

# Functional Dependencies

Gary KL Tam

Department of Computer Science  
Swansea University

A primary goal of database design is to decide what tables to create. Usually there are two principles:

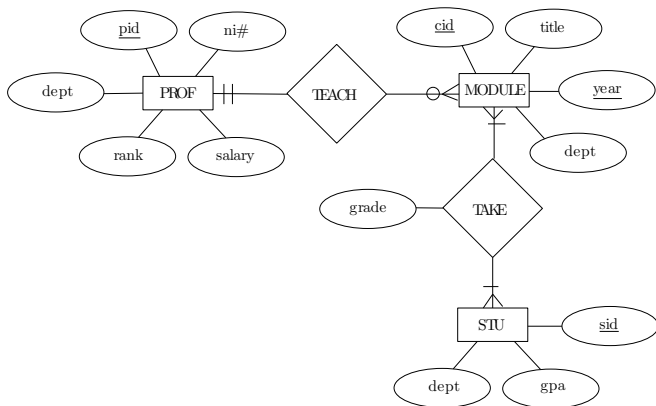
- 1 Capture all the information that needs to be captured by the underlying application.
- 2 Achieve the above with little redundancy.

The first principle is enforced with an **entity relationship (ER) diagram**, while the second with **normalization**.

This and the next few lectures are devoted to normalization.

- ① We need to study **functional dependencies**.
  - What is FD and its relation to redundancy?
  - Properties of FDs (Axioms, Rules and Closure Test)
  - Powerful Closure Test algorithm in detail.
  - Candidate keys and Closure Test
  - Inferring FDs
- ② We proceed to **normalization** in next set of lecture slides.

Tables created from an ER diagram may still contain redundancy.



- PROF (pid, ni#, dept, rank, salary)
- MODULE (cid, year, title, dept)
- STU (sid, dept, gpa)
- TEACH (pid, cid, year), foreign key (pid), foreign key (cid, year)
- TAKE (cid, year, sid, grade), foreign key (sid), foreign key (cid, year)

Where is redundancy (things that are unnecessarily duplicated in tables)?

Answer:

MODULE (cid, title, year, dept)

Why? Because every time the same course is offered again, its title and department are duplicated.

For example, consider  $c1 = \text{"CS250"}$

cid	title	year	dept
c1	database	2010	cs
c1	database	2011	cs
c1	database	2012	cs

The red values are redundant.

Note that the "database" and "cs" of the first tuple are not redundant.

Why?

cid	title	year	dept
c1	database	2010	cs
c1	database	2011	cs
c1	database	2012	cs

Observations: cid **implies** title, dept. This is written as:

$\text{cid} \rightarrow \text{title}$

$\text{cid} \rightarrow \text{dept}$

which are called **functional dependencies**.

## Definition

A **functional dependency** (FD) has the form of  $X \rightarrow Y$  (reads:  **$X$  implies  $Y$** ), where  $X$  and  $Y$  are sets of attributes. It means that whenever two tuples are identical on **all** the attributes in  $X$ , they must also be identical on all the attributes in  $Y$ .

Alternatively, you can interpret  $X \rightarrow Y$  as: each possible value of  $X$  can correspond to exactly one value of  $Y$ .

Functional dependencies are constraints that are required by the underlying application.

# Common examples

- $NI \rightarrow \text{Name, Address, Birthdate}$   
Your national insurance number determines name, address and date of birth
- $ISBN \rightarrow \text{Booktitle, Author, Publisher}$   
wikipedia: The International Standard Book Number (ISBN) is a unique numeric commercial book identifier...



# Example

Assume that the following FDs hold:

$\text{cid} \rightarrow \text{title}$   
 $\text{title} \rightarrow \text{dept}$   
 $\text{cid}, \text{year} \rightarrow \text{dept}$   
 $\text{cid}, \text{year} \rightarrow \text{cid}, \text{dept}$

Can the following tuples co-exist?

cid	title	year	dept
c1	database	2010	cs
c1	database	2011	cs
c2	database	2012	ee

# Example

Assume that the following FDs hold:

$cid \rightarrow title$   
 $title \rightarrow dept$   
 $cid, year \rightarrow dept$   
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Can the following tuples co-exist?

