



$$\vec{B} = \frac{\mu_0 I}{4\pi} \cdot \frac{d\vec{l} \times (\vec{r} - \vec{r}')}{|\vec{r} - \vec{r}'|^3}$$

$$d\vec{l} = dz \hat{e}_z = x \sec^2 \theta d\theta \hat{e}_z$$

$$z = x \tan \theta$$

$$dz = x \sec^2 \theta d\theta$$

$$\vec{r} - \vec{r}' = -x \tan \theta \hat{e}_z + x \hat{e}_x$$

$$d\vec{l} \times (\vec{r} - \vec{r}') = \begin{bmatrix} 0 \\ 0 \\ x \sec^2 \theta d\theta \end{bmatrix} \times \begin{bmatrix} x \\ 0 \\ x \tan \theta \end{bmatrix} = \begin{bmatrix} 0 \\ x^2 \sec^2 \theta d\theta \\ 0 \end{bmatrix}$$

$$d\vec{B} = \frac{\mu_0 I}{4\pi} \cdot \frac{x^2 \sec^2 \theta d\theta}{(x \sqrt{1 + \tan^2 \theta})^3} \hat{e}_y = \frac{\mu_0 I}{4\pi} \cdot \frac{d\theta}{x \sec \theta} \hat{e}_y = \frac{\mu_0 I}{4\pi x} \cos \theta d\theta \hat{e}_y$$

$$\vec{B} = \frac{\mu_0 I}{4\pi x} \int_{\theta_1}^{\theta_2} \cos \theta d\theta \hat{e}_y = \frac{\mu_0 I}{4\pi x} (\sin \theta_2 - \sin \theta_1) \hat{e}_y$$

$$\theta_1 \rightarrow -\frac{\pi}{2}$$

$$\theta_2 \rightarrow \frac{\pi}{2}$$

$$\vec{B} = \frac{\mu_0}{2\pi x} \hat{e}_y$$