

# Programmering og Problemløsning

## Datalogisk Institut, Københavns Universitet

### Arbejdsseddel 2 - gruppeopgave

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16. - 24. september.  
Afleveringsfrist: lørdag d. 24. september kl. 22:00.

Denne arbejdsseddel gælder for 1 uge, og med den skifter vi perspektiv til funktionsprogrammering. Derfor vil vi undgå mutérbare værdier og bruge rekursion til løkker. Curriculum for opgaverne er [Sparring, kapitel 3-6]. Denne arbejdsseddels læringsmål er:

- at kunne strukturere kode vha. funktioner og sum typer,
- at kunne håndkøre simple programmer,
- at kunne dokumentere kode vha. XML standarden.

Opgaverne er opdelt i øve- og afleveringsopgaver. I denne periode skal I arbejde i grupper med jeres afleveringsopgaver. Regler for gruppe- og individuelle afleveringsopgaver er beskrevet i ”Noter, links, software m.m.” → ”Generel information om opgaver”.

## Øveopgaver (in English)

2ø0 The following program,

```
let firstName = "Jon"
let lastName = "Sparring"
printfn "Hello %A!" firstName+lastName
```

is supposed to write “Hello Jon Sparring!” to the screen, but unfortunately, it contains at least one mistake. Correct the mistake(s) and rerun the program.

2ø1 Perform a trace-by-hand of the following program

```
let a = 3.0
let b = 4.0
let f x = a * x + b

let x = 2.0
let y = f x
printfn "%A * %A + %A = %A" a 2.0 b y
```

2ø2 Consider the factorial-function,

$$n! = \prod_{i=1}^n i = 1 \cdot 2 \cdot \dots \cdot n \quad (1)$$

(a) Write a function

```
fac : n:int -> int
```

which uses recursion to calculate the factorial-function as (1).

(b) Write a program, which asks the user to enter the number  $n$  using the keyboard, and which writes the result of `fac n`.

(c) Make a new version,

```
fac64 : n:int64 -> int64
```

which uses `int64` instead of `int` to calculate the factorial-function. What are the largest values  $n$ , for which `fac` and `fac64` respectively can correctly calculate the factorial-function for?

2ø3 Using Steps 1, 3, 5, 7, and 8 from the 8-step guide

(a) write a recursive function which takes two integer arguments  $x$  and  $n$  and returns the value  $x^n$ .

(b) write another function which takes one argument  $(x, n)$  and calls the former.

Document both functions using the `<summary>`, `<param>`, and `<returns>` XML tags. Consider what should happen, if  $n < 0$ , and whether there is any significant difference between the call of the two functions.

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In the following, you are to work with the discriminated union `weekday`:

```
type weekday =  
  Monday | Tuesday | Wednesday | Thursday | Friday | Saturday | Sunday
```

which represents the days of the week.

2ø4 Make a function `dayToNumber : weekday -> int` which given a `weekday` returns an integer, such that Monday is 1, Tuesday is 2, etc.

2ø5 Make a function `nextDay : weekday -> weekday` which given a day returns the next day, i.e., Tuesday is the next day of Monday, and Monday is the next day of Sunday.

2ø6 Make a function `numberToDay : n : int -> weekday option` which given an integer in the range  $1 \dots 7$  returns one of the weekdays Monday...Sunday as an option type. An integer not in the range, i.e.  $< 1$  or  $> 7$  should return `None`.

Examples:

The call `numberToDay 1` should return `Some Monday` and The call `numberToDay 42` should return `None`.

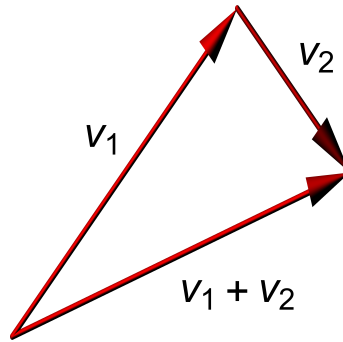


Figure 1: Illustration of vector addition in two dimensions.

