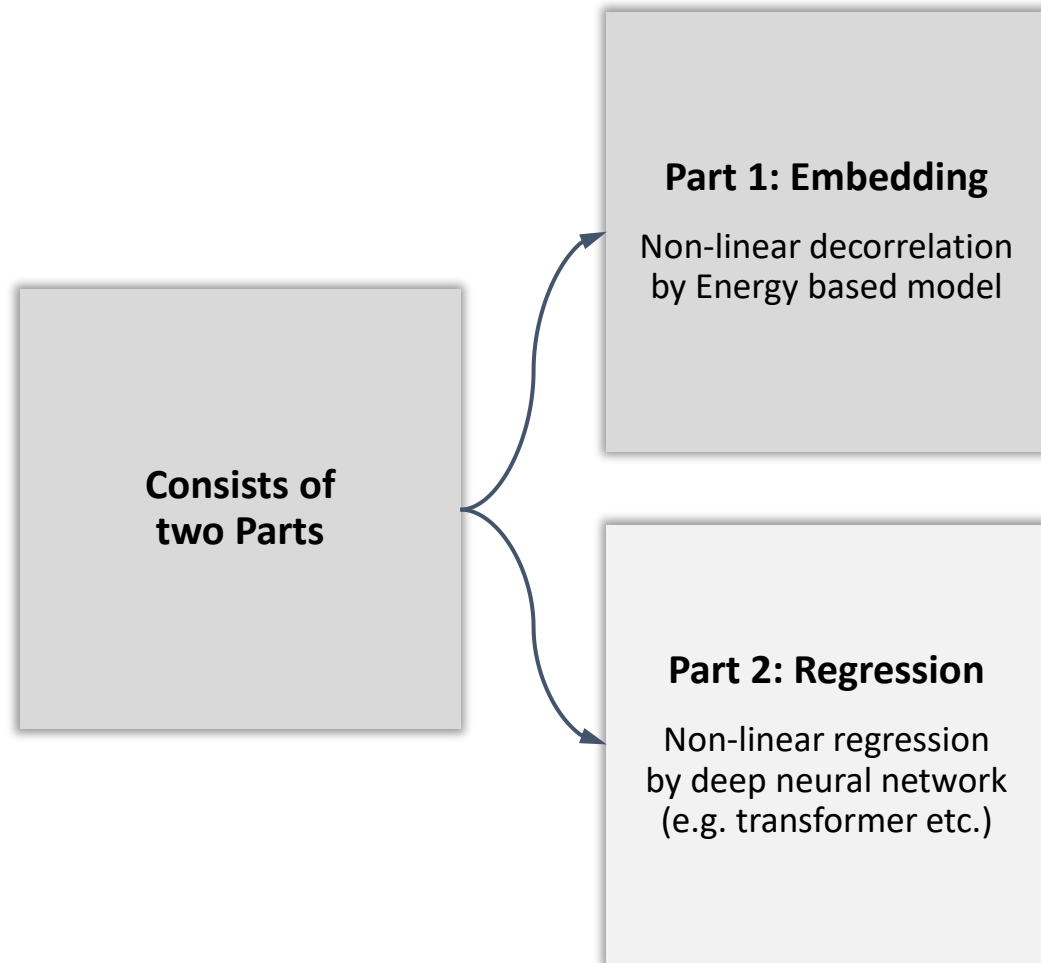
Non-linear **Regression** in Energy based Calibration



**Consists of
two Parts**







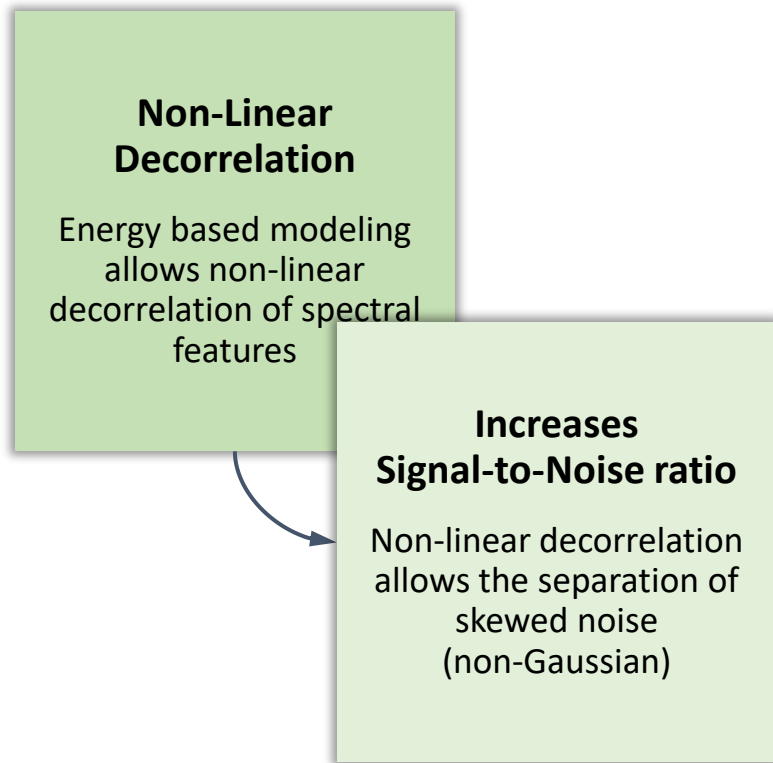
What can be concluded
about **Energy based Calibration**?

