

# Formal Verification Final Project

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GitHub link for the codes:

[https://github.com/elemenopi/Sokoban\\_nuXmv.git](https://github.com/elemenopi/Sokoban_nuXmv.git)



# Part 1

1. Define an FDS for a general  $n \times m$  Sokoban board. Use XSB format to describe the board.
2. Define a general temporal logic specification for a win of the Sokoban board.

1.

FDS for Sokoban board:

$$D = \{V, \theta, \rho, J, C\}$$

$$V = \{ @, \$_{1-n} \}$$

$$\theta = \{ @ = (x_{@}, y_{@}), \$_1 = (x_{\$1}, y_{\$1}) \dots \$_n = (x_{\$n}, y_{\$n}) \}$$

$$\rho = \{ ( @' = (x_{@+1}, y_{@}) \parallel @' = (x_{@-1}, y_{@}) \parallel @' = (x_{@}, y_{@+1}) \parallel @' = (x_{@}, y_{@-1}) \ \&\& \\ ( \$_t = \$'_t \parallel \$'_t = (x_{\$t+1}, y_{\$t}) \parallel \$'_t = (x_{\$t-1}, y_{\$t}) \parallel \$'_t = (x_{\$t}, y_{\$t+1}) \parallel \$'_t = (x_{\$t}, y_{\$t-1}) ) \\ \parallel \$'_t = *_t ) \\ \text{for } t \{ 1 \dots n \} \}$$

Symbol	Definition
@	warehouse keeper
+	warehouse keeper on goal
\$	box
*	box on goal
#	wall
.	goal
-	floor

עבור רו –

עבור השחקן – הוא זז למעלה/למטה/ימינה/שמאלה.

עבור כל כופסא – או שהיא זזה (בגלל שהשחקן הזיז אותה) או שהיא נמצאת על מטרה.

$$J = \{ \$_{1-n} = *, \$_{1-n} \neq \#, \$_{1-n} \neq @, @ \neq \#, \text{ for } i \text{ and } j: \$_i \neq \$_j \}$$

כל הכופסאות אין סוף פעמים נמצאות על נקודת מטרה,

אף פעם לא יהיה מצב ש 2 כופסאות / כופסא ואיש / כופסא וקיר / איש וקיר על אותה המשבצת בלוח.

$$C = \{ < @' = \#, @' = @ >, < @' = \$_i \ \&\& \$'_i = \#, @' = @ >, \\ < \$'_i = \#, \$'_i = \$_i >, < \$'_i = \$_j, \$'_i = \$_i > \}$$

אם האיש הולך לכיוון הקיר – הוא נשאר במקום, כנ"ל לגבי אם הוא מנסה לדחוף כופסא אבל היא צמודה לקיר.

בנוסף אם הכופסא צמודה לכופסא אחרת או כופסא צמודה לקיר – היא נשאר במקום.

2.

Win condition for Sokoban board:

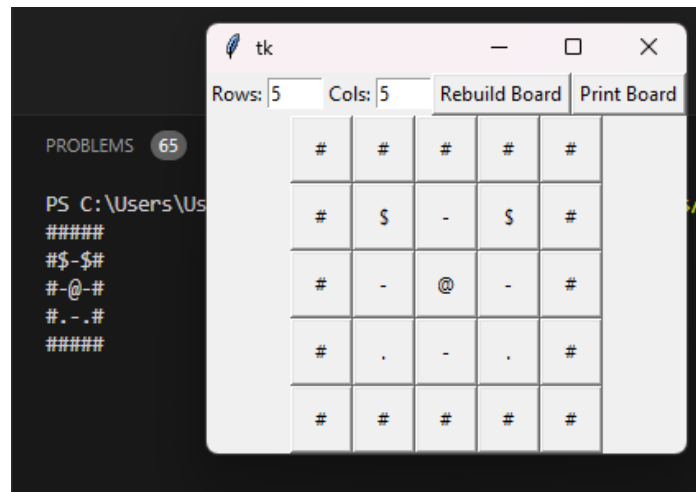
$$F(G(\$_{1-n} = *)), n = \text{num of boxes}$$

משלב מסוים, תמיד – כל הכופסאות ישבו על מטרה.

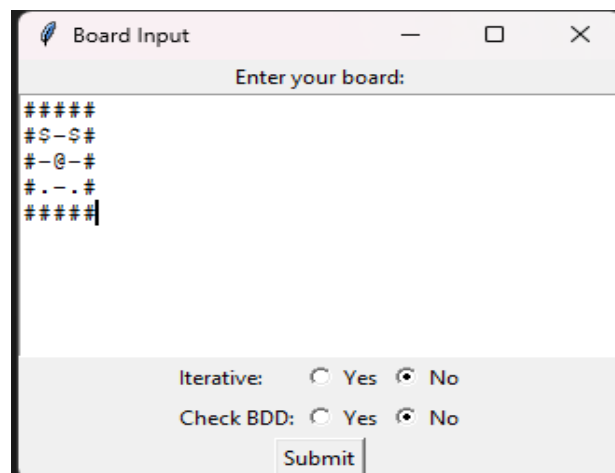
כלומר כל הפרמוטציות של כופסא כלשהי שיושבת על אחת המטרות כך שעל כל המטרות יש כופסאות מספקת את התנאי לנצחון.

מחלק זה אנחנו מבצעים אוטומציה ע"י פייתון – ראשית נגשנו למשימה בכך שניסינו לייצר קוד ללוח אחד של סוקובן ב smv על מנת לייצר את הבסיס לתנאים והחוקים של המשחק ולאחר מכן ביצענו הכללה ואוטומציה בפייתון כך שבנהתן לוח כלשהו הקוד שלנו ידע לקחת ממנו את המיקומים של כל האלמנטים ולייצר קובץ smv. לאחר כתיבת ה smv, הקוד יריץ את הקובץ ב nuXmv ויראה לנו את התוצאות.

