
Test for Gaussian elimination and solvers

```
%Define a random matrix and check that is non-singular with the
condition
%number of A
A=zeros(20,20);
tol=100;
i=1;
%The following loop will redefine the matrix A until one of them has a
%condition number below tol.
while cond(A)>tol
A=rand(20); %Redefine A
i=i+1;      %Count how many tries
end
A
i
b=rand(20,1)
%We proceed with the Gaussian Elimination with Partial Pivoting.
[L,U,piv]=GEpiv(A)
%Then we obtain PA=A(piv,:), L and U, where PA=LU
A(piv,:)
L*U
%Observe that they are equal
%We are going to solve the following system: PAx=LUx=Pb, where
Pb=b(piv).
%We start with the following: Lz=Pb, z=Ux.
z=Ltrisol(L,b(piv))
%Obtained z, we now calculate the solution x
x=Utrisol(U,z)
%Calculate the residue vector
r=b(piv)-A(piv,:)*x
%Calculate two norms of the residue vector
N1=norm(r,1)
N2=norm(r,2)

% About the row interchanges, the information is given by the vector
piv.
```

A =

Columns 1 through 7

0.7890	0.5965	0.6131	0.2629	0.8841	0.7386	0.6366
0.7744	0.2395	0.6565	0.4241	0.7346	0.2647	0.6778
0.1901	0.9098	0.2855	0.1459	0.7702	0.4528	0.9734
0.7428	0.7740	0.9430	0.0834	0.4128	0.9326	0.6976
0.0276	0.6960	0.9409	0.7455	0.8018	0.6600	0.3758
0.9291	0.7302	0.6883	0.0291	0.8269	0.3836	0.5081
0.2393	0.3673	0.4503	0.6064	0.0705	0.4570	0.3758
0.7255	0.9082	0.6915	0.1377	0.0709	0.5867	0.1724
0.6934	0.9470	0.2201	0.0425	0.7664	0.1590	0.3993

0.4937	0.4158	0.9855	0.3711	0.4603	0.9196	0.9223
0.0309	0.6935	0.2397	0.7380	0.3664	0.7962	0.3695
0.5046	0.7065	0.7412	0.6862	0.7158	0.1481	0.6890
0.8918	0.0828	0.1268	0.6470	0.6401	0.3996	0.7997
0.9787	0.1013	0.7459	0.3518	0.8869	0.0632	0.0447
0.3957	0.3280	0.9077	0.2617	0.7077	0.1860	0.9383
0.8929	0.5261	0.0477	0.4905	0.1270	0.8545	0.0499
0.8315	0.1665	0.3363	0.6790	0.0967	0.5432	0.6146
0.3322	0.1231	0.8889	0.8811	0.0932	0.4304	0.0869
0.0415	0.3986	0.0034	0.0861	0.9026	0.4219	0.0508
0.9661	0.6580	0.6814	0.3658	0.0902	0.2089	0.7651

Columns 8 through 14

0.0388	0.7864	0.8387	0.1606	0.9184	0.0206	0.0199
0.3879	0.2746	0.7095	0.9109	0.8577	0.3415	0.7313
0.3278	0.8985	0.5748	0.1869	0.1515	0.0140	0.1597
0.9236	0.3065	0.4061	0.2534	0.6289	0.3821	0.2462
0.6720	0.8511	0.6005	0.9198	0.0481	0.2381	0.9522
0.0976	0.8074	0.3011	0.8973	0.7750	0.8085	0.2164
0.6728	0.4944	0.5174	0.4433	0.2508	0.5523	0.4740
0.3904	0.4158	0.4289	0.6372	0.4232	0.5088	0.7661
0.8889	0.8819	0.3731	0.5436	0.7323	0.4627	0.3842
0.4560	0.4848	0.8103	0.5374	0.8510	0.5345	0.5654
0.5687	0.8717	0.5836	0.3001	0.4008	0.9273	0.1058
0.4438	0.1246	0.4417	0.5000	0.4710	0.4688	0.6939
0.2630	0.9540	0.3059	0.9602	0.1496	0.9604	0.9112
0.7030	0.9345	0.6755	0.6615	0.7345	0.8642	0.2094
0.3494	0.7688	0.2283	0.9478	0.0735	0.6384	0.9691
0.5966	0.5195	0.8501	0.7148	0.5806	0.1245	0.0903
0.5286	0.1100	0.9752	0.7167	0.2275	0.2161	0.1068
0.7615	0.7285	0.6128	0.8856	0.4885	0.8829	0.0778
0.8506	0.8409	0.7446	0.0688	0.1508	0.9579	0.5428
0.9624	0.4256	0.7716	0.5412	0.9387	0.1198	0.8527