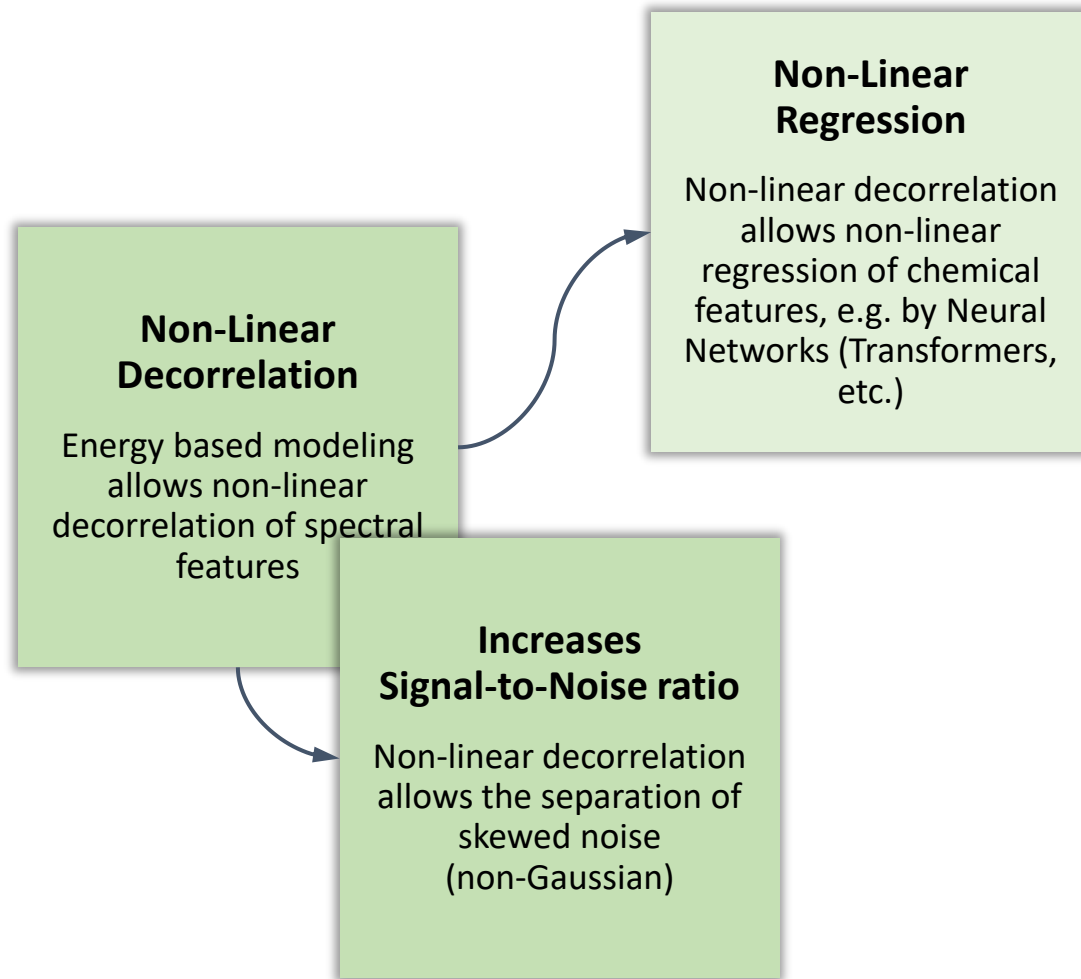


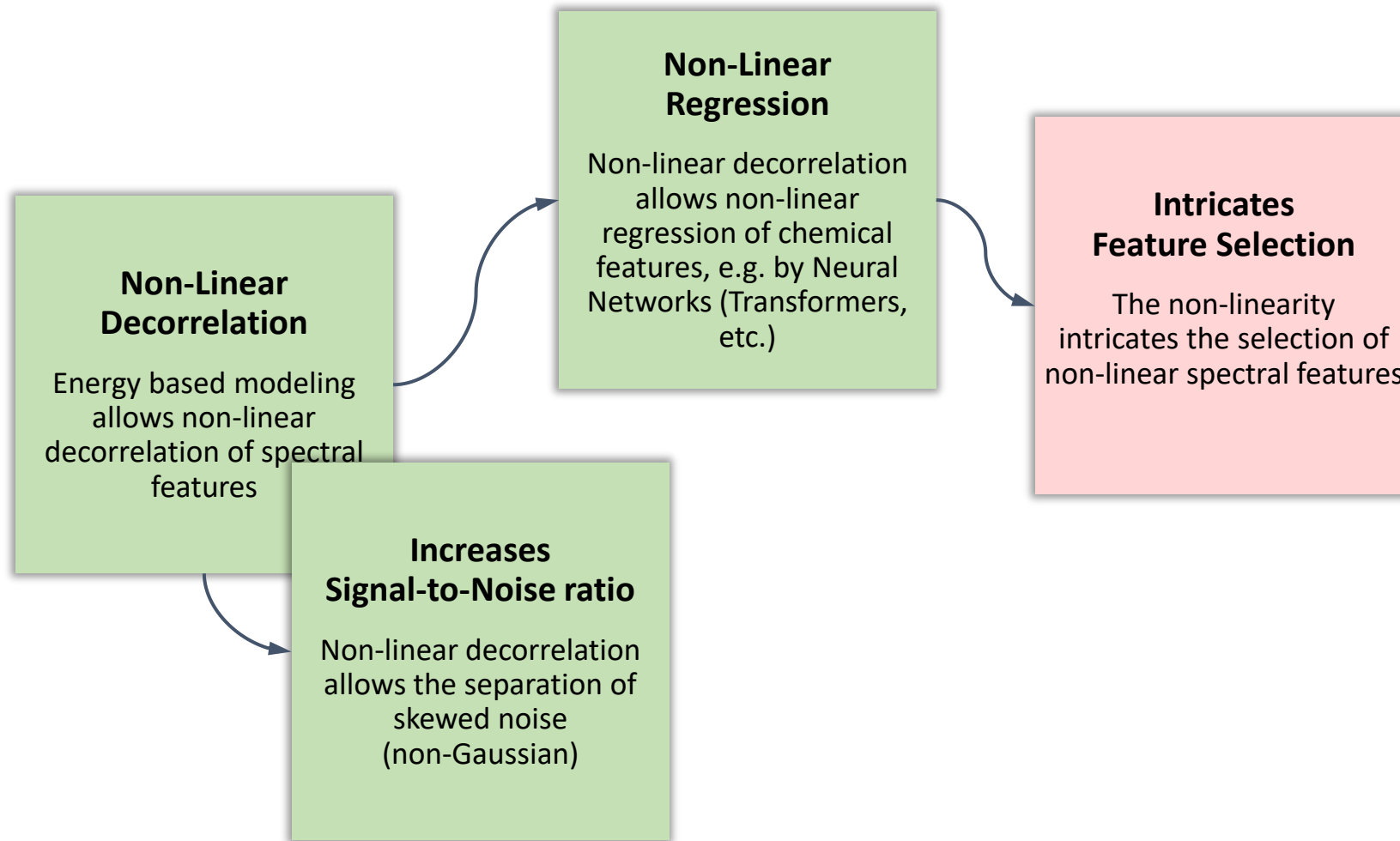
Non-Linear Decorrelation

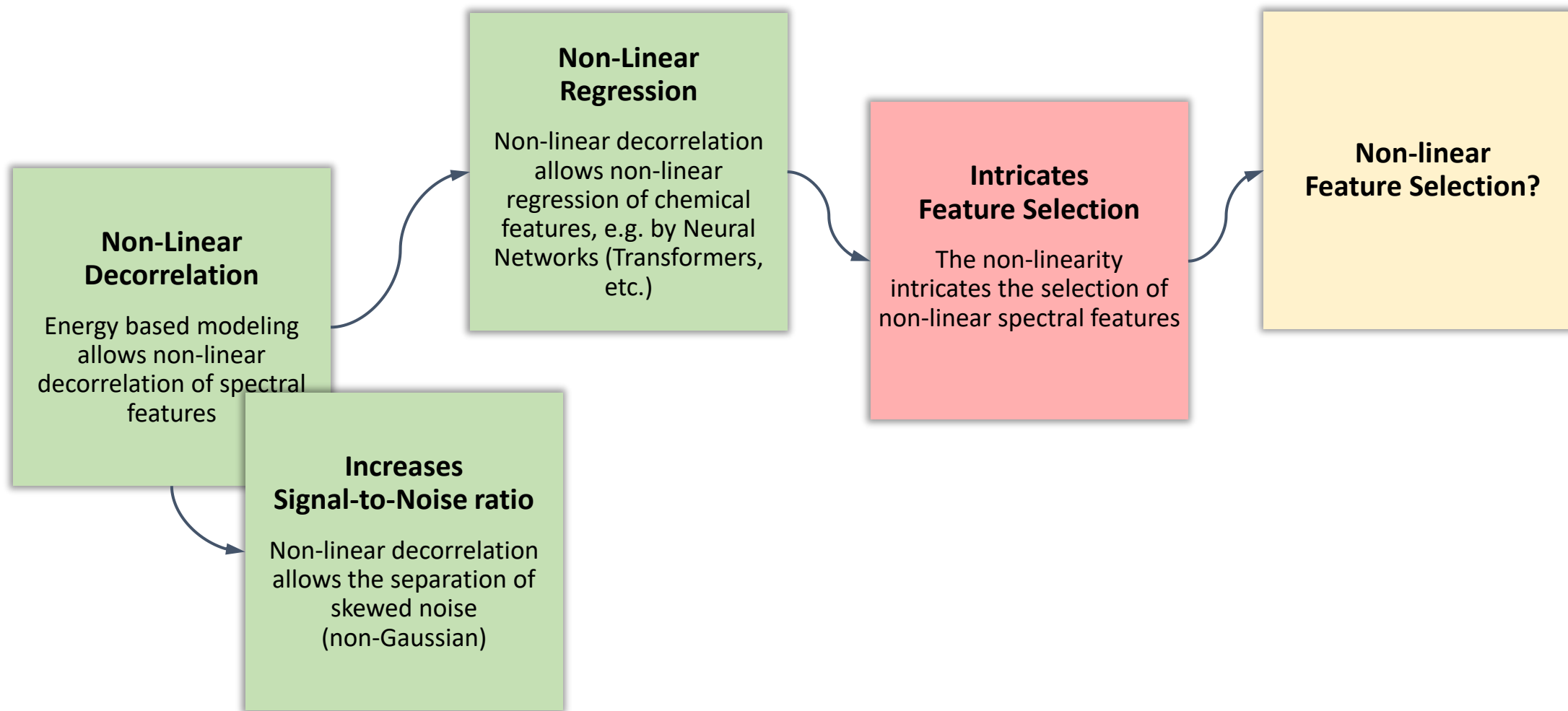
Energy based modeling
allows non-linear
decorrelation of spectral
features

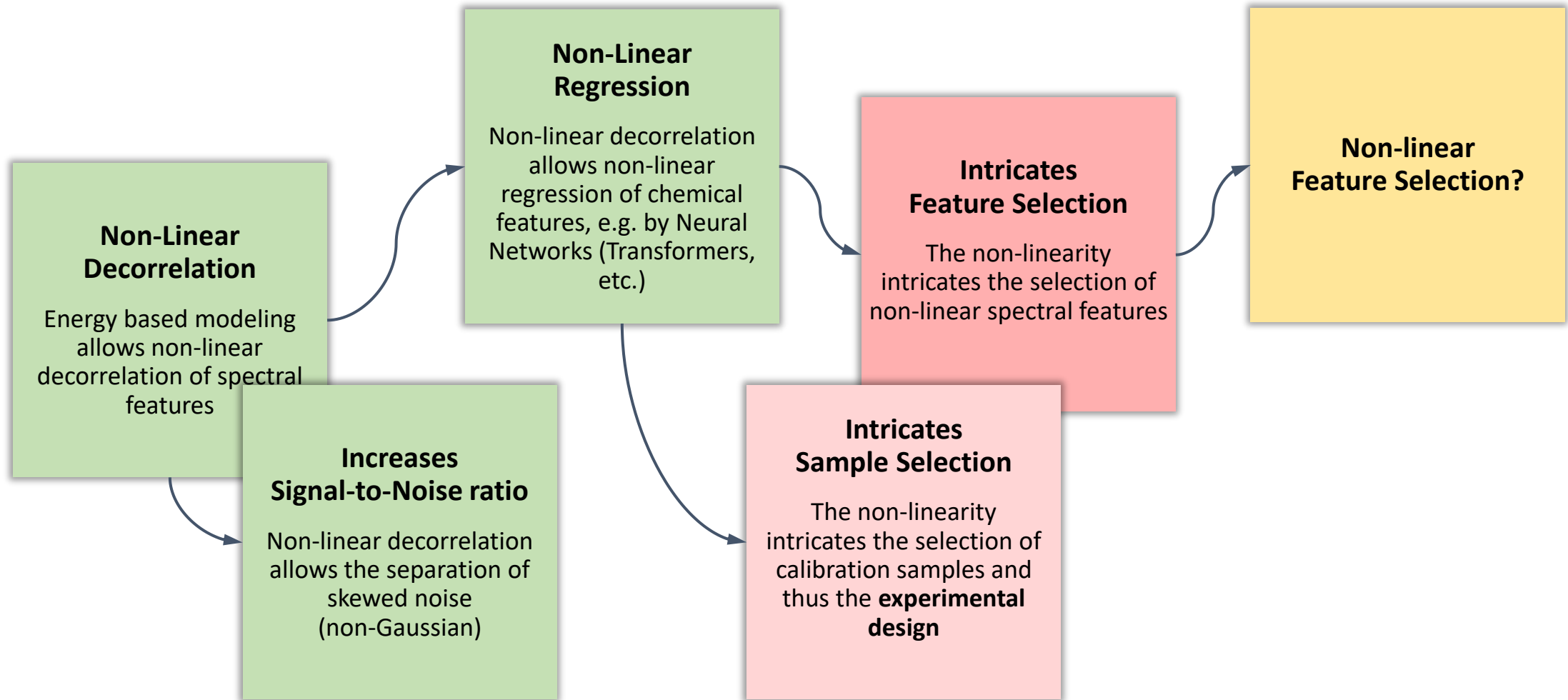


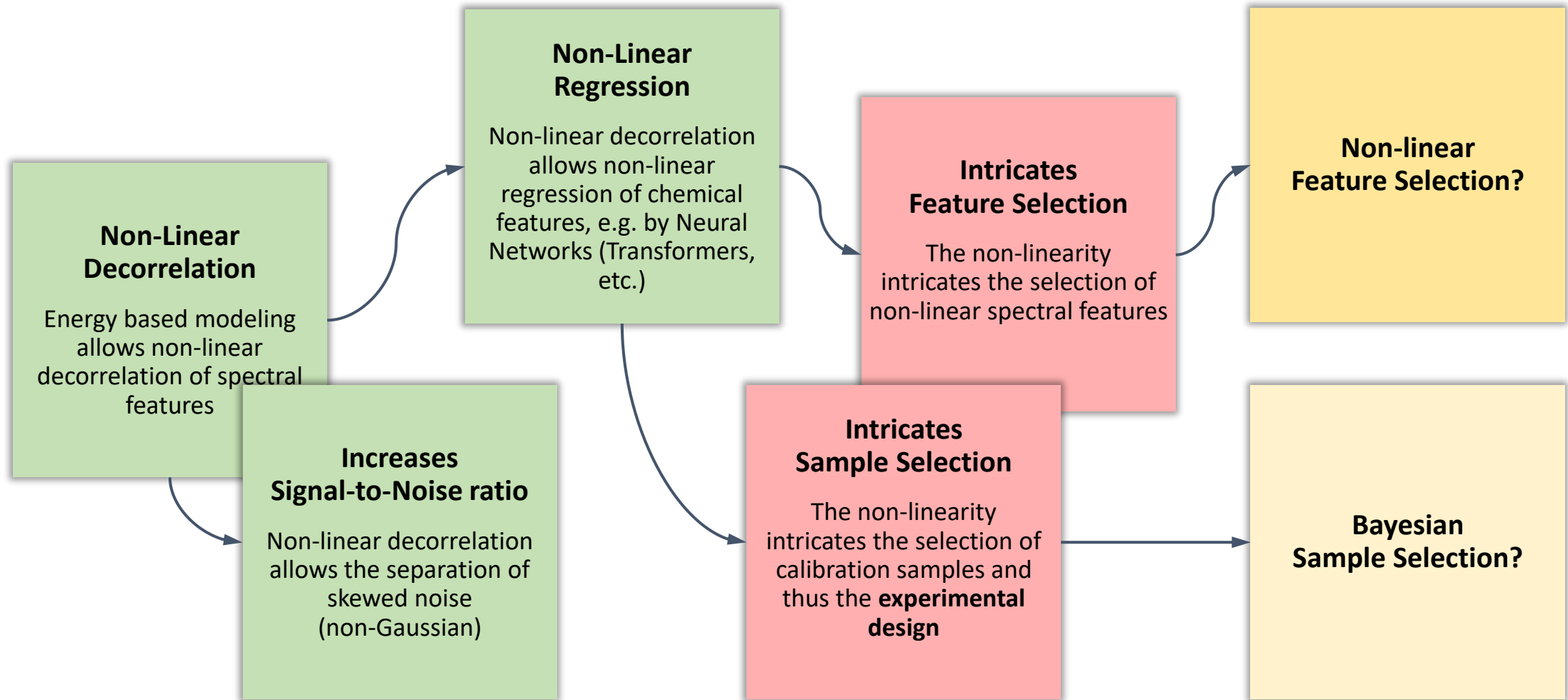












Part 4

Non-linear feature selection

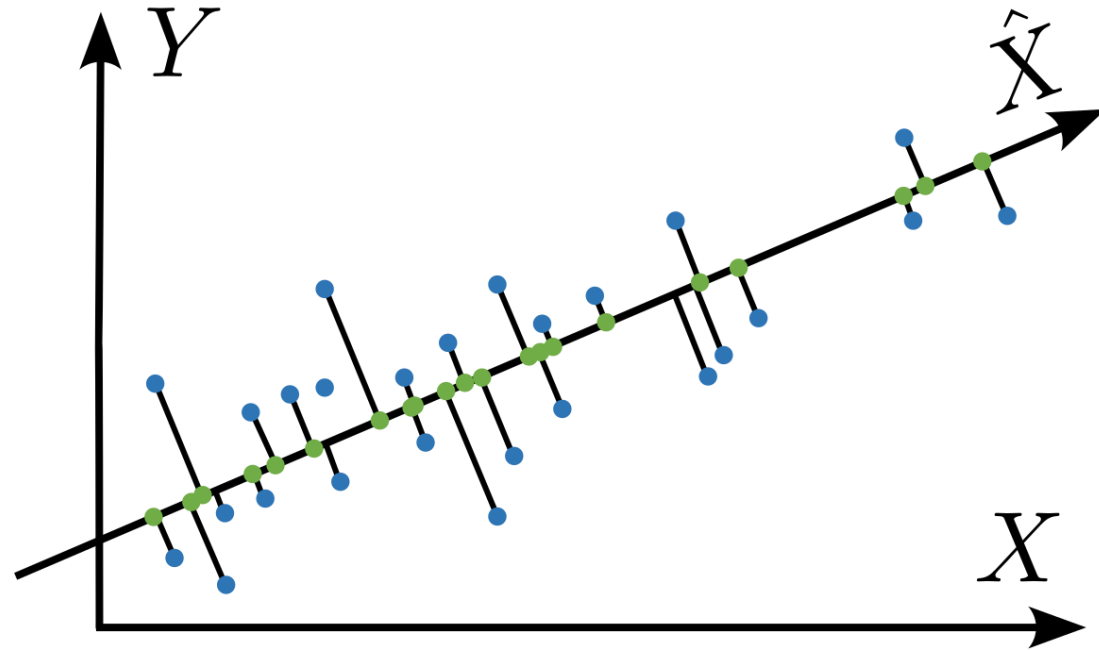


Differential Geometric feature selection for *Principal Components*



Example (Line)

Feature Selection for
Principal Component

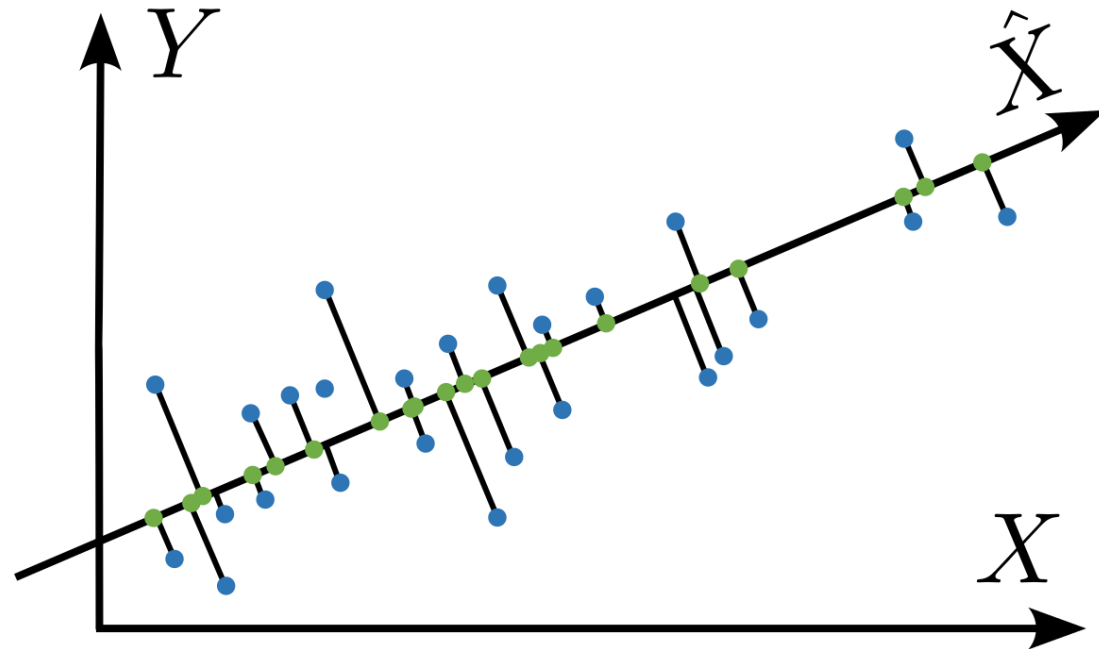


Example (Line)

