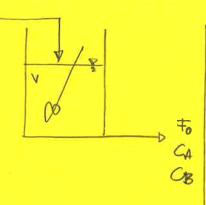
## CSTR FIRST - ORDER IRREVERSIBLE REACTION

Ŧi. CAT CBF



Consider a single treversible reaction A>B

-> Assume a rate of generation per unit volume that is first order with respects CA

MO THOUAR RATE OF REACTION OF A TER UNIT VOWINE = TA

-> EACH TWO IE OF A CREATES A TWO E OF B

AND THOLAR RATE OF FORTHATION OF B PER UNIT VOWINE - FR

WE START BY WRITING THE DYNATIC MODELLING EQUATIONS

- COTUPONENT A

\_ dVCA = FCAF - FCA - VICA (WITH K THE REACTION CONSTANT)

ASSUTUNG FAT V IS CONSTANT, WE HAVE

$$\frac{dC_A}{dt} = \frac{F}{V}C_{AF} - \frac{F}{V}C_A - KC_A$$

$$= \frac{F}{V}C_{AF} - \left(\frac{F}{V} + K\right)C_A$$

dVGB = FCBF - FCB + VKGA

ASSUTUNG CONSTANT VOLUTE AND NO B IN THE FEED

$$\frac{dCA}{dt} = \frac{\mp}{V}CAF - (\frac{\mp}{V} + \mathbf{k})CA$$

$$\frac{dCB}{dt} = -\frac{\mp}{V}CB + KCA$$

The conantration of B does not play ony role in the dynamics of component A

$$\begin{bmatrix} \dot{c}_{A} \\ \dot{c}_{B} \end{bmatrix} = \begin{bmatrix} \mp/v C_{AF} - (\mp/v + K) C_{A} \\ -\mp/v C_{B} + KC_{A} \end{bmatrix}$$
 or

OR 
$$\begin{bmatrix} \times_{1} \\ \times_{2} \end{bmatrix} = \begin{bmatrix} CA \\ CB \end{bmatrix}, \begin{bmatrix} U_{1} \\ U_{2} \end{bmatrix} = \begin{bmatrix} F \\ CAF \end{bmatrix}$$

$$\Theta = \begin{bmatrix} K, V \end{bmatrix}$$

$$\begin{bmatrix} \dot{x}_1 \\ \dot{x}_2 \end{bmatrix} = \begin{bmatrix} u_1/\sqrt{u_2 - (u_1/v + k) \times 1} \\ -u_2/\sqrt{x_2 + k \times 1} \end{bmatrix} = \begin{bmatrix} f_1(x_1, x_2, u_1, u_2 | \theta_1, \theta_2) \\ -f_2(x_1, x_2, u_1, u_2 | \theta_1, \theta_2) \end{bmatrix}$$

$$=\begin{bmatrix} f_{\Lambda}(X_{1}, X_{2}, N_{1}, N_{2} | \theta_{1}, \theta_{2}) \\ -f_{2}(X_{1}, X_{2}, M_{1}, M_{2} | \theta_{1}, \theta_{2}) \end{bmatrix}$$

BASIC LIMEARIZATION AROUND A FIXED POINT

$$\frac{\partial f_1/\partial x_1 = -M_1/V - K}{\partial f_1/\partial x_2 = 0}$$

$$\frac{\partial f_2/\partial x_1 = K}{\partial f_2/\partial x_2 = -M_1/V}$$

$$\frac{\partial f_1}{\partial u} = \frac{M_1}{V} - \frac{\chi_1}{V}$$

$$\frac{\partial f_2}{\partial u} = \frac{M_2}{V}$$

$$\frac{\partial f_2}{\partial u} = -\frac{M_2}{V}$$

$$\frac{\partial f_2}{\partial u} = 0$$

 $M_1/V|_{\leq S} = 0.2 \text{ min}^{-1}$ 

$$K = 0.2 \text{ min}^{-1}$$

$$A = \begin{bmatrix} -0.4 & 0 \\ 0.2 & -0.2 \end{bmatrix}$$

$$B = \begin{bmatrix} ** & 0.2 \\ ** & 0 \end{bmatrix}$$

TO BE COTIPUTED - SEE (2)

