

# Programmering og Problemløsning

14.1: Nedarvning

# Resumé

- Med overloading kan vi genbruge navne til små variationer i inputparametre
- Association: “kender-til” - besked relation
- Aggregation: “har-en/flere” – udveksling af ejerskab
- Composition: “har-en/flere” – een ejer
- Overshadow: Navnesammenfald i nedarvning skygger i underklassen
- Abstrakte klasser og override: Abstrakte klasser kan kræve nedarvning og metodedefinitioner.

# Interface (is-a)

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Listing 22.5 umlInterface.fsx:

The television and the car class both implement the button interface.

```
1  type button =  
2      abstract member press : unit -> string  
3  type television () =  
4      interface button with  
5          member this.press () = "Changing channel"  
6  type car () =  
7      interface button with  
8          member this.press () = "Activating wipers"  
9  let pressIt (elm : #button) =  
10     elm.press()  
11  
12  let t = television()  
13  let c = car()  
14  printfn "%s" (pressIt t)  
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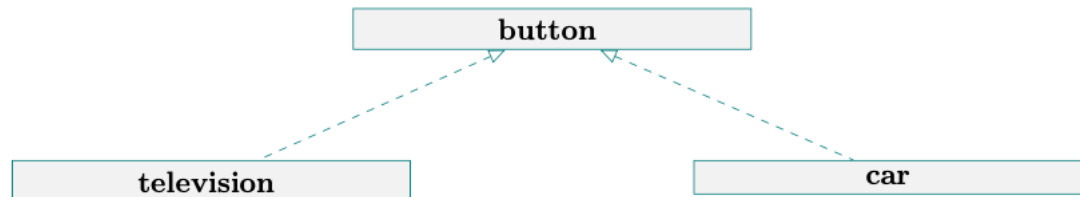
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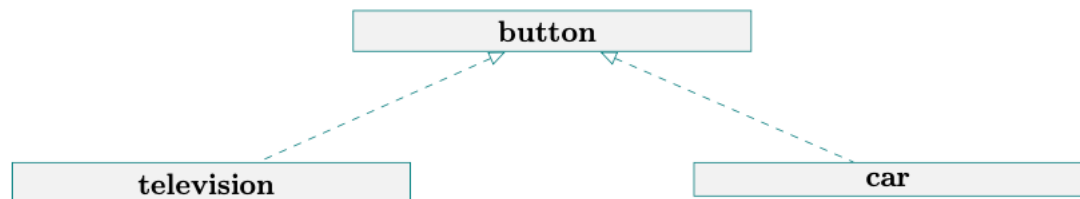
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```

Fordele: Angiver egenskaber, semantisk graf  
Bagdele: Risiko for megen up- og downcasting



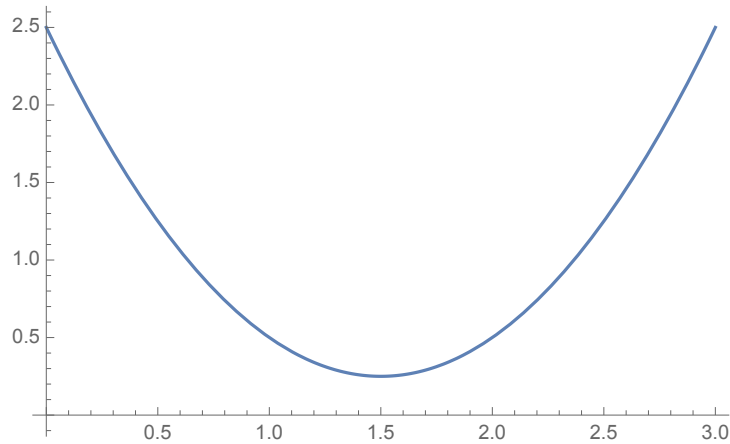
# Operatorer: Komplekse tal

For reelle tal:  $ax^2 + bx + c = 0 \Rightarrow x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$

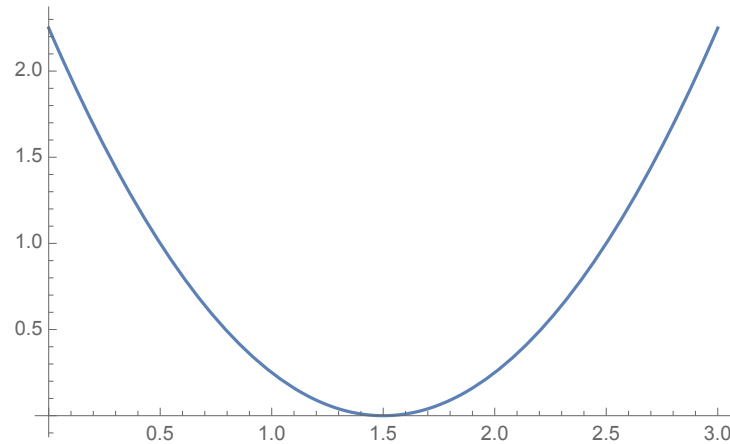
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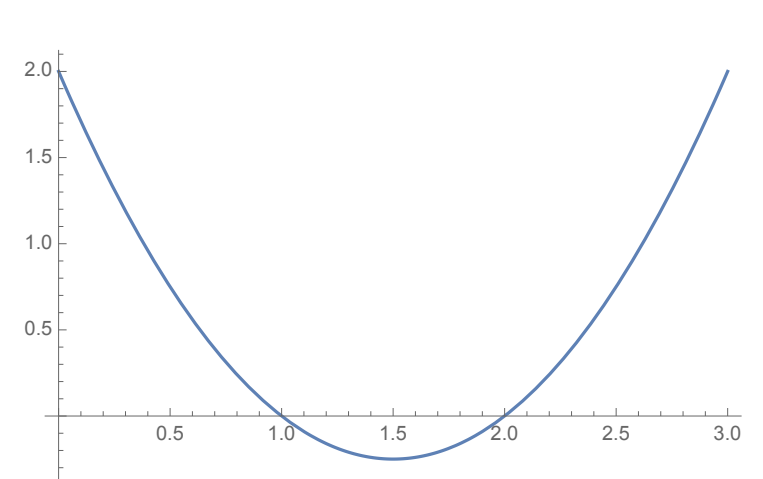
$b^2 - 4ac < 0$  0 løsninger



$b^2 - 4ac = 0$  1 løsning



$b^2 - 4ac > 0$  2 løsninger

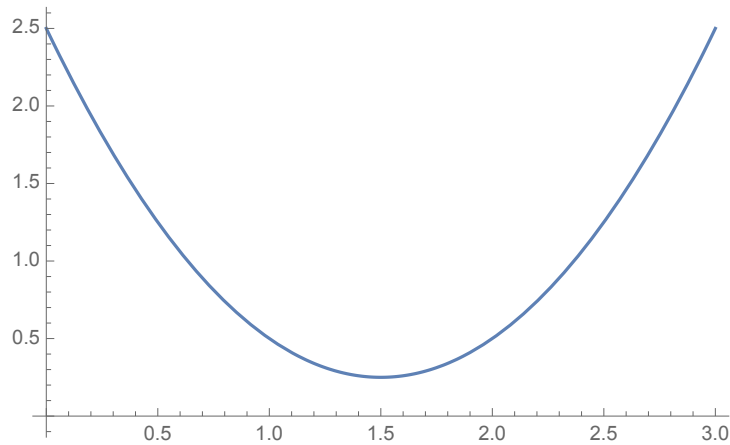




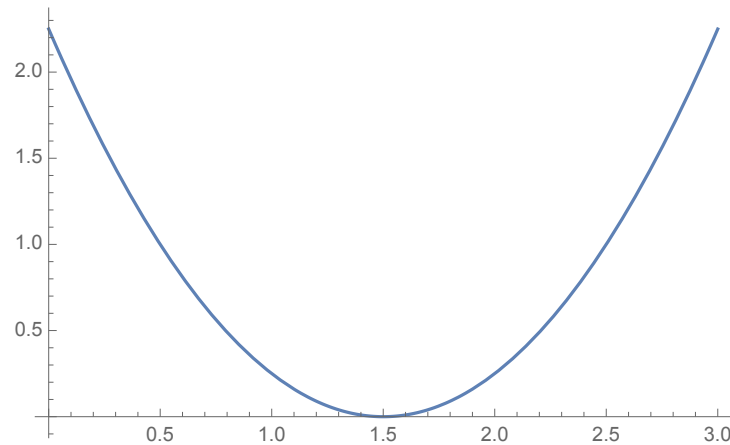
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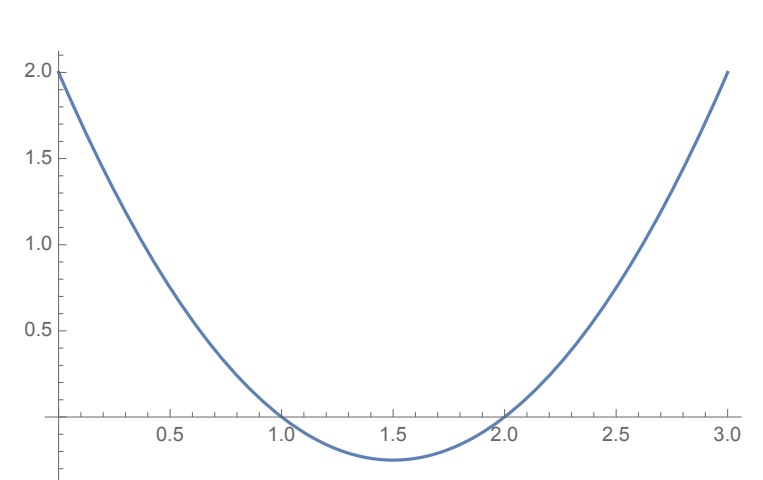