Feature Selection for
Principal Component

Approach 1: Statistical

Calculate empirical
correlations:



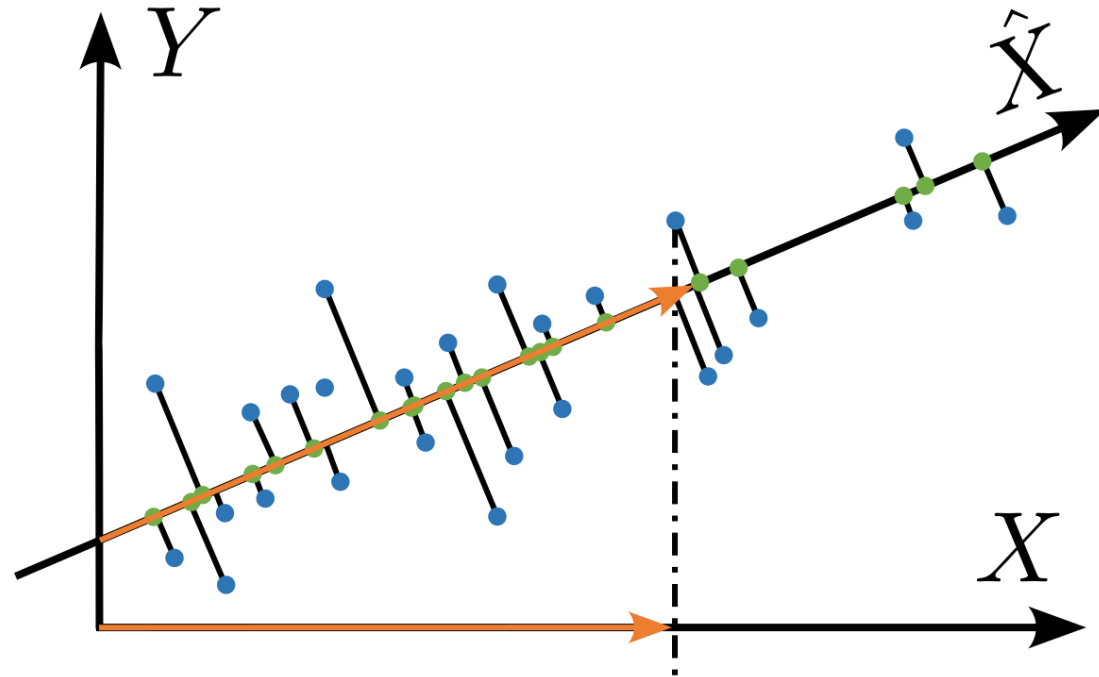
Example (Line)

Feature Selection for
Principal Component

Approach 1: Statistical

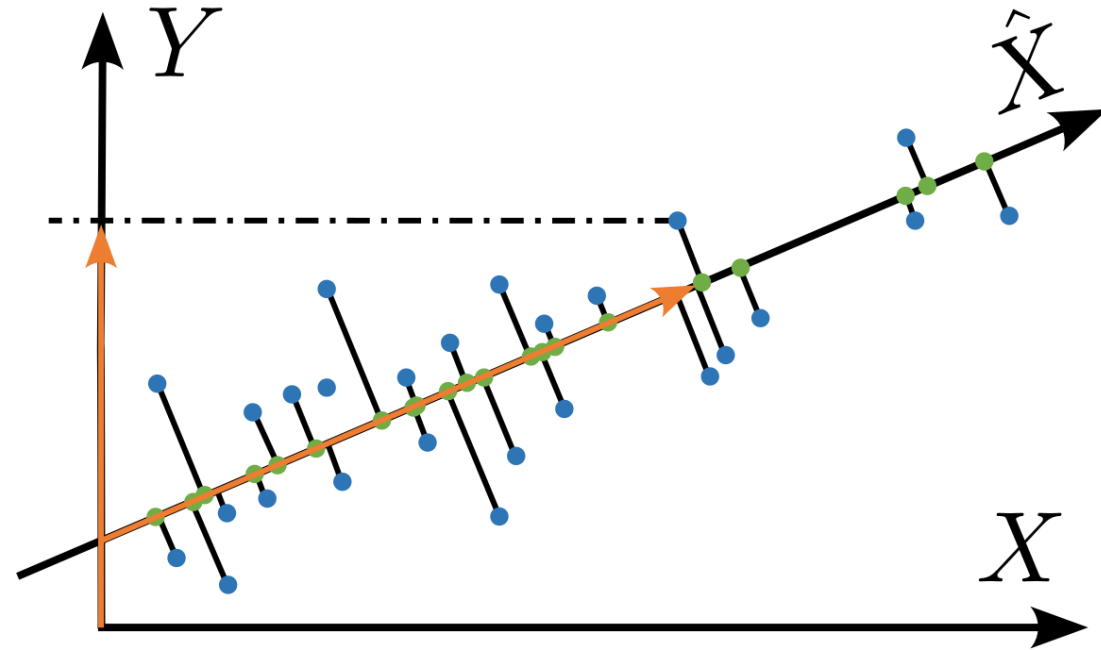
Calculate empirical
correlations:

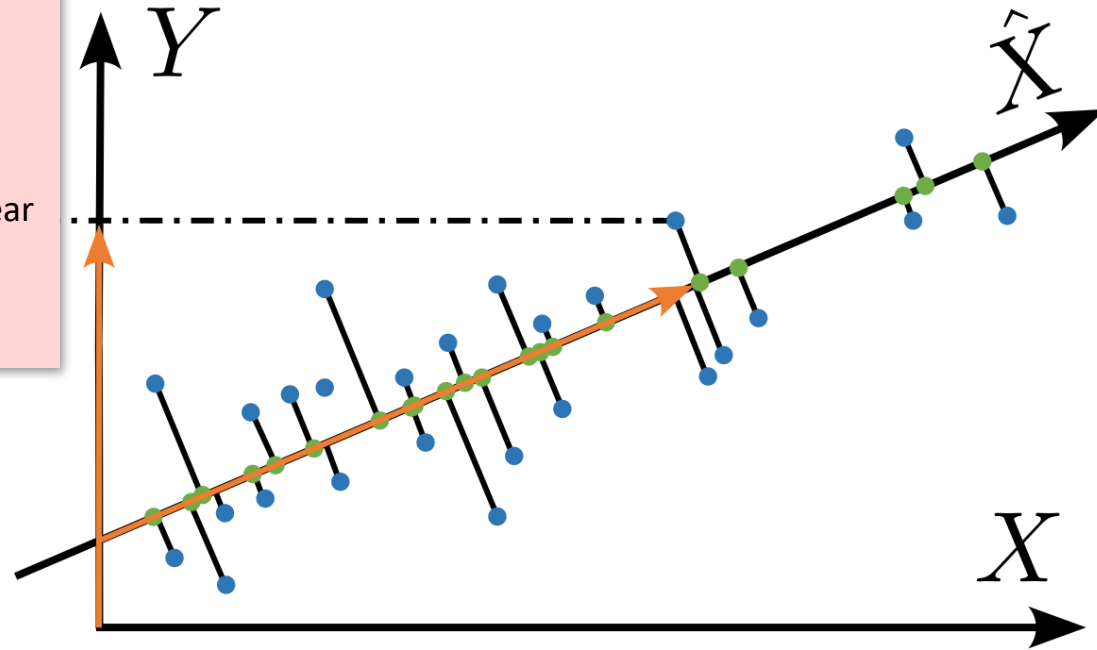
$$\text{corr}(\hat{X}, X)$$



Feature Selection for Principal Component

Calculate empirical correlations:

$$\text{corr}(\hat{X}, X) > \text{corr}(\hat{X}, Y)$$


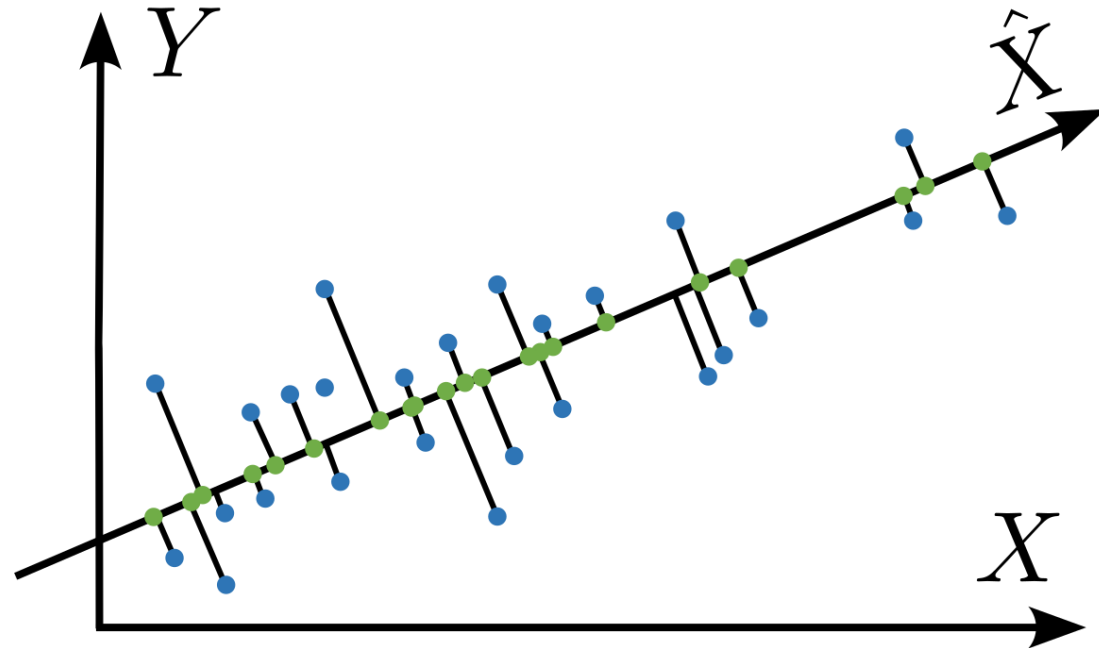


Example (Line)

Feature Selection for
Principal Component

Approach 2: Geometrical

Calculate partial
derivatives:



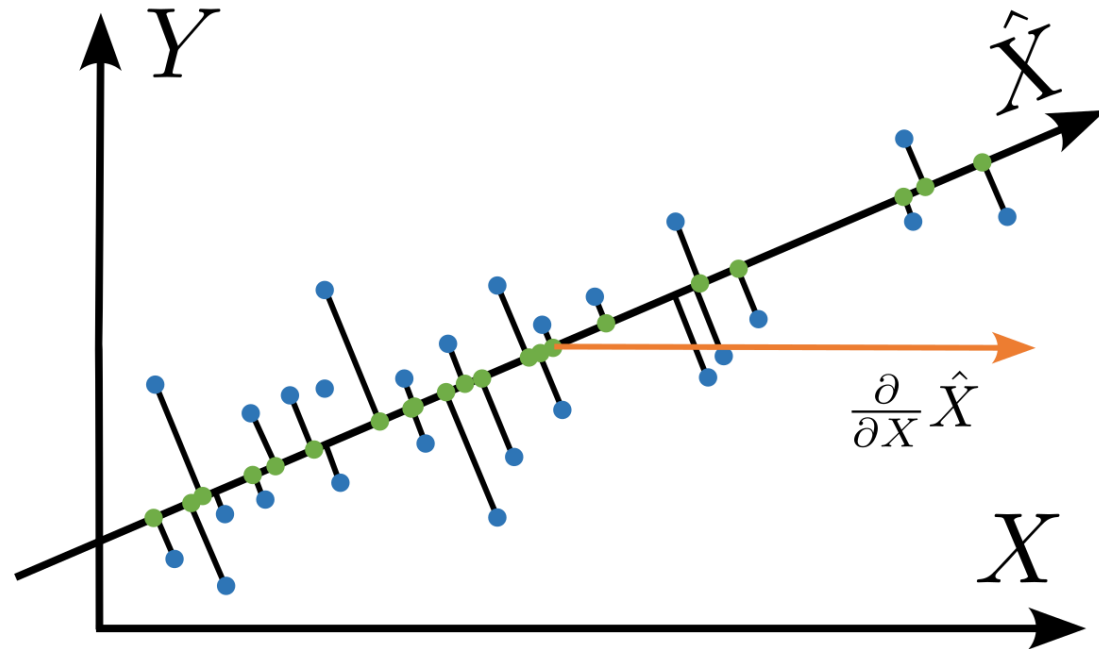
Example (Line)