Columns 15 through 20

0.3123	0.9008	0.3597	0.0793	0.3221	0.4032
0.8039	0.0981	0.8399	0.1733	0.9021	0.8560
0.0741	0.8181	0.5949	0.3901	0.3350	0.1194
0.1334	0.2337	0.5697	0.9838	0.2871	0.7819
0.1517	0.6117	0.9931	0.4385	0.4587	0.2263
0.8125	0.2151	0.9808	0.6382	0.8898	0.2880
0.7856	0.8930	0.6132	0.5575	0.2089	0.0950
0.1104	0.2159	0.8694	0.0957	0.8928	0.3521
0.6581	0.2675	0.6658	0.9891	0.2139	0.5294
0.0467	0.4617	0.8198	0.2967	0.3321	0.6841
0.3366	0.3201	0.5328	0.9716	0.1067	0.9110
0.4787	0.2353	0.8042	0.0216	0.3982	0.2528
0.0970	0.3042	0.8078	0.0313	0.2384	0.0360
0.5807	0.7792	0.8646	0.9663	0.9775	0.2637
0.6617	0.6330	0.9480	0.7011	0.7369	0.5181
0.4056	0.9197	0.1909	0.9438	0.6061	0.6551
0.8415	0.6272	0.1674	0.3092	0.3222	0.8350

0.3671	0.8444	0.4057	0.0566	0.2898	0.3228
0.9796	0.5898	0.3688	0.8428	0.5066	0.1427
0.7742	0.7687	0.4371	0.4471	0.2307	0.3842

$i =$

7

$b =$

0.0700
0.3889
0.0795
0.2239
0.7407
0.6784
0.1971
0.7385
0.8155
0.6832
0.3044
0.8339
0.5149
0.5258
0.3336
0.0432
0.3672
0.1656
0.2625
0.7029

$L =$

Columns 1 through 7

1.0000	0	0	0	0	0	0
0.1942	1.0000	0	0	0	0	0
0.0282	0.7787	1.0000	0	0	0	0
0.9112	-0.0107	-0.6804	1.0000	0	0	0
0.7413	0.9360	0.0086	-0.2562	1.0000	0	0
0.5045	0.4098	0.6807	-0.3785	0.3741	1.0000	0
0.0424	0.4429	-0.1116	0.1427	-0.5526	0.5420	1.0000
0.9872	0.6269	-0.1766	0.1133	0.9779	-0.6620	-0.9383
0.5156	0.7350	0.3125	0.3010	0.2582	-0.9016	-0.7776
0.7590	0.7831	0.3292	-0.5933	0.7053	0.9583	0.2425
0.0316	0.7755	0.1322	0.7341	0.1788	-0.0813	0.3348
0.7085	0.9833	-0.5511	0.1132	0.2500	-0.4565	0.0982
0.9123	0.4871	-0.8653	0.9102	0.6598	0.2762	0.7854
0.8062	0.5783	-0.0858	-0.0097	0.1317	0.7112	0.5036
0.9494	0.7123	-0.1481	-0.3308	0.3331	0.2525	0.1336
0.8496	0.0904	-0.3827	0.8027	0.5562	-0.0490	-0.2299

0.3395	0.0997	0.7671	0.3000	0.4587	-0.2785	-0.4916
0.2445	0.3848	0.2639	0.3971	0.4211	-0.2432	-0.2986
0.7913	0.1790	0.0507	0.1240	0.0847	0.0455	-0.2855
0.4043	0.3225	0.6919	-0.4738	0.0311	0.0957	-0.6853