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Imaginært tal:  $x = a + ib$

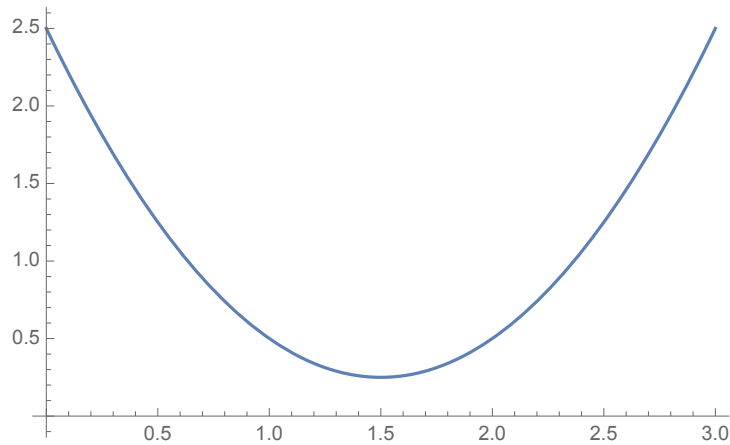
$$i = \sqrt{-1}$$

Altid 2 løsninger!

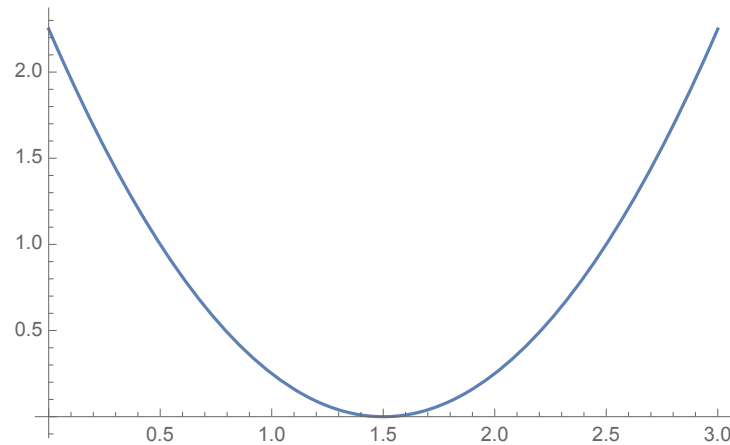
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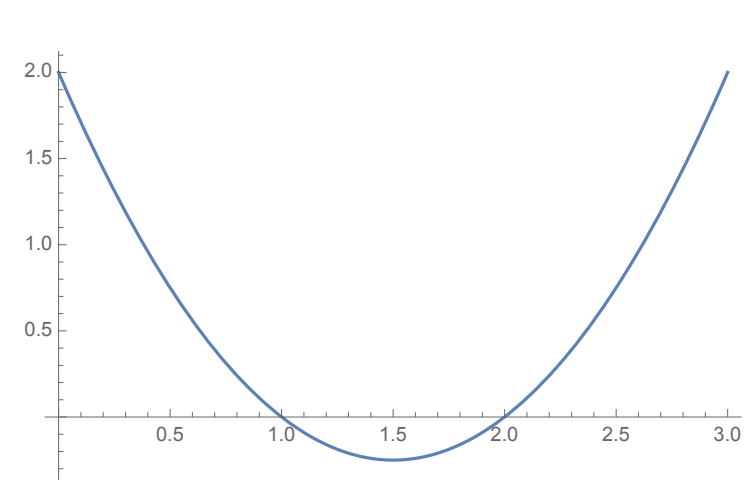
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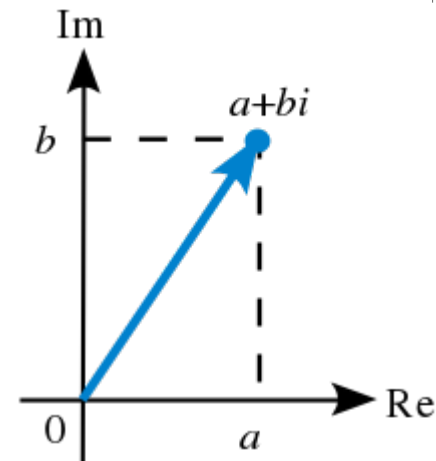
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# Komplekse tal

[https://en.wikipedia.org/wiki/Complex\\_number](https://en.wikipedia.org/wiki/Complex_number)

**Kompleks konstant:**  $i^2 = -1$

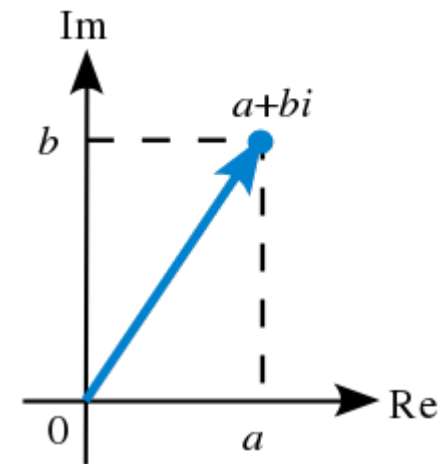
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**Reelle del:**  $\text{Re}(a + ib) = a$

**Lig med:**  $(a + ib) = (c + id) \Leftrightarrow a = c \text{ and } b = d$

**Addition:**  $(a + ib) + (c + id) = (a + c) + i(b + d)$

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# Komplekse tal: Mutable