Feature Selection for
Principal Component

Approach 2: Geometrical

Calculate partial
derivatives:

$$\left| \frac{\partial}{\partial X} \hat{X} \right|$$



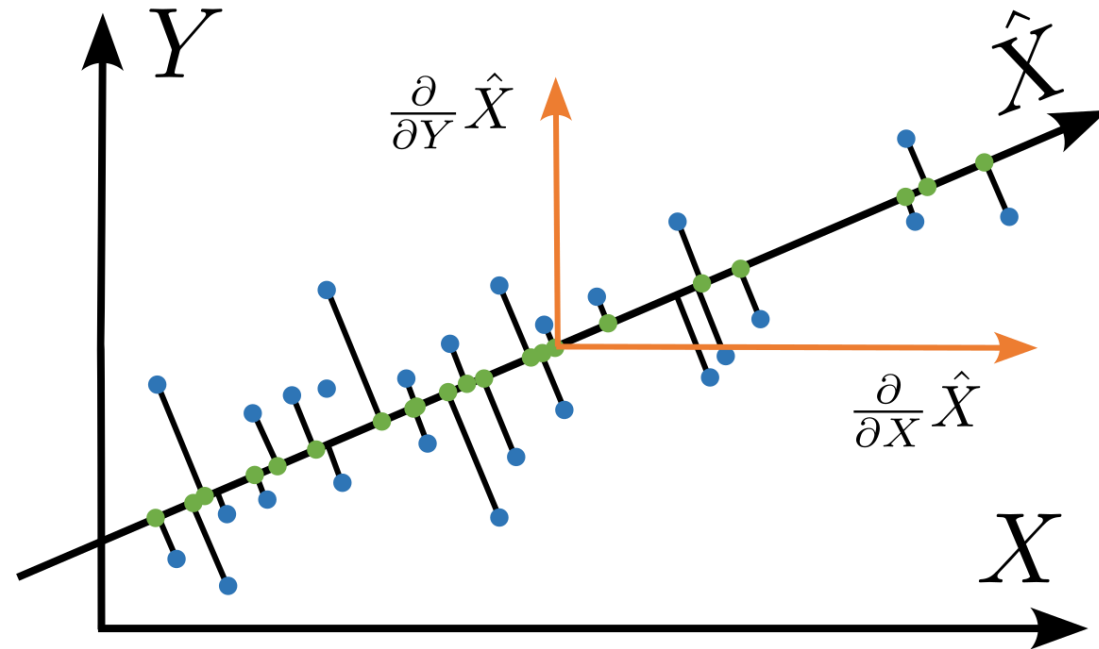
Example (Line)

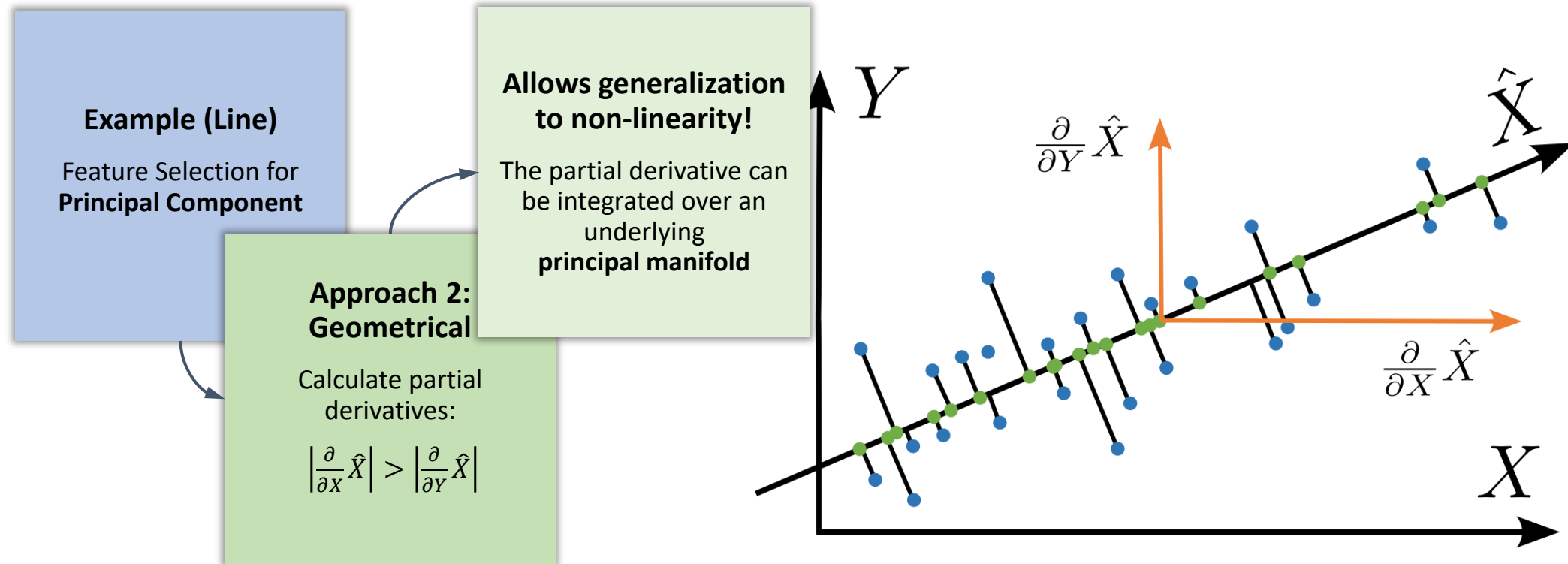
Feature Selection for
Principal Component

Approach 2: Geometrical

Calculate partial
derivatives:

$$\left| \frac{\partial}{\partial X} \hat{X} \right| > \left| \frac{\partial}{\partial Y} \hat{X} \right|$$



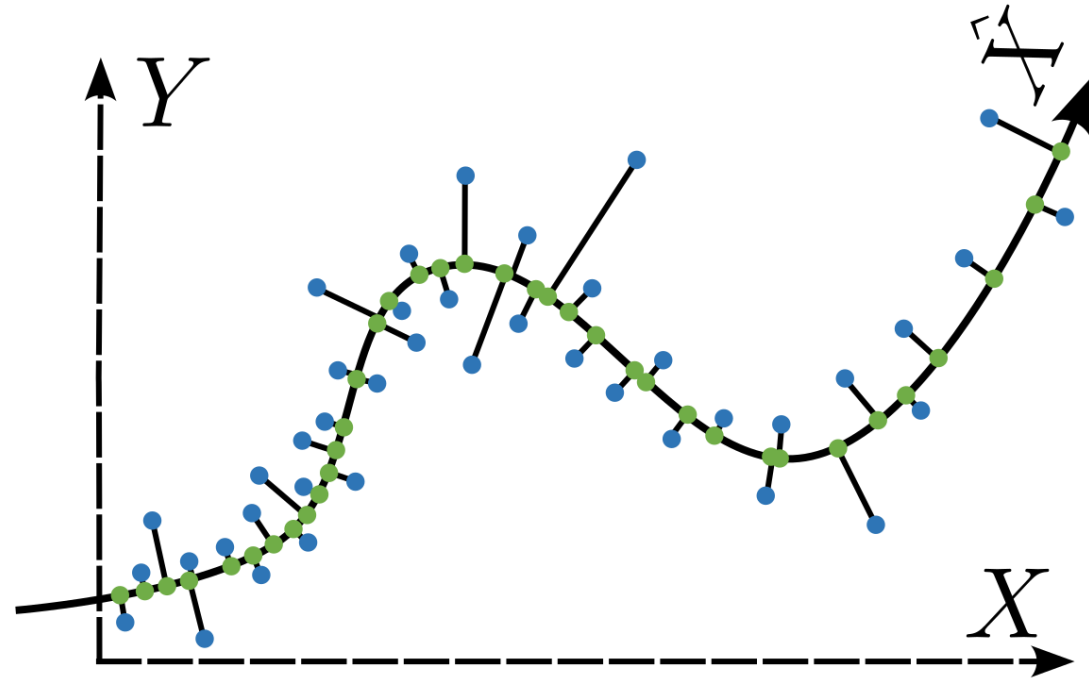


Differential Geometric feature selection for *Principal Manifolds*



Example (Curve)

Feature Selection for
Principal Curve

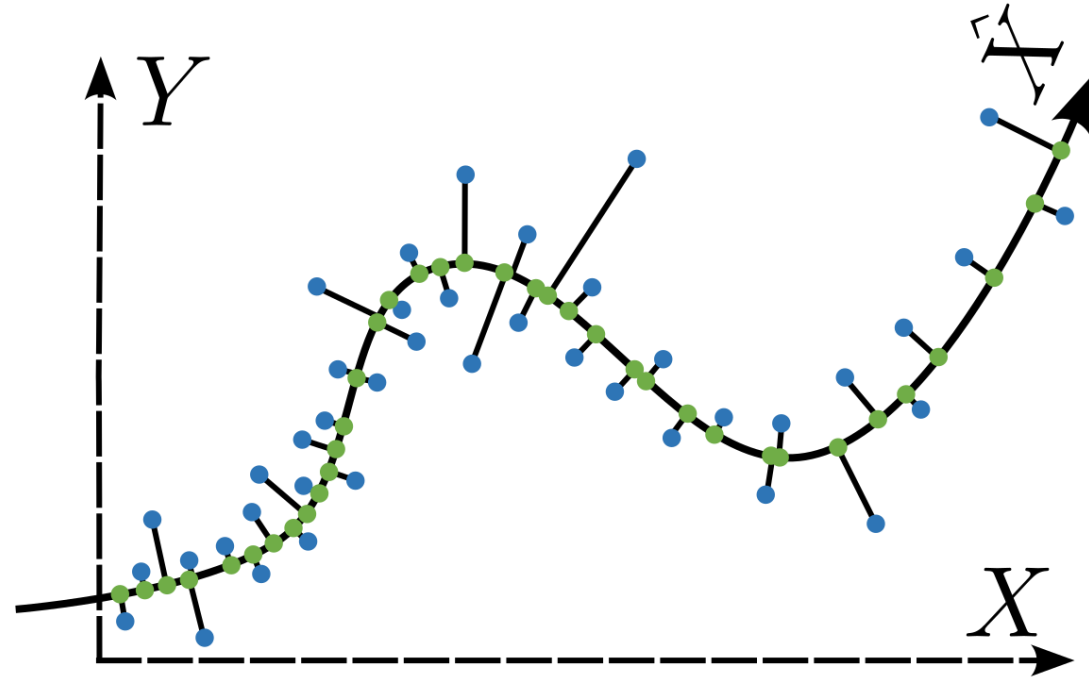


Example (Curve)

