

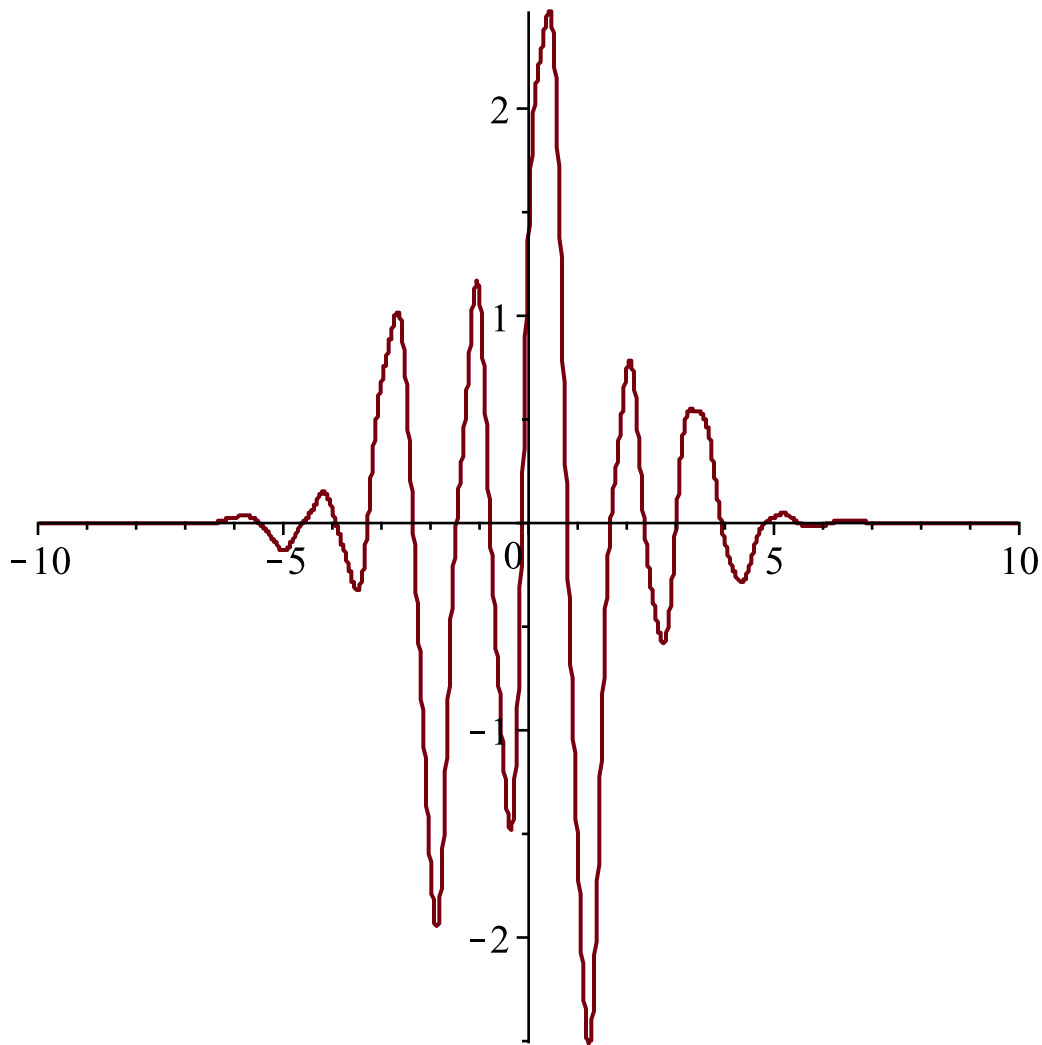
restart;

$$f := x \rightarrow (\cos(2 \cdot x) + 2 \cdot \sin(4 \cdot x) + 0.4 \cdot \cos(2 \cdot x) \cdot \cos(10 \cdot x)) \cdot \exp\left(-\frac{x^2}{8}\right)$$

$$x \rightarrow (\cos(2x) + 2 \sin(4x) + 0.4 \cos(2x) \cos(10x)) e^{-\frac{1}{8}x^2}$$

(1)

plot(f, -10..10, numpoints = 2000)



$a_0 := \text{value}\left(\frac{1}{2 \cdot \text{Pi}}\right) * \text{Int}(f(x), x = -\text{Pi} .. \text{Pi})$  ; # the value of  $a_0$

$$-0.01831626531 - 3.819718633 \cdot 10^{-15} \text{I}$$

(2)

$a := n \rightarrow \text{value}\left(\frac{1}{\text{Pi}}\right) * \text{Int}(f(x) * \cos(n * x), x = -\text{Pi} .. \text{Pi})$  ; # the value of  $a_n$

$$n \rightarrow \text{value}\left(\frac{\int_{-\pi}^{\pi} f(x) \cos(nx) \, dx}{\pi}\right)$$

