

Theory of automata and Formal languages

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Practice 1

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Exercise 1

Let $R = \{(1, 1), (1, 2), (2, 3), (3, 4)\}$ be a binary relation. Exercise 1 asks us to find R^3 .

$$R^2 = \{(a, b) : \exists x \in A, (a, x) \in R \wedge (x, b) \in R\} = \{(1, 1), (1, 2), (1, 3), (2, 4)\}$$

$$R^3 = \{(a, b) : \exists x \in A, (a, x) \in R^2 \wedge (x, b) \in R\} = \{(1, 1), (1, 2), (1, 3), (1, 4)\}$$

Checking the answer with Octave:

```
octave:1> powerrelation({'1', '1'}, ['1', '2'], ['2', '3'], ['3', '4'], 3)
ans =
{
  [1,1] = 11
  [1,2] = 12
  [1,3] = 13
  [1,4] = 14
}
```