

2 zad. 3.7,

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$$\phi(r) = \frac{1}{4\pi\epsilon_0} \frac{e_0}{r}$$

$$\rho(r) = -\frac{e_0}{\pi a_0^3} e^{-\frac{2r}{a_0}}$$

$$W = \frac{1}{2} \int_0^\infty \int_0^\pi \int_0^{2\pi} \frac{-e_0}{\pi a_0^3} e^{-\frac{2r}{a_0}} \cdot \frac{1}{4\pi\epsilon_0} \frac{e_0}{r} r^2 \sin\theta d\varphi d\theta dr =$$

$$= \frac{-e_0^2}{2\pi a_0^3 \epsilon_0} \int_0^\infty r e^{-\frac{2r}{a_0}} dr = \frac{-e_0^2}{8\pi\epsilon_0 a} \approx -2,17 \cdot 10^{-18} \text{ J} \approx -13,6 \text{ eV}$$

$$\downarrow - \left[r \frac{a_0}{2} e^{-\frac{2r}{a_0}} + \frac{a_0^2}{4} e^{-\frac{2r}{a_0}} \right]_0^\infty =$$

$$\begin{array}{l} + r \rightarrow e^{-\frac{2r}{a_0}} \\ - 1 \rightarrow -\frac{a_0}{2} e^{-\frac{2r}{a_0}} \\ + 0 \rightarrow \frac{a_0^2}{4} e^{-\frac{2r}{a_0}} \end{array}$$

$$= \frac{a_0^2}{4}$$