(3)

$b := n \rightarrow \text{value}\left(\frac{1}{\text{Pi}}\right) * \text{Int}(f(x) * \sin(n * x), x = -\text{Pi} .. \text{Pi})$  ; # the value of  $b_n$

$$n \rightarrow value \left( \frac{\int_{-\pi}^{\pi} f(x) \sin(n x) \, dx}{\pi} \right) \quad (4)$$

abs(*a0*)

0.01831626531

(5)

```
for j from 1 by 1 to 25 do print( [j], abs(a(j)) ) end do
[1], 0.1689352965
[2], 0.6997913956
[3], 0.1639504845
[4], 0.02131923542
[5], 0.01173682840
[6], 0.009845704196
[7], 0.03653179993
[8], 0.1372609244
[9], 0.03582556008
[10], 0.008915777563
[11], 0.03504938027
[12], 0.1389502637
[13], 0.03358240613
[14], 0.004845510193
[15], 0.002664029127
[16], 0.001784969863
[17], 0.001331466062
[18], 0.001056006945
[19], 0.0008706973172
[20], 0.0007372293492
[21], 0.0006363674129
[22], 0.0005574061177
[23], 0.0004939059027
[24], 0.0004417517322
[25], 0.0003981843462
```

(6)

```
for j from 1 by 1 to 25 do print( [j], abs(b(j)) ) end do
[1], 0.01050139527
[2], 0.03191534929
[3], 0.3171675791
[4], 1.412572635
[5], 0.3183464179
```

[6], 0.03451620402  
 [7], 0.01514965726  
 [8], 0.008154429497  
 [9], 0.004990677877  
 [10], 0.003315434140  
 [11], 0.002331820945  
 [12], 0.001710634903  
 [13], 0.001296442641  
 [14], 0.001008383427  
 [15], 0.0008011744704  
 [16], 0.0006479430091  
 [17], 0.0005319759580  
 [18], 0.0004424681294  
 [19], 0.0003722023342  
 [20], 0.0003162218538  
 [21], 0.0002710395211  
 [22], 0.0002341498905  
 [23], 0.0002037191620  
 [24], 0.0001783828166  
 [25], 0.0001571104239

(7)

# With tolerance of 0.01 we obtain

$a0 + \text{Sum}(a(n) \cdot \cos(n \cdot x), n = 1 \dots 5) + \text{Sum}(a(n) \cdot \cos(n \cdot x), n = 7 \dots 9) + \text{Sum}(a(n) \cdot \cos(n \cdot x), n = 11 \dots 13) + \text{Sum}(b(n) \cdot \sin(n \cdot x), n = 1 \dots 7);$

$$-0.01831626531 - 3.819718633 \cdot 10^{-15} I + \sum_{n=1}^5$$

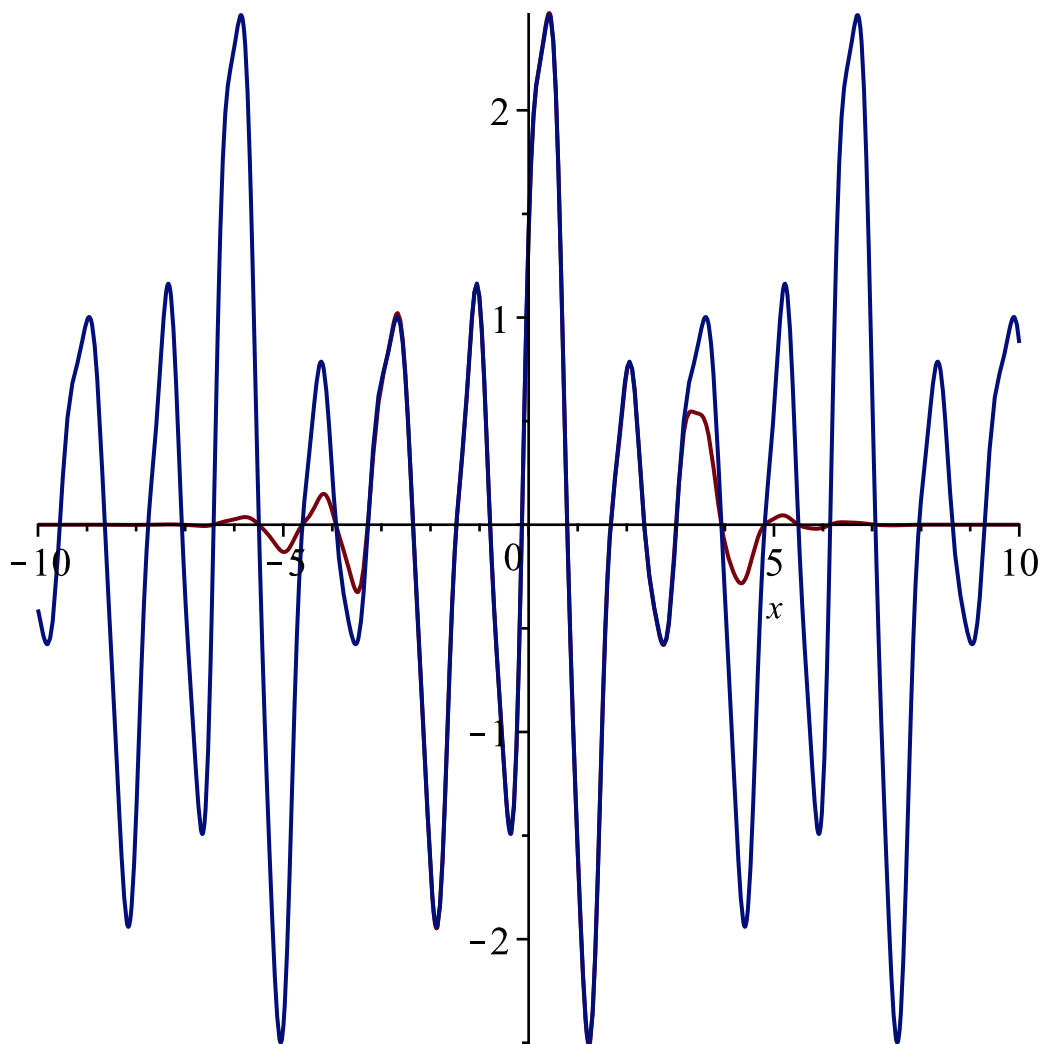
(8)

