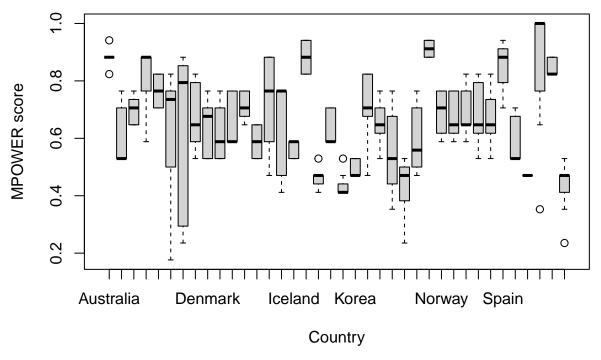
Mpower index analysis

2023-07-05

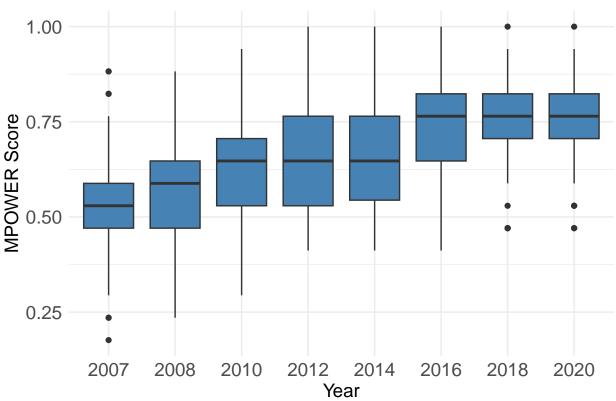
Plotting mPOWER distributions over years

MPOWER score distribution over OCSE countries



Plotting mPOWER distributions across countries

MPOWER Score Distribution in 2008-2020



Index seems to have increased

```
#First we check that the difference between 2020 and 2008 is 0

compute_t_stat=function(df,med0){
   med_diff<-median((df)-med0)
   return (abs(med_diff))
}

med0<-0
T0<-compute_t_stat(df,med0)
T0</pre>
```

[1] 0.1764706

```
symmetric_perm_wrapper = function(df, med0) {
  n = dim(df)[1]
  p = dim(df)[2] #2 #I am confronting two things
  medOmatrix <- matrix(med0,</pre>
                        nrow = n,
                        ncol = p,
                        byrow = TRUE)
  # In this case we use changes of signs in place of permutations
  signs.perm <- rbinom(n, 1, 0.5) * 2 - 1
  df_perm <- med0matrix + (as.numeric(df) - med0) * matrix(signs.perm,</pre>
                                                             ncol = p,
                                                             byrow = FALSE)
  compute_t_stat(df_perm, med0matrix)
}
# parallel
n_cores <- detectCores()</pre>
cl = makeCluster(n_cores)
clusterExport(cl, varlist = list("symmetric_perm_wrapper", "df",
                                  "compute_t_stat","seed"))
set.seed(seed)
T2 <- pbreplicate(1e3, symmetric_perm_wrapper(df, med0), cl = cl)
stopCluster(cl)
diagnostic_permutation <- function(T20, T2) {</pre>
 B <- length(T2)
 # Compare real test statistic with the ones given by the permuted data
 # hist(T2, xlim = range(c(T2, T20)))
# abline(v = T20, col = 3, lwd = 4)
  # Empirical cumulative distribution function
 # plot(ecdf(T2))
# abline(v = T20, col = 3, lwd = 4)
  # P-value
 p_val \leftarrow sum(T2 >= T20) / B
  cat("p-value: ", p_val)
```

p-value: 0

So the difference is significant! I can reject the null hypothesis Now I want to compute a bootstrap confidence interval on this difference An alternative approach is to use bootstrap on the differences