cid	title	year	dept
c1	database	2010	cs
c1	database	2011	cs
c2	database	2012	ee

No, By  $title \rightarrow dept$ , last two tuple cannot co-exists

# Example

Assume that the following FDs hold:

$\text{cid} \rightarrow \text{title}$

$\text{title} \rightarrow \text{dept}$

$\text{cid}, \text{year} \rightarrow \text{dept}$

$\text{cid}, \text{year} \rightarrow \text{cid}, \text{dept}$

Can the following tuples co-exist?

cid	dept
c1	cs
c1	ee

# Example

Assume that the following FDs hold:

$\text{cid} \rightarrow \text{title}$

$\text{title} \rightarrow \text{dept}$

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Can the following tuples co-exist?

cid	dept
c1	cs
c1	ee

No.  $\text{cid} \rightarrow \text{dept}$

# Example

Assume that the following FDs hold:

$cid \rightarrow title$   
 $title \rightarrow dept$   
 $cid, year \rightarrow dept$   
 $cid, year \rightarrow cid, dept$

Can the following tuples co-exist?

cid	dept
c1	cs
c1	ee

No.  $cid \rightarrow dept$

Hey, there is no such FD... how do we know?

# Properties of Functional Dependencies

We need some helpers.

- 1 Armstrong's Axioms
- 2 Splitting Rule
- 3 Closure Test (powerful)

# Armstrong's Axioms

- 1 (Reflexivity)  $X \rightarrow Y$  for any  $Y \subset X$
- 2 (Augmentation)  $X \rightarrow Y$  for any  $XZ \rightarrow YZ$
- 3 (Transitivity)  $X \rightarrow Y$  and  $Y \rightarrow Z$ , then  $X \rightarrow Z$

# Armstrong's Axioms

- 1 (Reflexivity)  $X \rightarrow Y$  for any  $Y \subset X$

## Trivial FD

sid, name  $\rightarrow$  name

- 2 (Augmentation)  $X \rightarrow Y$  for any  $XZ \rightarrow YZ$

## Example

sid  $\rightarrow$  address,      then sid, name  $\rightarrow$  address, name

- 3 (Transitivity)  $X \rightarrow Y$  and  $Y \rightarrow Z$ , then  $X \rightarrow Z$



# Armstrong's Axioms

- ① (Reflexivity)  $X \rightarrow Y$  for any  $Y \subset X$

Trivial FD

sid, name  $\rightarrow$  name

- ② (Augmentation)  $X \rightarrow Y$  for any  $XZ \rightarrow YZ$

Example

sid  $\rightarrow$  address,      then sid, name  $\rightarrow$  address, name

- ③ (Transitivity)  $X \rightarrow Y$  and  $Y \rightarrow Z$ , then  $X \rightarrow Z$

By transitivity

cid  $\rightarrow$  title and title  $\rightarrow$  dept,      then cid  $\rightarrow$  dept

# Splitting Right Sides of FD's

- $X \rightarrow A_1 A_2 \dots A_N$  holds for R iff each of

$$\frac{X \rightarrow A_1}{\phantom{X \rightarrow A_1}}$$

$$\frac{X \rightarrow A_2}{\phantom{X \rightarrow A_2}}$$

...

$$\frac{X \rightarrow A_N}{\phantom{X \rightarrow A_N}}$$

hold for R.

## Example

$A \rightarrow BC$  is equivalent to  $A \rightarrow B$  and  $A \rightarrow C$

- There is no splitting rule for left sides.
- We'll generally express FD's with singleton right sides.

There is a useful & powerful algorithm: Closure Test

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Think of Closure Test as an algorithm.

Given **input**  $X$  and some FDs  $F$ , it computes **output**  $X^+$ .

Closure of  $X$  ( $X^+$ ) contains all attributes implied by  $X$ .

There is a useful & powerful algorithm: Closure Test

Think of Closure Test as an algorithm. <sup>this is sex</sup>

Given **input**  $X$  and some FDs  $F$ , it computes **output**  $X^+$ .

Closure of  $X$  ( $X^+$ ) contains all attributes implied by  $X$ .