## Afleveringsopgaver (in English)

This assignment is about 2-dimensional vectors. A 2-dimensional vector or just a vector is a geometric object consisting of a direction and a length. Typically, vectors are represented as a coordinate pair  $\vec{v} = (x, y)$ . The vector's ends are called its tail and tip, and when the tail is placed in  $(0, 0)$ , then its tip will be in the  $(x, y)$ . Vectors have a number of standard operations on them:

$$\vec{v}_1 = (x_1, y_1) \quad (2)$$

$$\vec{v}_2 = (x_2, y_2) \quad (3)$$

$$a\vec{v}_1 = (ax_1, ay_1) \quad (4)$$

$$\vec{v}_1 + \vec{v}_2 = (x_1 + x_2, y_1 + y_2) \quad (5)$$

Addition can be drawn as shown in Figure 1. Rotation of a vector counter-clockwise around its tail by  $a$  can be done as,

$$R_a \vec{v}_1 = (x \cos(a) - y \sin(a), x \sin(a) + y \cos(a)) \quad (6)$$

In F#, the trigonometric functions are found in `System.Math.Cos` and `System.Math.Sin`, and they both take an angle in radians as the argument. The constant  $\pi$  is found in `System.Math.PI`.

2g0 Using Steps 1, 3, 5, 7, and 8 from the 8-step guide to write a small set of functions in F#:

(a) addition of vectors

```
add: float * float -> float * float -> float * float
```

(b) multiplication of a vector and a constant

```
mul: float * float -> float -> float * float
```

(c) dot-product of two vectors

```
dot: float * float -> float * float -> float
```

(d) rotation of a vector

```
rot: float * float -> float -> float * float
```

The functions are to be documented using the `<summary>`, `<param>`, and `<returns>` XML tags.

2g1 Using Canvas, you are to draw vectors.

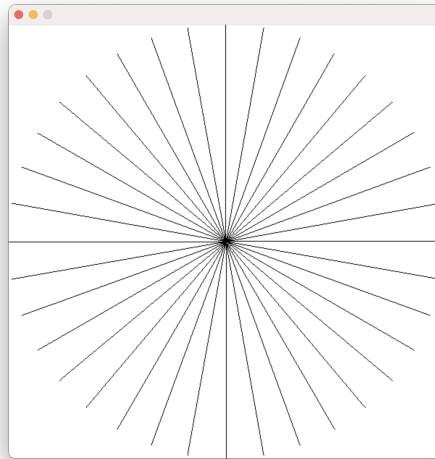


Figure 2: 36 radial lines from the center of a canvas.

- (a) make a function

```
toInt: float * float -> int * int
```

which takes a vector of floats and returns a vector of ints.

- (b) Using add and toInt, make a function

```
setVector: canvas -> color -> int * int -> int * int -> unit
```

which takes a canvas, a color, a vector, and a position for its tail and draws it as a line with setLine on the canvas. Demonstrate that this works by drawing the canvas with show.

- (c) make a function using rot and setVector

```
draw: int -> int -> canvas
```

which creates a canvas with a given width and height, adds 36 spokes as illustrated in Figure 2, and returns the canvas. Demonstrate that this works by drawing the canvas with show.

- (d) Optional: Use these in runApp to make an interactively rotating set of spokes as follows: Extend draw with a float state parameter  $s$ , which draws the spokes with the angular offset  $s$ . Add a reaction function react which changes the offset by  $\pm 0.01$  when the right and left arrow key are pressed respectively.

The functions are to be documented using the <summary>, <param>, and <returns> XML tags.

## Krav til afleveringen

Afleveringen skal bestå af

- en zip-fil, der hedder 2g.zip
- en opgavebesvarelse i pdf-format.

Zip-filen skal indeholde:

- filen `README.txt` som er en textfil med jeres navne og dato arbejdet.
- en `src` mappe med følgende og kun følgende filer:

`2g0.fsx` og `2g1.fsx`

svarende til afleveringsopgaverne

- en `tex` mappe med følgende og kun følgende filer:

`2g.tex` og to screenshots der viser resultaterne fra hhv. `2g1b.fsx` og `2g1c.fsx` i `png`-format.

$\text{\LaTeX}$ dokumentet `2g.tex` skal benytte `opgave.tex` skabelonen og ganske kort dokumentere jeres løsning. Et Screenshot af Canvas vinduet skal inkluderes i dokumentet.

God fornøjelse.