```
1 type complex (a : float, b : float) =  
2   let mutable u = (a, b)  
3   member this.re = fst u  
4   member this.im = snd u  
5   member this.add (v : complex) =  
6     u <- (this.re + v.re, this.im + v.im)
```

```
14  
15 let x = complex(1.0, 2.0)  
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8     if this.im >= 0.0 then
9       sprintf "(%g + i %g)" this.re this.im
10    else
11      sprintf "(%g - i %g)" this.re (- this.im)
12   member this.copy () =
13     complex(this.re, this.im)
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15 let x = complex(1.0, 2.0)
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- Mutable: copy needed, difficult to remember state

complexSideEffect.fsx



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7   override u.ToString () =  
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# Komplekse tal: Static

```
1 type complex (a : float, b : float) =  
2   let _u = (a, b)  
3   member u.re = fst _u  
4   member u.im = snd _u  
5   static member add (u : complex, v : complex) : complex =  
6     complex(u.re + v.re, u.im + v.im)  
7   override u.ToString () =  
8     if u.im >= 0.0 then  
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- This: No state to remember, operator difficult
- U: programming notation easier
- Static: Like a module, usage slightly more natural

# Komplekse tal: Operator

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1 type complex (a : float, b : float) =  
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4   member u.im = snd _u  
5   static member (+) (u : complex, v : complex) : complex =  
6     complex(u.re + v.re, u.im + v.im)  
7   override u.ToString () =  
8     if u.im >= 0.0 then  
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- Static: Like a module, usage slightly more natural
- Operator: 'normal' usage

# Komplekse tal: equality

(=) operator eksisterer ikke!

System.object klassen:

- Equals
- Finalize
- GetHashCode
- GetType
- ToString

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> let x = complex(1.0, 2.0);;  
val x : complex = (1 + i 2)  
  
> x.GetType();;
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val x : complex = (1 + i 2)  
  
> x.GetType();;
```

```
val it : System.Type =  
    FSI_0005+complex  
    {Assembly = FSI-ASSEMBLY, Version=0.0.0.0, Culture=neutral, PublicKeyToken=null;  
      AssemblyQualifiedName = "FSI_0005+complex, FSI-ASSEMBLY, Version=0.0.0.0, Culture=neutral, PublicKeyToken=null";  
      Attributes = AutoLayout, AnsiClass, Class, NestedPublic, Serializable;  
      BaseType = System.Object;  
      ContainsGenericParameters = false;  
      CustomAttributes = seq  
          [ [Microsoft.FSharp.Core.CompilationMappingAttribute((Microsoft.FSharp.Core.SourceConstructFlags)3)];  
            [System.SerializableAttribute()] ];  
      DeclaredConstructors = [|Void .ctor(Double, Double)|];  
      DeclaredEvents = [|]|;  
      DeclaredFields = [|System.Tuple`2[System.Double, System.Double] _u|];  
      DeclaredMembers = [|Double get_re(); Double get_im();  
                          complex op_Addition(complex, complex);  
                          System.String ToString(); Void .ctor(Double, Double);  
                          Double re; Double im;  
                          System.Tuple`2[System.Double, System.Double] _u|];  
      DeclaredMethods = [|Double get_re(); Double get_im();  
                          complex op_Addition(complex, complex);  
                          System.String ToString()|];  
      DeclaredNestedTypes = seq [|];  
      DeclaredProperties = [|Double re; Double im|];
```

