



$$I_2 = I_1 + I_3$$

$$\frac{Q_2}{C_2} = -\dot{I}_3 L + M \dot{I}_1$$

$$\frac{Q_1}{C_1} = -\dot{I}_1 L + \dot{I}_3 L + M \dot{I}_3 - \dot{I}_1 M$$

$$Q_2 = -L C_2 (\ddot{Q}_2 - \ddot{Q}_1) + L C_2 \ddot{Q}_1$$

$$M = L = L_1 = L_2$$

$$Q_1 = -2L C_1 \ddot{Q}_1 + (\ddot{Q}_2 - \ddot{Q}_1) 2L C_1$$

$$\begin{bmatrix} Q_1 \\ Q_2 \end{bmatrix} = \begin{bmatrix} -4L C_1 & 2L C_1 \\ 2L C_2 & -L C_2 \end{bmatrix} \begin{bmatrix} \ddot{Q}_1 \\ \ddot{Q}_2 \end{bmatrix}$$

$$Q_1 = A e^{i\omega t}$$

$$Q_2 = B e^{i\omega t}$$

$$\begin{bmatrix} 1 - 4L\omega^2 C_1 & 2L C_1 \omega^2 \\ 2L C_2 \omega^2 & 1 - L C_2 \omega^2 \end{bmatrix} \begin{bmatrix} A \\ B \end{bmatrix} = \vec{0}$$

$$(1 - 4L\omega^2 C_1)(1 - L C_2 \omega^2) - 4L^2 C_1 C_2 \omega^4 = 0$$

$$1 - \omega^2 (4L C_1 + L C_2) = 0$$

$$\omega = \sqrt{\frac{1}{L(4C_1 + C_2)}}$$