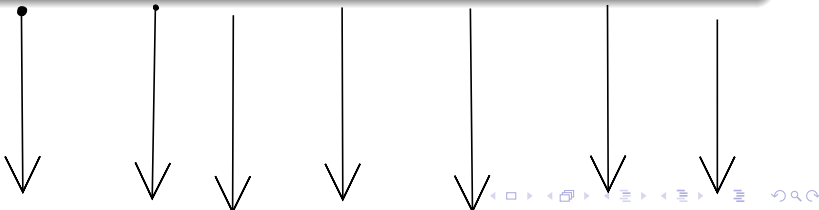
A peek into closure: does  $\text{cid} \rightarrow \text{dept}$ ?

We let  $X = \text{cid}$  and  $F$  be given FDs, and compute  $X^+$  ( $\text{cid}^+$ )

output:  $\text{cid}^+ = \{\text{cid}, \text{title}, \text{dept}\}$

which literally means:

$\left. \begin{array}{l} \text{cid} \rightarrow \text{cid} \\ \text{cid} \rightarrow \text{title} \\ \text{cid} \rightarrow \text{dept} \end{array} \right\} \text{Implies one another}$



There is a useful & powerful algorithm: Closure Test

Think of Closure Test as an algorithm.

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which literally means:

$\text{cid} \rightarrow \text{cid}$

$\text{cid} \rightarrow \text{title}$

$\text{cid} \rightarrow \text{dept}$

Next slides:

- 1 Definition of Closure
- 2 Closure Test algorithm

# Closure of an Attribute Set

Let  $F$  be the set of functional dependencies required by the underlying application.

## Definition

The **closure** ( $X^+$ ) of a set  $X$  of attributes is the set of all such attributes  $A$  that  $X \rightarrow A$  can be deducted from  $F$ .

**Example:** Let  $F$  be the set of following FDs:

$cid \rightarrow title$   
 $title \rightarrow dept$   
 $cid, year \rightarrow dept$   
 $cid, year \rightarrow cid, dept$

Let  $X = cid$ , and  $F$  be the above FDs.

How can we systematically find the following out:

Qn: Is "cid" in  $cid^+$ ?

Qn: Is "year" in  $cid^+$  too?

# Finding the Closure of an Attribute Set

**algorithm** ( $F, X$ )

/\*  $F$  is a set of FDs, and  $X$  is an attribute set \*/

1.  $C = X$
2. **while**  $F$  has a FD  $A \rightarrow B$  such that  $A \subseteq C$  **do**
3.      $C = C \cup B$
4.     remove  $A \rightarrow B$  from  $F$
5. **return**  $C$  /\* closure of  $X$  \*/



**Example:** Let  $F$  be the set of following FDs:

$\text{cid} \rightarrow \text{title}$   
 $\text{title} \rightarrow \text{dept}$   
 $\text{cid, year} \rightarrow \text{dept}$   
 $\text{cid, year} \rightarrow \text{cid, dept}$

What is the closure of  $X$  when  $X = \{\text{cid}\}$ ? We apply the algorithm:

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5. **return**  $C$

• Input:  $X = \{\text{cid}\}$ ,  $F$  is given FDs.

•  $C = \{\text{cid}\}$

**Example:** Let  $F$  be the set of following FDs:

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 $\text{title} \rightarrow \text{dept}$   
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• Input:  $X = \{\text{cid}\}$ ,  $F$  is given FDs.

•  $C = \{\text{cid}\}$

• By “ $\text{cid} \rightarrow \text{title}$ ”,  $\{\text{cid}\} \subseteq C$ , thus  $C = \{\text{cid, title}\}$

**Example:** Let  $F$  be the set of following FDs:

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• By " $\text{cid} \rightarrow \text{title}$ ",  $\{\text{cid}\} \subseteq C$ , thus  $C = \{\text{cid, title}\}$

• By " $\text{title} \rightarrow \text{dept}$ ",  $\{\text{title}\} \subseteq C$ ,  $C = \{\text{cid, title, dept}\}$

•  $X^+ = \{\text{cid, title, dept}\}$

**Example:** Let  $F$  be the set of following FDs:

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 $\text{title} \rightarrow \text{dept}$   
 $\text{cid}, \text{year} \rightarrow \text{dept}$   
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• Input:  $X = \{\text{cid}\}$ ,  $F$  is given FDs.