Feature Selection for
Principal Curve

Approach 1: Analytical Integration

Calculate integrals of
partial derivatives
along curve

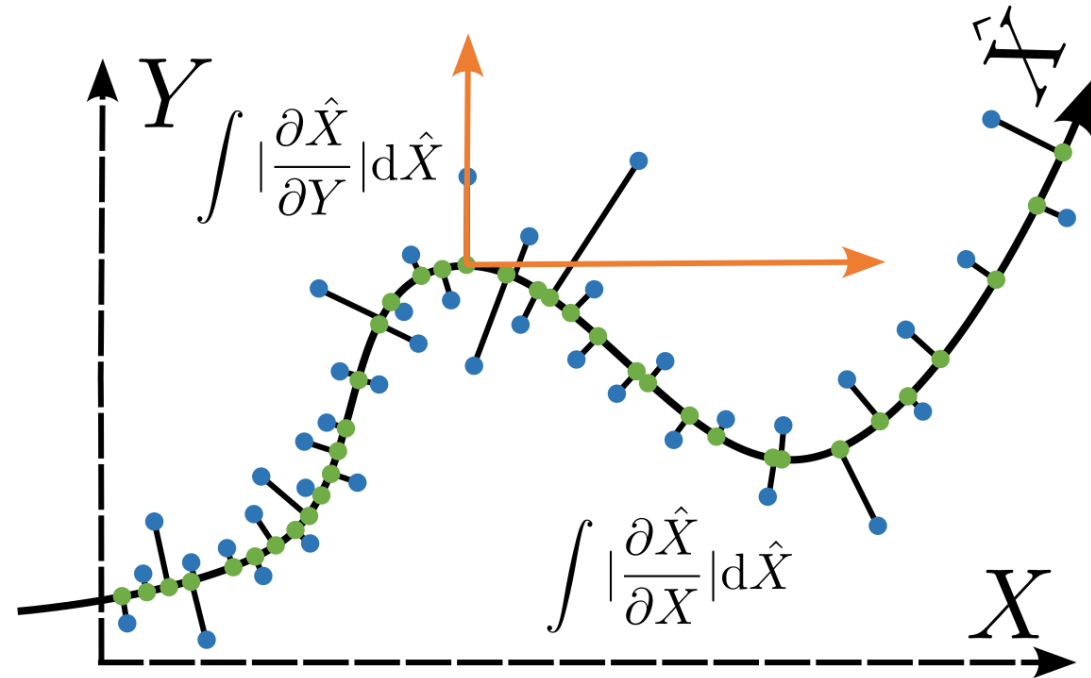


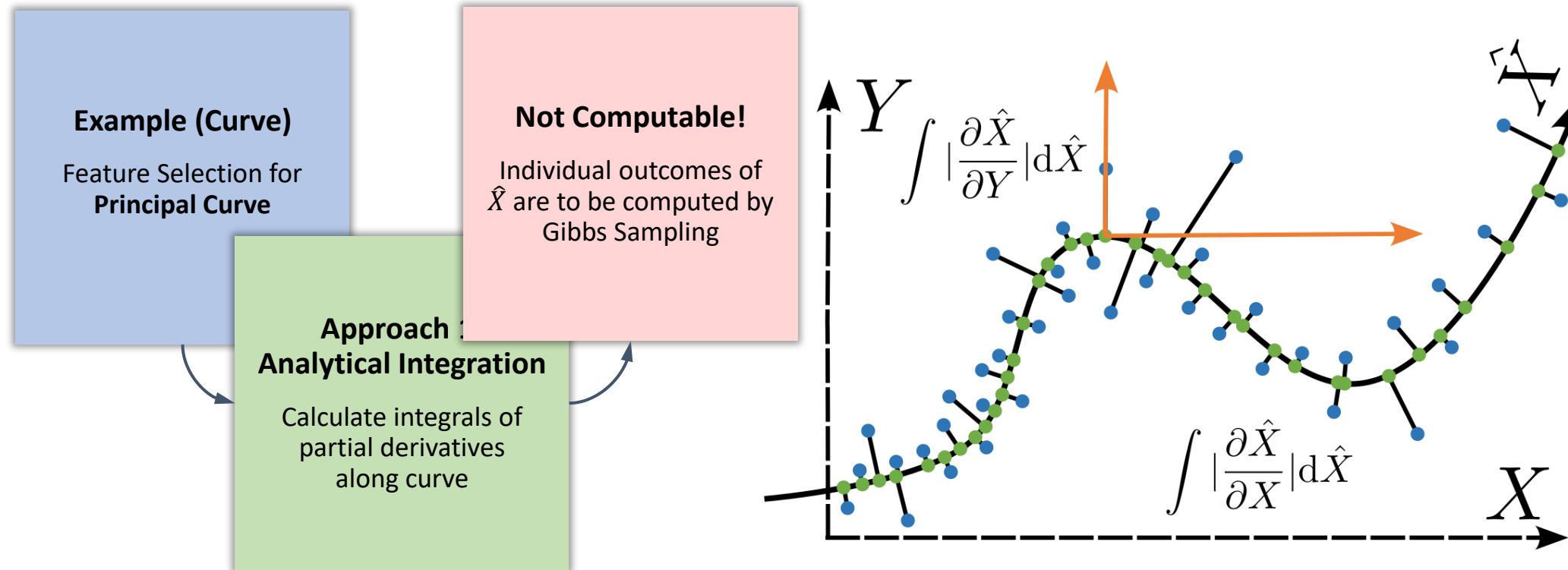
Example (Curve)

Feature Selection for
Principal Curve

Approach 1: Analytical Integration

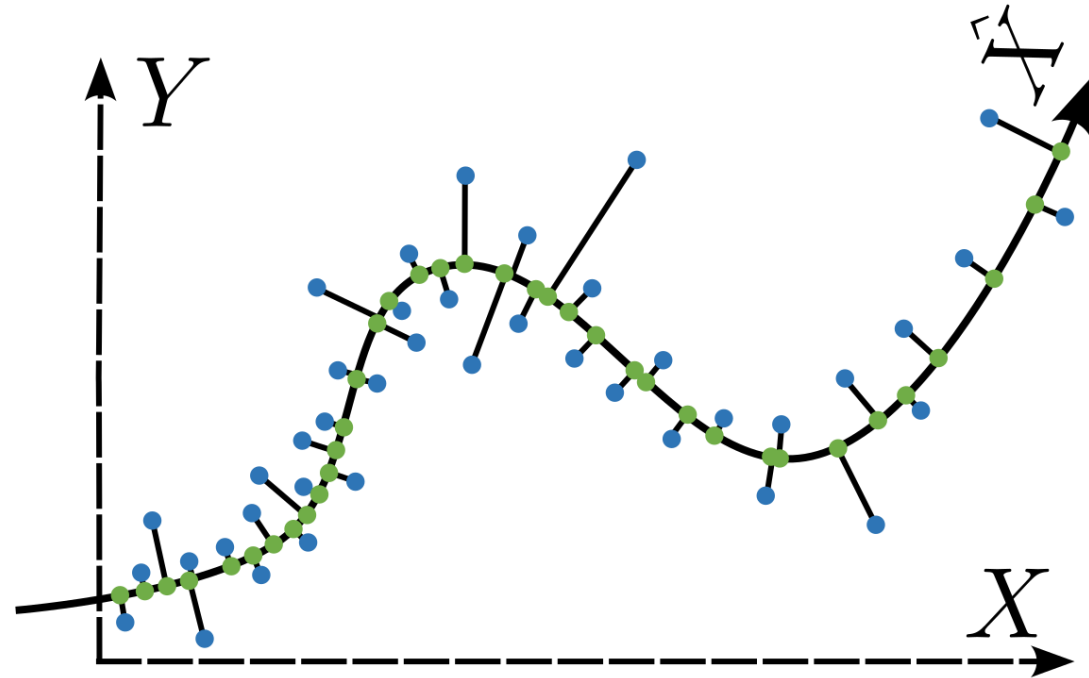
Calculate integrals of
partial derivatives
along curve





Example (Curve)

Feature Selection for
Principal Curve

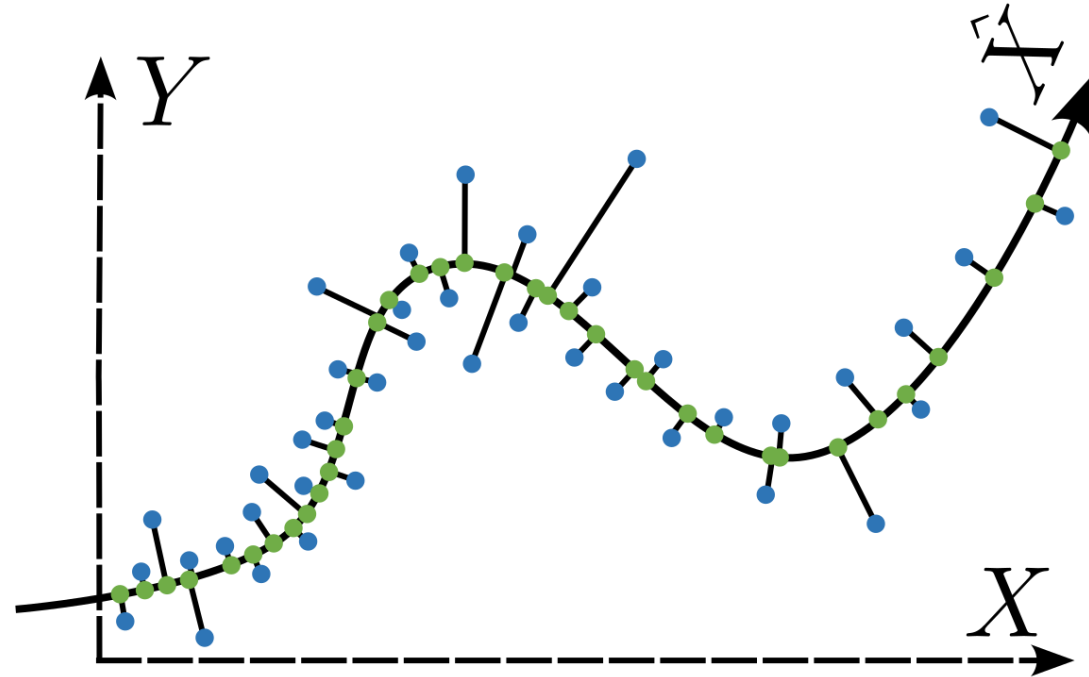


Example (Curve)

Feature Selection for
Principal Curve

Approach 2: Monte Carlo Integration

Approximate integrals
of partial derivatives
along curve

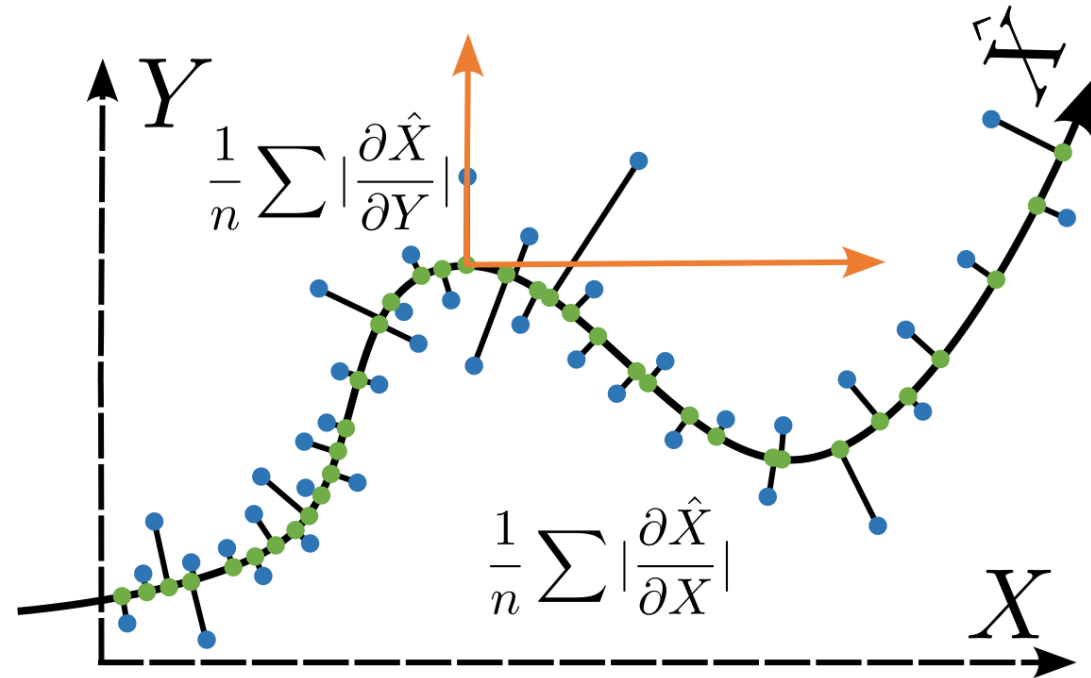


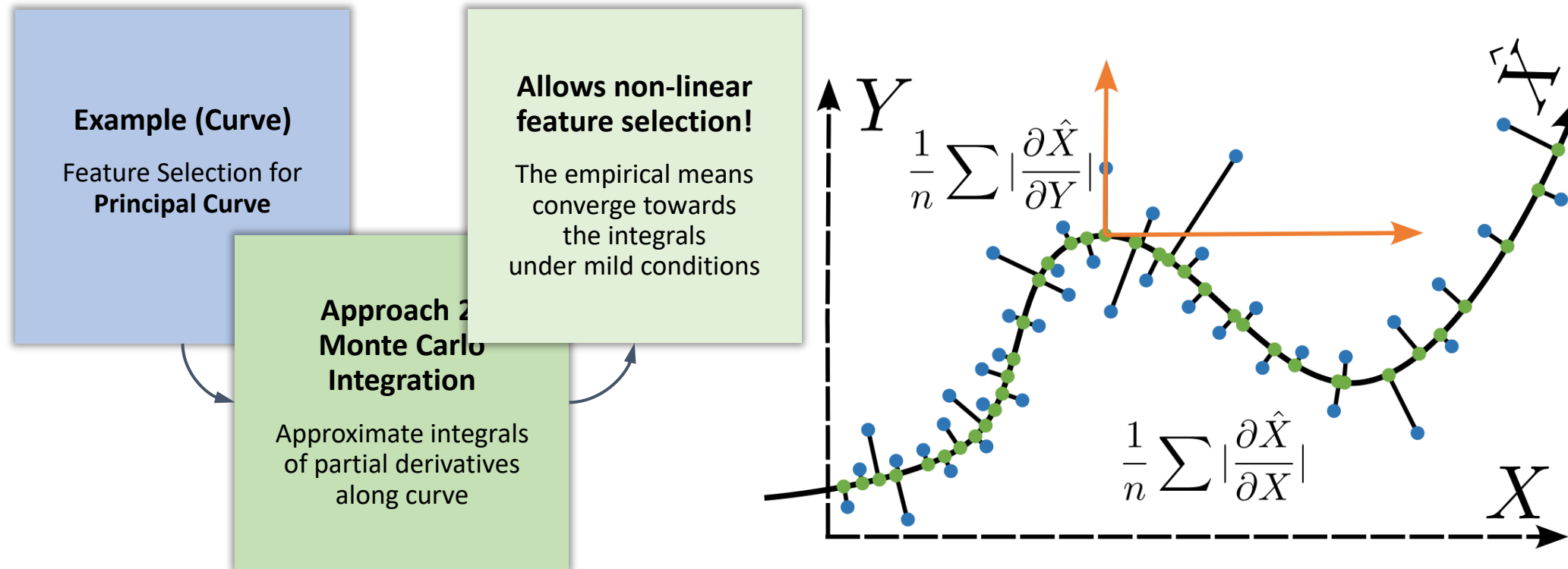
Example (Curve)

Feature Selection for
Principal Curve

Approach 2: Monte Carlo Integration

Approximate integrals
of partial derivatives
along curve





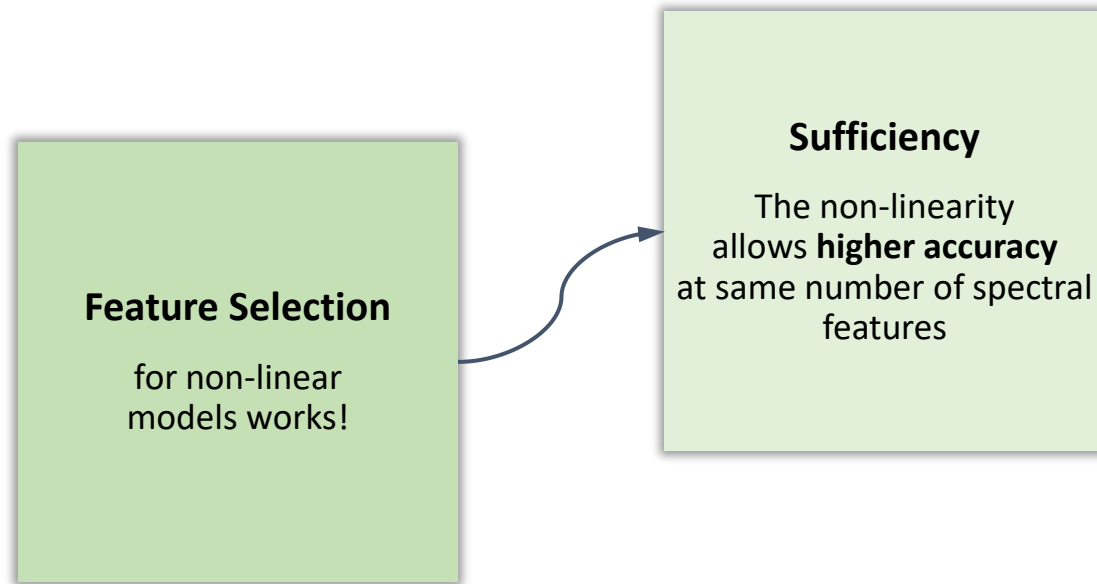
What can be concluded
about **non-linear feature selection**?

