

## Concurrent scheduling of rules

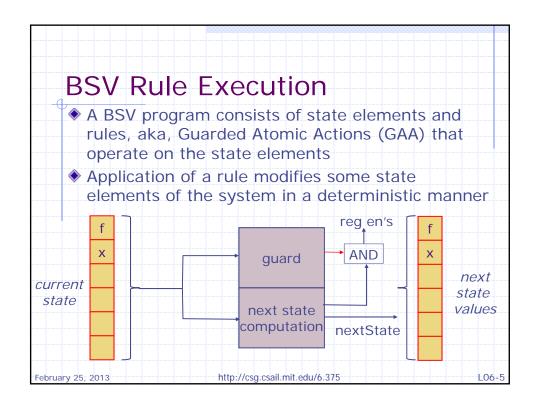
- The one-rule-at-a-time semantics plays the central role in defining functional correctness and verification but for meaningful hardware design it is necessary to execute multiple rules concurrently without violating the one-rule-at-a-time semantics
- What do we mean by concurrent scheduling?
  - First some hardware intuition
  - Second semantics of rule execution
  - Third semantics of concurrent scheduling

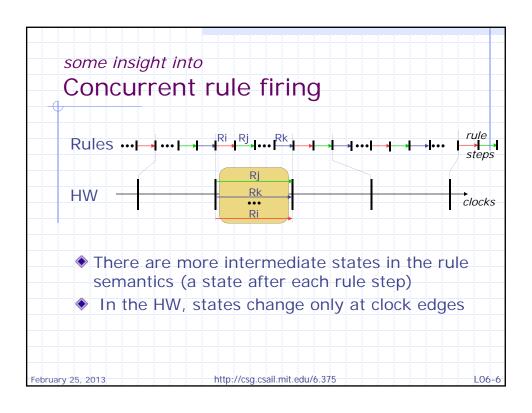
bruary 25, 2013 http://csq.csail.mit.edu/6.375

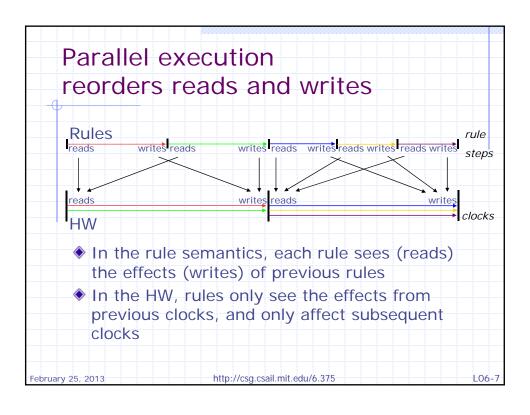
Hardware intuition for concurrent scheduling

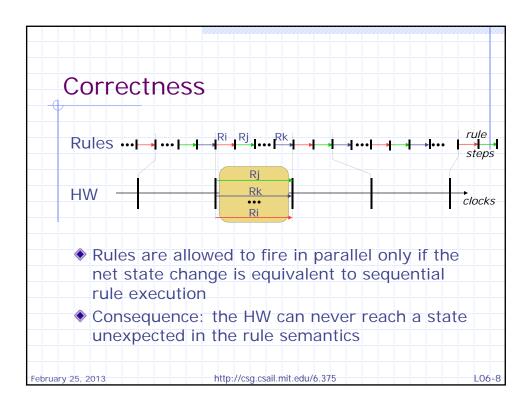
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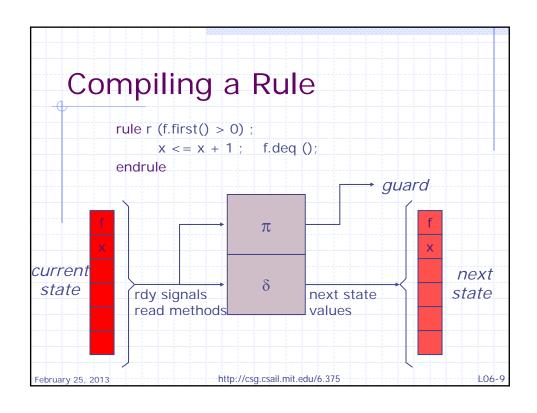
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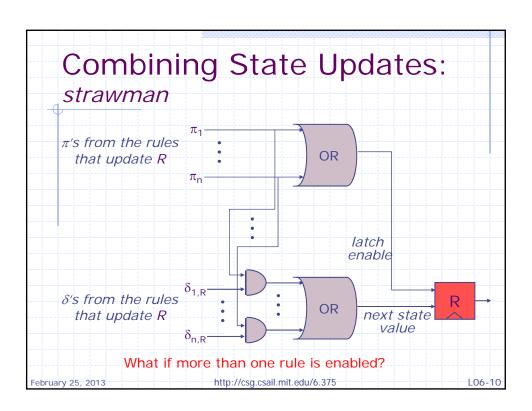


