Haar decompositions and Besov-type spaces

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Nowadays Besov spaces $B_{p,q}^s(\mathbb{R})$ are considered as a quite reasonable possibility to describe the regularity of a function. They are used in almost all parts of Approximation Theory and beyond. Since a few years there exists a generalization of Besov spaces, so-called Besov-type spaces $B_{p,q}^{s,\tau}(\mathbb{R})$. For small smoothness s and $\tau \in (0,1/p)$ they can be described as the collection of all tempered distributions f such that

$$||f|B_{p,q}^{s,\tau}(\mathbb{R})|| := \sup_{I} |I|^{-\tau} ||f|B_{p,q}^{s}(I)||,$$

where the supremum is taken with respect to all finite intervals $I \subset \mathbb{R}$. In my talk I will mainly discuss the discretization of these spaces by Haar wavelets.