Programmering og Problemløsning Datalogisk Institut, Københavns Universitet Arbejdsseddel 5 - individuel opgave

7. oktober - 15. oktober 2022. Afleveringsfrist: lørdag d. 15. oktober, 2022, kl. 22:00.

I denne periode skal vi arbejde med abstrakte datatyper. En *abstrakt datatype* er en type, der specificeres ved at angive operationer på typen og de egenskaber disse operationer opfylder. Med andre ord, en abstrakt datatype siger, hvordan kan kan bruges af en programmør, uden at vedkommende behøver at kende, hvordan den er implementeret. En implementering af en abstrakt datatype er en konkret type og konkrete funktioner (funktionsdefinitioner som kode), der skal opfylde de givne egenskaber.

I F# implementeres abstrakte datatyper ved hjælp af *moduler*. Et modul består af en signaturfil med definitionen af typen og navnene af operationerne og deres typer; en implementationsfil, der indeholder operationernes definition, dvs. deres kode; og en applikationsfil, som typisk indeholder anvendelser af operationerne for at afprøve, hvorvidt implementeringen af operationerne overholder de krævede egenskaber. Moduler kaldes også *biblioteker*, fordi de samler nogle operationer og stiller dem til rådighed for brugere (programmører), lige som et bibliotek samler bøger og stiller dem til rådighed for brugere (læsere).

Denne arbejdsseddels læringsmål er:

- at lave et bibliotek og en tilhørende applikation,
- at kunne oversætte biblioteksfiler og applikationsfiler både med dotnet fsi og run,
- at kunne arbejde med generiske moduler,

Opgaverne er opdelt i øve- og afleveringsopgaver. I denne periode skal I arbejde individuelt med jeres afleveringsopgaver. Regler for gruppe- og individuelle afleveringsopgaver er beskrevet i "'Noter, links, software m.m."

"'Generel information om opgaver".

Øveopgaver (in English)

5ø0 In an earlier assignment, you implemented a small set of functions for vector operations in F#:

(a) addition of vectors

```
add: vec -> vec -> vec
```

(b) multiplication of a vector and a floating-point number

```
mul: vec -> float -> vec
```

(c) rotation of a vector by radians

```
rot: vec -> float -> vec
```

and wrote a small program to test these functions. Convert your earlier programs into a library called Vec, consisting of a signature file, an implementation file, and an application file. Create a .fsproj project file, and run the code using first dotnet fsi and then dotnet run.

5ø1 A linked list is an abstract datatype that is built into F#.

In this exercise you will create your own implementations of a linked list, one only supporting int and a generic linked list that can be used with any datatype, just like the built-in F# lists.

(a) Copy the following signature into intLinkedList.fsi and write a corresponding implementation in intLinkedList.fs

```
module IntLinkedList
type intLinkedList = Nil | Cons of int * intLinkedList
val head : intLinkedList -> int
val tail : intLinkedList -> intLinkedList
val isEmpty : intLinkedList -> bool
val length : intLinkedList -> int
val add : int -> intLinkedList -> intLinkedList
```

Write a small test program to ensure your implementation works as expected. You can take inspiration from the following listing:

```
open IntLinkedList
let emptyList = Nil
let 11 = Cons (1, Nil)
let 12 = Cons (1, Cons (2, Nil))
let 13 = add 3 12
isEmpty emptyList |> printfn "Empty list is empty: %A"
isEmpty l1 |> not |> printfn "Non-empty list is not empty: %A"
head l1 = 1 |> printfn "head gives the first element: %A"
tail l1 = Nil |> printfn "tail gives the rest of the list: %A"
length l3 = 3 |> printfn "l3 has length 3: %A"
```

- (b) In the previous sub-exercise the linked list is restricted to the type int. In this sub-exercise you should construct a generic linked list module.
- (c) Copy and finish the following signature in linkedList.fsi and write a corresponding implementation in linkedList.fs.

```
module LinkedList
type LinkedList<'a> = Nil | Cons of 'a * intLinkedList<'a>
val head : LinkedList<'a> -> 'a
val tail : ?? // Fill in yourself
val isEmpty : ?? // Fill in yourself
val length : ?? // Fill in yourself
val add : ?? // Fill in yourself
```

Write a small test-program showing you can construct linked lists of all types. You should be able to reuse all of your test from the previous sub-exercise and thus create linked lists of LinkedList<int>, as well as the following:

```
open LinkedList
let emptyList = Nil
let l1Float = add 2.0 emptyList |> add 3.14 // A float list
let l1String = add "Linked lists are cool!" emptyList
let l2String = add "What is cool?" l1String
// A list of int lists
let intLstLst = add l1 emptyList |> add l2 |> add emptyList
// a list of string lists
let strLstLst = add l1String emptyList |> add l2String
```

- (d) Implement fold for your linked list module, similar to List.fold.
- (e) Implement foldBack for your linked list module, similar to List.foldBack.
- (f) Implement map for your linked list module, similar to List.map.

Afleveringsopgaver (in English)

In the following, you are to work with the abstract datatype known as a *queue*. A queue is a a sequence of elements that supports the following operations: checking whether the sequence is empty; removing an element from the front ("left"); adding an element at the end ("right"). Queues appear often in real life: The line¹ waiting for service at a shop counter, orders to be filled in a warehouse, students waiting to be examined at an oral examination.