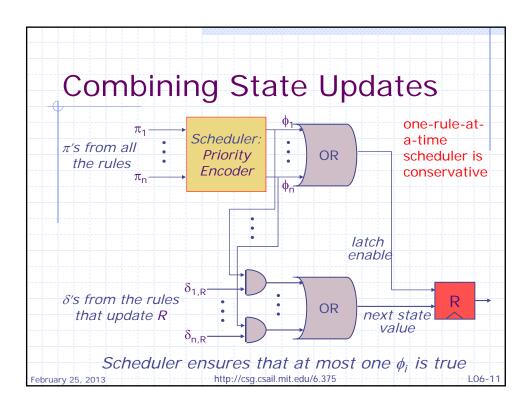


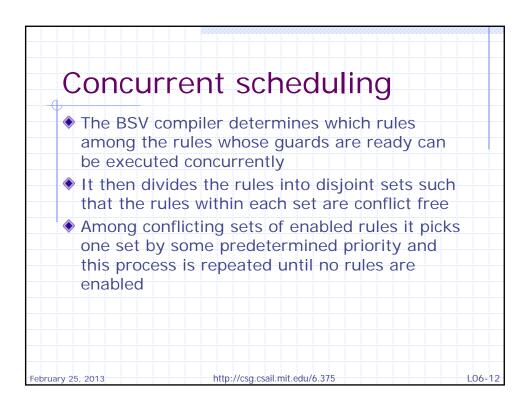




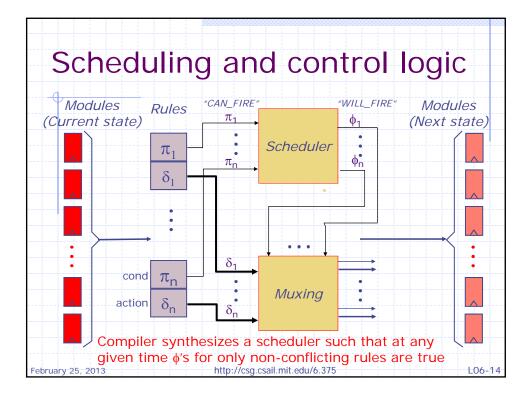


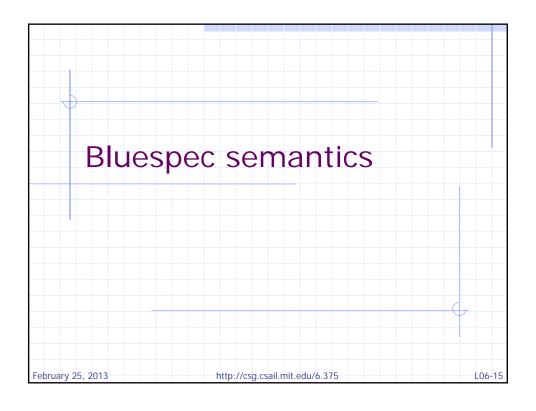


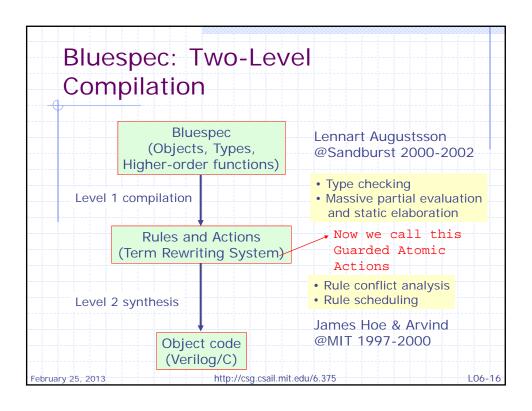


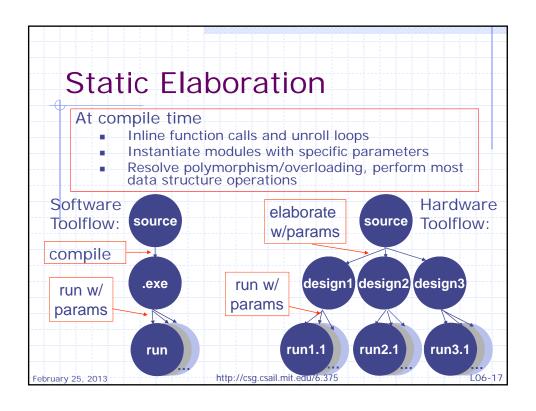


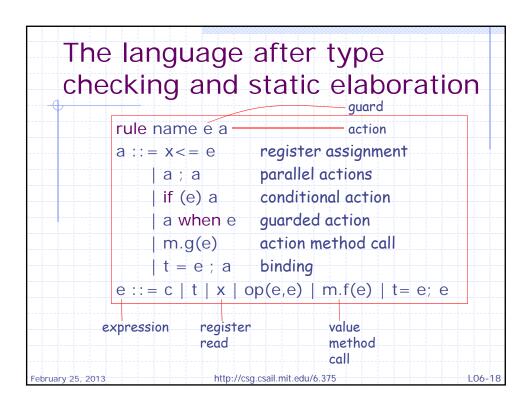
## A compiler test for concurrent rule firing James Hoe, Ph.D., 2000 Let RS(r) be the set of registers rule r may read Let WS(r) be the set of registers rule r may write Rules ra and rb are conflict free (CF) if (RS(ra)∩WS(rb) = φ) ∧ (RS(rb)∩WS(ra) = φ) ∧ (WS(ra)∩WS(rb) = φ) Rules ra and rb are sequentially composable (SC) (ra<rb) if (RS(rb)∩WS(ra) = φ) ∧ (WS(ra)∩WS(rb) = φ) If Rules ra and rb conflict if they are not CF or SC











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Guard Lifting rules
All the guards can be "lifted" to the top of a rule
   (a1 when p); a2
                             \Rightarrow (a1; a2) when p
   a1; (a2 when p)
                             \Rightarrow (a1; a2) when p
                           \Rightarrow (if (p) a) when q
   if (p when q) a
   if (p) (a when q)
                             \Rightarrow (if (p) a) when (q | !p)
   • (a when p1) when p2 \Rightarrow a when (p1 & p2)
                           \Rightarrow (x <= e) when p
   x <= (e when p)</p>
   • m.g_B(e \text{ when p}) \Rightarrow m.g_B(e) \text{ when p}
similarly for expressions ...
   Rule r (a when p)
                             \Rightarrow Rule r (if (p) a)
 We will give a procedure to evaluate rules after guard lifting
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Rule evaluation
    rule name e a
                       register assignment
    a ::= x<= e
                     parallel actions
         a;a
         | if (e) a
                       conditional action
                     action method call
        m.g(e)
         t = e; a
                       binding
    e := c | t | x | op(e,e) | m.f(e) | t = e; e
 evalA :: (Bindings, State, a) -> (Bindings, StateUpdates)