WE ASSUTE THAT F/V IS THE CONTROL VARIABLE OF INTEREST

- F/V is CAMED SPACE VELOCITY
- V/F IS CAMED PESIDENCE TIME

GONSIDER dCA = FCA+ - (F+K) CA AND ASSUTE SHADY-STATE

- THAT IS dCA/dt = 0, WE HATE CA = F/V CAF -

- AS F /V GETS LARGER ( HORE FEED), CASC TENDS TO CAF (the flow is so fast that there is no conversion)
- AS I / V GETS STAWER ( VESS FLED ), CA TENDS TO GETEO ( the flow is so show, that everything gets converted ) N.B ISS/V = 0 THANG IS = 0 ~ BATCH PEACTOR

The steady-state gain is the derivative of CASS wit #55/V

+ OGES = KCA+ (KV/FSS+K)2

DISTURBANCE - OUTPUT The steady - data gain is the defivative of CA'S with CA'F \* OCASS KV/FSS + K

$$\frac{1}{2} \frac{1}{2} \frac{1}{2} \frac{1}{2} = \frac{1}{2} \frac{1$$

K=0.2 min

\* 
$$b_{21} = -U_2/V = -\frac{1}{V}U_2^{SS} = -\frac{1}{V}$$

-> CONSIDER 
$$\frac{dG_B}{dt} = -\frac{\pm}{V}C_B + KG_A$$
 AND ASSUTE SEADY STATE GND.

- THAT IS  $\frac{dG_B}{dt} = 0$ , WE HAVE  $\frac{KG_A^{SS}}{T^{SS}} = \frac{KG_A^{SS}}{T^{SS}} =$ 

$$C_{0}^{A} = \frac{1}{F^{SS}/V + K}$$

$$C_{0}^{SS} = \frac{K}{F^{SV}/V + K} = \frac{0.2 \cdot 1}{F^{SV}/V + K} = \frac{0.2$$

LINEARISATION AROUND A STEADY-STATE (FIXED FOINT)

Define 
$$\begin{cases} X_1 = C_A - C_A^{SS} \\ X_2 = C_B - C_B^{SS} \end{cases}$$
 we have  $\begin{cases} \dot{X}_1 = dC_A/dt - o \\ \dot{X}_2 = dC_B/dt - o \end{cases}$ 

WE HAVE, BY SUBSTITUTING AND LINEARISING:

$$\frac{dx_1}{dt} = -\left(\frac{F^{ss}}{V} + \kappa\right)x_1 + \left(C_{A\pm} - C_A^{ss}\right)u_1 + \frac{F^{ss}}{V}u_2$$

$$\frac{dx_2}{dt} = Kx_1 + \left(-\frac{F^{ss}}{V}\right)x_2 - C_{\mathfrak{D}}^{ss}u_1$$

$$\begin{bmatrix} x_1 \\ x_2 \end{bmatrix} = \begin{bmatrix} -(F^{ss}/v + K) & 0 \\ K & -F^{ss}/v \end{bmatrix} \begin{bmatrix} x_1 \\ x_2 \end{bmatrix} + \begin{bmatrix} G^{ss} - G^{ss} \\ -G^{ss} \end{bmatrix} \begin{bmatrix} v_1 \\ v_2 \end{bmatrix}$$

$$= \begin{bmatrix} -0.4 & 0 \\ 0.2 & -0.2 \end{bmatrix} \begin{bmatrix} x_1 \\ x_2 \end{bmatrix} + \begin{bmatrix} 0.5 & 0.2 \\ -0.5 & 0 \end{bmatrix} \begin{bmatrix} u_1 \\ u_2 \end{bmatrix}$$

$$\frac{dC_{A}}{dt} = \frac{\mp}{V}C_{A+} - \left(\frac{\mp}{V} + \mu\right)C_{A}$$