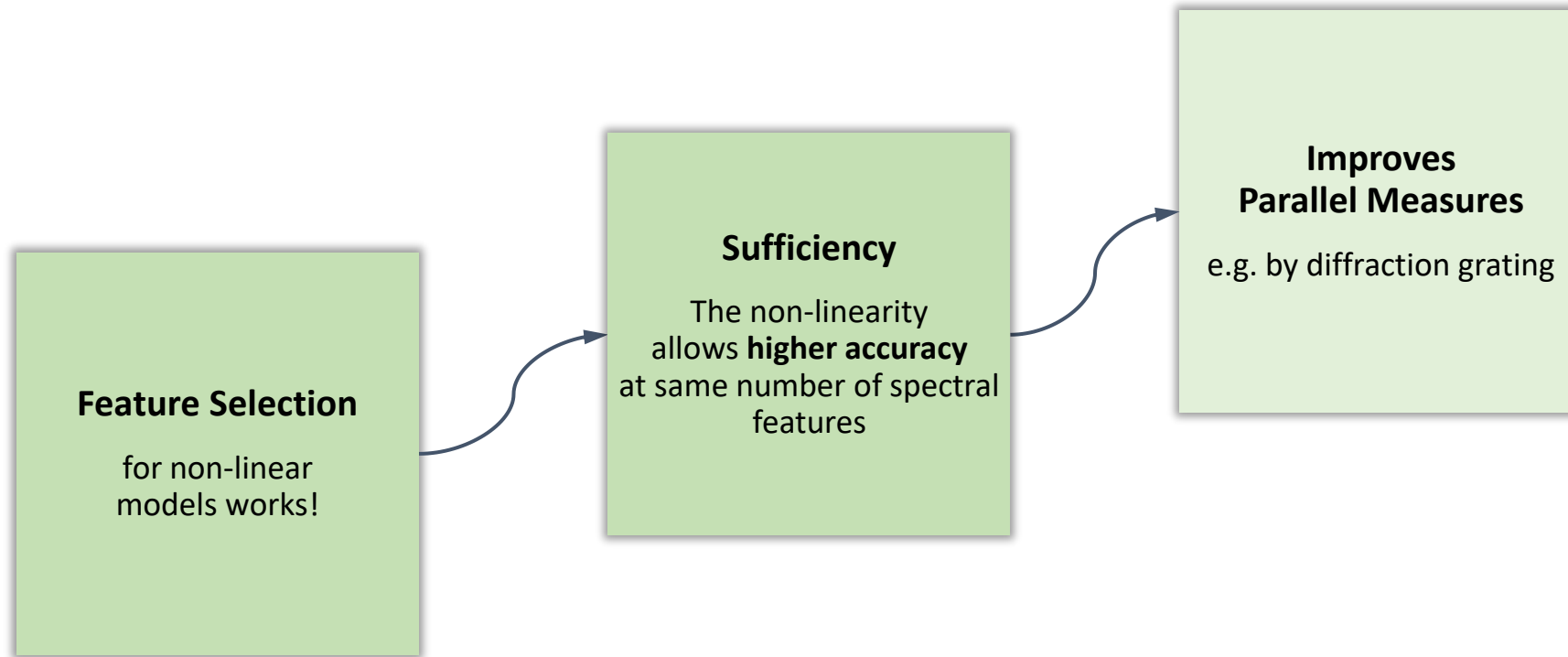


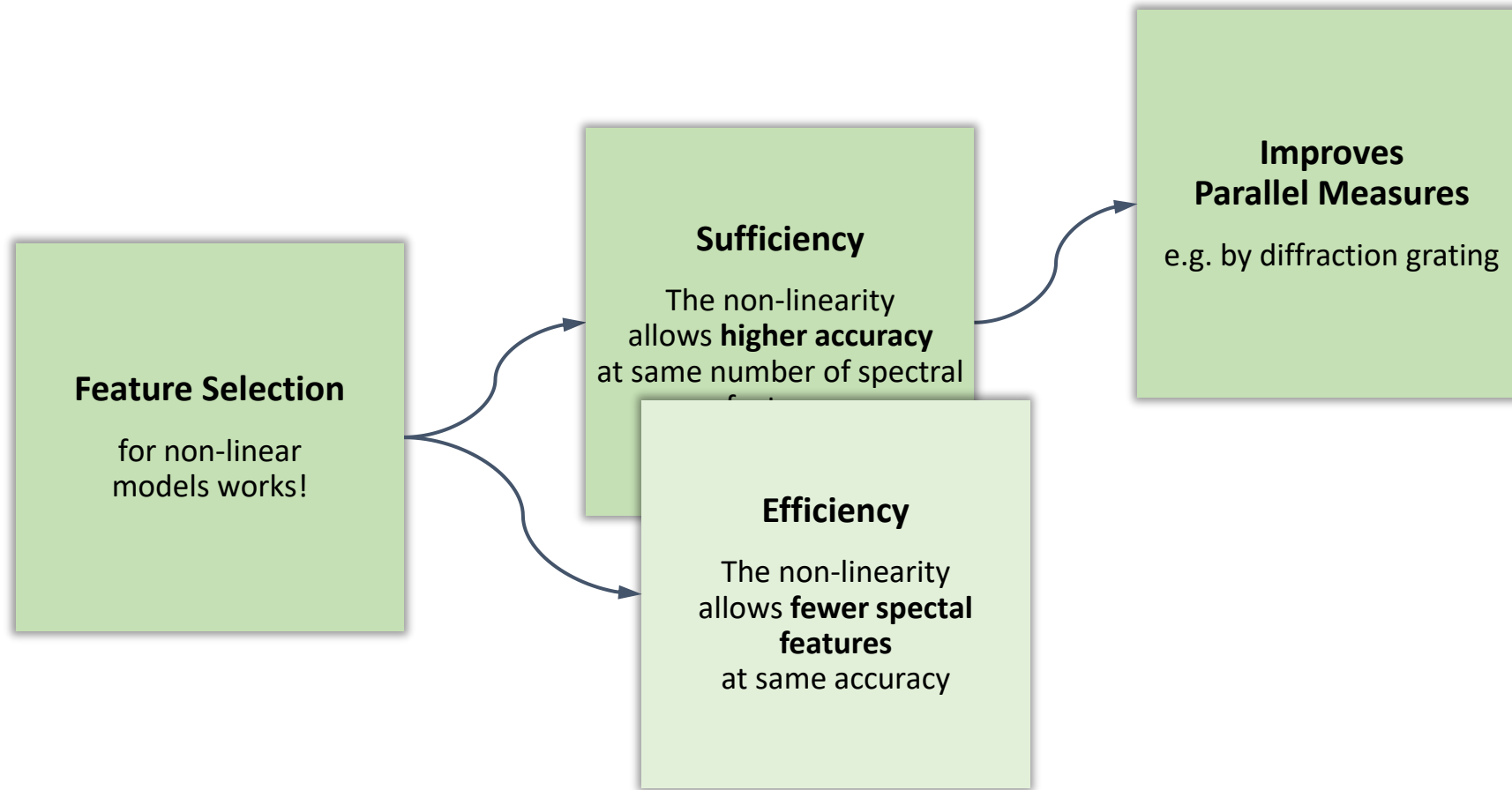
Feature Selection

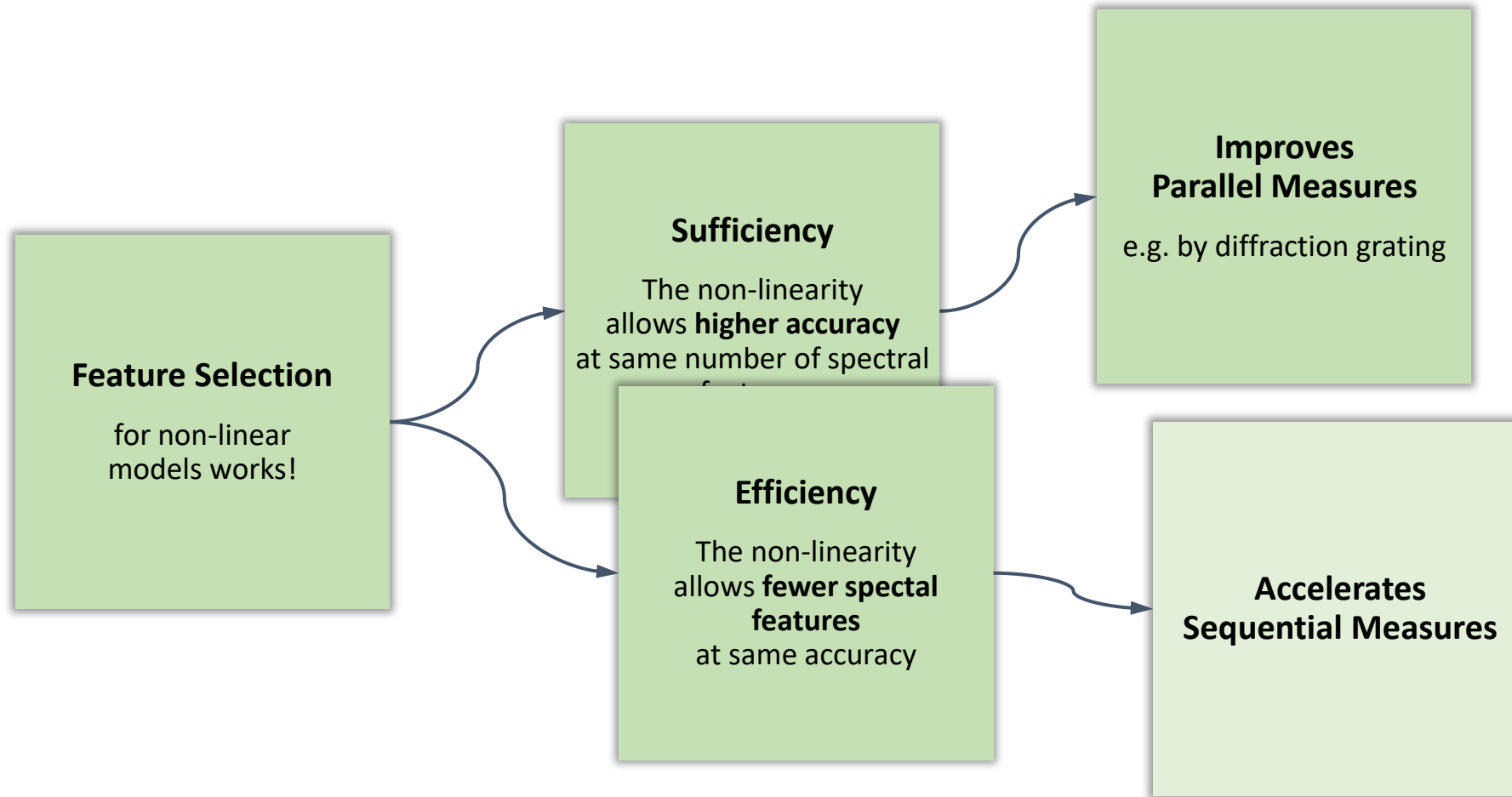
for non-linear
models works!











