Translating SQL Queries to Relational Algebra Expressions

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Outline

- Objective: Discuss an algorithm that translates a SQL query into an equivalent RA expression
- Motivation: Translate a declaratively specified query into a procedurally specified query
- Restriction: We do not attempt to get an efficient RA expression. Finding an equivalent efficient RA expression is done during query optimization

Strategy

- SQL queries with set predicates will be translated to equivalent SQL queries without set predicates
- WHERE conditions will be eliminated by translating them into FROM clauses using selections and join operations, or by decomposing them into more basic components (then translate these) and then use the set operations union, intersection, and set difference
- These SQL queries will then be translated into RA expressions

Query Forms (Basic case)

SELECT [DISTINCT]
$$L(t_1, ..., t_n)$$

FROM $R_1 \ t_1, ..., R_n \ t_n$
WHERE $C(t_1, ..., t_n)$

- $L(t_1, ..., t_n)$ is a list of (named) components of the tuple variables t_1 through t_n^{-1}
- R_1 through R_n are either relations or non-parameterized SQL queries aliased by the tuple variables t_1 through t_n
- $C(t_1, ..., t_n)$ is any valid SQL condition involving the components of the variables t_1 through t_n
- We do not handle SQL queries with aggregate functions or queries with subqueries in the FROM clause

¹There may also appear constants in *L*; these need special treatment

Query Forms (queries with set operations)

Assuming that Q, Q_1 , and Q_2 are SQL queries, we consider the following SQL query forms

```
Q_1
UNION
Q_2
Q_1
INTERSECT
Q_2
Q_1
EXCEPT
Q_2
```

Discussion: interaction between projection π and set operations \cup , \cap , and -

- Before we can start with the translation algorithm, it is crucial to discuss how the projection operator π interacts with the set operations \cup , \cap , and -.
- Understanding this is vital for the correct translations of SQL WHERE clauses that use the OR, AND, and NOT boolean operations
- We will consider the following interactions:
 - Projection π and union \cup
 - Projection π and intersection \cap
 - Projection π and set difference –

Projection π distributes over \cup

Given RA expressions E_1 and E_2 , it is the case that

$$\pi_L(E_1 \cup E_2) = \pi_L(E_1) \cup \pi_L(E_2)$$

An application of this is the following: (C_1 and C_2 are some conditions)

$$\pi_{L}(\sigma_{C_{1}\vee C_{2}}(E)) = \pi_{L}(\sigma_{C_{1}}(E)\cup\sigma_{C_{2}}(E)) = \pi_{L}(\sigma_{C_{1}}(E))\cup\pi_{L}(\sigma_{C_{2}}(E))$$

Translating OR in WHERE clause

SELECT
$$L(t_1, ..., t_n)$$

FROM $R_1 t_1, ..., R_n t_n$
WHERE $C_1(t_1, ..., t_n)$ OR $C_2(t_1, ..., t_n)$

SELECT
$$L(t_1, \ldots, t_n)$$

FROM $R_1 \ t_1, \ldots, R_n \ t_n$
WHERE $C_1(t_1, \ldots, t_n)$
UNION
SELECT $L(t_1, \ldots, t_n)$
FROM $R_1 \ t_1, \ldots, R_n \ t_n$
WHERE $C_2(t_1, \ldots, t_n)$

Projection π does not distributes over \cap

Given RA expressions E_1 and E_2 , it is the case that

$$\pi_L(E_1 \cap E_2) \subseteq \pi_L(E_1) \cap \pi_L(E_2)$$

But there exist cases where

$$\pi_L(E_1 \cap E_2) \neq \pi_L(E_1) \cap \pi_L(E_2)$$

This complexity features in reasoning about the expression $\pi_L(\sigma_{C_1 \wedge C_2}(E))$ since

$$\pi_L(\sigma_{C_1 \wedge C_2}(E)) = \pi_L(\sigma_{C_1}(E) \cap \sigma_{C_2}(E)) \subseteq \pi_L(\sigma_{C_1}(E)) \cap \pi_L(\sigma_{C_2}(E))$$

But there are cases where

$$\pi_L(\sigma_{C_1 \wedge C_2}(E)) \neq \pi_L(\sigma_{C_1}(E)) \cap \pi_L(\sigma_{C_2}(E))$$

Projection π does **not** distribute over intersection \cap



$$\pi_a(\sigma_{b=1 \, \land \, c=1}(R))$$

correct incorrect
$$\pi_a(\sigma_{b=1}(R)\cap\sigma_{c=1}(R)) \qquad \pi_a(\sigma_{b=1}(R))\cap\pi_a(\sigma_{c=1}(R))$$

Projection π does not distribute over intersection \cap (Predicate Logic)

The underlying reason why projection π does not distribute over intersection \cap is that an existential quantifier \exists does not distribute over a conjunction \wedge in Predicate Logic

$$\pi_{a}(\sigma_{b=1} \wedge c=1(R)) = \pi_{a}(\sigma_{b=1}(R) \cap \sigma_{c=1}(R)) = \pi_{a}(\sigma_{b=1}(R) \cap \sigma_{c=1}(R)) = \{a \mid \exists b \exists c [(R(a,b,c) \wedge b=1) \wedge (R(a,b,c) \wedge c=1)]\} \subseteq \{a \mid \exists b \exists c (R(a,b,c) \wedge b=1) \wedge \exists b \exists c (R(a,b,c) \wedge c=1)\} = \pi_{b=1}(R) \cap \pi_{c=1}(R)$$

Translating AND in WHERE clause (Correct)

```
\begin{array}{ll} \text{SELECT} & L(t_1,\ldots,t_n) \\ \text{FROM} & R_1 \ t_1,\ldots,R_n \ t_n \\ \text{WHERE} & C_1(t_1,\ldots,t_n) \ \text{AND} \ C_2(t_1,\ldots,t_n) \end{array}
```

