



$$\vec{M} = M \vec{e}_z \quad \text{dla } r \leq R$$

$$\vec{j}_{\text{surf}} = 0 \Rightarrow \vec{\nabla} \times \vec{H} = 0$$

$$\vec{j}_{\text{surf}} = \vec{\nabla} \times \vec{M}$$

$$\vec{H} = -\vec{\nabla} \Phi_m$$

$$\vec{B} = \mu_0 (\vec{H} + \vec{M}) / \vec{\nabla} \cdot$$

$$0 = \mu_0 (\vec{\nabla} H + \vec{\nabla} M)$$

$$\vec{\nabla} \cdot \vec{H} = -\vec{\nabla} \cdot \vec{M}$$

$$-\vec{\nabla} H = \vec{\nabla} (\vec{\nabla} \Phi_m) = \Delta \Phi_m$$

$$-\vec{\nabla} \cdot \vec{M} = -j_m$$

$$\Delta \Phi_m = -j_m \Rightarrow \Phi_m = \frac{1}{4\pi} \int_V \frac{j_m d^3 r}{|\vec{r} - \vec{r}'|}$$

$$\vec{M} = M \begin{bmatrix} \sin \theta \\ 0 \\ \cos \theta \end{bmatrix}$$

$$\vec{r} = \begin{bmatrix} \sin \theta' \cos \varphi \\ \sin \theta' \sin \varphi \\ \cos \theta' \end{bmatrix}$$

$$\vec{M} \cdot \vec{r} = M (\sin \theta \cos \varphi \sin \theta' + \cos \theta \cos \theta')$$

$$\Phi_m = \frac{1}{4\pi} \int_{S(R)} \frac{\sigma_m}{|\vec{r} - \vec{r}'|} dS' = \frac{MR^2}{2} \int_0^\pi \frac{\cos \theta \cos \theta' \sin \theta'}{|\vec{r} - \vec{r}'|} d\theta = \begin{cases} \frac{M}{3} r \cos \theta & r < R \\ \frac{M}{3} \frac{R^3}{r^2} \cos \theta & r > R \end{cases}$$

$$H = -\vec{\nabla} \Phi_m$$

$$r < R$$

$$\vec{H} = -\vec{\nabla} \left( \frac{M}{3} z \right) = \begin{bmatrix} 0 \\ 0 \\ -\frac{M}{3} \end{bmatrix}$$

$$r > R$$

$$\vec{H} = -\vec{\nabla} \left( \frac{MR^3}{3r^2} \cos \theta \right) = -\frac{R^3}{3} \left( \vec{\nabla} \left( \vec{M} \cdot \frac{\vec{r}}{r^3} \right) \right)$$

$$\vec{B} = \mu_0 (\vec{H} + \vec{M})$$

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$$\sigma_m = -M_\perp^+ + M_\perp^- = M_\perp = \vec{M} \cdot \vec{n}$$

