

Tablunek siebiezy nakuli

$$dW = \frac{1}{4\pi\epsilon_0} \frac{q}{r} dq \leftarrow \text{Tablunek wzucany z nieskonczoności}$$

$$q = \frac{4}{3}\pi r^3 \rho$$

$$dq = 4\pi r^2 \rho dr$$

$$dW = \frac{1}{4\pi\epsilon_0} \frac{1}{r} \left(\frac{4}{3}\pi r^3 \rho \right) (4\pi r^2 \rho) dr = \frac{4\pi \rho^2}{3\epsilon_0} r^4 dr$$

$$W = \frac{4\pi \rho^2}{3\epsilon_0} \int_0^R r^4 dr = \frac{4}{15} \frac{\pi \rho^2}{\epsilon_0} R^5 = \frac{3}{5} \cdot \frac{1}{4\pi\epsilon_0} \frac{q^2}{R}$$

$$Q = \frac{4}{3}\pi R^3 \rho$$