# Programmering og Problemløsning Datalogisk Institut, Københavns Universitet Arbejdsseddel 8 - individuel opgave

#### Jon Sporring

25. november - 3. december. Afleveringsfrist: lørdag d. 3. december kl. 22:00.

På denne uge skal vi tage et nøjere kig på imperativ programmering. Den væsentlige forskel på imperativ og funktionel programmering er, at imperativ programmering arbejder med tilstande, dvs. variable, som kan ændre sig over tid. Som konsekvens heraf kobler man ofte while og for løkker til imperativ programmering i modsætning til rekurssion. Yderligere bliver håndkøring kompliceret af, at man er nødt til at tilføje en bunke (heap), for at holde øje med tilstandene af variablene over tid.

Denne arbejdsseddels læringsmål er:

- Forklare forskellen på og løse problemer med rekursion, while og for løkker,
- Skrive programmer med variable, arrays i 1 og 2 dimensioner,
- Håndkøre funktioner med tilstande og while og for løkker.

Opgaverne er opdelt i øve- og afleveringsopgaver. I denne periode skal I arbejde individuelt med jeres afleveringsopgaver. Regler for gruppe- og individuelle afleveringsopgaver er beskrevet i "Noter, links, software m.m."  $\rightarrow$  "Generel information om opgaver".

## Øveopgaver (in English)

8ø0 Consider multiplication tables of the form,

|   | 1 | 2 | 3 | 4            | 5  | 6  | 7  | 8  | 9  | 10 |
|---|---|---|---|--------------|----|----|----|----|----|----|
| 1 | 1 | 2 | 3 | 4<br>8<br>12 | 5  | 6  | 7  | 8  | 9  | 10 |
| 2 | 2 | 4 | 6 | 8            | 10 | 12 | 14 | 16 | 19 | 20 |
| 3 | 3 | 6 | 9 | 12           | 15 | 18 | 21 | 24 | 27 | 30 |
|   |   |   |   |              |    |    |    |    |    |    |

where the elements of the top row and left column are multiplied and the result is written at their intersection.

In this assignment, you are to work with a function

```
mulTable : n:int -> string
```

which takes 1 argument and returns a string containing the first  $1 \le n \le 10$  lines in the multiplication table including <newline> characters. Each field must be 4 characters wide. The resulting string must be printable with a singleprintf "%s"statement. For example, the call mulTable 3 must return.

Listing 1: An example of the output from mulTable. printf "%s" (mulTable 3);; 

All entries must be padded with spaces such that the rows and columns are right-aligned. Consider the following sub-assignments:

(a) Create a function with type

```
mulTable : n:int -> string
```

such that it has one and only one value binding to a string, which is the resulting string for n = 10, and use indexing to return the relevant tabel for  $n \le 10$ . Test mulTable n for n = 1, 2, 3, 10. The function should return the empty string for values n < 1 and n > 10.

(b) Create a function with type

```
loopMulTable : n:int -> string
```

such that it uses a local string variable, which is built dynamically using 2 nested forloops and the sprintf-function. Test loopMulTable n for n = 1, 2, 3, 10.

- (c) Make a program, which uses the comparison operator for strings, "=", and write a table to the screen with 2 columns: n, and the result of comparing the output of mulTable n with loopMulTable n as true or false, depending on whether the output is identical or not.
- (d) Use printf "%s"and printf "%A"to print the result of mulTable, and explain the difference.

8ø1 Consider the following sum of integers,

$$\sum_{i=1}^{n} i. \tag{1}$$

This assignment has the following sub-assignments:

(a) Write a function

which uses the counter value, a local variable (mutable value) s, and a while-loop to compute the sum  $1+2+\cdots+n$  also written in (1). If the function is called with any value smaller than 1, then it is to return the value 0.

(b) By induction one can show that

$$\sum_{i=1}^{n} i = \frac{n(n+1)}{2}, n \ge 0 \tag{2}$$

Make a function

```
simpleSum : n:int -> int
```

which uses (2) to calculate  $1 + 2 + \cdots + n$  and which includes a comment explaining how the expression implemented is related to the mentioned sum.

