CSTR FIRST - ORDER IRREVERSIBLE REACTION

CAT

Consider a single theversible reachon A>B

- Assume a rate of generation their unit volume that is first order with respect to CA
- UNIT VOWING = 14

ta = K.CA

> EACH NOTE OF A CREATES A TIONE OF B

~ TOLAR RATE OF FORTHATION OF B PER UNIT VOWINE = FE

to = KCA

WE START BY WRITING THE DYNATIC MODELLING EQUATIONS

- COTUPONENT A

- dVCA = FCAF - FCA - VKCA (WITH K THE REACTION CONSTANT)

ASSUTUING FAT V IS CONSTANT, WE HAVE (TI = FO)

$$\frac{dC_A}{dt} = \frac{F}{V}C_{AF} - \frac{F}{V}C_A - KC_A$$
$$= \frac{F}{V}C_{AF} - \left(\frac{F}{V} + K\right)C_A$$

- COMPONENT B

dva = FCB+ - FCB + VKCA

ASSUTTING CONSTANT VOLUTIE AND NO B IN THE FEED -

$$\frac{dC_A}{dt} = \frac{\mp}{V}C_{A} \mp - \left(\frac{\mp}{V} + \kappa\right)C_A$$

$$\frac{dC_B}{dt} = -\frac{\mp}{V}C_{B} + \kappa C_{A}$$

The concentration of B does not play ony vole in the dynamics of component A

$$\begin{bmatrix} \dot{c}_{A} \\ \dot{c}_{B} \end{bmatrix} = \begin{bmatrix} \pm / v C_{AF} - (\mp / v + K) C_{A} \\ - \mp / v C_{B} + K C_{A} \end{bmatrix}$$

$$\begin{bmatrix} \dot{c}_{A} \\ \dot{c}_{B} \end{bmatrix} = \begin{bmatrix} \pm/\sqrt{C_{A}} + (\pm/\sqrt{C_{A}} + K)C_{A} \\ -\pm/\sqrt{C_{B}} + KC_{A} \end{bmatrix} \quad \text{or} \quad \begin{bmatrix} \times 1 \\ \times 2 \end{bmatrix} = \begin{bmatrix} C_{A} \\ (B) \end{bmatrix} = \begin{bmatrix} U_{1} \\ U_{2} \end{bmatrix} = \begin{bmatrix} \pm 1 \\ (A \pm 1) \end{bmatrix}$$

$$\begin{bmatrix} \dot{x}_1 \\ \dot{x}_2 \end{bmatrix} = \begin{bmatrix} u_1/\sqrt{u_2 - (u_1/\sqrt{u_1} + k) \times 1} \\ -u_1/\sqrt{x_1 + k \times 1} \end{bmatrix} = \begin{bmatrix} f_A(x_1, x_2, u_1, u_1 | \theta_1, \theta_2) \\ -f_2(x_1, x_1, u_1, u_2 | \theta_1, \theta_2) \end{bmatrix}$$

BASIC LIMEARIZATION AROUND A FIXED POINT

$$A = \begin{bmatrix} \frac{1}{2} & \frac{1}{2} & \frac{1}{2} & \frac{1}{2} \\ \frac{1}{2} & \frac{1}{2} & \frac{1}{2} & \frac{1}{2} & \frac{1}{2} \\ \frac{1}{2} & \frac{1}{2} & \frac{1}{2} & \frac{1}{2} & \frac{1}{2} & \frac{1}{2} \end{bmatrix}$$

$$A = \begin{bmatrix} \frac{\partial f_1}{\partial x_1} |_{SS} & \frac{\partial f_2}{\partial x_2} |_{SS} \\ \frac{\partial f_2}{\partial x_1} |_{SS} & \frac{\partial f_2}{\partial x_2} |_{SS} \end{bmatrix} \qquad B = \begin{bmatrix} \frac{\partial f_1}{\partial u_1} |_{SS} & \frac{\partial f_2}{\partial u_2} |_{SS} \\ \frac{\partial f_2}{\partial x_1} |_{SS} & \frac{\partial f_2}{\partial x_2} |_{SS} \end{bmatrix}$$

$$\partial f_1/\partial x_1 = -M_1/V - K$$

 $\partial f_1/\partial x_2 = 0$
 $\partial f_2/\partial x_1 = K$
 $\partial f_2/\partial x_2 = -M_1/V$

$$M_A/V|_{SS} = 0.2 \text{ min}^{-1}$$

$$A = \begin{bmatrix} 0.1 & -0.2 \end{bmatrix}$$

$$B = \begin{bmatrix} ** & 0.1 \\ ** & 0 \end{bmatrix}$$

TO BE COTIPUTED - SEE (2)

WE ASSUTE THAT F/V IS THE CONTROL VARIABLE OF INTEREST

- F/V is CAMED SPACE VELOCITY
- V/F is CAMED RESIDENCE TITLE

CONDITIONS dt = FCA+ - (F+K) C4 AND ASSUTE STEADY-STATE

- THAT IS dCA/dt = 0, WE HAR CA = 55
- AS F /V GETS LARGER (TWORE FOED), CA" TENDS TO CAF (the flow is so fast that there is no conversion)
- AS I / V GETS SHAWER (VESS FEED), CA TENDS TO REDO (the flow is so slow, that everything gots converted) NB FSS/V = 0 TRANS FS = 0 ~ BATCH PEACTOR

The steady-state gain is the derivative of Gs wit = 55/v

$$\star \frac{\partial \mathcal{L}_{cr}}{\partial \mathcal{L}_{cr}} = \frac{\left(\frac{K}{K}\right)^{+} \frac{1}{cr} + K}{\left(\frac{K}{K}\right)^{+} \frac{1}{cr} + K} \frac{1}{r}$$