We now compute the bootstrap confidence interval on the differences

```
#Utils
diagnostic_bootstrap <- function(distro, obs, alpha) {
  variance_pred <- var(distro)
  print(paste("Variance: ", variance_pred))</pre>
```

```
sd_pred <- sd(distro)</pre>
  print(paste("Standard deviation: ", sd_pred))
  bias_pred <- mean(distro) - obs</pre>
  print(paste("Bias: ", bias_pred))
  MSE_pred <- variance_pred + bias_pred^2</pre>
  print(paste("MSE: ", MSE_pred))
  # computing quantiles
  right.quantile <- quantile(distro, 1 - alpha / 2)
  left.quantile <- quantile(distro, alpha / 2)</pre>
  CI <- c(
    obs - (right.quantile - obs),
    obs,
    obs - (left.quantile - obs)
  names(CI) <- c("lower", "center", "upper")</pre>
  print(CI)
  plot(ecdf(distro), main = "Bootstrap distribution")
  abline(v = CI[2], col = 3, lwd = 2)
  abline(v = CI[c(1, 3)], lty = 3)
}
T0=median(df)
## [1] 0.1764706
compute_bootstrap_sample <- function(df) {</pre>
  permutation <- sample(1:nrow(df), replace = T)</pre>
  df.boot <- df[permutation, ]</pre>
  #Using the median
  med <- median(df.boot)</pre>
  return(med)
}
n_cores <- detectCores()</pre>
cl <- makeCluster(n_cores)</pre>
invisible(clusterEvalQ(cl, library(np)))
clusterExport(cl, varlist = list("df",
                                    "compute_bootstrap_sample",
                                    "seed"))
set.seed(seed)
T.boot <- pbreplicate(B, compute_bootstrap_sample(df), cl = cl)</pre>
stopCluster(cl)
```

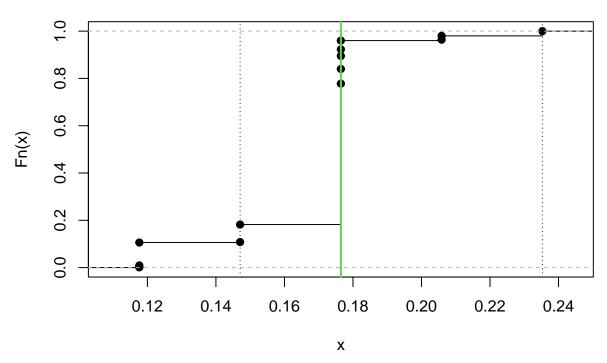
```
## [1] "Variance: 0.000474536820557582"
## [1] "Standard deviation: 0.0217838660608622"
## [1] "Bias: -0.00670588235294114"
```

diagnostic_bootstrap(T.boot, T0, alpha = myalpha)

myalpha=0.05

```
## [1] "MSE: 0.00051950567868907"
## lower center upper
## 0.1470588 0.1764706 0.2352941
```

Bootstrap distribution



The bootstrap interval does no contain 0, so we can say that the median difference between MPOWER value at 2008 and at 2020 is greater than 0

There has been an increase of around 14.6-0.23 in the MPOWER compound score

Now we perform bootstrap on 2008

```
df<-as.numeric(mpower_table[2,-1])
T0=median(df)
T0</pre>
```

[1] 0.5882353

```
set.seed(seed)
T.boot <- pbreplicate(B, compute_bootstrap_sample(df), cl = cl)
stopCluster(cl)

myalpha=0.05
diagnostic_bootstrap(T.boot, T0, alpha = myalpha)

## [1] "Variance: 0.000753899227947662"

## [1] "Standard deviation: 0.0274572254233319"

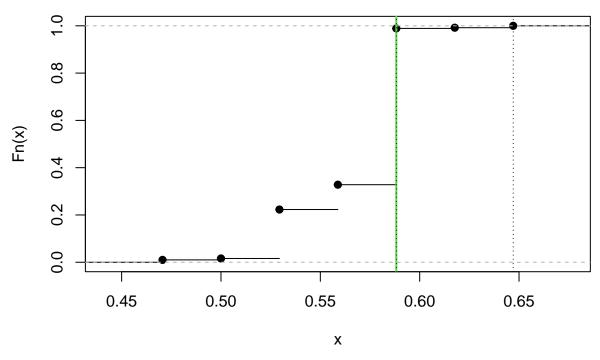
## [1] "Bias: -0.0164117647058823"

## [1] "MSE: 0.00102324524870891"

## lower center upper

## 0.5882353 0.5882353 0.6470588</pre>
```

Bootstrap distribution



Bootstrap on 2020

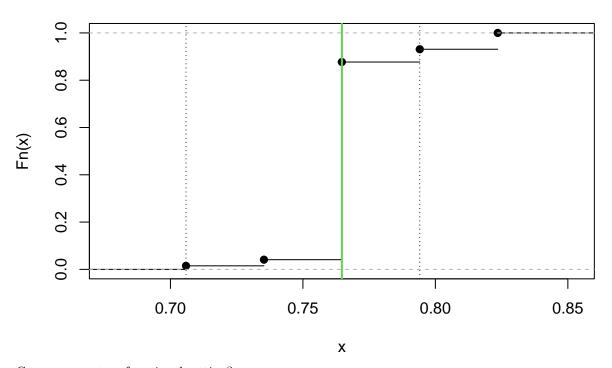
```
df<-as.numeric(mpower_table[8,-1])
T0=median(df)
T0</pre>
```

