## 2<sup>nd</sup> week

# **Topics: Simulation & Minimum Spanning Tree & DFS**

#### P1.Ducci Sequence

(Time Limit: 3 seconds)

A Ducci sequence is a sequence of n-tuples of integers. Given an n-tuple of integers (a1, a2,  $\cdots$ , an), the next n-tuple in the sequence is formed by taking the absolute differences of neighboring integers:

$$(a_1, a_2, \dots, a_n) \rightarrow (|a_1 - a_2|, |a_2 - a_3|, \dots, |a_n - a_1|)$$

Ducci sequences either reach a tuple of zeros or fall into a periodic loop. For example, the 4-tuple sequence starting with 8,11,2,7 takes 5 steps to reach the zeros tuple:

$$(8, 11, 2, 7) \rightarrow (3, 9, 5, 1) \rightarrow (6, 4, 4, 2) \rightarrow (2, 0, 2, 4) \rightarrow (2, 2, 2, 2) \rightarrow (0, 0, 0, 0).$$

The 5-tuple sequence starting with 4,2,0,2,0 enters a loop after 2 steps:

$$(4, 2, 0, 2, 0) \rightarrow (2, 2, 2, 2, 4) \rightarrow (0,0,0,2,2) \rightarrow (0, 0, 2, 0, 2) \rightarrow (0, 2, 2, 2, 2) \rightarrow (2, 0, 0, 0, 2) \rightarrow$$

$$(2, 0, 0, 2, 0) \rightarrow (2, 0, 2, 2, 2) \rightarrow (2, 2, 0, 0, 0) \rightarrow (0, 2, 0, 0, 2) \rightarrow (2, 2, 0, 2, 2) \rightarrow (0, 2, 2, 0, 0) \rightarrow$$

$$(2, 0, 2, 0, 0) \rightarrow (2, 2, 2, 0, 2) \rightarrow (0, 0, 2, 2, 0) \rightarrow (0, 2, 0, 2, 0) \rightarrow (2, 2, 2, 2, 2, 0) \rightarrow (0,0,0,2,2) \rightarrow \cdots$$

Given an n-tuple of integers, write a program to decide if the sequence is reaching to a zeros tuple or a periodic loop.

#### Input

Your program is to read the input from standard input. The input consists of T test cases. The number of test cases T is given in the first line of the input. Each test case starts with a line containing an integer n ( $3 \le n \le 15$ ), which represents the size of a tuple in the Ducci sequences. In the following line, n integers are given which represents the n-tuple of integers. The range of integers are from 0 to 1,000. You may assume that the maximum number of steps of a Ducci sequence reaching zeros tuple or making a loop does not exceed 1,000.

#### Output

Your program is to write to standard output. Print exactly one line for each test case. Print 'LOOP' if the Ducci sequence falls into a periodic loop, print 'ZERO' if the Ducci sequence reaches to a zeros tuple.

#### Sample Input

4

4

8 11 2 7

5

42020

7

000000

6

123123		
Sample Input		
ZERO		
LOOP		
ZERO		
LOOP		

## P2. Qin Shi Huang's National Road System

(Time Limit: 3 seconds)

During the Warring States Period of ancient China(476 BC to 221 BC), there were seven kingdoms in China — they were Qi, Chu, Yan, Han, Zhao, Wei and Qin. Ying Zheng was the king of the kingdom Qin. Through 9 years of wars, he finally conquered all six other kingdoms and became the first emperor of a unified China in 221 BC. That was Qin dynasty — the first imperial dynasty of China(not to be confused with the Qing Dynasty, the last dynasty of China). So Ying Zheng named himself "Qin Shi Huang" because "Shi Huang" means "the first emperor" in Chinese.

Qin Shi Huang undertook gigantic projects, including the first version of the Great Wall of China, the now famous city-sized mausoleum guarded by a life-sized Terracotta Army, and a massive national road system. There is a story about the road system: There were n cities in China and Qin Shi Huang wanted them all be connected by n-1 roads, in order that he could go to every city from the capital city Xianyang. Although Qin Shi Huang was a tyrant, he wanted the total length of all roads to be minimum, so that the road system may not cost too many people's life. A daoshi (some kind of monk) named Xu Fu told Qin Shi Huang that he could build a road by magic and that magic road would cost no money and no labor. But Xu Fu could only build ONE magic road for Qin Shi Huang. So Qin Shi Huang had to decide where to build the magic road. Qin Shi Huang wanted the total length of all none magic roads to be as small as possible, but Xu Fu wanted the magic road to benefit as many people as possible So Qin Shi Huang decided that the value of A/B (the ratio of A to B) must be the maximum, which A is the total population of the two cites connected by the magic road, and B is the total length of none magic roads.



Would you help Qin Shi Huang?

A city can be considered as a point, and a road can be considered as a line segment connecting two points.

#### Input

The first line contains an integer t meaning that there are t test cases ( $t \le 10$ ).

For each test case:

The first line is an integer n meaning that there are n cities  $(2 \le n \le 1000)$ .

Then n lines follow. Each line contains three integers X, Y and P ( $0 \le X$ , Y  $\le 1000$ , 0 < P < 100000).

(X, Y) is the coordinate of a city and P is the population of that city.

It is guaranteed that each city has a distinct location.

### Output

For each test case, print a line indicating the above mentioned maximum ratio A/B. The result should be rounded to 2 digits after decimal point.

## Sample Input

2

4

1 1 20

1 2 30

200 2 80

200 1 100

3

1 1 20

1 2 30

2 2 40

## Sample Output

65.00

70.00