## 1 Big O

## Time Complexity

The time complexity of an algorithm estimates how much time the algorithm will use for a given input. The time complexity is denoted by  $O(\cdots)$  where the three dots represent some function based on the input size, usually denoted by n.

## **Common Time Complexities**

- O(1) Constantant time. The running time does not depend on the input size. A typical constant-time is a direct formula that calculates the answer.
- $O(\log n)$  The logarithmic often halves the input size at each step. The running time of such an algorithm is logarithmic, because  $\log_2 n$  equals the number of times n must be divided by 2 to get 1.
- $O(\sqrt{n})$  A square root algorithm is slower than  $O(\log n)$  but faster than O(n). A special property of square roots is that  $\sqrt{n} = n/\sqrt{n}$ , so n elements can be divided into  $O(\sqrt{n})$  blocks of  $O(\sqrt{n})$  elements.
- O(n) A linear algorithm goes through the input a constant number of times. This is often the best possible time complexity, because it is usually necessary to access each input element at least once before reporting the answer.
- O(nlogn) This time complexity often indicates that the algorithm sorts the input, because the time complexity of efficient sorting algorithms is O(nlogn). Another possibility is that the algorithm uses a data structure where each operation takes O(logn) time.
- O(n2) A quadratic algorithm often contains two nested loops. It is possible to go through all pairs of the input elements in O(n2) time.
- O(n3) A cubic algorithm often contains three nested loops. It is possible to go through all triplets of the input elements in O(n3) time.
- $\mathrm{O}(2\mathrm{n})$  This time complexity often indicates that the algorithm iterates through all subsets of the input elements.
- O(n!) This time complexity often indicates that the algorithm iterates through all permutations of the input elements.