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BaseType = System.Object;  
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# Komplekse tal: equality

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1 type complex (a : float, b : float) =
2   let _u = (a, b)
3   member u.re = fst _u
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5   static member (+) (u : complex, v : complex) : complex =
6     complex(u.re + v.re, u.im + v.im)
7   override u.ToString () =
8     if u.im >= 0.0 then
9       sprintf "(%g + i %g)" u.re u.im
10    else
11      sprintf "(%g - i %g)" u.re (- u.im)
12   override u.Equals obj =
13     match obj with
14     :? complex as v -> u.re = v.re && u.im = v.im
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18 let x = complex(1.0, 2.0)
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20 printfn "%A = %A = %A" x y (x=y)
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Compare types operator: "?:?"

# Komplekse tal: equality

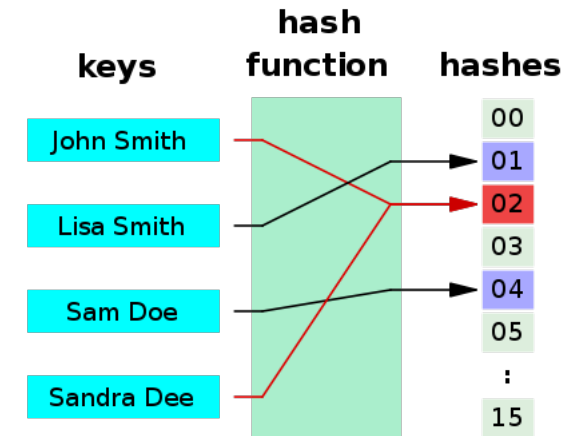
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Compare types operator: "?:?"

Hash function: map from infinite domain to fixed sized domain. For computational and storage efficient data access



[https://en.wikipedia.org/wiki/Hash\\_function](https://en.wikipedia.org/wiki/Hash_function)



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System.object klassen:

- Equals
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Compare types operator: "?:?"

```
sporrington@Jons-mac 14.1-3 % fsharp complexEqual.fsx
(1 + i 2) = (2.5 - i 1.2) = false
(1 + i 2) = (1 + i 2) = true
```

# Komplekse tal: List.sort (comparable)

```
[> List.sort;;  
val it : ('a list -> 'a list) when 'a : comparison
```

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1 type complex (a : float, b : float) =  
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3   member u.re = fst _u  
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5   static member (+) (u : complex, v : complex) : complex =  
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15      | _ -> false  
16  override u.GetHashCode() = hash _u  
17  interface System.IComparable with  
18    member u.CompareTo obj =  
19      match obj with  
20        :? complex as v -> compare u.re v.re  
21        | _ -> invalidArg "obj" "cannot compare values of different types"  
22  
23 let x = complex(1.0, 2.0)  
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25 let lst = [y;x]  
26 printfn "List.sort %A = %A" lst (List.sort lst)
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```
[sporrington@Jons-mac 14.1-3 % fsharp complexCompareTo.fsx  
List.sort [(2.5 - i 1.2); (1 + i 2)] = [(1 + i 2); (2.5 - i 1.2)]
```

# Opsummering

- Abstrakte klasser og override: Abstrakte klasser kan kræve nedarvning og metodedefinitioner.
- Komplekse tal: Mutable, immutable, self-identifier, static, operator
- Copy constructor
- equality og comparable type begrænsninger

God Jul