$$V(b,i) = \begin{cases} E(b,i), & b = e \\ M(b,i), & b = 3 \lor t \lor d \text{ } https://www.overleaf.com/project/6425b7f724296e65f98d45d7} \\ I(b,i), & b = h \lor p \lor c \end{cases}$$

$$(1)$$

$$E(b,i) = \begin{cases} 1 + V(b+1,\emptyset), & b = e \land i = \emptyset \\ min(2 + V(b+1,\emptyset), 3 + V(b+1,h)) & b = e \land i = h \\ min(2 + V(b+1,\emptyset), 3 + V(b+1,p)) & b = e \land i = p \\ min(2 + V(b+1,\emptyset), 3 + V(b+1,c)) & b = e \land i = c \end{cases}$$
 (2)

$$M(b,i) = \begin{cases} Fill3 & b = 3\\ FillT & b = t\\ FillD & b = d \end{cases}$$

$$(3)$$

$$Fill3(b,i) = \begin{cases} \infty & b = 3 \land i = \emptyset \\ 4 + V(b+1,h) & b = 3 \land i = h \\ 5 + V(b+1,p) & b = 3 \land i = p \\ 6 + V(b+1,d) & b = 3 \land i = c \end{cases}$$
(4)

$$FillT(b,i) = \begin{cases} \infty & b = t \land i = \emptyset \\ \infty & b = t \land i = h \\ 5 + V(b+1,p) & b = t \land i = p \\ 6 + V(b+1,d) & b = t \land i = c \end{cases}$$
 (5)

$$FillD(b,i) = \begin{cases} \infty & b = d \land i = \emptyset \\ \infty & b = d \land i = h \\ \infty & b = d \land i = p \\ 6 + V(b+1,d) & b = d \land i = c \end{cases}$$

$$(6)$$

$$I(b,i) = \begin{cases} FillH & b = h \\ FillP & b = p \\ FillC & b = c \end{cases}$$

$$(7)$$

$$FillH(b,i) = \begin{cases} min(1+V(b+1,\emptyset), 3+V(b+1,h)) & b=h \land i=\emptyset \\ min(2+V(b+1,\emptyset), 3+V(b+1,h)) & b=h \land i=h \\ min(2+V(b+1,\emptyset), 3+V(b+1,p), 3+V(b+1,h)) & b=h \land i=p \\ min(2+V(b+1,\emptyset), 3+V(b+1,c), 3+V(b+1,h)) & b=h \land i=c \end{cases}$$
 (8)

$$FillP(b,i) = \begin{cases} min(1 + V(b+1,\emptyset), 3 + V(b+1,p)) & b = p \land i = \emptyset \\ min(2 + V(b+1,\emptyset), 3 + V(b+1,h), 3 + V(b+1,p)) & b = p \land i = h \\ min(2 + V(b+1,\emptyset), 3 + V(b+1,p)) & b = p \land i = p \\ min(2 + V(b+1,\emptyset), 3 + V(b+1,c), 3 + V(b+1,p)) & b = p \land i = c \end{cases}$$
(9)

$$FillC(b,i) = \begin{cases} min(1+V(b+1,\emptyset), 3+V(b+1,c)) & b=p \land i=\emptyset \\ min(2+V(b+1,\emptyset), 3+V(b+1,h), 3+V(b+1,c)) & b=p \land i=h \\ min(2+V(b+1,\emptyset), 3+V(b+1,p), 3+V(b+1,c)) & b=p \land i=p \\ min(2+V(b+1,\emptyset), 3+V(b+1,c)) & b=p \land i=c \end{cases}$$
(10)