# 22. Parts Orienting Mechanics of Manipulation

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### Outline.

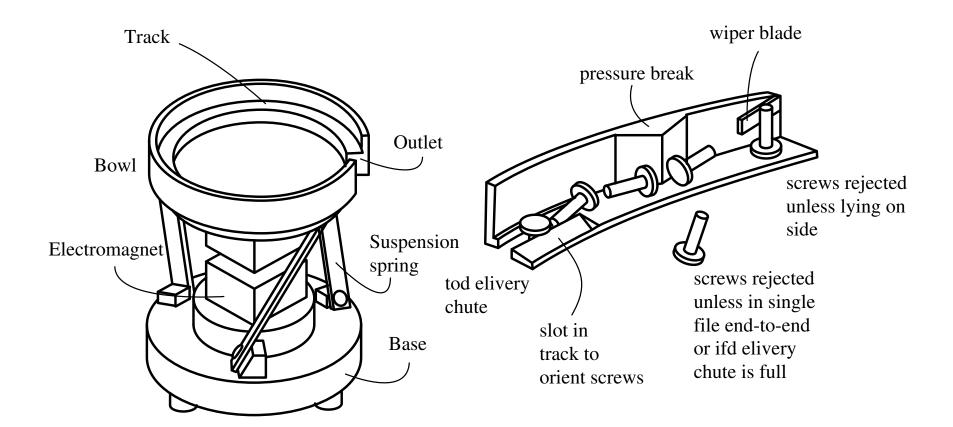
- Manufacturing
- Radius function and diameter function
- Push function
- Representing uncertainty
- Planning

# **Automation and parts orienting**

Assembly systems need oriented parts

Recall SONY Smart cell and APOS

# Most common example: bowl feeder



Lecture 22. Mechanics of Manipulation - p.5

# Orienting by pushing

Pushing is a good way to orient a part.

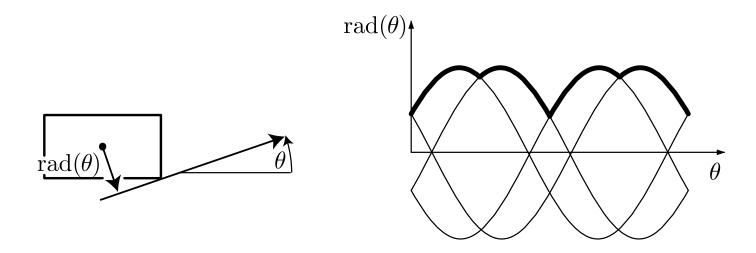
- Generic and flexible: with a flat support surface and a flat pusher, the same hardware can be used for a very broad variety of parts.
- An important problem: to find a sequence of motions that will orient a given part.

Lecture 22.

### **Assumptions**

- 1. Isolated rigid planar polygon, on a planar support surface.
- 2. Coulomb's law, uniform coefficient of friction.
- 3. Square pushing: pusher translates along its normal.
- 4. The part makes contact only with the face of the pusher. Each push proceeds until the part reaches a stable orientation.
- 5. Quasistatic: a balance of contact forces and gravity determines the object motion with sufficient accuracy.

### **Radius function**



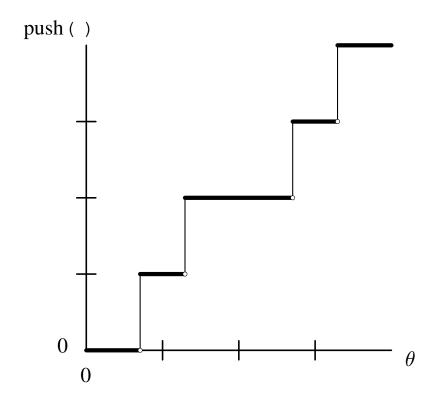
Definition of the radius function.

# **Square pushing and radius function**

For square pushing, radius function behaves like a potential function.

- For a square push, the contact normal is the line of pushing, which splits the votes of the friction cone edges.
- So decision can switch when center of friction crosses contact normal (peak of radius function)
- ... or when we switch from one vertex to another (valley of radius function).

### **Push function**



Define the push function mapping given object orientation  $\theta$  to orientation resulting from square push.

# **Uncertainty**

- The push function maps area between two maxes to a min.
- One push can eliminate a little bit of orientation uncertainty.
- Can a sequence of pushes eliminate a lot?

We represent uncertain orientation as a closed interval  $\Theta = [\alpha, \beta]$ . Define  $\bar{p}(\Theta)$  to return the smallest interval containing  $\{\operatorname{push}(\theta)|\theta\in\Theta\}$ .

### **Possibilism**

Possibilistic approach: Representing uncertainty by set of possibilities.

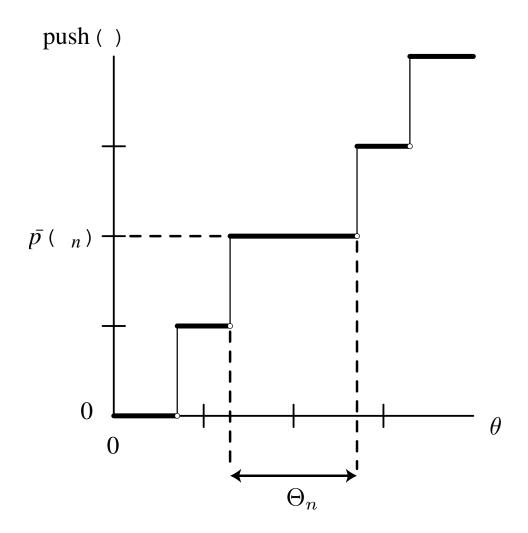
Conservative approximation: approximating the set of the possible states by a superset. (A plan that works for the approximation will work for the actual possibilities.)

Sometimes probabilistic approach would be better.

# Planning the last step

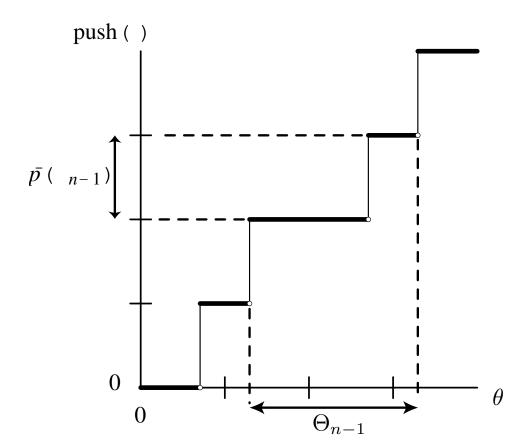
To plan *last* step of n-step plan:

- $\Theta_n$ : set of orientations before step n.
- What is the largest set that can be oriented in one push? I.e. what is the largest  $\Theta$  such that  $\bar{p}(\Theta)$  is a single point?



### Planning the next-to-last step

- Result must be at least as large as  $\Theta_n$ .
- To find  $\Theta_{n-1}$ :
  - What is the largest interval  $\Theta$  that can be oriented in two pushes? I.e. what is the largest  $\Theta$  such that  $\bar{p}(\Theta)$  is smaller than  $\Theta_n$ ?



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