$$\begin{aligned}
 & 0.07978845607 \left( 8.378942534 \cdot 10^{-126} \operatorname{erf}(1.110720735 + 16.97056275 I + 1.414213562 I n) \right. \\
 & + 8.378942534 \cdot 10^{-126} \operatorname{erf}(1.110720735 - 16.97056275 I - 1.414213562 I n) \\
 & + e^{96 \cdot n - 288} \operatorname{erf}(1.110720735 + 16.97056275 I - 1.414213562 I n) \\
 & + e^{-128 + 16 \cdot n} \operatorname{erf}(1.110720735 + 11.31370850 I + 1.414213562 I n) \\
 & + e^{80 \cdot n - 128} \operatorname{erf}(1.110720735 + 11.31370850 I - 1.414213562 I n) \\
 & + 5 \cdot e^{-8 + 40 \cdot n} \operatorname{erf}(1.110720735 + 2.828427125 I + 1.414213562 I n) \\
 & + 5 \cdot e^{56 \cdot n - 8} \operatorname{erf}(1.110720735 + 2.828427125 I - 1.414213562 I n) \\
 & + 5 \cdot e^{56 \cdot n - 8} \operatorname{erf}(1.110720735 - 2.828427125 I + 1.414213562 I n) \\
 & + 5 \cdot e^{-8 + 40 \cdot n} \operatorname{erf}(1.110720735 - 2.828427125 I - 1.414213562 I n) \\
 & + e^{80 \cdot n - 128} \operatorname{erf}(1.110720735 - 11.31370850 I + 1.414213562 I n) \\
 & + e^{-128 + 16 \cdot n} \operatorname{erf}(1.110720735 - 11.31370850 I - 1.414213562 I n) \\
 & \left. + e^{96 \cdot n - 288} \operatorname{erf}(1.110720735 - 16.97056275 I + 1.414213562 I n) \right) e^{-2 \cdot n^2 - 48 \cdot n} \cos(n x)
 \end{aligned}$$