 $^{^{2}}L^{q}(t_{1},...,t_{n})$ indicates that the components of t_{1} through t_{n} in L may need to be renamed as components of q

Translating AND in WHERE clause (Incorrect)

SELECT
$$L(t_1, ..., t_n)$$

FROM $R_1 t_1, ..., R_n t_n$
WHERE $C_1(t_1, ..., t_n)$ AND $C_2(t_1, ..., t_n)$

is not equivalent3 with

```
SELECT L(t_1, \ldots, t_n)

FROM R_1 \ t_1, \ldots, R_n \ t_n

WHERE C_1(t_1, \ldots, t_n)

INTERSECT

SELECT L(t_1, \ldots, t_n)

FROM R_1 \ t_1, \ldots, R_n \ t_n

WHERE C_2(t_1, \ldots, t_n)
```

³Projection does not distribute over intersection

Translating AND in WHERE clause (Correct)

```
SELECT e.sid FROM Enroll e
```

WHERE e.cno = 100 AND e.grade = 'A'

```
SELECT
         q.sid
FROM
          (SELECT
                        e.sid, e.cno, e.grade
          FROM
                        Enroll e
          WHERE
                        e.cno = 100
          INTERSECT
          SELECT
                        e.sid, e.cno, e.grade
                        Fnroll e
          FROM
          WHERE
                        e.grade = 'A'
          ) q
```

Translating AND in WHERE clause (Incorrect)

SELECT *e*.sid FROM Enroll *e*

WHERE e.cno = 100 AND e.grade = 'A'

is not equivalent4 with

SELECT e.sid FROM Enroll e

WHERE e.cno = 100

INTERSECT

SELECT *e*.sid FROM Enroll *e*

WHERE *e*.grade = 'A'

⁴Projection does not distribute over intersection

Projection π does not distributes over -

Given RA expressions E_1 and E_2 , it is the case that

$$\pi_L(E_1 - E_2) \supseteq \pi_L(E_1) - \pi_L(E_2)$$

But there exist cases where

$$\pi_L(E_1 - E_2) \neq \pi_L(E_1) - \pi_L(E_2)$$

This complexity features in reasoning about the expression $\pi_L(\sigma_{\neg C}(E))$ since

$$\pi_L(\sigma_{\neg C}(E)) = \pi_L(E - \sigma_C(E)) \supseteq \pi_L(E) - \pi_L(\sigma_C(E))$$

But there are cases where

$$\pi_L(\sigma_{\neg C}(E)) \neq \pi_L(E) - \pi_L(\sigma_C(E))$$

Projection π does **not** distribute over set difference –

$$\pi_{a}(\sigma_{\neg(b=1)}(R))$$

$$\boxed{a}$$

correct incorrect
$$\pi_a(R - \sigma_{b=1}(R)) \qquad \pi_a(R) - \pi_a(\sigma_{b=1}(R))$$

Projection π does not distribute over set difference – (Predicate Logic)

The underlying reason why projection π does not distribute over distribution \cap is that an existential quantifier \exists does not distribute over a conjunction-negation $\land \neg$ sequence in Predicate Logic

$$\pi_{a}(\sigma_{\neg(b=1)}(R))$$

$$=$$

$$\pi_{a}(R - \sigma_{b=1}(R))$$

$$=$$

$$\{a \mid \exists b (R(a,b) \land \neg (R(a,b) \land b = 1))\}$$

$$\supseteq$$

$$\{a \mid \exists b R(a,b) \land \neg \exists b (R(a,b) \land b = 1))\}$$

$$=$$

$$\pi_{a}(R) - \pi_{a}(\sigma_{b=1}(R))$$

Translating NOT in WHERE clause (Correct)

```
SELECT L(t_1, ..., t_n)
FROM R_1 \ t_1, ..., R_n \ t_n
WHERE NOT C(t_1, ..., t_n)
```

```
SELECT L^q(t_1,\ldots,t_n)

FROM (SELECT t_1.*,\ldots,t_n.*

FROM R_1 t_1,\ldots,R_n t_n

EXCEPT SELECT t_1.*,\ldots,t_n.*

FROM R_1 t_1,\ldots,R_n t_n

WHERE C(t_1,\ldots,t_n)
```

Translating NOT in WHERE clause (Incorrect)

SELECT
$$L(t_1, ..., t_n)$$

FROM $R_1 t_1, ..., R_n t_n$
WHERE NOT $C(t_1, ..., t_n)$

is not equivalent⁵ with

```
SELECT L(t_1, ..., t_n)

FROM R_1 \ t_1, ..., R_n \ t_n

EXCEPT

SELECT L(t_1, ..., t_n)

FROM R_1 \ t_1, ..., R_n \ t_n

WHERE C(t_1, ..., t_n)
```

⁵Projection do not distribute over set difference

Translating NOT in WHERE clause (Correct)

```
SELECT e.sid
FROM Enroll e
WHERE NOT e.grade = 'A'
```

```
SELECT q.sid
FROM (SELECT e.sid, e.cno, e.grade
FROM Enroll e
EXCEPT
SELECT e.sid, e.cno, e.grade
FROM Enroll e
WHERE e.grade = 'A'
) q
```

Translating NOT in WHERE clause (Incorrect)

SELECT e.sid FROM Enroll e WHERE NOT e.grade = 'A'

is not equivalent⁶ with

SELECT e.sid
FROM Enroll e

EXCEPT
SELECT e.sid
FROM Enroll e
WHERE e.grade = 'A'

