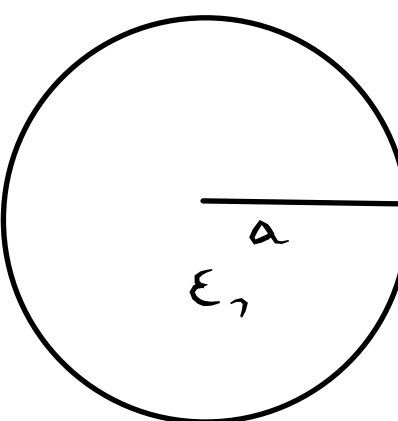


$\uparrow \vec{E} = E \vec{e}_z$



$\Phi(\vec{r}) = \begin{cases} \sum_{l=0}^{\infty} \left(A_l r^l + \frac{B_l}{r^{l+1}} \right) P_l(\cos \vartheta) & r < a \\ \sum_{l=0}^{\infty} \left(C_l r^l + \frac{D_l}{r^{l+1}} \right) P_l(\cos \vartheta) & r > a \end{cases}$

1) $\Phi(r=0) < \infty \Rightarrow B_l = 0$

2) $\Phi(r \rightarrow \infty) = -Ez = -Er \cos(\vartheta) = -E r P_1(\cos \vartheta)$

$C_1 = -E \quad C_{l \neq 1} = 0$

3) $\Phi(a^-) = \Phi(a^+)$

$\sum_{l=0}^{\infty} A_l a^l P_l(\cos \vartheta) = -E a P_1(\cos \vartheta) + \sum_{l=0}^{\infty} \frac{D_l}{a^{l+1}} P_l(\cos \vartheta)$

dla $l \neq 1$

$A_l a^l = \frac{D_l}{a^{l+1}}$

$D_l = A_l a^{2l+1}$

dla $l = 1$

$-E a + \frac{D_1}{a^2} = A_1 a$

$D_1 = a^3(A_1 + E)$

4) $D_{\perp}^-(a) = D_{\perp}^+(a)$

$\epsilon_1 \frac{\partial \Phi}{\partial r} \Big|_{a^-} = \epsilon_2 \frac{\partial \Phi}{\partial r} \Big|_{a^+}$

$\epsilon_1 \sum_{l=0}^{\infty} A_l l a^{l-1} P_l(\cos \vartheta) = -\epsilon_2 E P_1(\cos \vartheta) - \sum_{l=0}^{\infty} (l+1) \epsilon_2 \frac{D_l}{a^{l+2}} P_l(\cos \vartheta)$

dla $l = 1$

$\epsilon_1 A_1 = -\epsilon_2 E - 2 \epsilon_2 \frac{D_1}{a^3}$

$\epsilon_1 A_1 = -\epsilon_2 E - 2 \epsilon_2 A_1 - 2 \epsilon_2 E$

$\begin{cases} A_1 = \frac{-3 \epsilon_2}{\epsilon_1 + 2 \epsilon_2} E \\ D_1 = \frac{\epsilon_1 - \epsilon_2}{\epsilon_1 + 2 \epsilon_2} a^3 E \end{cases}$

dla $l \neq 1$

$\epsilon_1 A_l l a^{l-1} = -(l+1) \epsilon_2 \frac{D_l}{a^{l+2}}$

$\epsilon_1 A_l l a^{l-1} = -(l+1) \epsilon_2 a^{l-1} A_l$

$\begin{cases} A_l = 0 \\ D_l = 0 \end{cases}$

$\Phi(\vec{r}) = \begin{cases} \frac{-3 \epsilon_2}{\epsilon_1 + 2 \epsilon_2} E r \cos(\vartheta) & r < a \\ -E r \cos \vartheta + \frac{\epsilon_1 - \epsilon_2}{\epsilon_1 + 2 \epsilon_2} \frac{a^3 E}{r^2} \cos(\vartheta) & r > a \end{cases}$

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