על מנת להקל על כתיבת לוח משחק והכנסתם כאינפוט יצרנו קוד נוסף, שקראנו לו board\_to\_XSB\_gui, קוד זה פותח לוח בגוי בו אפשר למקם כל אלמנט (אדם, כופסא, מטרה) על הלוח וכנלחץ print הוא ידפיס את הלוח כפלט של פייתון.



לאחר שיש לנו פורמט מוכן של לוח נפעיל את הפייתון sokoban.py מ cmd בתוך התקייה בה נמצא nuXmv כדי ש nuXmv ימצא את קובץ ה smv ויצליח להריץ אותו.



נעתיק את הלוח לתוך הגוי ונבחר באפשרות שאנחנו מעוניינים להריץ. (חשוב לזכור להיות על אנגלית אחרת זה לא ידביק את הלוח על המסך)

## Part 2

1. Using Python, or another coding language, and your answers to Part 1, automate definition of given input boards into SMV models. These models should contain both the model and the temporal logic formulae defining a win.
2. Run each of these models in nuXmv. Indicate the commands you used to run nuXmv, as well as screenshots of the nuXmv outputs.
3. For each board, indicate if it is winnable. If it is, indicate your winning solution in LURD format.

## Part 3

1. Measure performance of nuXmv's BDD and SAT Solver engines on each of the models.
2. Compare the performance of the two engines. Is one engine more efficient than the other?

עבור חלק 2 ו3 נסמן check BDD כדי שנקבל כפלט את הזמנים גם של sat וגם של bdd, כדיפולט עשינו הרצה של sat. הגדרנו בדיקה עד ל40 צעדים במידה ולא מוצאים פתרון ללוח.

נקבל כפלט שלושה קבצים חדשים:

```
output_sat.out
result_model_for_iteration_1
results_for_model_iteration_1.out
```

- קובץ result\_model\_for\_iteration זה קובץ ה smv שאנחנו יוצרים אותו נריץ ב nuXmv.
- קובץ output\_sat קובץ שמראה את פלט ה nuXmv אחרי ההרצה, כולל בסופו זמן ריצה (sat)
- קובץ result\_for\_model\_iteration קובץ שמראה את תוצאת הריצה בפורמט LURD + זמני ריצה.

\*\*בגלל שעשינו את כל החלקים 2,3,4 באותו הקוד שמות הקבצים כוללים iteration שיהיה רלוונטי בחלק 4.

## להלן ההרצות והפליטים של חלק 2 ו3:

ריצה 1:



Rows: 3	Cols: 5	Rebuild Board	Print Board	
#	#	#	#	#
#	@	\$	.	#
#	#	#	#	#

פלט mvnux:

-- as demonstrated by the following execution sequence

Trace Description: BMC Counterexample

Trace Type: Counterexample

-> State: 1.1 <-

i\_person = 1

j\_person = 1

i\_box1 = 1

j\_box1 = 2

action\_person = no-action

boxes\_overlap = FALSE

box\_on\_wall = FALSE

man\_on\_box = FALSE

man\_on\_wall = FALSE

j\_box\_goal1 = 3

i\_box\_goal1 = 1

M = 5

N = 3

grid[0][0] = 1

grid[0][1] = 1

grid[0][2] = 1

grid[0][3] = 1

grid[0][4] = 1

```

grid[1][0] = 1
grid[1][1] = 0
grid[1][2] = 0
grid[1][3] = 0
grid[1][4] = 1
grid[2][0] = 1
grid[2][1] = 1
grid[2][2] = 1
grid[2][3] = 1
grid[2][4] = 1
-> State: 1.2 <-
j_person = 2
j_box1 = 3
action_person = right
-> State: 1.3 <-
j_person = 1
action_person = left
nuXmv > elapse: 0.02 seconds, total: 0.02 seconds

```

תוצאות:

```

results in lurd format : R
runtime results SAT:

    Runtime after check_ltlspec_bmc -k 30: 0.02 seconds (Total time: 0.02 seconds)
Last checked bound: 1

    runtime results BDD:

    Runtime after check_ltlspec: 0.04 seconds (Total time: 0.04 seconds)

```

ריצה 2:



Rows: 3	Cols: 5	Rebuild Board	Print Board	
#	#	#	#	#
#	\$	@	.	#
#	#	#	#	#

פלט מ-nuxmv:

```
nuXmv > nuXmv > nuXmv > nuXmv > -- no counterexample found with bound 0
-- no counterexample found with bound 1
-- no counterexample found with bound 2
-- no counterexample found with bound 3
-- no counterexample found with bound 4
-- no counterexample found with bound 5
.....
-- no counterexample found with bound 40
nuXmv > elapse: 1.28 seconds, total: 1.28 seconds
```

תוצאות:

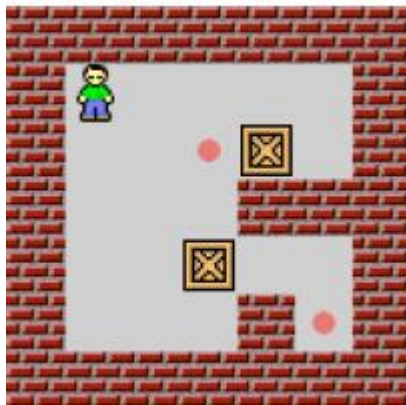
```
results in lurd format :
runtime results SAT:

    Runtime after check_ltlspec_bmc -k 30: 1.28 seconds (Total time: 1.28 seconds)
Last checked bound: 40

runtime results BDD:

    Runtime after check_ltlspec: 0.02 seconds (Total time: 0.02 seconds)
```

ריצה 3:



Rows: 7	Cols: 7	Rebuild Board	Print Board			
#	#	#	#	#	#	#
#	@	-	-	-	-	#
#	-	-	.	\$	-	#
#	-	-	-	#	#	#
#	-	-	\$	-	-	#
#	-	-	-	#	.	#
#	#	#	#	#	#	#