⁶Projection does not distribute over set difference

Projection π does not distribute over set difference –

	R	
Α	В	С
1	1	2
1	2	1

$$\pi_{A}(\sigma_{B=1 \, \land \neg(C=1)}(R))$$

$$\boxed{A}$$

$$\boxed{1}$$

correct incorrect
$$\pi_{A}(\sigma_{B=1}(R) - \sigma_{C=1}(R)) \qquad \pi_{A}(\sigma_{B=1}(R)) - \pi_{A}(\sigma_{C=1}(R))$$

Translating AND NOT in WHERE clause (Correct)

```
SELECT L(t_1, \ldots, t_n)
FROM R_1 \ t_1, \ldots, R_n \ t_n
WHERE C_1(t_1, \ldots, t_n) AND NOT C_2(t_1, \ldots, t_n)
```

```
SELECT L^{q}(t_1,\ldots,t_n)
FROM
             (SELECT
                               t_1.*,\ldots,t_n.*
                                R_1 t_1, \ldots, R_n t_n
              FROM
                                C_1(t_1,\ldots,t_n)
              WHERE
              EXCEPT
              SELECT
                                t_1 \cdot *, \ldots, t_n \cdot *
              FROM
                                R_1 t_1, \ldots, R_n t_n
              WHERE
                                C_2(t_1,\ldots,t_n)
             ) q
```

Translating AND NOT in WHERE clause (Incorrect)

```
SELECT L(t_1, \ldots, t_n)
FROM R_1 \ t_1, \ldots, R_n \ t_n
WHERE C_1(t_1, \ldots, t_n) AND NOT C_2(t_1, \ldots, t_n)
```

is not equivalent7 with

```
SELECT L(t_1, \ldots, t_n)

FROM R_1 \ t_1, \ldots, R_n \ t_n

WHERE C_1(t_1, \ldots, t_n)

EXCEPT

SELECT L(t_1, \ldots, t_n)

FROM R_1 \ t_1, \ldots, R_n \ t_n

WHERE C_2(t_1, \ldots, t_n)
```

⁷Projection do not distribute over set difference

Translating AND NOT in WHERE clause (Correct)

```
SELECT e.sid
FROM Enroll e
WHERE e.cno = 100 AND NOT e.grade = 'A'
```

```
SELECT
         q.sid
FROM
         (SELECT e.sid, e.cno, e.grade
          FROM
                   Enroll e
          WHERE
                   e.cno = 100
          EXCEPT
          SELECT
                    e.sid, e.cno, e.grade
          FROM
                    Enroll e
          WHERE
                    e.grade = 'A'
         ) q
```

Translating AND NOT in WHERE clause (Incorrect)

SELECT *e*.sid FROM Enroll *e*

WHERE e.cno = 100 AND NOT e.grade = 'A'

is not equivalent8 with

SELECT *e*.sid FROM Enroll *e*

WHERE e.cno = 100

EXCEPT

SELECT e.sid FROM Enroll e WHERE e.grade = 'A'

⁸Projection does not distribute over set difference

Translating AND NOT in WHERE clause (Also correct)

```
SELECT L(t_1, \ldots, t_n)
FROM R_1 \ t_1, \ldots, R_n \ t_n
WHERE C_1(t_1, \ldots, t_n) AND NOT C_2(t_1, \ldots, t_n)
```

can be also be translated to become

```
SELECT L^q(t_1,\ldots,t_n)
FROM
            (SELECT
                         t_1.*,...,t_n.*
             FROM
                             R_1 t_1, \ldots, R_n t_n
                             C_1(t_1,\ldots,t_n)
             WHERE
             EXCEPT
             SELECT
                             t_1.*,\ldots,t_n.*
                             R_1 t_1, \ldots, R_n t_n
             FROM
             WHERE
                             C_1(t_1,\ldots,t_n) AND C_2(t_1,\ldots,t_n)
            ) q
```

Translating AND NOT in WHERE clause (Also correct)

```
SELECT e.sid
FROM Enroll e
WHERE e.cno = 100 AND NOT e.grade = 'A'
```

```
SELECT
         q.sid
FROM
         (SELECT
                    e.sid, e.cno, e.grade
          FROM
                    Enroll e
          WHERE
                    e.cno = 100
          EXCEPT
          SELECT
                    e.sid, e.cno, e.grade
          FROM
                    Enroll e
          WHERE
                    e.cno= 100 AND e.grade = 'A'
         ) q
```

Translating **EXISTS** in **WHERE** clause (Example)

Let R(a, b) and S(b, c) be two relations.

```
SELECT r.a

FROM R r

WHERE EXISTS (SELECT S.c

FROM S s

WHERE r.b = s.b)
```

In Predicate Logic,

$$\{a \mid \exists b (R(a, b) \land \{c \mid S(b, c)\} \neq \emptyset)\}$$

$$=$$

$$\{a \mid \exists b (R(a, b) \land \exists c S(b, c)))\}$$

$$=$$

$$\{a \mid \exists b \exists c (R(a, b) \land S(b, c)\}$$

$$=$$

$$\pi_{R.a}(\sigma_{R.b=S.b}(R \times S))$$

Translating **EXISTS** in WHERE clause (Example in Predicate Logic)

$$\{a \mid \exists b (R(a, b) \land \{c \mid S(b, c)\} \neq \emptyset)\}$$

$$=$$

$$\{a \mid \exists b (R(a, b) \land \exists c S(b, c)))\}$$

$$=$$

$$\{a \mid \exists b \exists c (R(a, b) \land S(b, c)\}$$

$$=$$

$$\pi_{R.a}(\sigma_{R.b=S.b}(R \times S))$$

In SQL,

SELECT DISTINCT r.a FROM R r, S s WHERE r.b = s.b

Translating EXISTS in WHERE clause (Example)