The steady - data gain is the derivative of GAS with CASE * OCA52 = KV/752 + K

$$b_{M} = \frac{A_{1}}{\partial U_{1}}\Big|_{SS} = U_{2}/V - \chi_{1}/V\Big|_{SS} = \frac{1}{V}\Big(U_{2}^{SS} - \chi_{1}^{SS}\Big)$$
 $V_{2}^{SS} = C_{AT}^{SS} = 1.0$
 $V_{1}^{SS} = C_{A}^{SS} = \frac{T^{SS}/V \cdot (C_{AT}^{SS})}{T^{SS}/V + K} = \frac{(0.2) \cdot (1.0)}{0.2 + 0.2} = \frac{0.2}{0.4} = 0.56$

$$* b_{21} = - U_2 / V = - \frac{1}{V} U_{22}^{22} = - \frac{1}{V}$$

-> CONSIDER
$$\frac{dG_0}{dt} = -\frac{\pm}{V}C_0 + KG_1$$
 AND ASSUTE SHADY STATE GOVD.

- THAT IS $\frac{dG_0}{dt} = 0$, WE HAVE $\frac{dG_0}{dt} = \frac{KG_0^{SS}}{T^{SS}}$ WITH $\frac{GSS}{T^{SS}}$ WI

LINEARISATION AROUND A STEADY-STATE (FIXED FOINT)

Tetine
$$\begin{cases} X_1 = C_4 - C_4 & \text{o} \\ X_2 = C_3 - C_6 & \text{o} \end{cases}$$
, we have $\begin{cases} \dot{X}_1 = dC_4/dt - o \\ \dot{X}_2 = dC_6/dt - o \end{cases}$

WE HAVE, BY SUBSTITUTING AND LINEARISING.

$$\frac{dx_1}{dt} = -\left(\frac{\mp ss}{V} + \kappa\right) x_1 + \left(C_{A\pm} - C_{A}^{ss}\right) u_1 + \frac{\mp ss}{V} u_2$$

$$\frac{dx_2}{dt} = Kx_1 + \left(-\frac{\mp cc}{V}\right)x_2 - C_{\mathcal{D}}^{3c}u_1$$

$$\begin{bmatrix} x_1 \\ x_2 \end{bmatrix} = \begin{bmatrix} -(\mp^{ss}/v + \kappa) & 0 \\ \kappa & -\pm^{ss}/v \end{bmatrix} \begin{bmatrix} x_1 \\ x_2 \end{bmatrix} + \begin{bmatrix} (A_{\overline{1}} - C_{\overline{1}}^{ss} - C_{\overline{1}}^{ss}) \\ -C_{\overline{1}}^{ss} & 0 \end{bmatrix} \begin{bmatrix} w_1 \\ w_2 \end{bmatrix}$$

$$= \begin{bmatrix} -0.4 & 0 \\ 0.5 & 0.5 \\ 0.5 & 0.5 \end{bmatrix} \begin{bmatrix} w_1 \\ w_2 \end{bmatrix}$$

$$\frac{dC_{A}}{dt} = \frac{T}{V}C_{A}Y - \left(\frac{T}{V} + K\right)C_{A}$$

$$\frac{dC_{B}}{dt} = -\frac{T}{V}C_{B} + KC_{A}$$

$$\frac{dC_{B}}{dt} = -\frac{T}{V}C_{B} + KC_{A}$$

$$\frac{dX_{1}}{dt} = U_{1}U_{2} - \left(U_{1} + K\right)X_{1}$$

$$\frac{dX_{2}}{dt} = -U_{1}X_{2} + KX_{4}$$

$$\frac{dX_{2}}{dt} = -U_{1}X_{2} + KX_{4}$$

$$\frac{dX_{3}}{dt} \approx \int_{A} \left(X_{1}^{C_{3}}U_{1}^{C_{3}}\right) + \frac{\partial I_{1}}{\partial X_{1}} \left(X_{2}^{C_{3}}U_{1}^{C_{3}}\right) + \frac{\partial I_{2}}{\partial X_{1}} \left(X_{2}^{C_{3}}U_{1}^{C_{3}}\right) + \frac{\partial I_{3}}{\partial X_{2}} \left(X_{2}^{C_{3}}U_{2}^{C_{3}}\right) + \frac{\partial I_{4}}{\partial X_{1}} \left(X_{2}^{C_{3}}U_{2}^{C_{3}}\right) + \frac{\partial I_{4}}{\partial X_{1}} \left(X_{2}^{C_{3}}U_{2}^{C_{3}}\right) + \frac{\partial I_{4}}{\partial X_{1}} \left(X_{2}^{C_{3}}U_{2}^{C_{3}}\right) + \frac{\partial I_{4}}{\partial X_{2}} \left(X_{2}^{C_{3}}U_{2}^{C_{3}}\right) + \frac{\partial I_{4}}{\partial X_{1}} \left(X_{2}^{C_{3}}U_{2}^{C_{3}}\right) + \frac{\partial I_{4}}{\partial X_{2}} \left(X_{2}^{C_{3}}U_{2}^{C_{3}}U_{2}^{C_{3}}\right) + \frac{\partial I_{4}}{\partial X_{2}} \left(X_{2}^{C_{3}}U_{2}^{C_{3}}U_{2}^{C_{3}}\right) + \frac{$$

>> expmAt = expm (Axt)

DISCOUTE IN CLASS HOW to DO

THE FORCED RESPONSE