Columns 8 through 14

0	0	0	0	0	0	0
0	0	0	0	0	0	0
0	0	0	0	0	0	0
0	0	0	0	0	0	0
0	0	0	0	0	0	0
0	0	0	0	0	0	0
0	0	0	0	0	0	0
1.0000	0	0	0	0	0	0
0.2320	1.0000	0	0	0	0	0
0.2781	0.2574	1.0000	0	0	0	0
0.1366	-0.2458	-0.3807	1.0000	0	0	0
0.3584	0.1577	0.5545	-0.4547	1.0000	0	0
0.0207	0.1588	-0.6731	0.3855	-0.1959	1.0000	0
-0.6990	0.3471	-0.4550	0.5495	-0.1843	0.7226	1.0000
-0.5247	0.2471	0.3032	-0.6467	0.8605	-0.0684	-0.1553
0.4262	0.4293	-0.7816	0.0959	-0.9570	0.5435	-0.8633
0.5225	-0.5924	-0.3338	0.5576	-0.1721	-0.3167	-0.7126
0.5531	-0.2624	-0.1746	0.4915	-0.2865	-0.1537	-0.2648
0.0202	0.6822	-0.1608	-0.7286	0.4413	0.2975	-0.1442
0.1561	-0.1906	0.5896	-0.8277	0.2942	-0.7294	-0.5417

Columns 15 through 20

0	0	0	0	0	0
0	0	0	0	0	0
0	0	0	0	0	0
0	0	0	0	0	0
0	0	0	0	0	0
0	0	0	0	0	0
0	0	0	0	0	0
0	0	0	0	0	0
0	0	0	0	0	0
0	0	0	0	0	0
0	0	0	0	0	0
0	0	0	0	0	0
0	0	0	0	0	0
0	0	0	0	0	0
1.0000	0	0	0	0	0
0.6669	1.0000	0	0	0	0
0.3378	-0.3291	1.0000	0	0	0
0.4518	-0.5023	-0.6229	1.0000	0	0
0.4237	0.5935	-0.4536	0.2425	1.0000	0
0.9348	-0.3715	0.1868	-0.3423	-0.3393	1.0000

$U =$

Columns 1 through 7

0.9787	0.1013	0.7459	0.3518	0.8869	0.0632	0.0447
0	0.8901	0.1406	0.0776	0.5979	0.4406	0.9647
0	0	0.8104	0.6752	0.3112	0.3152	-0.3767
0	0	0	0.7866	0.0500	0.5612	0.5130
0	0	0	0	-1.1361	0.2686	-0.6290
0	0	0	0	0	0.6046	1.1903
0	0	0	0	0	0	-1.4863
0	0	0	0	0	0	0
0	0	0	0	0	0	0
0	0	0	0	0	0	0
0	0	0	0	0	0	0
0	0	0	0	0	0	0
0	0	0	0	0	0	0
0	0	0	0	0	0	0
0	0	0	0	0	0	0
0	0	0	0	0	0	0
0	0	0	0	0	0	0
0	0	0	0	0	0	0
0	0	0	0	0	0	0
0	0	0	0	0	0	0
0	0	0	0	0	0	0
0	0	0	0	0	0	0
0	0	0	0	0	0	0
0	0	0	0	0	0	0

Columns 8 through 14

0.7030	0.9345	0.6755	0.6615	0.7345	0.8642	0.2094
0.1913	0.7170	0.4436	0.0584	0.0089	-0.1539	0.1191
0.5033	0.2665	0.2360	0.8557	0.0205	0.3335	0.8536
-0.0331	0.2915	-0.1443	0.9402	-0.5057	0.3981	1.3024
-0.3225	-0.8756	-0.5261	0.3257	-0.2592	0.1113	0.8258
-0.2115	-0.0240	0.2693	-0.1686	0.3685	0.0436	0.0140
0.7334	0.0010	0.1298	0.2477	-0.1527	1.0077	0.8394
1.1047	-0.0910	0.6991	-0.3016	0.6230	0.2426	0.5640
0	-0.8289	0.0543	-0.4079	0.3673	0.6501	0.1609
0	0	-0.7443	0.0424	-0.6432	-0.6264	-0.5120
0	0	0	-0.7671	0.6269	0.2174	-1.7220
0	0	0	0	0.8803	0.2904	-0.5673
0	0	0	0	0	-2.0965	-1.6427
0	0	0	0	0	0	1.4608
0	0	0	0	0	0	0
0	0	0	0	0	0	0
0	0	0	0	0	0	0
0	0	0	0	0	0	0
0	0	0	0	0	0	0
0	0	0	0	0	0	0
0	0	0	0	0	0	0
0	0	0	0	0	0	0