$$\begin{aligned}
& + \sum_{n=7}^9 0.07978845607 \left( 8.378942534 \cdot 10^{-126} \operatorname{erf}(1.110720735 + 16.97056275 I \right. \\
& + 1.414213562 I n) + 8.378942534 \cdot 10^{-126} \operatorname{erf}(1.110720735 - 16.97056275 I \\
& - 1.414213562 I n) + e^{96 \cdot n - 288} \operatorname{erf}(1.110720735 + 16.97056275 I - 1.414213562 I n) \\
& + e^{-128 + 16 \cdot n} \operatorname{erf}(1.110720735 + 11.31370850 I + 1.414213562 I n) \\
& + e^{80 \cdot n - 128} \operatorname{erf}(1.110720735 + 11.31370850 I - 1.414213562 I n) \\
& + 5 \cdot e^{-8 + 40 \cdot n} \operatorname{erf}(1.110720735 + 2.828427125 I + 1.414213562 I n) \\
& + 5 \cdot e^{56 \cdot n - 8} \operatorname{erf}(1.110720735 + 2.828427125 I - 1.414213562 I n) \\
& + 5 \cdot e^{56 \cdot n - 8} \operatorname{erf}(1.110720735 - 2.828427125 I + 1.414213562 I n) \\
& + 5 \cdot e^{-8 + 40 \cdot n} \operatorname{erf}(1.110720735 - 2.828427125 I - 1.414213562 I n) \\
& + e^{80 \cdot n - 128} \operatorname{erf}(1.110720735 - 11.31370850 I + 1.414213562 I n) \\
& + e^{-128 + 16 \cdot n} \operatorname{erf}(1.110720735 - 11.31370850 I - 1.414213562 I n) \\
& + e^{96 \cdot n - 288} \operatorname{erf}(1.110720735 - 16.97056275 I + 1.414213562 I n) \left. \right) e^{-2 \cdot n^2 - 48 \cdot n} \cos(n x) \\
& + \sum_{n=11}^{13} 0.07978845607 \left( 8.378942534 \cdot 10^{-126} \operatorname{erf}(1.110720735 + 16.97056275 I \right. \\
& + 1.414213562 I n) + 8.378942534 \cdot 10^{-126} \operatorname{erf}(1.110720735 - 16.97056275 I \\
& - 1.414213562 I n) + e^{96 \cdot n - 288} \operatorname{erf}(1.110720735 + 16.97056275 I - 1.414213562 I n) \\
& + e^{-128 + 16 \cdot n} \operatorname{erf}(1.110720735 + 11.31370850 I + 1.414213562 I n) \\
& + e^{80 \cdot n - 128} \operatorname{erf}(1.110720735 + 11.31370850 I - 1.414213562 I n) \\
& + 5 \cdot e^{-8 + 40 \cdot n} \operatorname{erf}(1.110720735 + 2.828427125 I + 1.414213562 I n) \\
& + 5 \cdot e^{56 \cdot n - 8} \operatorname{erf}(1.110720735 + 2.828427125 I - 1.414213562 I n) \\
& + 5 \cdot e^{56 \cdot n - 8} \operatorname{erf}(1.110720735 - 2.828427125 I + 1.414213562 I n) \\
& + 5 \cdot e^{-8 + 40 \cdot n} \operatorname{erf}(1.110720735 - 2.828427125 I - 1.414213562 I n) \\
& + e^{80 \cdot n - 128} \operatorname{erf}(1.110720735 - 11.31370850 I + 1.414213562 I n) \\
& + e^{-128 + 16 \cdot n} \operatorname{erf}(1.110720735 - 11.31370850 I - 1.414213562 I n) \\
& + e^{96 \cdot n - 288} \operatorname{erf}(1.110720735 - 16.97056275 I + 1.414213562 I n) \left. \right) e^{-2 \cdot n^2 - 48 \cdot n} \cos(n x) \\
& + \sum_{n=1}^7 \left( -0.7978845607 e^{-2 \cdot n^2 - 16 \cdot n - 32} \left( -1 \cdot e^{32 \cdot n} \operatorname{erf}(1.110720735 - 5.656854249 I \right. \right. \\
& + 1.414213562 I n) - 1 \cdot e^{32 \cdot n} \operatorname{erf}(1.110720735 + 5.656854249 I - 1.414213562 I n) \\
& + \operatorname{erf}(1.110720735 - 5.656854249 I - 1.414213562 I n) + \operatorname{erf}(1.110720735 \\
& + 5.656854249 I + 1.414213562 I n) \left. \right) \sin(n x) )
\end{aligned}$$

$S := \text{value}(\%) :$

$\text{plot}(\{f(x), S\}, x = -10..10)$



# With tolerance of 0.3 we obtain

$a(2) \cdot \cos(2 \cdot x) + \text{Sum}(b(n) \cdot \sin(n \cdot x), n = 3 \dots 5);$

$$(0.6997913956 + 0. \text{I}) \cos(2 x) + \sum_{n=3}^5 \left( -0.7978845607 e^{-2 \cdot n^2 - 16 \cdot n - 32} \cdot \left( -1 \cdot e^{32 \cdot n} \operatorname{erf}(1.110720735 - 5.656854249 \text{I} + 1.414213562 \text{I} n) - 1 \cdot e^{32 \cdot n} \operatorname{erf}(1.110720735 + 5.656854249 \text{I} - 1.414213562 \text{I} n) + \operatorname{erf}(1.110720735 - 5.656854249 \text{I} - 1.414213562 \text{I} n) + \operatorname{erf}(1.110720735 + 5.656854249 \text{I} + 1.414213562 \text{I} n) \right) \sin(n x) \right) \quad (9)$$

$S := \text{value}(\%) :$

$\text{plot}(\{f(x), S\}, x = -10 \dots 10)$