Let R(a, c) and S(b, c) be two relations.

```
SELECT r.a

FROM R r

WHERE EXISTS (SELECT S.c

FROM S s

WHERE r.b = s.b)
```

is translated to

```
SELECT DISTINCT r.a
FROM R r, S s
WHERE r.b = s.b
```

Translating **EXISTS** in **WHERE** clause (General case)

```
SELECT L(t_1, \ldots, t_n)

FROM R_1 \ t_1, \ldots, R_n \ t_n

WHERE EXISTS (SELECT 1

FROM S_1 \ u_1, \ldots, S_m \ u_m

WHERE C(u_1, \ldots, u_m, t_1, \ldots, t_n))
```

is translated to

```
SELECT DISTINCT L(t_1, ..., t_n)
FROM R_1 \ t_1, ..., R_n \ t_n, S_1 \ u_1, ..., S_m \ u_m
WHERE C(u_1, ..., u_m, t_1, ..., t_n)
```

Translating **EXISTS** in **WHERE** clause

```
SELECT s.sid

FROM Student s

WHERE EXISTS (SELECT 1

FROM Enroll e, Course c
```

WHERE e.sid = s.sid AND e.cno = c.cno AND c.dept = 'CS')

is translated to

```
SELECT DISTINCT s.sid
FROM Student s, Enroll e, Course c
```

WHERE e.sid = s.sid AND e.cno = c.cno AND c.dept = 'CS'

Translating NOT EXISTS in WHERE clause (Example)

Let R(a, b) and S(b, c) be two relations.

```
SELECT r.a

FROM R r

WHERE NOT EXISTS (SELECT S.c

FROM S s

WHERE r.b = s.b)
```

In Predicate Logic,

$$\{a \mid \exists b (R(a, b) \land \{c \mid S(b, c)\} = \emptyset)\}$$

$$=$$

$$\{a \mid \exists b (R(a, b) \land \neg \exists c S(b, c)))\}$$

$$=$$

$$\{a \mid \exists b (R(a, b) \land \neg \exists c (R(a, b) \land S(b, c)))\}$$

$$=$$

$$\pi_{R.a}(R - \pi_{R.a,R.b}(\sigma_{R.b=S.b}(R \times S)))$$

Translating NOT EXISTS in WHERE clause (Example)

$$\{a \mid \exists b(R(a, b) \land \{c \mid S(b, c)\} = \emptyset)\}$$

$$=$$

$$\pi_{R.a}(R - \pi_{R.a,R.b}(\sigma_{R.b=S.b}(R \times S)))$$

In SQL,

```
        SELECT
        DISTINCT q.a

        FROM
        (SELECT
        R.a, R.b

        FROM
        R r

        EXCEPT
        SELECT
        R.a, R.b

        FROM
        R r, S s

        WHERE
        r.b = s.b

        ) q
```

Translating NOT EXISTS in WHERE clause (Example)

```
SELECT r.a

FROM R r

WHERE NOT EXISTS (SELECT S.c

FROM S s

WHERE r.b = s.b)
```

```
        SELECT
        DISTINCT q.a

        FROM
        (SELECT
        R.a, R.b

        FROM
        R r

        EXCEPT
        SELECT
        R.a, S.b

        FROM
        R r, S s

        WHERE
        r.b = s.b

        ) q
```

Translating NOT EXISTS in WHERE clause (General case)

```
\begin{array}{lll} \text{SELECT} & \textit{L}(t_1, \dots, t_n) \\ \text{FROM} & \textit{R}_1 \ t_1, \dots, \textit{R}_n \ t_n \\ \text{WHERE} & \text{NOT EXISTS (SELECT 1} \\ & & \text{FROM} \quad \textit{S}_1 \ \textit{u}_1, \dots, \textit{S}_m \ \textit{u}_m \\ & & \text{WHERE} \ \textit{C}(\textit{u}_1, \dots, \textit{u}_m, t_1, \dots, t_n)) \end{array}
```

Translating NOT EXISTS in WHERE clause

```
SELECT s.sid
 FROM
           Student s
 WHERE
           NOT EXISTS (SELECT 1
                        FROM Enroll e
                        WHERE e.sid = s.sid AND e.grade = 'A')
is translated to
      SELECT
                q.sid
      FROM
                (SELECT
                          s.sid. s.sname
                FROM
                           Student s
                EXCEPT
                SELECT
                           s.sid, s.sname
                FROM
                           Student s, Enroll e
                WHERE
                           e.sid = s.sid AND e.grade = 'A'
                ) q
```

Translating AND NOT EXISTS in WHERE clause

```
\begin{array}{ll} \mathsf{SELECT} & s.\mathsf{sid} \\ \mathsf{FROM} & \mathsf{Student} \ s \end{array}
```

WHERE s.sname = 'Ann' AND

NOT EXISTS (SELECT 1

FROM Enroll e

WHERE e.sid = s.sid AND e.grade = 'A')

```
SELECT q.sid

FROM (SELECT s.sid, s.sname
FROM Student s
WHERE s.sname = 'Ann'
EXCEPT
SELECT s.sid, s.sname
FROM Student s, Enroll e
WHERE e.sid = s.sid AND e.grade = 'A'
) q
```

Translating AND NOT EXISTS in WHERE clause (Alternative)

```
SELECT s.sid
FROM Student s
```

WHERE s.sname = 'Ann' AND

NOT EXISTS (SELECT 1

FROM Enroll e

WHERE e.sid = s.sid AND e.grade = 'A')

```
SELECT q.sid

FROM (SELECT s.sid, s.sname
FROM Student s
WHERE s.sname = 'Ann'
EXCEPT
SELECT s.sid, s.sname
FROM Student s, Enroll e
WHERE s.sname='Ann' AND e.sid = s.sid AND e.grade = 'A'
) q
```