פלט nuxmv:

```

nuxmv > nuxmv > nuxmv > nuxmv > -- no counterexample found with bound 0
no counterexample found with bound 1 --
no counterexample found with bound 2 --
no counterexample found with bound 3 --
no counterexample found with bound 4 --
no counterexample found with bound 5 --
.....
no counterexample found with bound 40 --
nuxmv > elapse: 136.72 seconds, total: 136.72 seconds

```

תוצאות:

```

results in lurd format :
runtime results SAT:

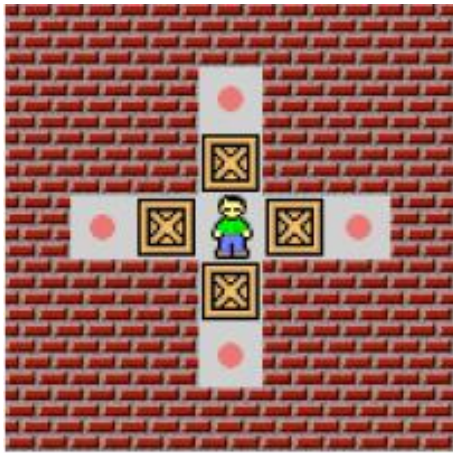
    Runtime after check_ltlspec_bmc -k 30: 136.72 seconds (Total time: 136.72 seconds)
Last checked bound: 40

runtime results BDD:

    Runtime after check_ltlspec: 0.66 seconds (Total time: 0.66 seconds)

```





Rows: 7	Cols: 7	Rebuild Board	Print Board			
#	#	#	#	#	#	#
#	#	#	.	#	#	#
#	#	#	\$	#	#	#
#	.	\$	@	\$	.	#
#	#	#	\$	#	#	#
#	#	#	.	#	#	#
#	#	#	#	#	#	#

ריצה 4:

פלט מnuX:

Trace Type: Counterexample

-> State: 1.1 <-

i\_person = 3

j\_person = 3

i\_box1 = 2

j\_box1 = 3

i\_box2 = 3

j\_box2 = 2

i\_box3 = 3

j\_box3 = 4

i\_box4 = 4

j\_box4 = 3

action\_person = no-action

boxes\_overlap = FALSE

box\_on\_wall = FALSE

man\_on\_box = FALSE

man\_on\_wall = FALSE

j\_box\_goal4 = 3

i\_box\_goal4 = 5

j\_box\_goal3 = 5

i\_box\_goal3 = 3

j\_box\_goal2 = 1

i\_box\_goal2 = 3

j\_box\_goal1 = 3

i\_box\_goal1 = 1

M = 7

N = 7

grid[0][0] = 1

grid[0][1] = 1

grid[0][2] = 1

grid[0][3] = 1

grid[0][4] = 1

grid[0][5] = 1

grid[0][6] = 1

grid[1][0] = 1

grid[1][1] = 1

grid[1][2] = 1

grid[1][3] = 0

grid[1][4] = 1

grid[1][5] = 1

grid[1][6] = 1

grid[2][0] = 1

grid[2][1] = 1

grid[2][2] = 1

grid[2][3] = 0

grid[2][4] = 1

grid[2][5] = 1

grid[2][6] = 1

grid[3][0] = 1

grid[3][1] = 0

grid[3][2] = 0

grid[3][3] = 0

grid[3][4] = 0

grid[3][5] = 0

grid[3][6] = 1

grid[4][0] = 1

grid[4][1] = 1

grid[4][2] = 1

grid[4][3] = 0

grid[4][4] = 1

grid[4][5] = 1

grid[4][6] = 1

grid[5][0] = 1

grid[5][1] = 1

grid[5][2] = 1

grid[5][3] = 0

grid[5][4] = 1

grid[5][5] = 1

grid[5][6] = 1

grid[6][0] = 1

grid[6][1] = 1

grid[6][2] = 1

grid[6][3] = 1

grid[6][4] = 1

grid[6][5] = 1

grid[6][6] = 1

-> State: 1.2 <-

i\_person = 4

i\_box4 = 5

action\_person = down

-> State: 1.3 <-

i\_person = 3

```

    action_person = up
-> State: 1.4 <-
    i_person = 2
    i_box1 = 1
-> State: 1.5 <-
    i_person = 3
    action_person = down
-> State: 1.6 <-
    j_person = 2
    j_box2 = 1
    action_person = left
-> State: 1.7 <-
    j_person = 3
    action_person = right
-> State: 1.8 <-
    j_person = 4
    j_box3 = 5
-> State: 1.9 <-
    j_person = 3
    action_person = left
nuXmv > elapse: 0.19 seconds, total: 0.19 seconds

```

תוצאות:

```
results in lurd format : DUUDLRR
```

```
runtime results SAT:
```

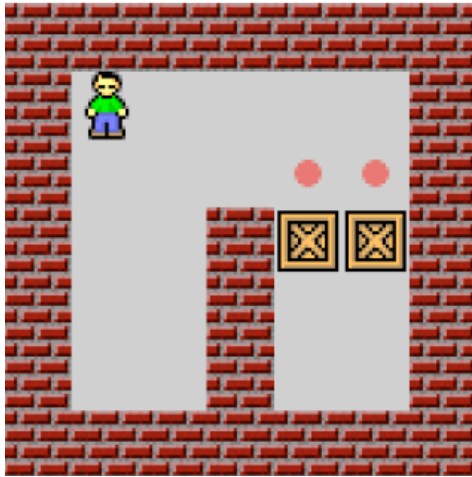
```

    Runtime after check_ltlspec_bmc -k 30: 0.19 seconds (Total time: 0.19 seconds)
Last checked bound: 7

```

```
runtime results BDD:
```

```
Runtime after check_ltlspec: 0.86 seconds (Total time: 0.86 seconds)
```



Rows: 7 Cols: 7 Rebuild Board Print Board

#	#	#	#	#	#	#
#	@	-	-	-	-	#
#	-	-	-	.	.	#
#	-	-	#	\$	\$	#
#	-	-	#	-	-	#
#	-	-	#	-	-	#
#	#	#	#	#	#	#

ריצה 5:

פלט nuXmv:

```

nuXmv > nuXmv > nuXmv > nuXmv > -- no counterexample found with bound 0
-- no counterexample found with bound 1
-- no counterexample found with bound 2
-- no counterexample found with bound 3
-- no counterexample found with bound 4
-- no counterexample found with bound 5
.....
-- no counterexample found with bound 40
nuXmv > elapse: 246.91 seconds, total: 246.91 seconds

```

תוצאות:

```

results in lurd format :
runtime results SAT:

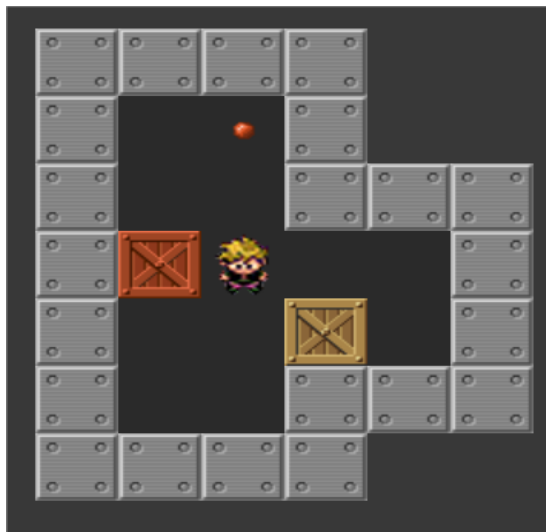
    Runtime after check_ltlspec_bmc -k 30: 246.91 seconds (Total time: 246.91 seconds)
Last checked bound: 40

runtime results BDD:

    Runtime after check_ltlspec: 0.09 seconds (Total time: 0.09 seconds)

```

ריצה 6:



Rows:	7	Cols:	6	Rebuild Board	Print Board
#	#	#	#	#	#
#	-	.	#	#	#
#	-	-	#	#	#
#	*	@	-	-	#
#	-	-	\$	-	#
#	-	-	#	#	#
#	#	#	#	#	#

nuXmv output

Trace Type: Counterexample

-> State: 1.1 <-

i\_person = 3

j\_person = 2

i\_box1 = 3

j\_box1 = 1

i\_box2 = 4

j\_box2 = 3

action\_person = no-action

boxes\_overlap = FALSE

box\_on\_wall = FALSE

man\_on\_box = FALSE

man\_on\_wall = FALSE

j\_box\_goal2 = 1

i\_box\_goal2 = 3

j\_box\_goal1 = 2

i\_box\_goal1 = 1

M = 6

N = 7

grid[0][0] = 1

grid[0][1] = 1

grid[0][2] = 1

grid[0][3] = 1

grid[0][4] = 1

grid[0][5] = 1

grid[1][0] = 1

grid[1][1] = 0

grid[1][2] = 0

grid[1][3] = 1

grid[1][4] = 1

grid[1][5] = 1

grid[2][0] = 1

grid[2][1] = 0

grid[2][2] = 0

grid[2][3] = 1

grid[2][4] = 1

grid[2][5] = 1

grid[3][0] = 1

grid[3][1] = 0

grid[3][2] = 0

grid[3][3] = 0

grid[3][4] = 0

grid[3][5] = 1

grid[4][0] = 1

grid[4][1] = 0

grid[4][2] = 0

grid[4][3] = 0

grid[4][4] = 0

grid[4][5] = 1

grid[5][0] = 1

grid[5][1] = 0

grid[5][2] = 0

grid[5][3] = 1

grid[5][4] = 1

grid[5][5] = 1

grid[6][0] = 1

grid[6][1] = 1

grid[6][2] = 1

grid[6][3] = 1

grid[6][4] = 1

grid[6][5] = 1

-> State: 1.2 <-

i\_person = 4

action\_person = down

-> State: 1.3 <-

j\_person = 1

action\_person = left

-> State: 1.4 <-

i\_person = 3

i\_box1 = 2

action\_person = up

-> State: 1.5 <-

j\_person = 2

action\_person = right

-> State: 1.6 <-

j\_person = 3

-> State: 1.7 <-

j\_person = 4

-> State: 1.8 <-

i\_person = 4



```
    action_person = down
-> State: 1.9 <-
    j_person = 3
    j_box2 = 2
    action_person = left
-> State: 1.10 <-
    i_person = 3
    action_person = up
-> State: 1.11 <-
    j_person = 2
    action_person = left
-> State: 1.12 <-
    j_person = 1
-> State: 1.13 <-
    i_person = 4
    action_person = down
-> State: 1.14 <-
    i_person = 5
-> State: 1.15 <-
    j_person = 2
    action_person = right
-> State: 1.16 <-
    i_person = 4
    i_box2 = 3
    action_person = up
-> State: 1.17 <-
    j_person = 1
    action_person = left
-> State: 1.18 <-
    i_person = 3
    action_person = up
```

-> State: 1.19 <-  
j\_person = 2  
j\_box2 = 3  
action\_person = right  
-> State: 1.20 <-  
i\_person = 2  
action\_person = up  
-> State: 1.21 <-  
i\_person = 1  
-> State: 1.22 <-  
j\_person = 1  
action\_person = left  
-> State: 1.23 <-  
i\_person = 2  
i\_box1 = 3  
action\_person = down  
-> State: 1.24 <-  
j\_person = 2  
action\_person = right  
-> State: 1.25 <-  
i\_person = 3  
action\_person = down  
-> State: 1.26 <-  
i\_person = 4  
-> State: 1.27 <-  
j\_person = 3  
action\_person = right  
-> State: 1.28 <-  
j\_person = 4  
-> State: 1.29 <-  
i\_person = 3

```

    action_person = up
-> State: 1.30 <-
    j_person = 3
    j_box2 = 2
    action_person = left
-> State: 1.31 <-
    i_person = 4
    action_person = down
-> State: 1.32 <-
    j_person = 2
    action_person = left
-> State: 1.33 <-
    i_person = 3
    i_box2 = 2
    action_person = up
-> State: 1.34 <-
    i_person = 2
    i_box2 = 1
-> State: 1.35 <-
    j_person = 1
    action_person = left
nuXmv > elapse: 43.16 seconds, total: 43.16 seconds