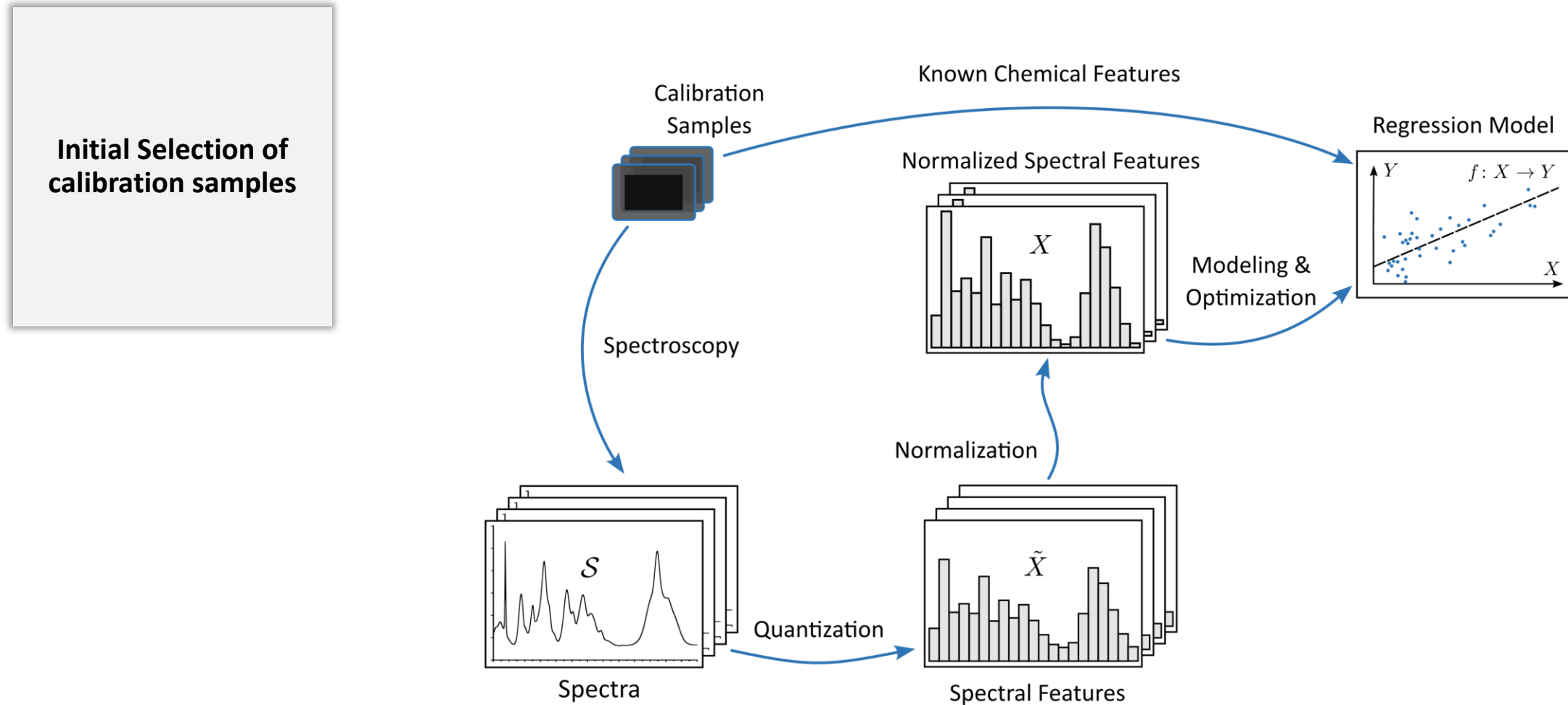
Part 5

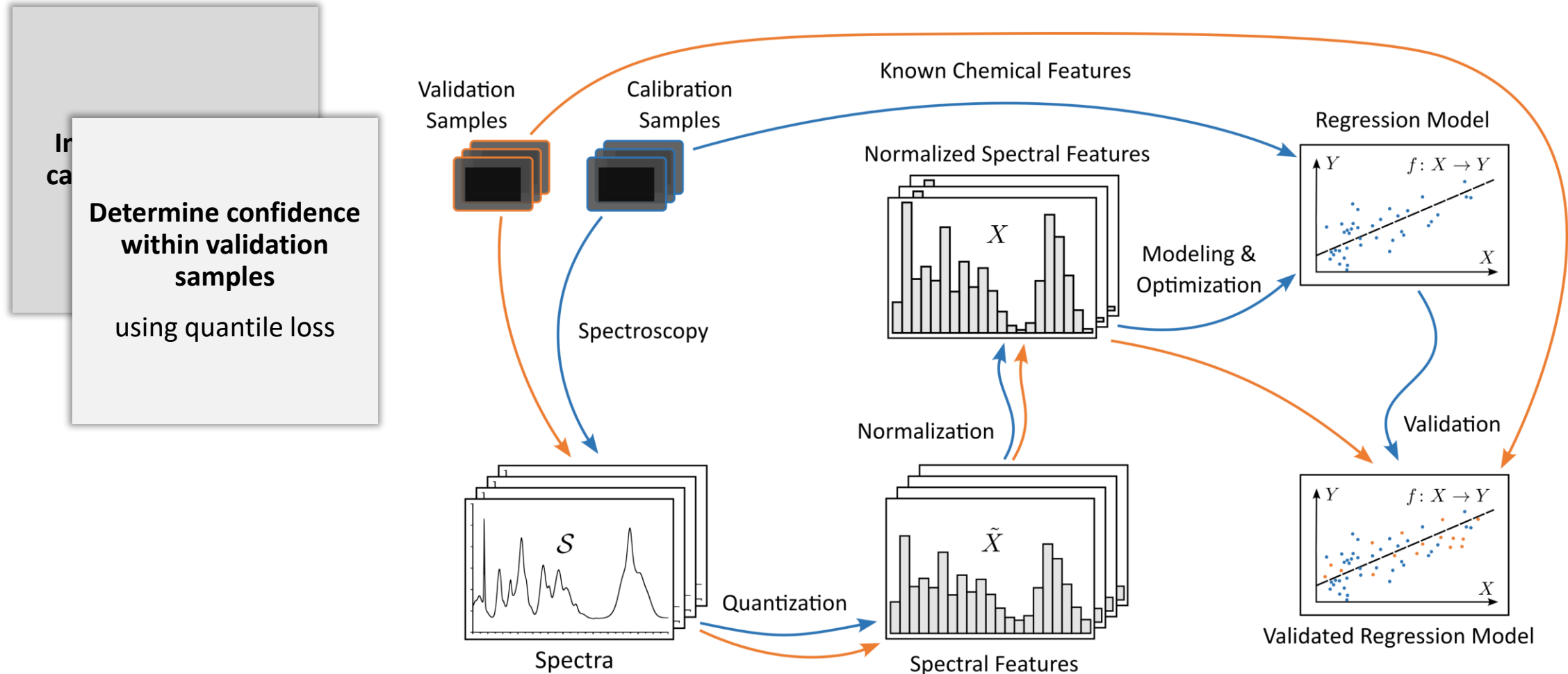
Bayesian sample selection

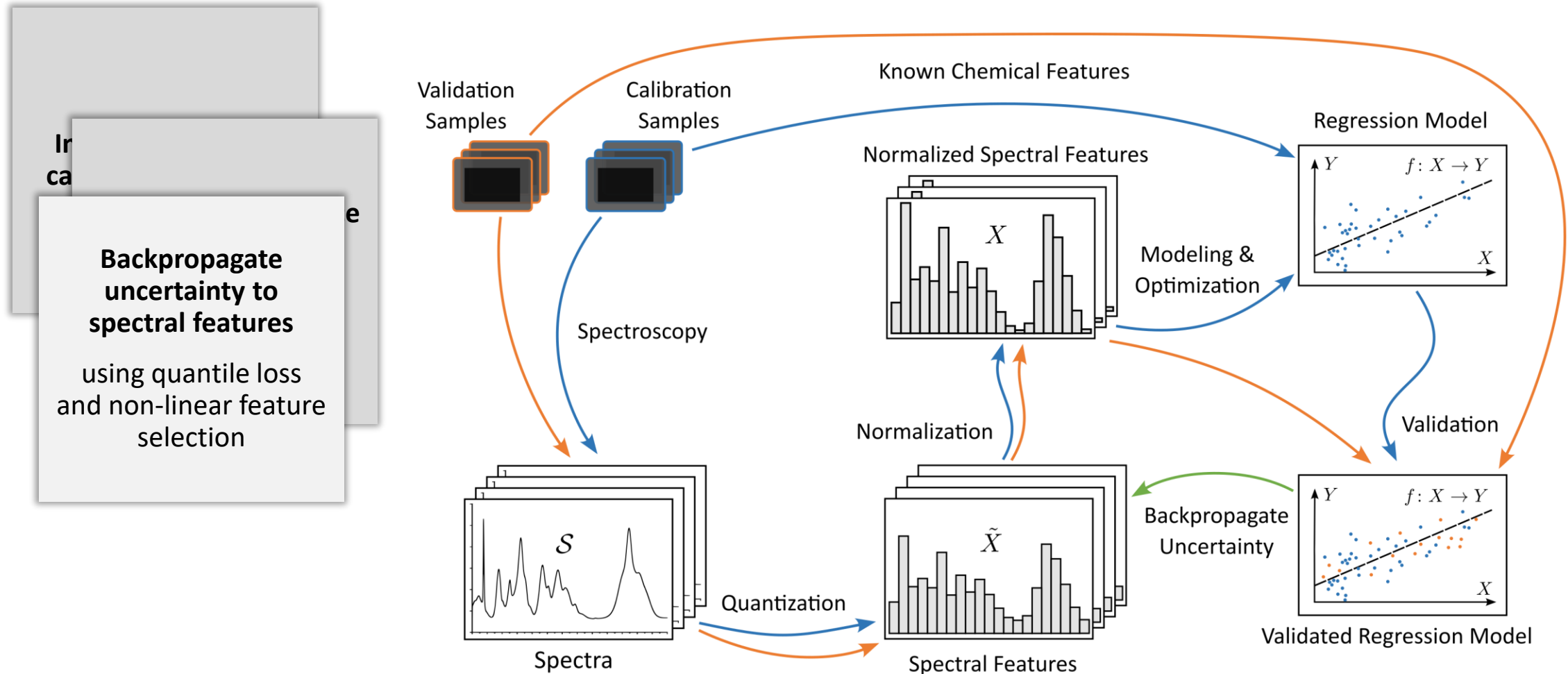


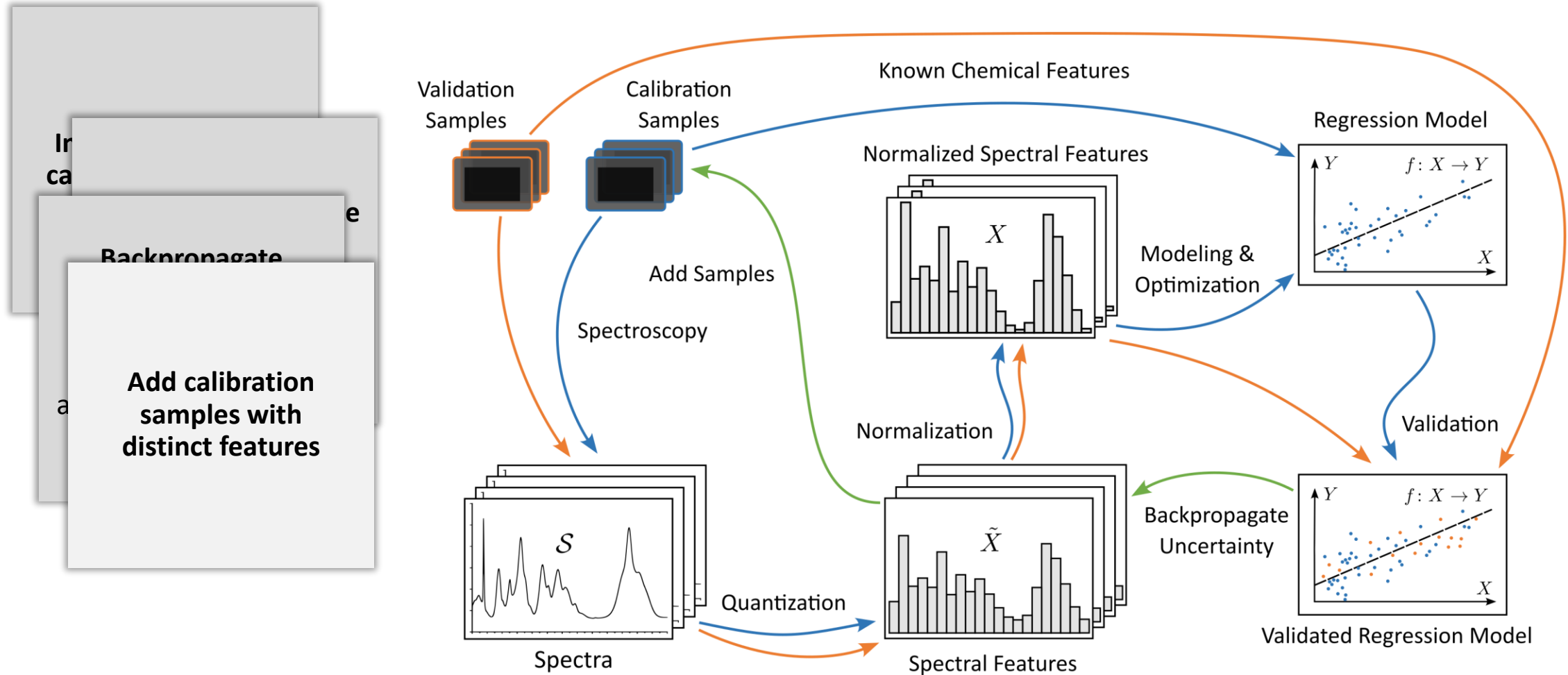
Bayesian Experimental Design











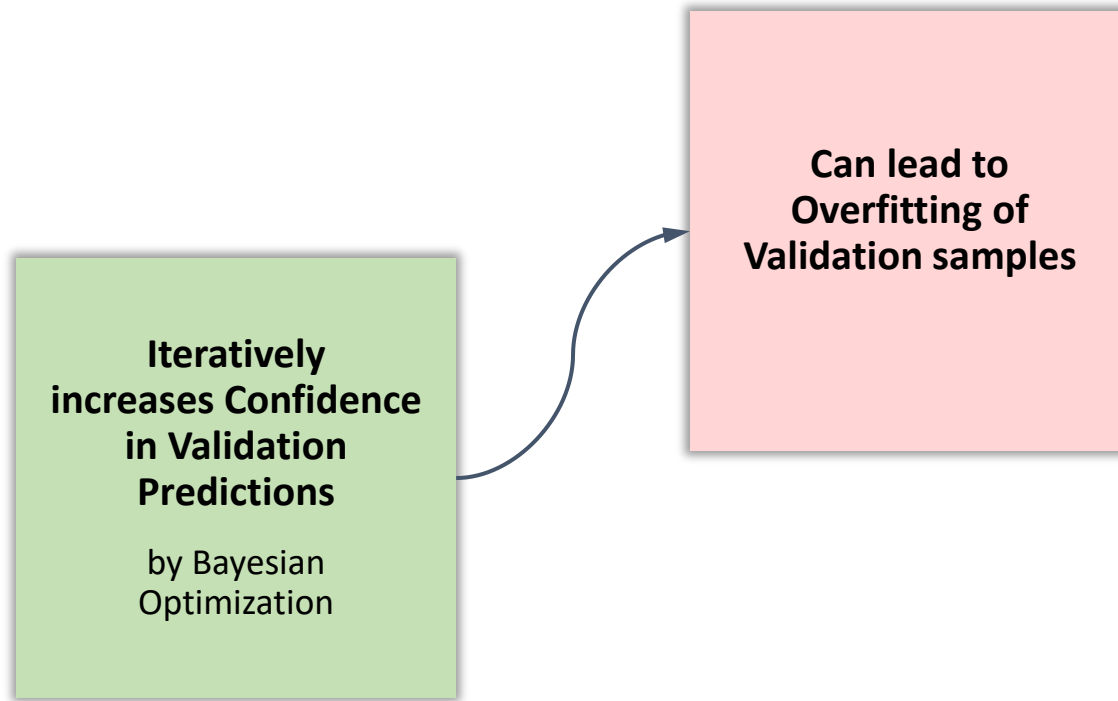
Conclusions about **Bayesian** sample selection