Translating IN in WHERE clause

```
\begin{array}{lll} \text{SELECT} & L(t_1,\ldots,t_n) \\ \text{FROM} & R_1 \ t_1,\ldots,R_n \ t_n \\ \text{WHERE} & (t_{i_1}.A_{j_1},\ldots,t_{i_k}.A_{j_k}) \ \textcolor{red}{\text{IN}} \\ & (\text{SELECT} \ u_{l_1}.B_{m_1},\ldots,u_{l_k}.B_{m_k} \\ & \text{FROM} \quad S_1 \ u_1,\ldots,S_m \ u_m \\ & \text{WHERE} \ C(u_1,\ldots,u_m,t_1,\ldots,t_n)) \end{array}
```

```
SELECT DISTINCT L(t_1,\ldots,t_n)
FROM R_1 t_1,\ldots,R_n t_n,S_1 u_1,\ldots,S_m u_m
WHERE C(u_1,\ldots,u_m,t_1,\ldots,t_n) AND t_{i_1}.A_{j_1}=u_{l_1}.B_{m_1} AND \cdots AND t_{i_k}.A_{j_k}=u_{l_k}.B_{m_k}
```

Translating **NOT IN** in WHERE clause

```
\begin{array}{lll} \text{SELECT} & \textit{L}(t_{1}, \dots, t_{n}) \\ \text{FROM} & \textit{R}_{1} \ t_{1}, \dots, \textit{R}_{n} \ t_{n} \\ \text{WHERE} & (t_{i_{1}}.\textit{A}_{j_{1}}, \dots, t_{i_{k}}.\textit{A}_{j_{k}}) \ \textbf{NOT IN} \\ & & (\text{SELECT} \ \textit{U}_{l_{1}}.\textit{B}_{m_{1}}, \dots, \textit{U}_{l_{k}}.\textit{B}_{m_{k}} \\ & & \text{FROM} \quad \textit{S}_{1} \ \textit{u}_{1}, \dots, \textit{S}_{m} \ \textit{u}_{m} \\ & & \text{WHERE} \ \textit{C}(\textit{u}_{1}, \dots, \textit{u}_{m}, t_{1}, \dots, t_{n})) \end{array}
```

```
SELECT
              L^{\mathbf{q}}(t_1,\ldots,t_n)
               (SELECT
FROM
                                  t_1.*,\ldots,t_n.*
                                    R_1 t_1, \ldots, R_n t_n
                FROM
                EXCEPT
                SELECT.
                                    t1.*....tn.*
                FROM
                                    R_1 t_1, \ldots, R_n t_n, S_1 u_1, \ldots, S_m u_m
                WHERE
                                    C(u_1,\ldots,u_m,t_1,\ldots,t_n) AND
                                    t_i, A_{i_1} = u_{i_1}, B_{m_1} AND \cdots AND t_{i_k}, A_{i_k} = u_{i_k}, B_{m_k}
               ) q
```

Translating *θ* **SOME** in **WHERE** clause

```
SELECT L(t_1, \dots, t_n)

FROM R_1 \ t_1, \dots, R_n \ t_n

WHERE t_{i_1}.A_{j_1} \ \theta SOME

(SELECT u_{l_1}.B_{m_1}

FROM S_1 \ u_1, \dots, S_m \ u_m

WHERE C(u_1, \dots, u_m, t_1, \dots, t_n))
```

```
SELECT DISTINCT L(t_1, \ldots, t_n)
FROM R_1 t_1, \ldots, R_n t_n, S_1 u_1, \ldots, S_m u_m
WHERE C(u_1, \ldots, u_m, t_1, \ldots, t_n) AND t_{i_1}.A_{j_1} \theta u_{i_1}.B_{m_1}
```

Translating θ ALL in WHERE clause

```
SELECT L(t_1, \ldots, t_n)
                      R_1 t_1, \ldots, R_n t_n
             FROM
             WHFRF
                           t_i A_i \theta ALL
                                      (SELECT u_l, B_m,
                                       FROM S_1 u_1, \ldots, S_m u_m
                                       WHERE C(u_1, \ldots, u_m, t_1, \ldots, t_n)
is translated to
          SELECT
                        L^{\mathbf{q}}(t_1,\ldots,t_n)
                        (SELECT
                                         t_1.*,\ldots,t_n.*
          FROM
                         FROM
                                           R_1 t_1, \ldots, R_n t_n
                         EXCEPT
                         SELECT
                                           t_1 * \dots t_n *
                                           R_1 t_1, \ldots, R_n t_n, S_1 u_1, \ldots, S_m u_m
                         FROM
                         WHFRF
                                           C(u_1,\ldots,u_m,t_1,\ldots,t_n) AND
                                           NOT t_{i_1}.A_{i_1}\theta u_{i_1}.B_{m_1}
                        ) q
```

Translating θ ALL in WHERE clause

```
SELECT p.pid

FROM Person p

WHERE p.age \leq ALL

(SELECT p_1.age

FROM Person p_1)
```

Translating SQL with doubly-nested set predicates

"Find the sid of each student who is only enrolled CS courses."