```

תוצאות:

```

]results in lurd format : DLURRRDLULLDDRULURUULDRDDRRULDLUU
runtime results SAT:

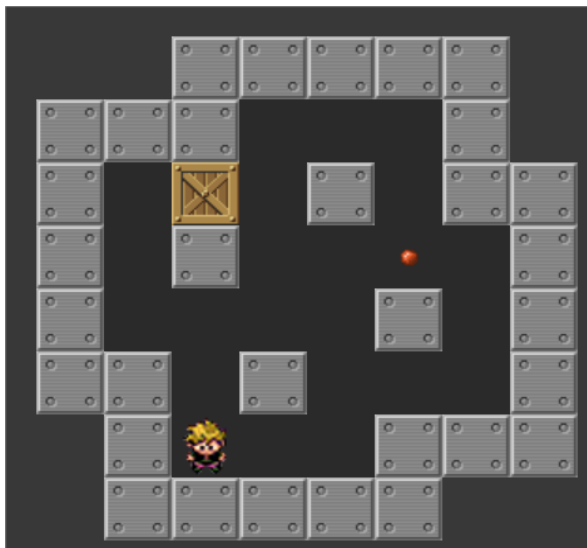
    Runtime after check_ltlspec_bmc -k 30: 43.16 seconds (Total time: 43.16 seconds)
Last checked bound: 33

    runtime results BDD:

    Runtime after check_ltlspec: 0.18 seconds (Total time: 0.18 seconds)

```

ריצה 7:



Rows:	8	Cols:	8	Rebuild Board	Print Board		
#	#	#	#	#	#	#	#
#	#	#	-	-	-	#	#
#	-	\$	-	#	-	#	#
#	-	#	-	-	.	-	#
#	-	-	-	-	#	-	#
#	#	-	#	-	-	-	#
#	#	@	-	-	-	-	#
#	#	#	#	#	#	#	#

:Output

Trace Type: Counterexample

-> State: 1.1 <-

i\_person = 6

j\_person = 2

i\_box1 = 2

j\_box1 = 2

action\_person = no-action

boxes\_overlap = FALSE

box\_on\_wall = FALSE

man\_on\_box = FALSE

man\_on\_wall = FALSE

j\_box\_goal1 = 5

i\_box\_goal1 = 3

M = 8

N = 8

grid[0][0] = 1

grid[0][1] = 1

grid[0][2] = 1

```
grid[0][3] = 1
grid[0][4] = 1
grid[0][5] = 1
grid[0][6] = 1
grid[0][7] = 1
grid[1][0] = 1
grid[1][1] = 1
grid[1][2] = 1
grid[1][3] = 0
grid[1][4] = 0
grid[1][5] = 0
grid[1][6] = 1
grid[1][7] = 1
grid[2][0] = 1
grid[2][1] = 0
grid[2][2] = 0
grid[2][3] = 0
grid[2][4] = 1
grid[2][5] = 0
grid[2][6] = 1
grid[2][7] = 1
grid[3][0] = 1
grid[3][1] = 0
grid[3][2] = 1
grid[3][3] = 0
grid[3][4] = 0
grid[3][5] = 0
grid[3][6] = 0
grid[3][7] = 1
grid[4][0] = 1
grid[4][1] = 0
```

grid[4][2] = 0

grid[4][3] = 0

grid[4][4] = 0

grid[4][5] = 1

grid[4][6] = 0

grid[4][7] = 1

grid[5][0] = 1

grid[5][1] = 1

grid[5][2] = 0

grid[5][3] = 1

grid[5][4] = 0

grid[5][5] = 0

grid[5][6] = 0

grid[5][7] = 1

grid[6][0] = 1

grid[6][1] = 1

grid[6][2] = 0

grid[6][3] = 0

grid[6][4] = 0

grid[6][5] = 0

grid[6][6] = 0

grid[6][7] = 1

grid[7][0] = 1

grid[7][1] = 1

grid[7][2] = 1

grid[7][3] = 1

grid[7][4] = 1

grid[7][5] = 1

grid[7][6] = 1

grid[7][7] = 1

-> State: 1.2 <-

```
i_person = 5
action_person = up
-> State: 1.3 <-
i_person = 4
-> State: 1.4 <-
j_person = 1
action_person = left
-> State: 1.5 <-
i_person = 3
action_person = up
-> State: 1.6 <-
i_person = 2
-> State: 1.7 <-
j_person = 2
j_box1 = 3
action_person = right
-> State: 1.8 <-
j_person = 1
action_person = left
-> State: 1.9 <-
i_person = 3
action_person = down
-> State: 1.10 <-
i_person = 4
-> State: 1.11 <-
j_person = 2
action_person = right
-> State: 1.12 <-
j_person = 3
-> State: 1.13 <-
j_person = 4
```

