



$$d\phi_B = B \frac{L^2}{2} d\varphi$$

$$\mathcal{E}_{ind} = \frac{-d\phi_B}{dt} = -B \frac{L^2}{2} \dot{\varphi} \quad I = \frac{\mathcal{E}_{ind}}{R} = \frac{-B L^2 \dot{\varphi}}{2R}$$

$$\mathcal{J} = m l^2 \quad d\vec{M} = \vec{r} \times d\vec{F} = I \vec{r} \times (\vec{I} \times \vec{B})$$

$$\vec{M} = \int_0^L B \cdot \left(\frac{-B L^2 \dot{\varphi}}{2R} \right) r dr = -\frac{B^2 L^4 \dot{\varphi}}{4R}$$

$$\mathcal{J} \ddot{\varphi} = -mg l \sin \varphi - \frac{B^2 L^4 \dot{\varphi}}{4R} \quad \sin \varphi \approx \varphi$$

$$\ddot{\varphi} + \frac{B^2 L^2}{4Rm} \dot{\varphi} + \frac{g}{l} \varphi = 0$$

$$\ddot{x} + 2\beta \dot{x} + \omega^2 x = 0$$

$$x = A e^{\lambda t} \quad \lambda^2 + 2\beta \lambda + \omega^2 = 0$$

$$\lambda = \frac{-2\beta \pm 2\sqrt{\beta^2 - \omega^2}}{2} = \beta \pm \sqrt{\beta^2 - \omega^2}$$

$$x = e^{\beta t} (A e^{\sqrt{\beta^2 - \omega^2} t} + B e^{-\sqrt{\beta^2 - \omega^2} t}) \quad \beta = \frac{B^2 L^2}{8Rm}$$

Stabe + Tenuenā dla $\beta < \omega$

$$\frac{B^2 L^2}{8Rm} < \sqrt{\frac{g}{l}}$$

$$R > \frac{B^2 L^{\frac{5}{2}}}{8m \sqrt{g}}$$

$$\text{stne dla } R < \frac{B^2 L^{\frac{5}{2}}}{8m \sqrt{g}}$$

$$\omega = \sqrt{\frac{g}{l}}$$

$$x = \varphi$$