$$\frac{dC_{B}}{dt} = -\frac{\mp}{V}C_{B} + \mu C_{A}$$

$$\frac{dC_{A}}{dt} = -\frac{\pm}{V}C_{B} + \mu C_{A}$$

$$\frac{dC_{A}}{dt} = U_{1}U_{2} - \left(U_{1} + \mu\right)X_{1}$$

$$\frac{dX_{1}}{dt} = U_{1}X_{2} + \mu X_{A}$$

$$\frac{dX_{2}}{dt} = -U_{1}X_{2} + \mu X_{A}$$

$$\frac{dX_{1}}{dt} \approx -\frac{1}{V}(x_{1}, \mu_{1}) + \frac{3+a}{\partial X_{1}}|_{SS}(x_{1} - x_{1}^{CL}) + \frac{3+a}{\partial X_{2}}|_{SS}(x_{2} - x_{2}^{CL}) + \frac{3+a}{\partial X_{2}}|_{SS}(x_{1} - x_{1}^{CL}) + \frac{3+a}{\partial X_{2}}|_{SS}(x_{2} - x_{2}^{CL}) + \frac{3+a}{\partial X_{2}}|_{S$$

$$\begin{cases}
x_1' = x_1 - x_{1}c_1 \\
x_2' = x_2 - x_2c_2
\end{cases}$$

let ) 
$$N_1' = N_1 - N_1^{CL}$$
  
 $N_2' = N_2 - N_2^{CL}$ 

$$\frac{\partial x_{1}^{2}}{\partial t} = \frac{\partial x_{1}}{\partial t}$$

$$\frac{\partial x_{2}^{2}}{\partial t} = \frac{\partial x_{2}}{\partial t}$$

$$\frac{dx_{1}^{\prime}}{\partial t} \approx \frac{\partial f_{1}}{\partial x_{1}} \left| \begin{array}{c} x_{1}^{\prime} + \frac{\partial f_{1}}{\partial x_{2}} \right| x_{2}^{\prime} + \frac{\partial f_{1}}{\partial u_{1}} \left| \begin{array}{c} u_{1}^{\prime} \\ \frac{\partial f_{1}}{\partial u_{2}} \right| x_{3}^{\prime} \\ \frac{\partial f_{2}}{\partial u_{2}} \right| x_{3}^{\prime} + \frac{\partial f_{2}}{\partial u_{1}} \left| \begin{array}{c} u_{1}^{\prime} \\ \frac{\partial f_{2}}{\partial u_{2}} \right| x_{3}^{\prime} \\ \frac{\partial f_{2}}{\partial u_{2}} \right| x_{3}^{\prime} + \frac{\partial f_{2}}{\partial u_{1}} \left| \begin{array}{c} u_{1}^{\prime} \\ \frac{\partial f_{2}}{\partial u_{2}} \right| x_{3}^{\prime} \\ \frac{\partial f_{2}}{\partial u_{2}} \right| x_{3}^{\prime} \\ \frac{\partial f_{2}}{\partial u_{2}} \right| x_{3}^{\prime} + \frac{\partial f_{2}}{\partial u_{1}} \left| \begin{array}{c} u_{1}^{\prime} \\ \frac{\partial f_{2}}{\partial u_{2}} \right| x_{3}^{\prime} \\ \frac{\partial f_{2}}{\partial u_{2}} \right| x_{3}^{\prime} \\ \frac{\partial f_{2}}{\partial u_{2}} \right| x_{3}^{\prime} + \frac{\partial$$

$$\begin{bmatrix} X_1' \\ X_2' \end{bmatrix} = \begin{bmatrix} -0.4 & 0 \\ 0.2 & -0.2 \end{bmatrix} \begin{bmatrix} X_1' \\ X_2' \end{bmatrix} + \begin{bmatrix} 0.5 & 0.2 \\ 0.5 & 0 \end{bmatrix} \begin{bmatrix} W_1' \\ W_2' \end{bmatrix}$$

$$A + B$$

$$x'(t) = \underbrace{At}_{FF} A(t-\tau) Butt) d\tau$$

FORCE - FREE

DISCONER IN CLASS HOW to bo

THE FORCED RESPONSE