Eliminate first-level **NOT EXISTS** predicate

"Find the sid of each student who is only enrolled in CS COURSES."

```
SELECT L(t1, ..., tn)
                                                                               FROM R1 t1. .... Rn tn
SELECT
               q<sub>1</sub>.ssid
                                                                               WHERE NOT EXISTS (SELECT 1
FROM
                                                                                      FROM S1 u1, ..., Sm um
                (SELECT s.sid AS ssid, s.sname
                                                                                      WHERE C(u1, ..., um, t1, ..., tn))
                 FROM Student s
                                                                               is translated to
                 FXCFPT
                                                                               SELECT DISTINCT Lq(t1, ..., tn)
                 SELECT s.sid, s.sname
                                                                               FROM (SELECT t1.*, ..., tn.*
                                                                                  FROM R1 t1, ..., Rn tn
                 FROM Student s, Enroll e
                                                                                  EXCEPT
                                                                                  SELECT t1.*. .... tn.*
                 WHERE e.sid = s.sid AND
                                                                                  FROM R1 t1, ..., Rn tn, S1 u1, ..., Sm um
                                    e.cno NOT IN (SELECT c.cno
                                                                                  WHERE C(u1, ..., um, t1, ..., tn)
                                                                                 ) q
                                                         FROM
                                                                   Course c
                                                         WHERE c.dept = (CS') a_1
```

Eliminate second-level AND NOT IN

Translating NOT IN in WHERE

SELECT L(t1, ..., tn)

"Find the sid of each student who is only enrolled (in i) ..., No to SECRET will bin ..., ulk Bmk Courses."

```
is translated to
SFI FCT
              q_1.ssid
                                                                SELECT Lq(t1, ..., tn)
                                                                FROM (SELECT t1: , ..., tn:
FROM
               (SELECT s.sid AS ssid, s.sname
                                                                   FROM R1 t1, ..., Rn tn
                                                                  EXCEPT
                FROM Student s
                                                                  SELECT t1: , ..., tn:
                                                                  FROM R1 t1, ..., Rn tn; S1 u1, ..., Sm um
                FXCFPT
                                                                   WHERE C(u1, ..., um; t1, ..., tn) AND
                                                                  ti1.Ai1 = ul1.Bm1 AND ... AND tik.Aik = ulk.Bmk
               SELECT q<sub>2</sub>.ssid, s.sname
                                                                  ) a
                FROM (SELECT s.sid AS ssid, s.sname, e.sid, e.cno, e.grade
                         FROM Student s, Enroll e
                         WHFRE e.sid = s.sid
                         FXCFPT
                         (SELECT s.sid, s.sname, e.sid, e.cno, e.grade
                          FROM Student s, Enroll e, Course c
                          WHERE e.cno = c.cno AND c.dept = 'CS') q_2) q_1
```

Translating SQL with doubly-nested set predicates

"Find the sid of each student who is enrolled in all CS courses."

```
SELECT s.sid

FROM Student s

WHERE NOT EXISTS (SELECT 1

FROM Course c

WHERE c.dept = 'CS' AND

c.cno NOT IN (SELECT e.cno

FROM Enroll e

WHERE e.sid = s.sid))
```

Eliminate first-level **NOT EXISTS** predicate

"Find the sid of each student who is only enrolled in CS courses."

```
SELECT q<sub>1</sub>.ssid

FROM (SELECT s.sid AS ssid, s.sname
FROM Student s
EXCEPT
SELECT s.sid, s.sname
FROM Student s, Course c
WHERE c.dname = 'CS' AND
c.cno NOT IN (SELECT e.cno
FROM Enroll e
WHERE e.sid = s.sid)) q<sub>1</sub>
```

Eliminate second-level AND NOT IN

"Find the sid of each student who is enrolled in all CS courses."

```
 \begin{array}{lll} \text{SELECT} & \textit{q}_1.\text{ssid} \\ \text{FROM} & (\text{SELECT } s.\text{sid AS } \textbf{ssid}, \, s.\text{sname} \\ & \text{FROM} & \text{Student } s \\ & & \text{EXCEPT} \\ & \text{SELECT } \textit{q}_2.\text{ssid}, \, s.\text{sname} \\ & \text{FROM } (\text{SELECT } s.\text{sid AS } \text{ssid}, \, s.\text{sname}, \, c.\text{cno}, \, c.\text{dname} \\ & & \text{FROM } & \text{Student } s, \, \text{Course } c \\ & & \text{WHERE } c.\text{dname} = \text{`CS'} \\ & & \text{EXCEPT} \\ & (\text{SELECT } s.\text{sid}, \, s.\text{sname}, \, c.\text{cno}, \, c.\text{dname} \\ & & \text{FROM } & \text{Student } s, \, \text{Enroll } e, \, \text{Course } c \\ & & \text{WHERE } e.\text{cno} = c.\text{cno } \text{AND } e.\text{sid} = s.\text{sid} ) \; \textit{q}_2) \; \textit{q}_1 \\ \end{array}
```

Moving WHERE condition to FROM clause

- In the previous slides we have shown how set predicates can be translated
- After that process, we will have SQL queries wherein the WHERE clauses consist of boolean combinations of conditions of the form
 - *t*.*A* θ **a**; or
 - $t_i.A \theta t_i.B$
- In the following slides we will show how these WHERE clauses can be moved to FROM clauses
- We might also have queries without a WHERE clause and/or without a FROM clause; these require special treatment

SQL queries without **WHERE** and **FROM** clauses

SELECT a AS A

This query is translated to the RA expression

(*A* : **a**)

SQL queries without **WHERE** clause

SELECT
$$L(t_1, ..., t_n)$$

FROM $R_1 t_1, ..., R_n t_n$

This query is translated to the RA expression

$$\pi_{L(t_1,\ldots,t_n)}(R_1\times\cdots\times R_n)$$

Moving WHERE condition to FROM clause (condition on at least three relations)

Assume that the condition C applies to a least three relations, i.e., the condition is of the form $C(t_{i_1}, t_{i_2}, t_{i_3}, \dots, t_{i_k})$ with $k \ge 3$