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• By “ $\text{cid} \rightarrow \text{title}$ ”,  $\{\text{cid}\} \subseteq C$ , thus  $C = \{\text{cid}, \text{title}\}$

• By “ $\text{title} \rightarrow \text{dept}$ ”,  $\{\text{title}\} \subseteq C$ ,  $C = \{\text{cid}, \text{title}, \text{dept}\}$

•  $X^+ = \{\text{cid}, \text{title}, \text{dept}\}$

**Think:** Is “year” in the closure of  $X$ ?

Can “ $\text{cid} \rightarrow \text{year}$ ” be deduced from  $F$ ?

**Example:** Let  $F$  be the set of following FDs:

$\text{cid} \rightarrow \text{title}$   
 $\text{title} \rightarrow \text{dept}$   
 $\text{cid, year} \rightarrow \text{dept}$   
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What is the closure of  $X$  when  $X = \{\text{cid, year}\}$ ?

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• By “ $\text{cid} \rightarrow \text{title}$ ”,  $\{\text{cid}\} \subseteq C$ ,  $C = \{\text{cid, year, title}\}$

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- Input:  $X = \{\text{cid, year}\}$ ,  $F$  is given FDs.
- $C = \{\text{cid, year}\}$
- By " $\text{cid} \rightarrow \text{title}$ ",  $\{\text{cid}\} \subseteq C$ ,  $C = \{\text{cid, year, title}\}$
- By " $\text{title} \rightarrow \text{dept}$ ",  $C = \{\text{cid, year, title, dept}\}$
- $X^+ = \{\text{cid, year, title, dept}\}$

# Candidate Key Revisited

In creating a table, it may seem that so far we have been specifying candidate keys based on our preferences. This illusion is created because we did not understand FDs. In fact, candidate keys are **not** up to us at all. Instead, they are uniquely determined by the set  $F$  of functional dependencies from the underlying application. See the next slide.



# Candidate Key Revisited

Let  $F$  be a set of FDs, and  $R$  a relation.

## Definition

A **candidate key** is a set  $X$  of attributes in  $R$  such that

- $X^+$  includes all the attributes in  $R$ .
- There is no proper subset  $Y$  of  $X$  such that  $Y^+$  includes all the attributes in  $R$ .

Note: A proper subset  $Y$  is a subset of  $X$  such that  $Y \neq X$  (i.e.,  $X$  has at least one element not in  $Y$ ).

**Example.** Consider a table  $R(A, B, C, D)$ , and that  $F = A \rightarrow B, B \rightarrow C$ .

Prove that  $AD$  is a candidate key by definition.

- 1  $AD^+ = \{A, B, C, D\}$ . That is,  $AD$  implies all attributes in  $R$ .
- 2 Now we enumerate all proper subsets of  $AD$ :  $\{A\}$  and  $\{D\}$ .
- 3 And compute their closures.
  - $A^+ = \{A, B, C\}$ .
  - $D^+ = \{D\}$ .
- 4 No proper subset of  $AD$  can imply all attributes in  $R$ .
- 5 By definition,  $AD$  is a candidate key. (QED)

**Example.** Consider a table  $R(A, B, C, D)$ , and that  $F = A \rightarrow B, B \rightarrow C$ .

Prove that  $AD$  is a candidate key by definition.

- ❶  $AD^+ = \{A, B, C, D\}$ . That is,  $AD$  implies all attributes in  $R$ .
- ❷ Now we enumerate all proper subsets of  $AD$  :  $\{A\}$  and  $\{D\}$ .
- ❸ And compute their closures.
  - $A^+ = \{A, B, C\}$ .
  - $D^+ = \{D\}$ .
- ❹ No proper subset of  $AD$  can imply all attributes in  $R$ .
- ❺ By definition,  $AD$  is a candidate key. (QED)

Similarly, can you show that  $ABD$  is NOT a candidate key of  $R$ ?

- In designing a database, for the purpose of minimizing redundancy, we need to collect a set of functional dependencies (FD) that reflect the constraints of the underlying application.
- This can be either given through discussion with clients, or identify them yourself and **verify with clients**.
  - We have an FD only if it holds for **every** instance of the relation.
  - You can't know this just by looking at one instance.
  - You can only determine this based on **domain knowledge**.