Columns 15 through 20

0.5807	0.7792	0.8646	0.9663	0.9775	0.2637
-0.0386	0.6668	0.4269	0.2025	0.1452	0.0682
0.1655	0.0705	0.6363	0.2536	0.3182	0.1658
-0.3199	-0.3506	0.4574	-0.6745	-0.4342	-0.0907
-0.3672	-1.0762	-0.0594	-0.9850	-0.0816	0.0682
-0.3268	0.0173	-0.0290	-0.3332	-0.5709	0.3504

1.0105	-0.2847	0.1317	0.4730	0.7626	-0.0195
1.3815	0.4303	-0.4611	0.6739	-0.3024	0.2677
0.5176	-0.6009	-0.0934	-0.3363	-0.0116	0.2632
-0.7117	-0.2644	-0.1689	0.4068	-0.4240	-0.1014
-0.0704	0.0086	-0.3055	1.2166	-0.1701	0.9068
0.0414	-0.4656	0.0556	0.5085	-0.4440	0.8531
-0.6866	1.0072	-0.6885	1.1112	-0.3720	0.1829
0.6541	-0.2668	-0.2542	-1.2781	-0.6138	-0.5075
1.0635	0.1751	-0.3888	0.2800	-0.0447	-0.2328
0	-0.7256	-0.0663	-0.6003	-0.7623	0.7567
0	0	-0.4523	-1.5497	-0.6799	-0.1694
0	0	0	-1.4840	-0.8337	0.0228
0	0	0	0	0.7961	0.1333
0	0	0	0	0	1.1923

piv =

14
3
5
13
8
10
19
20
12
4
11
9
16
1
6
17
18
7
2
15

ans =

Columns 1 through 7

0.9787	0.1013	0.7459	0.3518	0.8869	0.0632	0.0447
0.1901	0.9098	0.2855	0.1459	0.7702	0.4528	0.9734
0.0276	0.6960	0.9409	0.7455	0.8018	0.6600	0.3758
0.8918	0.0828	0.1268	0.6470	0.6401	0.3996	0.7997
0.7255	0.9082	0.6915	0.1377	0.0709	0.5867	0.1724
0.4937	0.4158	0.9855	0.3711	0.4603	0.9196	0.9223
0.0415	0.3986	0.0034	0.0861	0.9026	0.4219	0.0508
0.9661	0.6580	0.6814	0.3658	0.0902	0.2089	0.7651
0.5046	0.7065	0.7412	0.6862	0.7158	0.1481	0.6890
0.7428	0.7740	0.9430	0.0834	0.4128	0.9326	0.6976

0.0309	0.6935	0.2397	0.7380	0.3664	0.7962	0.3695
0.6934	0.9470	0.2201	0.0425	0.7664	0.1590	0.3993
0.8929	0.5261	0.0477	0.4905	0.1270	0.8545	0.0499
0.7890	0.5965	0.6131	0.2629	0.8841	0.7386	0.6366
0.9291	0.7302	0.6883	0.0291	0.8269	0.3836	0.5081
0.8315	0.1665	0.3363	0.6790	0.0967	0.5432	0.6146
0.3322	0.1231	0.8889	0.8811	0.0932	0.4304	0.0869
0.2393	0.3673	0.4503	0.6064	0.0705	0.4570	0.3758
0.7744	0.2395	0.6565	0.4241	0.7346	0.2647	0.6778
0.3957	0.3280	0.9077	0.2617	0.7077	0.1860	0.9383

