Reg. No.:

Name



TERM END EXAMINATIONS (TEE) – August- September 2021

Programme	:B.Tech	Semester	: Interim 2021-22
Course Name	: Applied Linear Algebra	Course Code	: MAT3002
Faculty Name	: Dr. Md Abu Talhamainuddin Ansary	Slot / Class No	: A11/ BL2021225000139
Time	: 1½ hours	Max. Marks	: 50

Answer ALL the Questions

Q. No. Question Description Marks

PART - A (30 Marks)

1 (a) Find the *LU* decomposition of

$$A = \begin{pmatrix} 4 & 1 & 1 \\ 1 & 4 & -2 \\ 3 & 2 & -4 \end{pmatrix}$$

Choose $U_{11} = U_{22} = U_{33} = 1$

OR

(b) Consider two bases of R^3 as

$$B = \{(1,0,1), (0,1,0), (-1,0,1)\}$$

$$C = \{(1,1,1), (0,1,1), (0,0,1)\}$$

Find the transition matrix from B coordinate to C coordinate.

2 (a) Consider two bases of R^2 as

$$B = \{(1,0), (0,1)\}\$$

$$C = \{(1,1), (-1,1)\}\$$
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Suppose $T: \mathbb{R}^2 \to \mathbb{R}^2$ be a linear transformation defined by

$$T(x, y) = (3x - 4y, -x + 2y)$$

Show that the matrix representation of T with respect to B (A_{BB}) is similar to the matrix representation of T with respect to C (A_{CC}).

OR

(b) Consider the vector space P_n (set of all polynomials of degree $\leq n$). Suppose $p, q \in P_n$, where

$$p = a_n x^n + a_{n-1} x^{n-1} + \dots + a_1 x + a_0$$

$$q = b_n x^n + b_{n-1} x^{n-1} + \dots + b_1 x + b_0$$

An inner product in P_n is defined by

$$\langle p,q \rangle = a_n b_n + a_{n-1} b_{n-1} + \dots + a_1 b_1 + a_0 b_0$$

Show that $B = \{x^2 + 2x + 2, 2x^2 - 2x + 1, 2x^2 + x - 2\}$ forms an orthogonal basis of P_2 .

Find the coordinate of $p=2x^2-x+1$ with respect to B.

3 (a) Consider the subspace of R^3 defined as

$$W = \{(x, y, z) \in R^3 | x + y - z = 0\}$$

Express x = (4, 3, 2) as x = p + q, where $p \in W$, and $q \in W^{\perp}$ (where W^{\perp} is the orthogonal complement of W).

OR

(b) Find the QR-decomposition of

$$A = \begin{bmatrix} 2 & 1 \\ 1 & 1 \\ 2 & 1 \end{bmatrix}$$
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PART - B (20 Marks)

Consider vector space C[-1,1] (set of all real valued continuous functions in [-1,1]). Justify whether

$$W = \left\{ f \in C[-1,1] \middle| \int_{-1}^{1} f(x) dx = 0 \right\}$$

forms a subspace of C[-1,1] or not.

- (ii) Consider vector space $M_{3\times3}$ (set of all 3×3 matrices). Justify whether $W=\{A\in M_{3\times3}|\det(A)=0\}$ forms a subspace of $M_{3\times3}$ or not.
- 5 Using Gram-Schmidt method convert

$$B = \{(1, 1, 0), (1, 0, 1), (0, 1, 1)\}$$

to an orthogonal basis of R^3 .

Find the coordinate of (2, 4, 6) with respect to the orthogonal basis.