# Coincidence or FD?

ID	Email	City	Country	Surname
5123	tff@gmail.com	Toronto	Canada	Fairgrieve
9999	cuz@bell.com	London	Canada	Samways
8798	sms@gmail.com	Winnipeg	Canada	Samways
5645	birds@gmail.com	Aachen	Germany	Lakemeyer

## Think

In this instance, are these FDs?

- Surname → Country
- City → Country

# Coincidence or FD?

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## Think

In this instance, are these FDs?

- Surname  $\rightarrow$  Country
- City  $\rightarrow$  Country

Paris, France	VS	Paris, Texas
Aberdeen, Scotland	VS	Aberdeen, Washington
Venice, Italy	VS	Venice, Louisiana
Perth, Australia	VS	Perth, Scotland

# Swansea, New South Wales 2281, Australia



- Given a set of FDs, we can often infer further FDs.
- This will come in handy when we apply FDs to the problem of database design.
- **Big** task: given a set of FDs, infer **every** other FD that must also hold.
- **Simpler** task: given a set of FDs, infer whether **a given** FD must also hold.



## Examples of Simpler Tasks:

- If  $A \rightarrow B$ ,  $B \rightarrow C$  hold, must  $A \rightarrow C$  hold?
- If  $A \rightarrow H$ ,  $C \rightarrow F$ ,  $FG \rightarrow AD$ ,  
must  $FA \rightarrow D$  hold?  
must  $CG \rightarrow FH$  hold?
- If  $H \rightarrow GD$ ,  $HD \rightarrow CE$ ,  $BD \rightarrow A$  hold,  
must  $EH \rightarrow C$  hold?
- Aside: we are not generating new FDs, but testing a specific possible one.

Two methods:

- ① Using first principles - Show it by referring back to
  - The FDs that you know hold
  - The Armstrong's Axioms
  - The definition of functional dependency.
- ② Using the closure test
  - Assume you know the values of the LHS attributes, and figure out everything else that is determined.
  - If it includes the RHS attributes, then you know that  $LHS \rightarrow RHS$

# Inferring FDs

If  $A \rightarrow B$ ,  $B \rightarrow C$  hold,  
must  $A \rightarrow C$  hold?

By applying transitivity,  
Yes. it holds.

If  $A \rightarrow H$ ,  $C \rightarrow F$ ,  $FG \rightarrow AD$ ,  
must  $FA \rightarrow D$  hold? *closure test*

$FA^+ = \{F, A\}$

$FA^+ = \{F, A, H\}$  by  $A \rightarrow H$

No.  $FA \rightarrow D$  does not hold.

# Inferring FDs

If  $A \rightarrow H$ ,  $C \rightarrow F$ ,  $FG \rightarrow AD$ ,  
must  $CG \rightarrow FH$  hold?

$$CG^+ = \{C, G\}$$

$$CG^+ = \{C, G, F\}, \text{ by } C \rightarrow F$$

$$CG^+ = \{C, G, F, A, D\}, \text{ by } FG \rightarrow AD$$

$$CG^+ = \{C, G, F, A, D, H\} \text{ by } A \rightarrow H$$

yes,  $CG \rightarrow FH$  hold.

If  $H \rightarrow GD$ ,  $HD \rightarrow CE$ ,  $BD \rightarrow A$  hold,  
must  $EH \rightarrow C$  hold?

$$EH^+ = \{E, H\}$$

$$EH^+ = \{E, H, G, D\}, \text{ by } H \rightarrow GD$$

$$EH^+ = \{E, H, G, D, C\}, \text{ by } HD \rightarrow CE$$

yes,  $EH \rightarrow C$  hold.

- Ideally, we do not want to miss any FD, i.e., we want to obtain a set of FDs that is as large as possible. However, in practice, FD collection is a difficult process. No one can guarantee always discovering all FDs.
- What about if we cannot find all FDs?  
There is nothing we can do about them, unfortunately, and will have to continue the design without them. This is why **even** an experienced database professional may not always be able to come up with a perfect design!