- (c) Write a program, which asks the user for the number n, reads the number from the keyboard, and write the result of sum n and simpleSum n to the screen.
- (d) Make a program, which writes a table to the screen with 3 columns: n, sum n and simpleSum n. The table should have a row for each of n = 1, 2, 3, ..., 10, and each field must be 4 characters wide. Verify that the two functions calculate identical results.
- (e) What is the largest value *n* that the two sum-functions can correctly calculate the value of? Can the functions be modified, such that they can correctly calculate the sum for larger values of *n*?
- 8ø2 Perform a trace-by-hand of the following program

```
let a = 3.0
let b = 4.0
let f x = a * x + b

let x = 2.0
let y = f x
printfn "%A * %A + %A = %A" a 2.0 b y
```

- 8ø3 Use Array.init to make a function squares: n:int  $\rightarrow$  int [], such that the call squares n returns the array of the first n square numbers. For example, squares 5 should return the array [|1; 4; 9; 16; 25|].
- 8ø4 Write a function reverseArray : arr: 'a [] -> 'a [] using Array.init and Array.length which returns an array with the elements in the opposite order of arr. For eksample, printfn "%A" (reverseArray [|1..5|]) should write [|5; 4; 3; 2; 1|] to the screen.
- 8ø5 Use Array2D.init, Array2D.length1 and Array2D.length2 to make the function transposeArr : 'a [,] -> 'a [,] which transposes the elements in input.

### Afleveringsopgaver (in English)

In the following you are to work with the movement of a small robot in two dimensions. The robot can be placed on integer positions type pos = int\*int, and in each step, it can move one position up, down, left, or right.

8i0 (a) Given a source and target grid point, write the function

```
dist: p1: pos \rightarrow p2: pos \rightarrow int ich calculates the squared distance between positions p_1
```

which calculates the squared distance between positions  $p_1$  and  $p_2$ . I.e., if  $p_1 = (x_1, y_1)$  and  $p_2 = (x_2, y_2)$  then  $\operatorname{dist}(p_1, p_2) = (x_2 - x_1)^2 + (y_2 - y_1)^2$ .

(b) Given a source and a target and dist, write the function

```
candidates: src: pos -> tg: pos -> pos list
```

which returns the list of candidate next positions, which brings the robot closer to its target. I.e., if src = (x,y), then the function must consider all the neighbouring positions,  $\{(x+1,y),(x-1,y),(x,y+1),(x,y-1)\}$ , and return those whose distance is equal to or smaller than dist(src,tg). This can be done with List.filter.

(c) Given a source and a target and by use of candidates the above functions, write a recursive function

```
routes: src: pos -> tg: pos -> pos list list
```

which calculates the list of all the shortest routes from src to tg. For example, the list of shortest routes from (3,3) to (1,1) are

```
[[(3, 3); (2, 3); (1, 3); (1, 2); (1, 1)];

[(3, 3); (2, 3); (2, 2); (1, 2); (1, 1)];

[(3, 3); (2, 3); (2, 2); (2, 1); (1, 1)];

[(3, 3); (3, 2); (2, 2); (1, 2); (1, 1)];

[(3, 3); (3, 2); (2, 2); (2, 1); (1, 1)];

[(3, 3); (3, 2); (3, 1); (2, 1); (1, 1)]]
```

Beware, this list grows fast, the further the source and target is from each other, so you will be wise to only work with short distances. This can be done with a recursive function and a List.map of a List.map.

(d) Consider now a robot, which also can move diagonally. Extend candidate to also consider the diagonal positions  $\{(x+1,y+1),(x+1,y-1),(x-1,y+1),(x-1,y-1)\}$ , and update routes to return the list of shortest routes only. For example, the shortest routes from (3,4) to (1,1) should be

```
[[(3, 4); (2, 3); (1, 2); (1, 1)];
[(3, 4); (2, 3); (2, 2); (1, 1)];
[(3, 4); (3, 3); (2, 2); (1, 1)]]
```

but not necessarily in that order.

(e) Optional: Make a Canvas program, which draws routes, and apply it to the routes found above.

## Krav til afleveringen

Afleveringen skal bestå af

- en zip-fil, der hedder 8i.zip
- en opgavebesvarelse i pdf-format.

Zip-filen skal indeholde:

• filen README. txt som er en textfil med jeres navne og dato arbejdet.

• en src mappe med følgende og kun følgende filer:

8i0abc.fsx, 8i0d.fsx, og evt. 8i0e

svarende til afleveringsopgaverne a-b-c, d og e. Funktionerne skal være dokumenteret med ifølge dokumentationsstandarden ved brug af <summary>, <param> og <returns> XML tagsne.

• pdf-dokumentet skal være lavet med LATEX, benytte opgave. tex skabelonen, ganske kort dokumentere din løsning og indeholde figurer, der viser outputgrafik fra canvas for opgaverne.

God fornøjelse.