SELECT
$$L(t_1, ..., t_n)$$

FROM $R_1 t_1, R_2 t_2, R_3 t_3, ..., R_n t_n$
WHERE $C(t_{i_1}, t_{i_2}, t_{i_3}, ..., t_{i_k})$

We can now introduce the CROSS JOIN in the FROM clause by replacing each ',' with CROSS JOIN

```
\begin{array}{ll} \text{SELECT} & L(t_1,\ldots,t_n) \\ \text{FROM} & R_1 \ t_1 \ \text{CROSS JOIN} \ R_2 \ t_2 \ \text{CROSS JOIN} \ R_3 \ t_3 \ \text{CROSS JOIN} \ \cdots \ \text{CROSS JOIN} \ R_n \ t_n \\ \text{WHERE} & C(t_{i_1},t_{i_2},t_{i_2},\ldots,t_{i_k}) \end{array}
```

In RA,

$$\pi_{L(t_1,...,t_n)}(\sigma_{C(t_{i_1},t_{i_2},t_{i_3},...,t_{i_k})}(R_1 \times R_2 \times R_3 \times \cdots \times R_n))$$

Moving WHERE condition to FROM clause (condition on at least three relations) Example

SELECT
$$L(t_1, t_2, t_3)$$

FROM $R_1 t_1, R_2 t_2, R_3 t_3$
WHERE $t_1.A_1 \theta_1 t_2.A_2$ OR $t_2.A_3 \theta_2 t_3.A_4$

$$\pi_{L(t_1,t_2,t_3)}(\sigma_{t_1.A_1\,\theta_1\,t_2.A_2\,\vee\,t_2.A_3\,\theta_2\,t_3.A_4}(R_1\times R_2\times R_3))$$

Moving WHERE condition to FROM clause (condition on single relation)

SELECT
$$L(t_1, ..., t_n)$$

FROM $R_1 t_1, R_2 t_2, ..., R_i t_i, ..., R_n t_n$
WHERE $C(t_i)$ [AND $C'(t_{i_1}, ..., t_{i_k})$]

Observe that $C(t_i)$ is only a condition on R_i . This query is translated to

```
SELECT L(t_1, ..., t_n)

FROM R_1 t_1, R_2 t_2 ...,

(SELECT t_i.* FROM R_i WHERE C(t_i)) t_i, ..., R_n t_n

[WHERE C'(t_{i_1}, ..., t_{i_k})]
```

Moving WHERE condition to FROM clause (condition on single relation)

```
SELECT L(t_1, \ldots, t_n)

FROM R_1 t_1, R_2 t_2, \ldots,

(SELECT t_i * FROM R_i WHERE C(t_i)) t_i, \ldots, R_n t_n

[WHERE C'(t_{i_1}, \ldots, t_{i_k})]
```

We can now introduce the CROSS JOIN in the FROM clause by replacing each ',' with CROSS JOIN

```
 \begin{array}{l} \mathsf{SELECT}\ L(t_1,\dots,t_n) \\ \mathsf{FROM}\ \ R_1\ t_1\ \mathsf{CROSS}\ \mathsf{JOIN}\ R_2\ t_2\ \mathsf{CROSS}\ \mathsf{JOIN} \cdots \mathsf{CROSS}\ \mathsf{JOIN} \\ & (\mathsf{SELECT}\ t_i,*\ \mathsf{FROM}\ R_i\ \mathsf{WHERE}\ C(t_i))\ t_i\ \mathsf{CROSS}\ \mathsf{JOIN} \cdots \mathsf{CROSS}\ \mathsf{JOIN}\ R_n\ t_n \end{array}
```

Which, in the notation of RA, corresponds to the expression

$$\pi_{L(t_1,...,t_n)}(\sigma_{C'(t_{i_1},...,t_{i_k})}(R_1 \times R_2 \times \cdots \times \sigma_{C(t_i)}(R_i) \times \cdots \times R_n))$$
 or, when $C'(t_{i_1},\ldots,t_{i_k})$ is missing, $\pi_{L(t_1,...,t_n)}(R_1 \times R_2 \times \cdots \times \sigma_{C(t_i)}(R_i) \times \cdots \times R_n)$

Moving WHERE condition to FROM clause (condition on two relations)

SELECT
$$L(t_1, \ldots, t_n)$$

FROM $R_1 t_1, \ldots, R_i t_i, \ldots, R_j t_j, \ldots, R_n t_n$
WHERE $C(t_i, t_j)$ [AND $C'(t_{i_1}, \ldots, t_{i_k})$]

Observe that $C(t_i, t_j)$ is a condition relating R_i and R_j . This query is translated to

```
SELECT L(t_1, \ldots, t_n)
FROM R_1 t_1, \ldots, R_{i-1} t_{j-1}, R_{i+1} t_{i+1}, \ldots, R_{j-1} t_{j-1}, R_{j+1} t_{j+1}, \ldots R_n t_n, R_i t_i \text{ JOIN } R_j t_j \text{ ON } C(t_i, t_j)
[WHERE C'(t_i, \ldots, t_{i_k})]
```

Moving WHERE condition to FROM clause (condition on two relations)

$$\begin{array}{ll} \text{SELECT } L(t_1, \dots, t_n) \\ \text{FROM} & R_1 \ t_1, \dots, R_{i-1} \ t_{j-1}, R_{i+1} \ t_{i+1}, \dots, R_{j-1} \ t_{j-1}, R_{j+1} \ t_{j+1}, \dots R_n \ t_n, \\ & R_i \ t_i \ \text{JOIN} \ R_j \ t_j \ \text{ON} \ C(t_i, t_j) \\ \text{[WHERE } C'(t_{i_1}, \dots, t_{i_k})] \end{array}$$