Columns 8 through 14

0.7030	0.9345	0.6755	0.6615	0.7345	0.8642	0.2094
0.3278	0.8985	0.5748	0.1869	0.1515	0.0140	0.1597
0.6720	0.8511	0.6005	0.9198	0.0481	0.2381	0.9522
0.2630	0.9540	0.3059	0.9602	0.1496	0.9604	0.9112
0.3904	0.4158	0.4289	0.6372	0.4232	0.5088	0.7661
0.4560	0.4848	0.8103	0.5374	0.8510	0.5345	0.5654
0.8506	0.8409	0.7446	0.0688	0.1508	0.9579	0.5428
0.9624	0.4256	0.7716	0.5412	0.9387	0.1198	0.8527
0.4438	0.1246	0.4417	0.5000	0.4710	0.4688	0.6939
0.9236	0.3065	0.4061	0.2534	0.6289	0.3821	0.2462
0.5687	0.8717	0.5836	0.3001	0.4008	0.9273	0.1058
0.8889	0.8819	0.3731	0.5436	0.7323	0.4627	0.3842
0.5966	0.5195	0.8501	0.7148	0.5806	0.1245	0.0903
0.0388	0.7864	0.8387	0.1606	0.9184	0.0206	0.0199
0.0976	0.8074	0.3011	0.8973	0.7750	0.8085	0.2164
0.5286	0.1100	0.9752	0.7167	0.2275	0.2161	0.1068
0.7615	0.7285	0.6128	0.8856	0.4885	0.8829	0.0778
0.6728	0.4944	0.5174	0.4433	0.2508	0.5523	0.4740
0.3879	0.2746	0.7095	0.9109	0.8577	0.3415	0.7313
0.3494	0.7688	0.2283	0.9478	0.0735	0.6384	0.9691

Columns 15 through 20

0.5807	0.7792	0.8646	0.9663	0.9775	0.2637
0.0741	0.8181	0.5949	0.3901	0.3350	0.1194
0.1517	0.6117	0.9931	0.4385	0.4587	0.2263
0.0970	0.3042	0.8078	0.0313	0.2384	0.0360
0.1104	0.2159	0.8694	0.0957	0.8928	0.3521
0.0467	0.4617	0.8198	0.2967	0.3321	0.6841
0.9796	0.5898	0.3688	0.8428	0.5066	0.1427
0.7742	0.7687	0.4371	0.4471	0.2307	0.3842
0.4787	0.2353	0.8042	0.0216	0.3982	0.2528
0.1334	0.2337	0.5697	0.9838	0.2871	0.7819
0.3366	0.3201	0.5328	0.9716	0.1067	0.9110
0.6581	0.2675	0.6658	0.9891	0.2139	0.5294
0.4056	0.9197	0.1909	0.9438	0.6061	0.6551
0.3123	0.9008	0.3597	0.0793	0.3221	0.4032
0.8125	0.2151	0.9808	0.6382	0.8898	0.2880
0.8415	0.6272	0.1674	0.3092	0.3222	0.8350
0.3671	0.8444	0.4057	0.0566	0.2898	0.3228
0.7856	0.8930	0.6132	0.5575	0.2089	0.0950

0.8039	0.0981	0.8399	0.1733	0.9021	0.8560
0.6617	0.6330	0.9480	0.7011	0.7369	0.5181

ans =

Columns 1 through 7

0.9787	0.1013	0.7459	0.3518	0.8869	0.0632	0.0447
0.1901	0.9098	0.2855	0.1459	0.7702	0.4528	0.9734
0.0276	0.6960	0.9409	0.7455	0.8018	0.6600	0.3758
0.8918	0.0828	0.1268	0.6470	0.6401	0.3996	0.7997
0.7255	0.9082	0.6915	0.1377	0.0709	0.5867	0.1724
0.4937	0.4158	0.9855	0.3711	0.4603	0.9196	0.9223
0.0415	0.3986	0.0034	0.0861	0.9026	0.4219	0.0508
0.9661	0.6580	0.6814	0.3658	0.0902	0.2089	0.7651
0.5046	0.7065	0.7412	0.6862	0.7158	0.1481	0.6890
0.7428	0.7740	0.9430	0.0834	0.4128	0.9326	0.6976
0.0309	0.6935	0.2397	0.7380	0.3664	0.7962	0.3695
0.6934	0.9470	0.2201	0.0425	0.7664	0.1590	0.3993
0.8929	0.5261	0.0477	0.4905	0.1270	0.8545	0.0499
0.7890	0.5965	0.6131	0.2629	0.8841	0.7386	0.6366
0.9291	0.7302	0.6883	0.0291	0.8269	0.3836	0.5081
0.8315	0.1665	0.3363	0.6790	0.0967	0.5432	0.6146
0.3322	0.1231	0.8889	0.8811	0.0932	0.4304	0.0869
0.2393	0.3673	0.4503	0.6064	0.0705	0.4570	0.3758
0.7744	0.2395	0.6565	0.4241	0.7346	0.2647	0.6778
0.3957	0.3280	0.9077	0.2617	0.7077	0.1860	0.9383

