Sampling recovery and sharp norm estimates of projection operators

Kateryna Pozharska

Institute of Mathematics of the NAS of Ukraine, Chemnitz University of Technology pozharska.k@gmail.com

Coauthor(s): D. Krieg, M. Ullrich, T. Ullrich

Special session: Stochastic Computation and Complexity

We consider the problem of optimal recovery of bounded complex-valued functions from their samples.

In the talk, we will discuss new sharp bounds for the n-th linear sampling numbers in L_p and conditions under which linear sampling algorithms are optimal among all (possibly non-linear) algorithms [1].

Besides, we show that there are sampling projections onto arbitrary n-dimensional subspaces of the space of bounded functions with at most 2n samples and norm of order \sqrt{n} [2]. This gives a more explicit form of the Kadets-Snobar theorem for the uniform norm.

- [1] Krieg, David, Pozharska, Kateryna, Ullrich, Mario, & Ullrich, Tino (2023). Sampling recovery in L_2 and other norms. arXiv. https://doi.org/10.48550/arxiv.2305.07539
- [2] Krieg, David, Pozharska, Kateryna, Ullrich, Mario, & Ullrich, Tino (2024). Sampling projections in the uniform norm. arXiv. https://doi.org/10.48550/arxiv.2401.02220