Recalling that each ',' in the FROM clause corresponds to a CROSS JOIN, this query can be formulated in RA as follows:

$$\pi_{\mathcal{L}(t_1,\ldots,t_n)}(\sigma_{\mathcal{C}'(t_{i_1},\ldots,t_{i_k})}(R_1\times\cdots\times R_{i-1}\times R_{i+1}\times\cdots\times R_{j-1}\times R_{j+1}\times\cdots\times R_n\times (R_i\bowtie_{\mathcal{C}(t_i,t_j)}R_j)))$$
or, when $C'(t_{i_1},\ldots,t_{i_k})$ is missing
$$\pi_{\mathcal{L}(t_1,\ldots,t_n)}(R_1\times\cdots\times R_{i-1}\times R_{i+1}\times\cdots\times R_{j-1}\times R_{i+1}\times\cdots\times R_n\times (R_i\bowtie_{\mathcal{C}(t_i,t_i)}R_j))$$

Moving WHERE condition to FROM clause (natural join condition on two relations)

Assume that A_1, \ldots, A_k are the common attributes of R_i and R_j and that $C(t_i, t_i)$ is the condition

$$t_i.A_1 = t_j.A_1 \text{ AND} \cdots \text{ AND } t_i.A_k = t_j.A_k$$

then

SELECT
$$L(t_1, \ldots, t_n)$$

FROM $B_1 t_1, \ldots, B_{i-1} t_{j-1}, B_{i+1} t_{i+1}, \ldots, B_{j-1} t_{j-1}, B_{j+1} t_{j+1}, \ldots B_n t_n, B_i t_i Join $B_j t_j$ on $C(t_i, t_j)$
[WHERE $C'(t_i, \ldots, t_{i_r})$]$

is translated to

SELECT
$$L(t_1,\ldots,t_n)$$
 FROM R_1 t_1,\ldots,R_{l-1} t_{j-1} , R_{l+1} t_{l+1},\ldots,R_{j-1} t_{j-1} , R_{j+1} $t_{j+1},\ldots R_n$ t_n , R_j t_j NATURAL JOIN R_j t_j [WHERE $C'(t_i,\ldots,t_k)$]

In RA,

$$\pi_{L(t_1,\ldots,t_n)}(\sigma_{C'(t_{j_1},\ldots,t_{j_k})}(R_1\times\cdots\times R_{i-1}\times R_{i+1}\times\cdots\times R_{j-1}\times R_{j+1}\times\cdots\times R_n\times (R_i\bowtie R_j)))$$

SQL queries with set operations UNION, INTERSECT, or EXCEPT

Assuming Q_1 and Q_2 SQL queries, the queries of the form

can be translated to RA as follows

$$E_{Q_1} \cup [\cap |-] E_{Q_2}$$

where E_{Q_1} and E_{Q_2} are the RA expressions corresponding to Q_1 and Q_2

Example

"Find the sid of each student who is only enrolled in CS courses."

```
SELECT q_1.ssid (SELECT s.sid AS ssid, s.sname FROM Student s EXCEPT SELECT q_2.ssid, s.sname FROM (SELECT s.sid AS ssid, s.sname, s
```

Example

"Find the sid of each student who is only enrolled in CS courses."

```
SELECT
FROM
(SELECT s.sid AS ssid, s.sname
FROM Student s
EXCEPT
SELECT q<sub>2</sub>.ssid, s.sname
FROM (SELECT s.sid AS ssid, s.sname, e.sid, e.cno
FROM Student s NATURAL JOIN Enroll e
EXCEPT
(SELECT s.sid, s.sname, e.sid, e.cno
FROM Student s CROSS JOIN Enroll E
NATURAL JOIN (SELECT c.* FROM Course c WHERE dept = 'CS') c) q<sub>2</sub>) q<sub>1</sub>
```

is translated to

```
\pi_{\textit{sid}}(\pi_{\textit{sid},\textit{sname}}(S) - \pi_{\textit{S.sid},\textit{sname}}(\pi_{\textit{S.sid},\textit{sname},\textit{E.sid},\textit{cno}}(S \bowtie E) - \pi_{\textit{S.sid},\textit{sname},\textit{E.sid},\textit{cno}}(S \times E \bowtie \sigma_{\textit{dept}='CS'}(C))))
```

where *S*, *E*, and *C* denote Student, Enroll, and Course, respectively.

Example (Optimization)

"Find the sid of each student who is only enrolled in CS courses."

$$\pi_{\textit{sid}}(\pi_{\textit{sid},\textit{sname}}(S) - \pi_{\textit{S.sid},\textit{sname}}(\pi_{\textit{S.sid},\textit{sname},\textit{E.sid},\textit{cno}}(S \bowtie E) - \pi_{\textit{S.sid},\textit{sname},\textit{E.sid},\textit{cno}}(S \times E \bowtie \sigma_{\textit{dept}='CS'}(C))))$$

This can be optimized to the RA expression

$$\pi_{\textit{sid}}(S) - \pi_{\textit{sid}}(\pi_{\textit{sid},\textit{cno}}(E) - \pi_{\textit{sid},\textit{cno}}(E) \ltimes \pi_{\textit{cno}}(\sigma_{\textit{dept}='CS'}(C)))$$

Notice that this is the RA expression for the only set semijoin If furthermore the schema of Enroll is (sid,cno), this expression becomes

$$\pi_{sid}(S) - \pi_{sid}(E - E \ltimes CS)) = \pi_{sid} - \pi_{sid}(E \overline{\ltimes} CS)$$

where CS denotes the RA expression $\pi_{cno}(\sigma_{dept=^{\cdot}CS'}(C))$