 evalE :: (Bindings, State, e) -> Value
            variable
                      register
            bindings
                      values
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Action evaluator
no method calls
  evalA:: (Bindings, State, a) -> (Bindings, StateUpdates)
evalA(bs, s, [[x <= e]]) = (bs, (x, evalE(bs, s, e)))
evalA(bs, s, [[a1; a2]]) =
  let (bs', u1) = evalA(bs, s, a1)
                                             merges two sets of
      (bs'', u2) = evalA(bs', s, a2)
                                             updates; the rule is
                                             illegal if there are
  in (bs", u1 + u2)
                                             multiple updates for
evalA(bs, s, [[if (e) a]]) =
                                             the same register
   if evalE(bs, s, e) then evalA(bs, s, a)
                    else (bs, {})
evalA(bs, s, [[t = e; a]]) =
  let v = evalE(bs, s, e)
                                            extends the bindings
   in evalA(bs + (t,v), s, a)
                                            by including one for t
  initially bs is empty and state contains old register values
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Expression evaluator
no method calls
        evalE :: (Bindings, State, exp) -> Value
    evalE (bs, s, [[c]]) = c
                                         if t does not
    evalE (bs, s, [[t]]) = lookup(bs,t) - exist in bs then
                                         the rule is illegal
    evalE (bs, s, [[x]]) = s.x
    evalE (bs, s, [[op(e1,e2)]]) =
                  op(evalE(bs, s, e1), evalE(bs, s, e2))
    Method calls can be evaluated by substituting the
    body of the method call, i.e., m.g(e) is a[e/x] where
    the definition of m.g is method g(x) = a
    To apply a rule, we first evaluate its guard and then if
    the guard is true we compute the state updates and
    then simultaneously update all the state variables
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Legal BSV rules

