



**fit@hcmus**

**MTH00051**

# **APPLIED MATHEMATICS AND STATISTICS**

**COURSE INTRODUCTION**

1. GENERAL INFORMATION
2. COURSE DESCRIPTION
3. COURSE OUTCOMES
4. CONTENT
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6. RESOURCES
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1. Course name: Applied Mathematics and Statistics
2. Course name (in Vietnamese): Toán ứng dụng và thống kê
3. Course ID: MTH00051
4. Knowledge block: General Education Knowledge
5. Number of credits: 4
6. Credit hours for theory: 45
7. Credit hours for practice: 30
8. Credit hours for self-study: 90
9. Prerequisite: none
10. Prior-course: none

Systematize math knowledge learned in the first 3 semesters of university (calculus, linear algebra, probability-statistics), introduce algorithmic skills to be able to solve problems related to machine learning, data analysis. Specifically, including 3 blocks of knowledge:

- ☐ Computational methods for matrix algebra.
- ☐ Computational methods for convex optimization
- ☐ Probability models

| CO   | Description  |
|------|--|
| G1.1 | Establish, organize, operate, and manage the team. |
| G1.2 | Participate in group discussions                   |
| G1.3 | Writing a technical report.                        |
| G2.1 | Be able to explain terminologies.                  |
| G2.2 | Reading English lectures and textbooks.            |
| G3.1 | Be able to explain basic concepts.                 |

| CO   | Description  |
|------|--|
| G3.2 | Ethics.  |
| G3.3 | Be able to self study.   |
| G4.1 | Be able to use the learned models.                                   |
| G5.1 | Be able to describe the learned mathematical and statistical methods |
| G5.2 | Be able to design an algorithm.                                      |

| ID | Topic   |
|----|---|
| 1  | <b>System of linear equations</b> <ul style="list-style-type: none"> <li>. Introduction to system of linear equations</li> <li>. System of linear equations and matrices <math>Ax = b</math></li> <li>. Equation systems of the special form</li> <li>. Generic equation systems</li> <li>. Gaussian elimination</li> </ul> |
| 2  | <b>Vector</b> <ul style="list-style-type: none"> <li>. Vector and vector operations</li> <li>. Norm, Dot product, Distance</li> <li>. Basis and Orthogonal Basis</li> <li>. Gram-Schmidt process</li> </ul>   |

| ID | Topic  |
|----|--|
| 3  | <b>Matrix</b> <ul style="list-style-type: none"> <li>. Matrix and matrix operations</li> <li>. Special matrix forms (sparse, symmetrical, triangular, diagonal matrices)</li> <li>. Invertible matrices</li> <li>. Determinant</li> <li>. Matrix equations</li> </ul>          |
| 4  | <b>Matrix decompositions</b> <ul style="list-style-type: none"> <li>. LU decomposition</li> <li>. QR decomposition using Gram - Schmidt.</li> <li>. Eigenvalues and Eigenvectors</li> <li>. Diagonalization</li> <li>. Introduction to Singular Value Decomposition</li> </ul> |

| ID | Topic  |
|----|--|
| 5  | <b>Applications</b> <ul style="list-style-type: none"><li>. Some applications in Information Technology</li><li>. Some applications in Physics/Chemistry</li><li>. Some applications in Polynomial interpolation</li></ul> |
| 6  | <b>Midterm review</b>  |
| 7  | <b>Introduction to optimization</b> <ul style="list-style-type: none"><li>. One variable optimization</li><li>. Sensitivity and Robustness</li><li>. Multivariable optimization</li></ul>                                  |

| ID | Topic  |
|----|--|
| 8  | <b>Convex optimization</b> <ul style="list-style-type: none"><li>. Convex and concave functions</li><li>. Least square method</li><li>. Data fitting</li></ul>                 |
| 9  | <b>Introduction to probability</b> <ul style="list-style-type: none"><li>. Axiom of probability</li><li>. Random variables</li><li>. Conditional probability formula</li></ul> |
| 10 | <b>Probability models</b> <ul style="list-style-type: none"><li>. Introduction to statistics</li><li>. Markov chains</li></ul>   |
| 11 | Review   |



# ASSESSMENTS



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| Topic                    | Description   | Ratio (%) |
|--------------------------|---|-----------|
| A1. Assignments Weekly   | HW#1: System of linear equations.<br>HW#2: Vector and Matrix<br>HW#3: Matrix decompositions.<br>HW#4: Least square optimization.<br>HW#5: Markov chain. | 0%        |
| A2. Projects Weekly Labs | Lab#1: Gaussian algorithm. Lab#2: QR process. Lab#3: Applications. Lab#4: Data fitting. Lab#5: Markov chains.   | 15%       |
| A3. Exams                |   | 85%       |
| A3.1. Final project Labs | In-class programming exam on computer   | 25%       |
| A3.2 Midterm exam        | Closed book exam.<br>Describe the understanding of different topics, analyze & program to solve problems  | 20%       |
| A3.3 Final exam          | Closed book exam.<br>Describe the understanding of different topics, analyze & program to solve problems  | 40%       |

❖ Textbooks: Stephen Boyd, Lieven Vandenberghe, *Introduction to Applied Linear: Algebra, Matrices, and Least Squares*, Cambridge University Press, 2018 (available in internet).

❖ Others:

- [1] G. H. Golub, C. F. Van Loan, *Matrix computations*, 4th edition, Johns Hopkins University Press, 2013.
- [2] Y. Saad, *Iterative methods for sparse linear systems*, 2nd edition, Society for Industrial and Applied Mathematics, 2003.
- [3] S. Boyd, L. Vandenberghe, *Convex optimization*, 7th edition, Cambridge University Press, 2009.
- [4] R. V. Hogg, J. W. McKean, A. T. Craig, *Introduction to mathematical statistics*, 7th edition, Pearson, 2013.
- [5] Đ. Đ. Trọng, Đ. N. Thanh, *Lý thuyết thống kê*, NXB ĐHQG Tp HCM, 2016.
- [6] Đ. N. Thanh et. al., *Bài tập và thực hành lý thuyết thống kê*, NXB ĐHQG Tp HCM, 2016.
- [7] Zed Shaw, *Learn Python: The Hard Way*. Addison Wesley, 3rd Edition, 2014

- All students are responsible for reading and following strictly the regulations and policies of the school and university.
- Students who are absent for more than 3 theory sessions are not allowed to take the exams.
- For any kind of cheating and plagiarism, students will be graded 0 for the course. The incident is then submitted to the school and university for further review.
- Students are encouraged to form study groups to discuss on the topics. However, individual work must be done and submitted on your own.