Columns 8 through 14

0.7030	0.9345	0.6755	0.6615	0.7345	0.8642	0.2094
0.3278	0.8985	0.5748	0.1869	0.1515	0.0140	0.1597
0.6720	0.8511	0.6005	0.9198	0.0481	0.2381	0.9522
0.2630	0.9540	0.3059	0.9602	0.1496	0.9604	0.9112
0.3904	0.4158	0.4289	0.6372	0.4232	0.5088	0.7661
0.4560	0.4848	0.8103	0.5374	0.8510	0.5345	0.5654
0.8506	0.8409	0.7446	0.0688	0.1508	0.9579	0.5428
0.9624	0.4256	0.7716	0.5412	0.9387	0.1198	0.8527
0.4438	0.1246	0.4417	0.5000	0.4710	0.4688	0.6939
0.9236	0.3065	0.4061	0.2534	0.6289	0.3821	0.2462
0.5687	0.8717	0.5836	0.3001	0.4008	0.9273	0.1058
0.8889	0.8819	0.3731	0.5436	0.7323	0.4627	0.3842
0.5966	0.5195	0.8501	0.7148	0.5806	0.1245	0.0903
0.0388	0.7864	0.8387	0.1606	0.9184	0.0206	0.0199
0.0976	0.8074	0.3011	0.8973	0.7750	0.8085	0.2164
0.5286	0.1100	0.9752	0.7167	0.2275	0.2161	0.1068
0.7615	0.7285	0.6128	0.8856	0.4885	0.8829	0.0778
0.6728	0.4944	0.5174	0.4433	0.2508	0.5523	0.4740
0.3879	0.2746	0.7095	0.9109	0.8577	0.3415	0.7313
0.3494	0.7688	0.2283	0.9478	0.0735	0.6384	0.9691

Columns 15 through 20

0.5807	0.7792	0.8646	0.9663	0.9775	0.2637
0.0741	0.8181	0.5949	0.3901	0.3350	0.1194
0.1517	0.6117	0.9931	0.4385	0.4587	0.2263
0.0970	0.3042	0.8078	0.0313	0.2384	0.0360
0.1104	0.2159	0.8694	0.0957	0.8928	0.3521
0.0467	0.4617	0.8198	0.2967	0.3321	0.6841
0.9796	0.5898	0.3688	0.8428	0.5066	0.1427
0.7742	0.7687	0.4371	0.4471	0.2307	0.3842
0.4787	0.2353	0.8042	0.0216	0.3982	0.2528
0.1334	0.2337	0.5697	0.9838	0.2871	0.7819
0.3366	0.3201	0.5328	0.9716	0.1067	0.9110
0.6581	0.2675	0.6658	0.9891	0.2139	0.5294
0.4056	0.9197	0.1909	0.9438	0.6061	0.6551
0.3123	0.9008	0.3597	0.0793	0.3221	0.4032
0.8125	0.2151	0.9808	0.6382	0.8898	0.2880
0.8415	0.6272	0.1674	0.3092	0.3222	0.8350
0.3671	0.8444	0.4057	0.0566	0.2898	0.3228
0.7856	0.8930	0.6132	0.5575	0.2089	0.0950
0.8039	0.0981	0.8399	0.1733	0.9021	0.8560
0.6617	0.6330	0.9480	0.7011	0.7369	0.5181

$z =$

0.5258
 -0.0226
 0.7435
 0.5415
 0.5022
 -0.0618
 0.5670
 0.2681
 0.3774
 -0.6852
 -0.6798
 0.5194
 -1.1974
 0.4998
 -0.3785
 0.7055
 -0.0521
 0.3642
 -1.0454
 -0.2393

$x =$

0.2553
 0.7290
 0.3956
 -0.5838
 0.0438
 -0.8720

```
-0.5064
-0.7411
-0.5871
 1.7947
 0.6928
-0.2646
 0.5820
 0.3402
-0.3490
-0.2723
 0.5023
 0.4704
-1.2796
-0.2007
```

```
r =
```

```
1.0e-15 *
-0.1110
-0.1249
-0.1110
 0
 0.3331
 0.5551
-0.2776
 0
 0
 0
-0.4441
-0.1110
 0.4441
-0.1665
 0
 0
-0.3331
-0.3053
 0
 0.5551
```

```
N1 =
```

```
3.8719e-15
```

```
N2 =
```

```
1.2179e-15
```

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