A legal BSV rule does not contain multiple assignments to the same state element or combinational cycles

Examples: legal?
rule ra if (z>10);
x <= x+1; endrule
rule rb;
x <= x+1; if (p) x <= 7 endrule
rule rc;
x <= y+1; y <= x+2 endrule
rule rd;
t1 = f(t2); t2 = g(t1); x <= t1; endrule
In general the legality of a rule can be determined only at run time.
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A legal BSV rules

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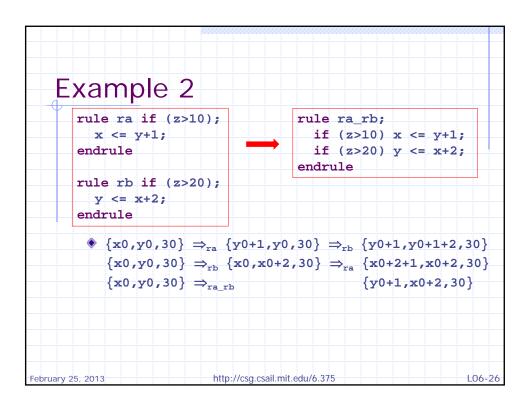
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Examples: legal?

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## Concurrent scheduling: Semantic view Suppose rule ra a and rule rb b are legal rules and a and b are free of guards. ra and rb are concurrently schedulable, iff, rule rab (a;b) is legal for all s, (a;b)(s) = a(b(s)) or b(a(s)) Theorm1: If rules ra and rb are conflict free (CF) then ∀s, (a;b)(s) = a(b(s)) = b(a(s)) Theorm2: If rules ra and rb are sequentially composable (SC) (ra<rb) then ∀s, (a;b)(s) = b(a(s))

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Example 1
   rule ra if (z>10);
                                           rule ra_rb;
      x \le x+1;
                                             if (z>10) x <= x+1;
   endrule
                                              if (z>20) y <= y+2;
                                           endrule
   rule rb if (z>20);
     y \ll y+2;
   endrule
     ♦ \{x0,y0,30\} ⇒<sub>ra</sub> \{x0+1,y0,30\} ⇒<sub>rb</sub> \{x0+1,y0+2,30\}
        \{x0,y0,30\} \Rightarrow_{rb} \{x0,y0+2,30\} \Rightarrow_{ra} \{x0+1,y0+2,30\}
        \{x0,y0,30\} \Rightarrow_{ra rb}
                                                      \{x0+1,y0+2,30\}
     ♦ \{x0,y0,15\} \Rightarrow_{ra} \{x0+1,y0,15\} \Rightarrow_{rb} \{x0+1,y0,15\}
        \{x0,y0,15\} \Rightarrow_{rb} \{x0,y0,15\} \Rightarrow_{ra} \{x0+1,y0,15\}
        \{x0,y0,15\} \Rightarrow_{ra\_rb}
                                                      \{x0+1,y0,15\}
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Example 3
       rule ra if (z>10);
                                           rule ra_rb;
                                             if (z>10) x <= y+1;
         x \ll y+1;
       endrule
                                             if (z>20) y <= y+2;
                                           endrule
       rule rb if (z>20);
         y \le y+2;
       endrule
         ♦ \{x0,y0,30\} ⇒<sub>ra</sub> \{y0+1,y0,30\} ⇒<sub>rb</sub> \{y0+1,y0+2,30\}
           \{x0,y0,30\} \Rightarrow_{xb} \{x0,y0+2,30\} \Rightarrow_{xa} \{y0+2+1,y0+2,30\}
                                                     {y0+1,y0+2,30}
            \{x0,y0,30\} \Rightarrow_{ra rb}
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                             http://csg.csail.mit.edu/6.375
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