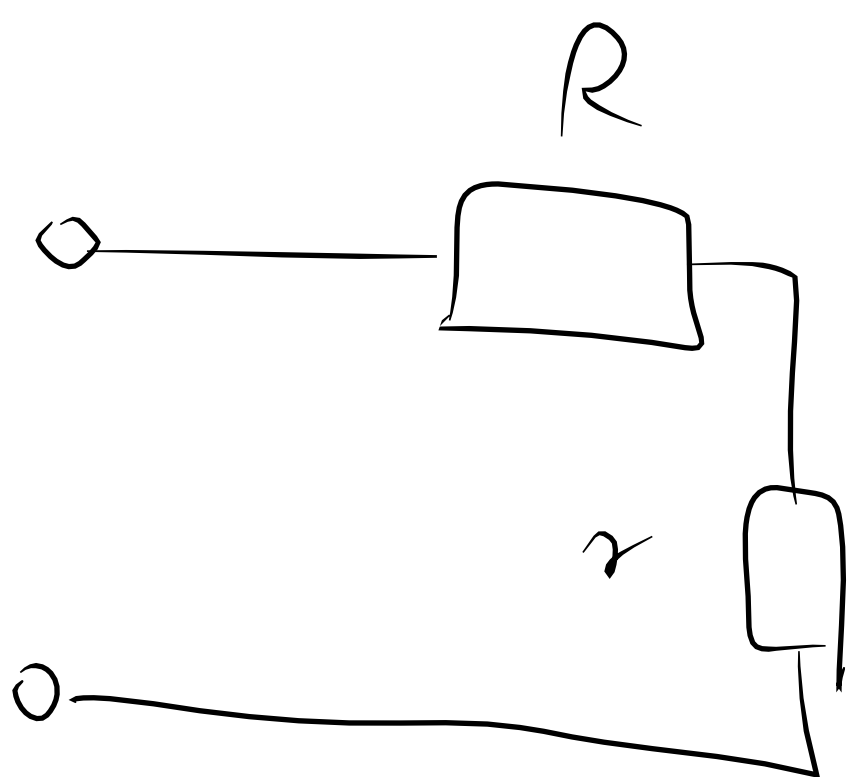
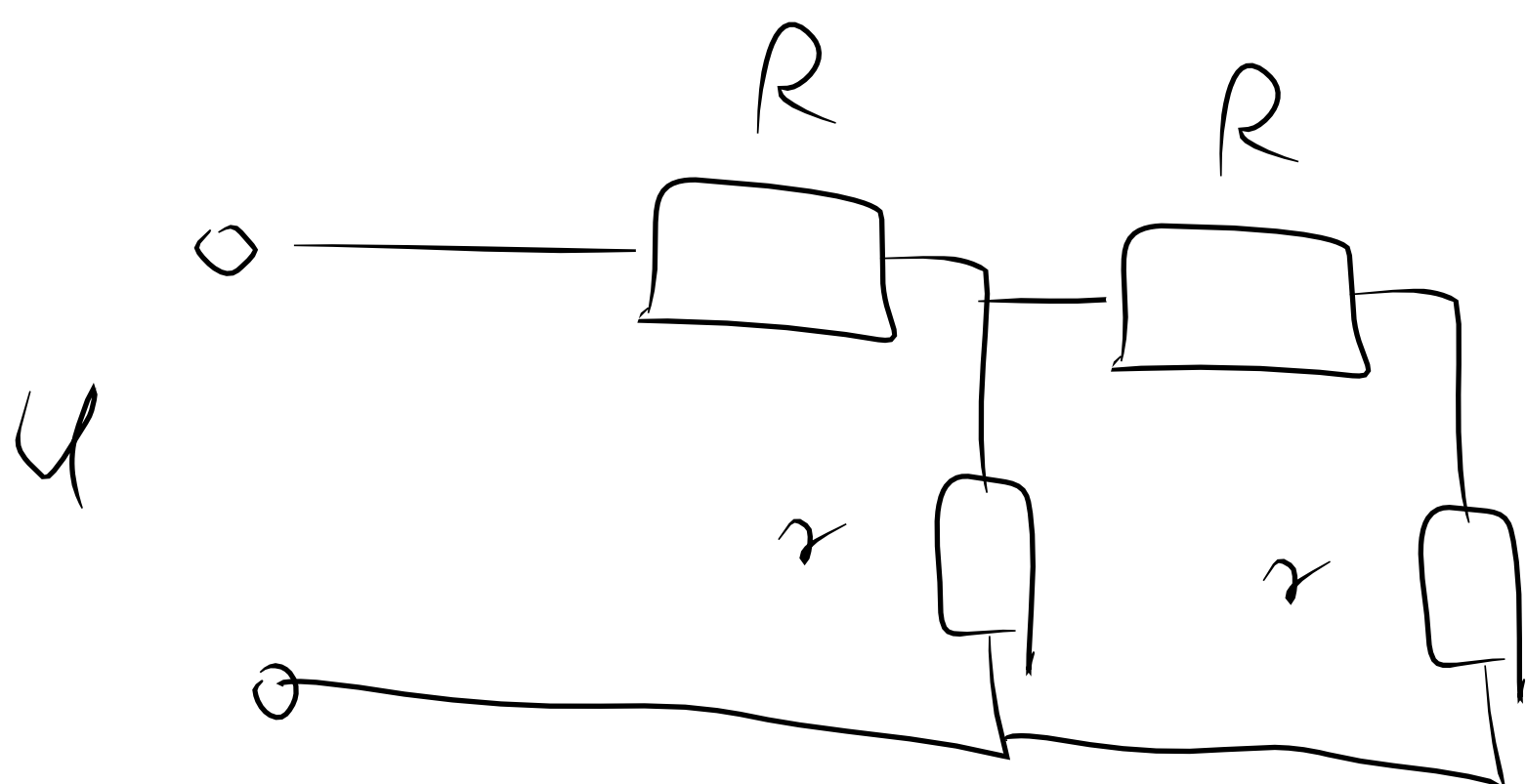