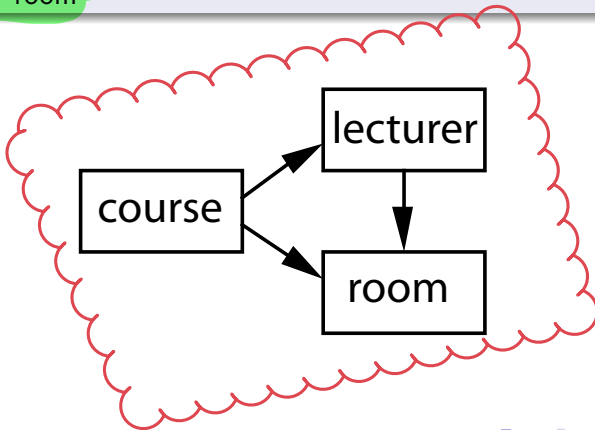
# Functional Dependence Diagram

Functional dependencies can be represented as diagram.

## Example

$\text{course} \rightarrow \text{lecturer, room}$

$\text{lecturer} \rightarrow \text{room}$



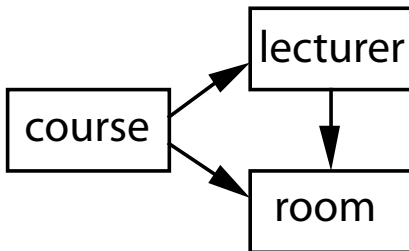
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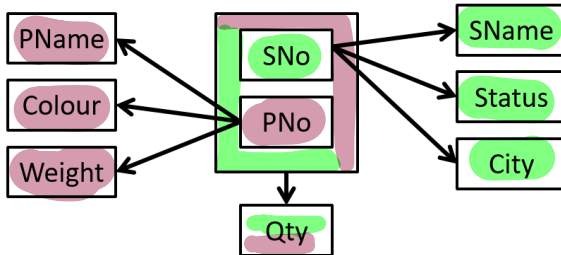


Remember: this is how you draw Functional Dependence Diagram.  
FD diagram also helps you spot the candidate key too.

# Functional Dependence Diagram

Given the following dependencies:

supplier:  $sno \rightarrow sname, status, city$   
part:  $pno \rightarrow pname, color, weight$   
supply:  $sno, pno \rightarrow qty$

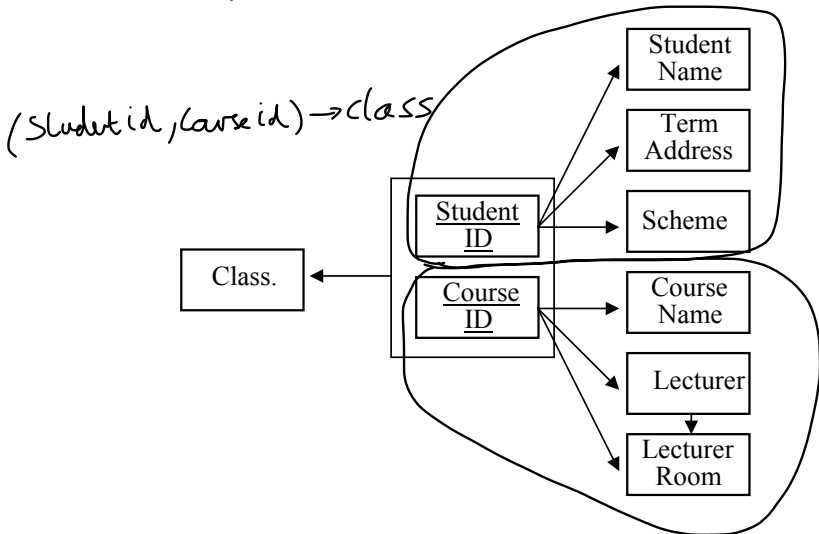


- direction of arrow
- how composite key is depicted
- real world constraints: e.g.  $sno \rightarrow city$   
means each supplier can only locate at exactly one city.



# Functional Dependence Diagram

Another example



# Candidate Keys & Primary Key

- Primary key - one of the candidate keys chosen by DB designer.

How to identify potential candidate keys?

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## Example - Elements table

- Element Name, Symbol and Atomic Number
- e.g. Hydrogen, H, 1
- Each of these attributes can be a candidate key
- Which one to choose?

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- ❸ Also computers are really good at integers!