-> State: 1.14 <-

i\_person = 3

action\_person = up

-> State: 1.15 <-

j\_person = 5

action\_person = right

-> State: 1.16 <-

i\_person = 2

action\_person = up

-> State: 1.17 <-

i\_person = 1

-> State: 1.18 <-

j\_person = 4

action\_person = left

-> State: 1.19 <-

j\_person = 3

-> State: 1.20 <-

i\_person = 2

i\_box1 = 3

action\_person = down

-> State: 1.21 <-

i\_person = 3

i\_box1 = 4

-> State: 1.22 <-

i\_person = 2

action\_person = up

-> State: 1.23 <-

j\_person = 2

action\_person = left

-> State: 1.24 <-

j\_person = 1



```
-> State: 1.25 <-  
  i_person = 3  
  action_person = down  
-> State: 1.26 <-  
  i_person = 4  
-> State: 1.27 <-  
  j_person = 2  
  action_person = right  
-> State: 1.28 <-  
  j_person = 3  
  j_box1 = 4  
-> State: 1.29 <-  
  j_person = 2  
  action_person = left  
-> State: 1.30 <-  
  i_person = 5  
  action_person = down  
-> State: 1.31 <-  
  i_person = 6  
-> State: 1.32 <-  
  j_person = 3  
  action_person = right  
-> State: 1.33 <-  
  j_person = 4  
-> State: 1.34 <-  
  i_person = 5  
  action_person = up  
-> State: 1.35 <-  
  i_person = 4  
  i_box1 = 3  
-> State: 1.36 <-
```

```

j_person = 3
action_person = left
-> State: 1.37 <-
i_person = 3
action_person = up
-> State: 1.38 <-
j_person = 4
j_box1 = 5
action_person = right
-> State: 1.39 <-
j_person = 3
action_person = left
nuXmv > elapse: 18.38 seconds, total: 18.38 seconds

```

תוצאות:

```

results in lurd format : UULUURLDDRRRRURUULLDDULLDDRRLDDRRLUR
runtime results SAT:

Runtime after check_ltlspec_bmc -k 30: 18.38 seconds (Total time: 18.38 seconds)
Last checked bound: 37

runtime results BDD:

Runtime after check_ltlspec: 0.07 seconds (Total time: 0.07 seconds)

```

מסקנה:

בריצות ארוכות / כאלה ללא פתרון BDD יותר טוב מ SAT  
בריצות קצרות ומהירות עם מס' צעדים קצר SAT טוב יותר מ BDD

## Part 4

1. Break the problem into sub-problems by solving the boards iteratively. For example, solve for one box at a time. Indicate the temporal logic formulae used for each iteration.
2. Indicate runtime for each iteration, as well as the total number of iterations needed for a given board.
3. Test your iterative solution on larger more complex Sokoban boards.

נפתור איטרטיבית באופן הבא:

1. נריץ את המודל עם SPEC שתואם להצלחה בקופסא אחת בלבד
2. במידה וקיבלנו תוצאה, נזיז את השחקן בהתאם לתוצאה ונסדר
3. נקבל לוח חדש ניקח אותו ונגדיר שהוא הלוח
4. נחזור על צעד אחד עם הלוח החדש אבל עם 2 קופסות, וכן הלאה עד שנגיע לכל הקופסאות בתוצאה.

עבור כל הלוחות השתמשנו בSAT למקסימום 30 צעדים, השתמשנו בSAT מכיוון שכאשר היה מדובר במספר רב של צעדים הוא עבד יותר טוב מאשר BDD.  
הרצנו את הפקודות הבאות:

```
Nuxmv -int "model_filename_{iteration}".smv
Read_model -i "model_filename_{iteration}".smv
Go_bmc
Check_ItlSpec_bmc -k 30
```

לכל איטרציה מודל שונה לפי הפעולות להאיטרציה הקודמת ולכן ה-{iteration}  
נראה כיצד השיטה האיטרטיבית עובדת על הלוחות הבאים:  
התנאי שלנו בסוף השתנה בהתאמה למספר האיטרציה.

בכל איטרציה אנחנו לקחנו לכל תת קבוצה אפשרית בגודל של מספר הקופסאות התואם לאיטרציה, את כל הפרמוטציות האפשריות בהתאם לתת קבוצה הזאת של BOX-GOALS.

כלומר בהנתן {boxn..., 3box, 2box, 1box} ובהתאמה {goaln..., 3goal, 2goal, 1goal}  
באיטרציה 1 ניקח את כל תתי הקבוצות בגודל 1:

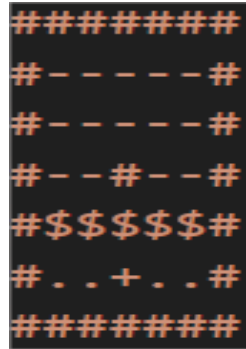
{goaln..., {3goal}, {2goal}, {1goal}} ונתאים אותן ל{boxn..., 3box, 2box, 1box} כך שלפחות אחת מהקופסאות שווה לGOAL.

באיטרציה 2 ניקח את כל תתי הקבוצות בגודל 2:

{goal1, goal2}, {goal1, goal3}, ..., {goaln-1, goaln}

ונתאים אותן ל{boxn..., 3box, 2box, 1box} כך שלפחות אחת מהקופסאות שווה לGOAL.  
וכן.

ריצה ופליטים עבור חלק 4:



The Runtime for iteration 1:

Runtime after check\_ltlspec\_bmc -k 30: 0.41 seconds (Total time: 0.41 seconds)

The Runtime for iteration 2:

Runtime after check\_ltlspec\_bmc -k 30: 0.78 seconds (Total time: 0.78 seconds)

The Runtime for iteration 3:

Runtime after check\_ltlspec\_bmc -k 30: 1.92 seconds (Total time: 1.92 seconds)

The Runtime for iteration 4:

Runtime after check\_ltlspec\_bmc -k 30: 2.11 seconds (Total time: 2.11 seconds)

The Runtime for iteration 5:

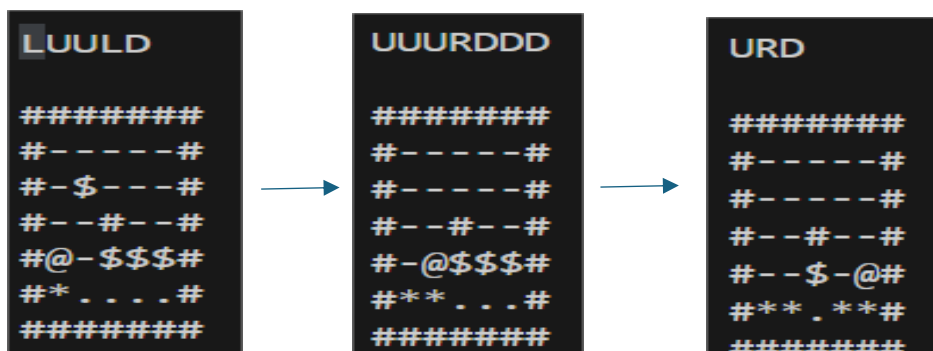
stop

Formula for iteration 1:

LTLSPEC G(!next(man\_on\_box) & !next(man\_on\_wall) & !next(box\_on\_wall) & !next(boxes\_overlap)) & ((i\_box1 = 5) & (j\_box1 = 1)) | ((i\_box1 = 5) & (j\_box1 = 2)) | ((i\_box1 = 5) & (j\_box1 = 3)) | ((i\_box1 = 5) & (j\_box1 = 4)) | ((i\_box1 = 5) & (j\_box1 = 5)) | ((i\_box2 = 5) & (j\_box2 = 1)) | ((i\_box2 = 5) & (j\_box2 = 2)) | ((i\_box2 = 5) & (j\_box2 = 3)) | ((i\_box2 = 5) & (j\_box2 = 4)) | ((i\_box2 = 5) & (j\_box2 = 5)) | ((i\_box3 = 5) & (j\_box3 = 1)) | ((i\_box3 = 5) & (j\_box3 = 2)) | ((i\_box3 = 5) & (j\_box3 = 3)) | ((i\_box3 = 5) & (j\_box3 = 4)) | ((i\_box3 = 5) & (j\_box3 = 5)) | ((i\_box4 = 5) & (j\_box4 = 1)) | ((i\_box4 = 5) & (j\_box4 = 2)) | ((i\_box4 = 5) & (j\_box4 = 3)) | ((i\_box4 = 5) & (j\_box4 = 4)) | ((i\_box4 = 5) & (j\_box4 = 5)) | ((i\_box5 = 5) & (j\_box5 = 1)) | ((i\_box5 = 5) & (j\_box5 = 2)) | ((i\_box5 = 5) & (j\_box5 = 3)) | ((i\_box5 = 5) & (j\_box5 = 4)) | ((i\_box5 = 5) & (j\_box5 = 5));

עבור איטרציות 2 ואלך, התנאים ארוכים מאוד בכדי לשים בדוח. מצורפות תוצאות למודלים בGITHUB.

כאן השחקן הגיע עד 4 קופסאות מכיוון שבהגעה ל2 קופסאות אחת מהקופסאות נתקעה בפינה. סידור הקופסאות:



### השוואה להרצת לוח בשיטה לא איטרטיבית:

אחרי ניסיון של להריץ את המודל עבור 5 קופסאות ישירות חיכינו שעה והמודל לא נתן פתרון עם זאת כאן יש סידור של 4 קופסאות.



#### The formula for iteration 1:

```
LTLSPEC G!(!next(man_on_box) & !next(man_on_wall) & !next(box_on_wall) &
!next(boxes_overlap)) & ((i_box1 = 3) & (j_box1 = 1)) | ((i_box1 = 3) & (j_box1 = 4)) |
((i_box2 = 3) & (j_box2 = 1)) | ((i_box2 = 3) & (j_box2 = 4)));
```

#### The formula for iteration 2:

```
LTLSPEC G!(!next(man_on_box) & !next(man_on_wall) & !next(box_on_wall) &
!next(boxes_overlap)) & ((i_box1 = 3) & (j_box1 = 1) & (i_box2 = 3) & (j_box2 = 4)) | ((i_box1
= 3) & (j_box1 = 4) & (i_box2 = 3) & (j_box2 = 1)));
```

#### Runtime iteration 1:

Runtime after check\_ltlspec\_bmc -k 30: 0.14 seconds (Total time: 0.14 seconds)  
Last checked bound: 7

#### Runtime iteration 2:

Runtime after check\_ltlspec\_bmc -k 30: 23.36 seconds (Total time: 23.36 seconds)  
Last checked bound: 23

### השוואה להרצת לוח בשיטה לא איטרטיבית:

Runtime after check\_ltlspec\_bmc -k 30: 32.12 seconds (Total time: 32.12 seconds)  
Last checked bound: 23

כאן השיטה האיטרטיבית עבדה יותר מהר  $32.12 > 23.36 + 0.14$

```
#####
#-----#####
#- -#- - - .###
#-$- - - -#####
#- -@#- - -#####
####- - - -*####
#####-$- - -#
#####- - -#
#####. - -#
#####
```

The formula for iteration 1:

LTLSPEC G(!next(man\_on\_box) & !next(man\_on\_wall) & !next(box\_on\_wall) & !next(boxes\_overlap)) & ((i\_box1 = 2) & (j\_box1 = 7)) | ((i\_box1 = 5) & (j\_box1 = 7)) | ((i\_box1 = 8) & (j\_box1 = 7)) | ((i\_box2 = 2) & (j\_box2 = 7)) | ((i\_box2 = 5) & (j\_box2 = 7)) | ((i\_box2 = 8) & (j\_box2 = 7)) | ((i\_box3 = 2) & (j\_box3 = 7)) | ((i\_box3 = 5) & (j\_box3 = 7)) | ((i\_box3 = 8) & (j\_box3 = 7));

The formula for iteration 2:

LTLSPEC G(!next(man\_on\_box) & !next(man\_on\_wall) & !next(box\_on\_wall) & !next(boxes\_overlap)) & ((i\_box1 = 2) & (j\_box1 = 7) & (i\_box2 = 5) & (j\_box2 = 7)) | ((i\_box1 = 2) & (j\_box1 = 7) & (i\_box2 = 8) & (j\_box2 = 7)) | ((i\_box1 = 5) & (j\_box1 = 7) & (i\_box2 = 2) & (j\_box2 = 7)) | ((i\_box1 = 5) & (j\_box1 = 7) & (i\_box2 = 8) & (j\_box2 = 7)) | ((i\_box1 = 8) & (j\_box1 = 7) & (i\_box2 = 2) & (j\_box2 = 7)) | ((i\_box1 = 8) & (j\_box1 = 7) & (i\_box2 = 5) & (j\_box2 = 7)) | ((i\_box1 = 2) & (j\_box1 = 7) & (i\_box3 = 5) & (j\_box3 = 7)) | ((i\_box1 = 2) & (j\_box1 = 7) & (i\_box3 = 8) & (j\_box3 = 7)) | ((i\_box1 = 5) & (j\_box1 = 7) & (i\_box3 = 2) & (j\_box3 = 7)) | ((i\_box1 = 5) & (j\_box1 = 7) & (i\_box3 = 8) & (j\_box3 = 7)) | ((i\_box1 = 8) & (j\_box1 = 7) & (i\_box3 = 2) & (j\_box3 = 7)) | ((i\_box1 = 8) & (j\_box1 = 7) & (i\_box3 = 5) & (j\_box3 = 7)) | ((i\_box2 = 2) & (j\_box2 = 7) & (i\_box3 = 5) & (j\_box3 = 7)) | ((i\_box2 = 2) & (j\_box2 = 7) & (i\_box3 = 8) & (j\_box3 = 7)) | ((i\_box2 = 5) & (j\_box2 = 7) & (i\_box3 = 2) & (j\_box3 = 7)) | ((i\_box2 = 5) & (j\_box2 = 7) & (i\_box3 = 8) & (j\_box3 = 7)) | ((i\_box2 = 8) & (j\_box2 = 7) & (i\_box3 = 2) & (j\_box3 = 7)) | ((i\_box2 = 8) & (j\_box2 = 7) & (i\_box3 = 5) & (j\_box3 = 7));

The formula for iteration 3:

LTLSPEC G(!next(man\_on\_box) & !next(man\_on\_wall) & !next(box\_on\_wall) & !next(boxes\_overlap)) & ((i\_box1 = 2) & (j\_box1 = 7) & (i\_box2 = 5) & (j\_box2 = 7) & (i\_box3 = 8) & (j\_box3 = 7)) | ((i\_box1 = 2) & (j\_box1 = 7) & (i\_box2 = 8) & (j\_box2 = 7) & (i\_box3 = 5) & (j\_box3 = 7)) | ((i\_box1 = 5) & (j\_box1 = 7) & (i\_box2 = 2) & (j\_box2 = 7) & (i\_box3 = 8) & (j\_box3 = 7)) | ((i\_box1 = 5) & (j\_box1 = 7) & (i\_box2 = 8) & (j\_box2 = 7) & (i\_box3 = 2) & (j\_box3 = 7)) | ((i\_box1 = 8) & (j\_box1 = 7) & (i\_box2 = 2) & (j\_box2 = 7) & (i\_box3 = 5) & (j\_box3 = 7)) | ((i\_box1 = 8) & (j\_box1 = 7) & (i\_box2 = 5) & (j\_box2 = 7) & (i\_box3 = 2) & (j\_box3 = 7));

Runtime iteration 1:

Runtime after check\_ltlspec\_bmc -k 30: 0.11 seconds (Total time: 0.11 seconds)

Last checked bound: 0

Runtime iteration 2:

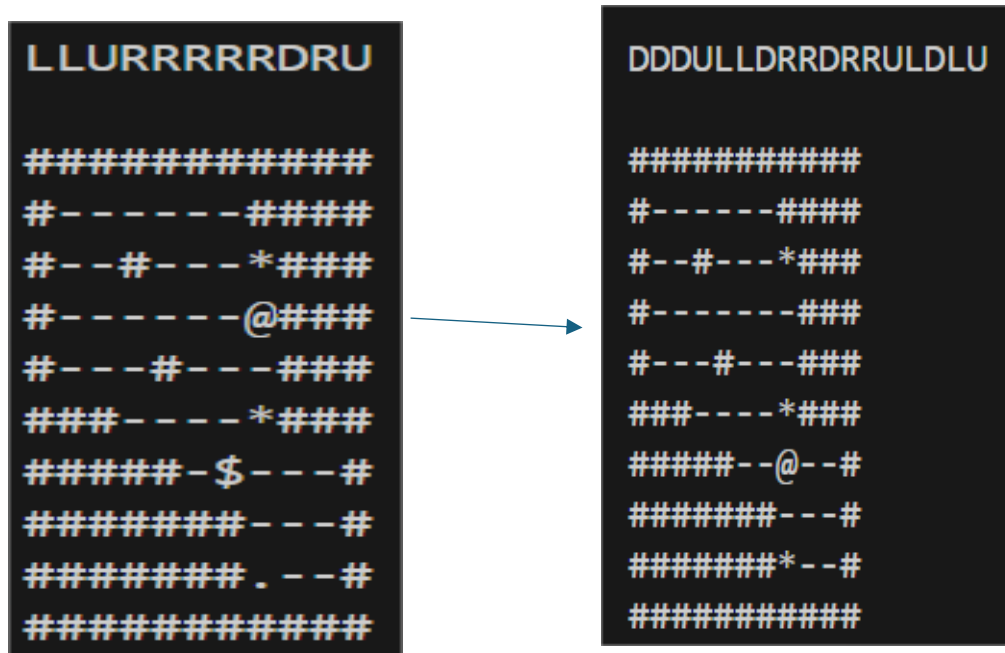
Runtime after check\_ltlspec\_bmc -k 30: 1.44 seconds (Total time: 1.44 seconds)

Last checked bound: 11

Runtime iteration 3:

Runtime after check\_ltlspec\_bmc -k 30: 5.56 seconds (Total time: 5.56 seconds)

Last checked bound: 17



השוואה להרצת לוח בשיטה לא איטרטיבית:

אחרי הרצה בשיטה הלא איטרטיבית קיבלנו את התוצאות הבאות:

results in lurd format : LLURRRRRDRUDDDULLDRRDRRULDLU

runtime results SAT:

Runtime after check\_ltlspec\_bmc -k 30: 365.16 seconds (Total time: 365.16 seconds)

Last checked bound: 28

ניתן לראות בבירור שכאן הריצה הלא איטרטיבית עובדת בהרבה פחות טוב.