$$n=1$$



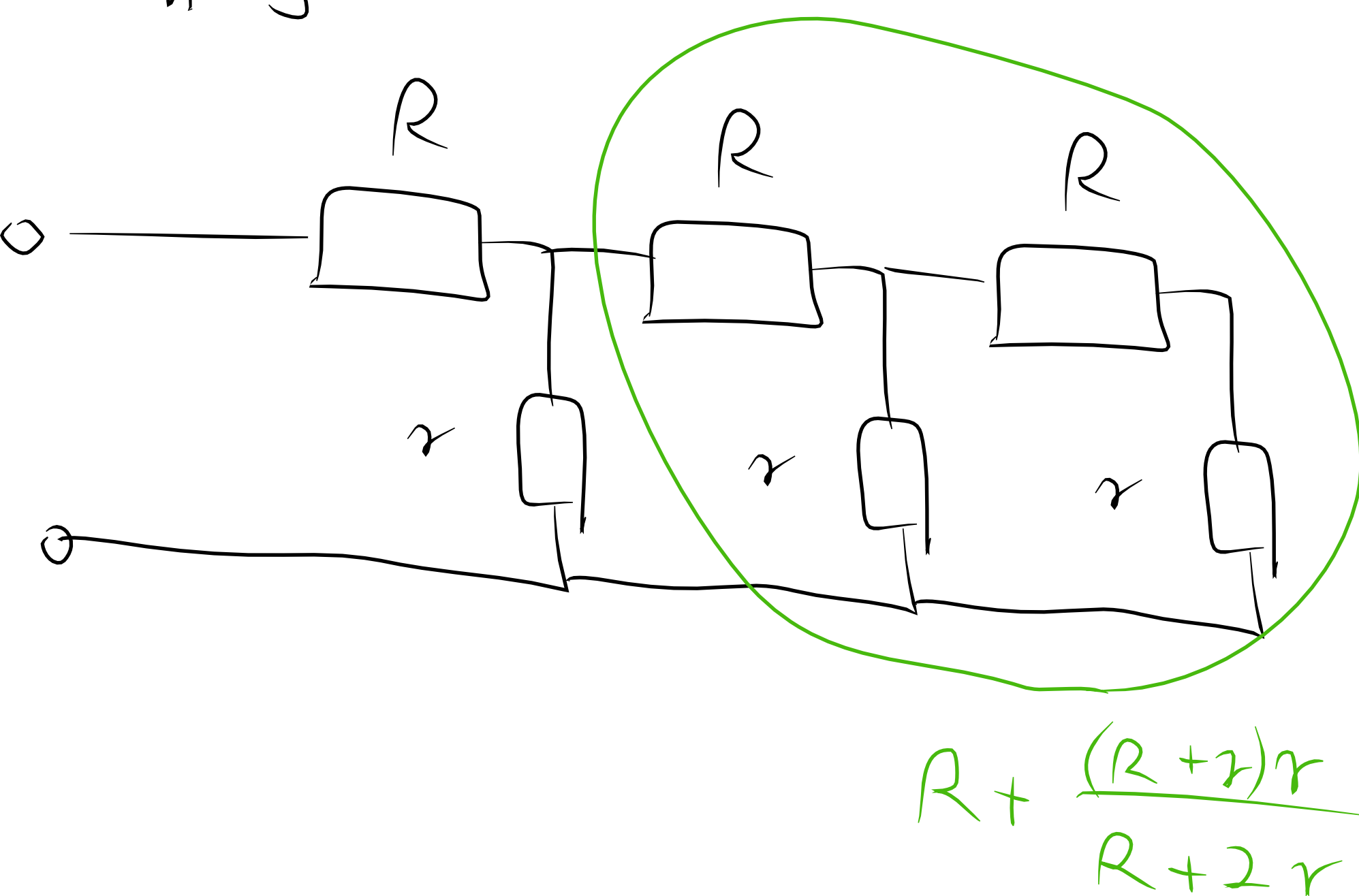
$$R_1 = R + r$$

$$n=2$$



$$R_2 = R + \frac{(R+r)r}{R+r+r}$$

$$n=3$$



$$R_3 = R + \frac{r \left( R + \frac{(R+r)r}{R+2r} \right)}{r + R + \frac{(R+r)r}{R+2r}}$$

$$R_{n+1} = R + \frac{r R_n}{r + R_n}$$

$$n \rightarrow \infty$$

$$R_\infty = R + \frac{r R_\infty}{r + R_\infty}$$

$$\cancel{r R_\infty} + R_\infty^2 = R r + R R_\infty + \cancel{r R_\infty}$$

$$R_\infty^2 - R R_\infty - R r = 0$$

$$R_\infty > 0$$

$$R_\infty = \frac{R + \sqrt{R^2 + 4 R r}}{2}$$

$$\text{dla } r=R$$

$$R_\infty = \frac{1+\sqrt{5}}{2} R$$