The abstract datatype of *purely functional queues* consists of:

- the types named element and queue, where element is the type of elements and queue the type of queues with such elements;
- the following value and two functions

```
// the empty queue
emptyQueue: queue
// add an element at the end of a queue
enqueue: element -> queue -> queue
// remove and return the element at the front of a queue
// precondition: input queue is not empty
dequeue: queue -> element * queue
// check if a queue is empty
isEmpty: queue -> bool
```

• the properties these operations must satisfy and that another programmer can rely on, such as queuing an element on an empty queue and then dequeuing from it yields the element added at first and leaves an empty queue behind; or, more generally, first repeatedly queuing elements and then dequeuing until the queue is empty yields the same elements.²

¹In American English. Called indeed *queue* in British English.

²This can be expressed as a precise mathematical property, which in turn can be used to systematically test one's implementation to find errors. We'll do this only informally here.

These queues are called (purely) functional because the enqueue and dequeue operations return a new queue whenever they are called, without destroying the old queue. For example, adding an element e_1 to a queue q_0 of length 15 results in a queue q_1 of length 16; then adding another element e_2 to q_0 also results in a queue q_2 of length 16, but one that is different from q_1 in its last element. At this point we have 3 separate queues, each of which we can used in future operations: q_0 , q_1 and q_2 .

In this exercise, you will work with functional queues in F#. We'll omit writing "functional" below.

- 5i0 In the following you are to create a dotnet project for the assignment.
 - (a) Using the dotnet command line tool, create a new F# console application named 5i. dotnet new console -lang "F#" -o 5i
 - (b) Rename the file Program.fs to testQueues.fs.
 - (c) Update 5i.fsproj to compile testQueues.fs instead of Program.fs.
 - (d) Ensure the project works by running dotnet build and dotnet run.
- 5i1 In the following, you are to implement your own queue module using lists in F# to represent the (sequence of elements in) a queue. The module is to be called IntQueue.
 - (a) Given the description of the abstract datatype Queue above, write a signature file intQueue.fsi for the functional queues.
 - (b) Write an implementation file intQueue.fs, implementing the signature file above using lists in F# where the elements are F# integers.
 - (c) Add intQueue.fsi and intQueue.fs to 5i.fsproj, so they are compiled *before* testQueues.fs.
 - (d) In testQueues.fs, show your implementation works by using your queue. As a minimum, you should add the following series of tests of your IntQueue module:

³There are also *ephemeral* (also called *imperative*) queues, where enqueue and replace the original queue with the new queue such that there is always just one "current" queue that changes over time. Ephemeral queues have more limited functionality and are easier to implement efficiently using imperative data structures, which we will encounter later in the course.

```
|> printfn "First in is first out: %A"

let allTestResults =
    emptyTestResult &&
    nonEmptyTestResult &&
    dequeueTestResult

allTestResults
|> printfn "All IntQueue tests passed: %A"
    // Return the test results as a boolean
    allTestResults

// Run the IntQueue tests
let intQueueTestResults = intQueueTests ()
```

5i2 A problem with the queue specification above is that there is a precondition on the dequeue operation: A programmer must always ensure that the argument to dequeue is nonempty before calling dequeue. In other words, even though the F# type system does not flag it as an error, it *is* an error (by the programmer) to call dequeue with the empty queue.

In the following, you are to implement another version of your queue module using lists in F# to represent the (sequence of elements in) a queue, with error handling. The module is to be called SafeIntQueue, the signature file safeIntQueue.fsi and the implementation file safeIntQueue.fs.

Change the queue specification such that SafeIntQueue.dequeue returns an (element option) * queue value and remove the precondition. Add the new module to 5i.fsproj and in testQueues.fs, add a corresponding test suite that shows your implementation works; that is, its operations perform queuing and dequeuing, and, additionally SafeIntQueue.dequeue(emptyQueue) returns None.

5i3 A queue is an abstract datatype, and as such the operations of a queue should not depend on the type of elements. In the following you are to implement a *generic queue*, so it is possible to create queues of any type, e.g. queues of int, queues of float, queues of string or even queues of queue.

The module is to be called Queue, the signature file queue.fsi and the implementation file queue.fs. Add the new module to 5i.fsproj and in testQueues.fs, add a corresponding test suite that shows your implementation works; that is, its operations perform queuing and dequeuing, and additionally that you can build queues of different types with the same generic library. As a minimum, demonstrate queues of int, float and string.

Krav til afleveringen

Afleveringen skal bestå af

- en zip-fil, der hedder 5i.zip
- en opgavebesvarelse i pdf-format.

Zip-filen skal indeholde:

- filen README.txt som er en tekstfil indeholdende jeres navn og en beskrivelse af hvordan man bygger projektet og kører jeres test.
- en src mappe med følgende og kun følgende filer:

5i.fsproj, intQueue.fsi, intQueue.fs, safeIntQueue.fsi, safeIntQueue.fs, queue.fsi, queue.fs, testQueues.fs

svarende til afleveringsopgaverne. Funktionerne skal være dokumenteret med ifølge dokumentationsstandarden ved brug af <summary>, <param> og <returns> XML tagsne.

• pdf-dokumentet skal være lavet med LATEX, benytte opgave. tex skabelonen, ganske kort dokumentere din løsning og indeholde evt. figurer.

God fornøjelse.