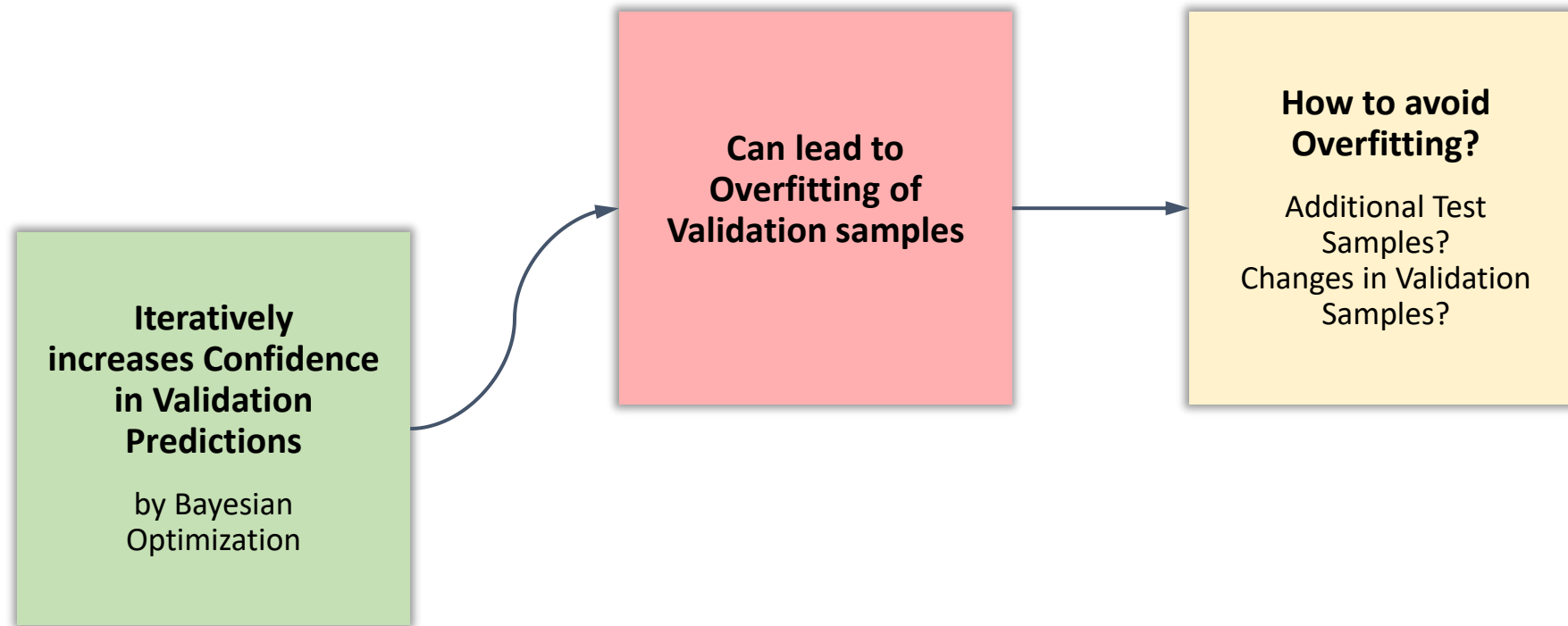


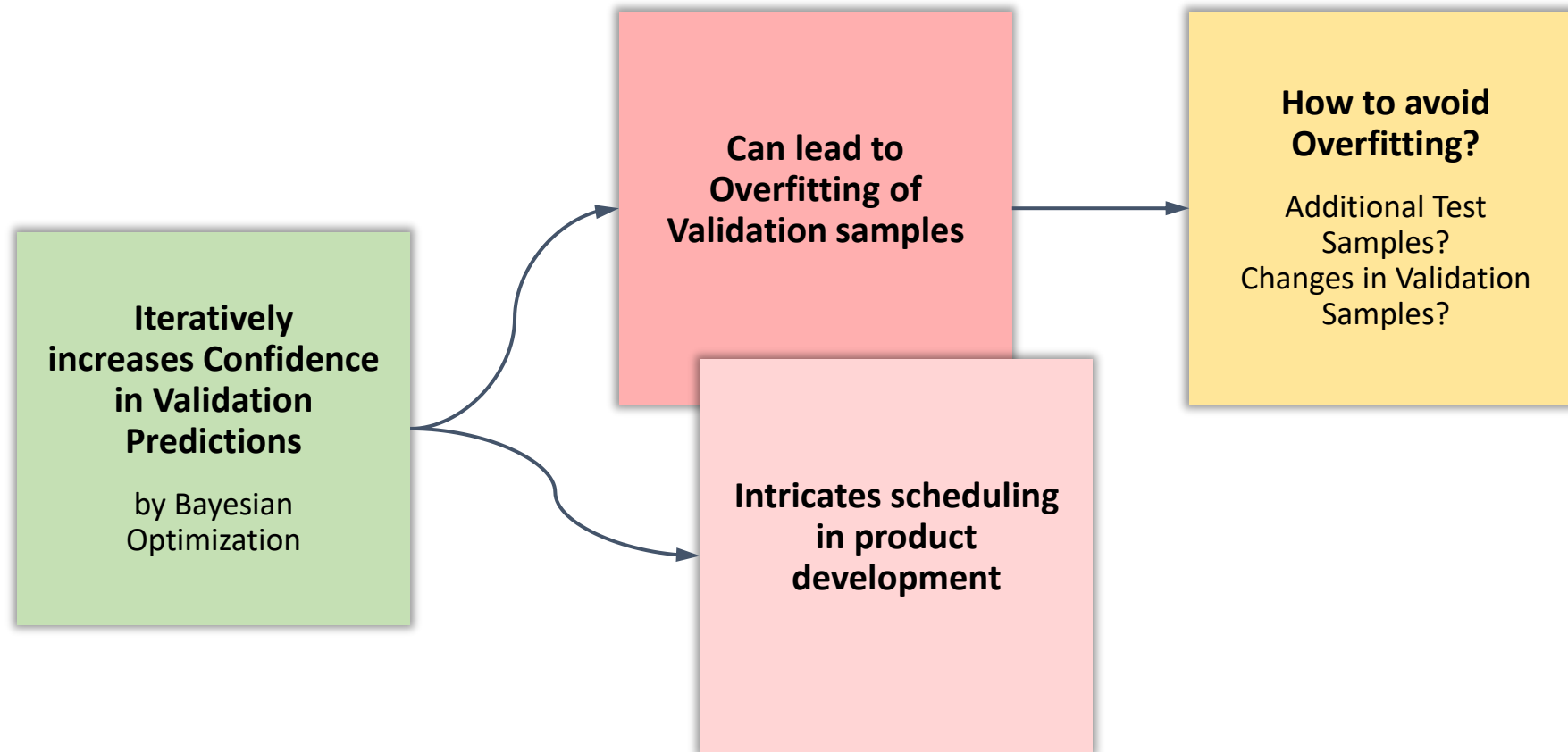
**Iteratively
increases Confidence
in Validation
Predictions**

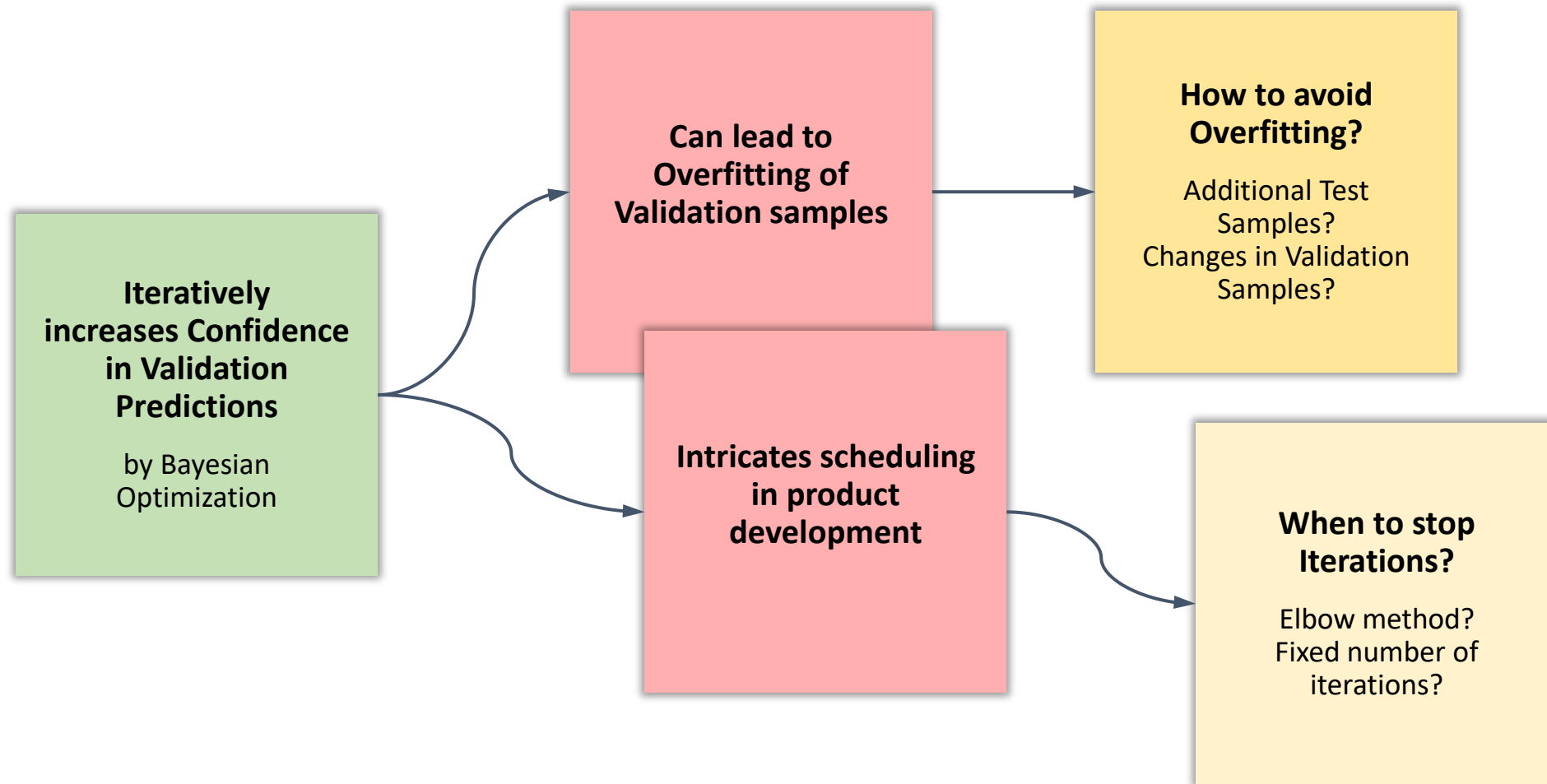
by Bayesian
Optimization











Summary

#1

Neural networks are by themselves **not suitable** for multivariate calibration in NIR due to missing generalizability

#1

Neural networks are by themselves **not suitable** for multivariate calibration in NIR due to missing generalizability

#2

A preceded embedding step with deep **non-linear decorrelation** using energy based modeling fixes this issue

#1

Neural networks are by themselves **not suitable** for multivariate calibration in NIR due to missing generalizability

#2

A preceded embedding step with deep **non-linear decorrelation** using energy based modeling fixes this issue

#3

The incorporation of non-linearity increases the **accuracy** and the **efficiency** of predictions

#1

Neural networks are by themselves **not suitable** for multivariate calibration in NIR due to missing generalizability

#2

A preceded embedding step with deep **non-linear decorrelation** using energy based modeling fixes this issue

#3

The incorporation of non-linearity increases the **accuracy** and the **efficiency** of predictions

#4

The incorporation of non-linearity intricates **feature selection** and the **design of experiments**

Thank you for your attention!