[1] 0.7647059

```
compute_bootstrap_sample <- function(df) {
  permutation <- sample(1:length(df), replace = T)
  df.boot <- df[permutation]
  #Using the median
  med <- median(df.boot)
  return(med)</pre>
```

```
n_cores <- detectCores()</pre>
cl <- makeCluster(n_cores)</pre>
invisible(clusterEvalQ(cl, library(np)))
clusterExport(cl, varlist = list("df",
                                  "compute_bootstrap_sample",
                                  "seed"))
set.seed(seed)
T.boot <- pbreplicate(B, compute_bootstrap_sample(df), cl = cl)</pre>
stopCluster(cl)
myalpha=0.05
diagnostic_bootstrap(T.boot, T0, alpha = myalpha)
## [1] "Variance: 0.000344205797492994"
## [1] "Standard deviation: 0.0185527840900764"
## [1] "Bias: 0.004"
## [1] "MSE: 0.000360205797492994"
##
       lower
                center
## 0.7058824 0.7647059 0.7941176
```

Bootstrap distribution



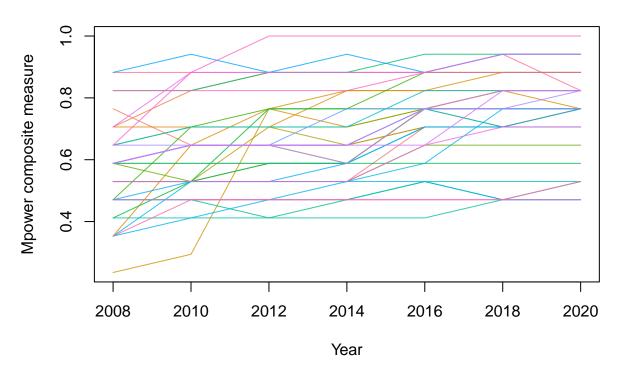
Can we move to a functional setting?

```
mpower_table_f<-as.data.frame(mpower_table[-1,-1])
grid <- seq(2008, 2020, by=2)

#Create functional data
f_data <- roahd::fData(grid,t(mpower_table_f))</pre>
```

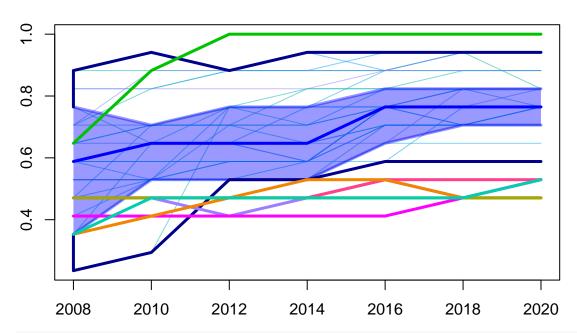
```
plot(f_data,
     xlab="Year",
     ylab="Mpower composite measure",
     main="Mpower")
```

Mpower



fb_plot = roahd::fbplot(f_data, main="Magnitude outliers - MBD", Depths = "MBD") # Functional Box Plot

Magnitude outliers - MBD



fb_plot\$ID_outliers

##	Israel	Japan	Korea	Mexico	Switzerland
##	18	20	21	25	35
##	Türkiye United States				
##	36	38			

```
MBD_f<-as.data.frame(t(MBD(f_data)))
MBD_f[fb_plot$ID_outliers]</pre>
```

```
## Israel Japan Korea Mexico Switzerland Türkiye United States ## 1 0.2031599 0.143416 0.261075 0.1958443 0.2072749 0.1199451 0.193101
```

The following seem to have increased less than others their MPOWER composite measure

mpower_table\$Israel

```
## [1] 0.4117647 0.4705882 0.4705882 0.4117647 0.4705882 0.5294118 0.4705882 ## [8] 0.4705882
```

mpower_table\$Japan

```
## [1] 0.4117647 0.4117647 0.4117647 0.4117647 0.4117647 0.4117647 0.4117647 0.4705882 ## [8] 0.5294118
```

mpower_table\$Korea

```
## [1] 0.4705882 0.4705882 0.4705882 0.4705882 0.4705882 0.5294118 0.5294118 ## [8] 0.5294118
```

mpower_table\$Mexico

```
## [1] 0.2352941 0.3529412 0.4117647 0.4705882 0.5294118 0.5294118 0.4705882 ## [8] 0.4705882
```

mpower_table\$Switzerland

```
## [1] 0.4705882 0.4705882 0.4705882 0.4705882 0.4705882 0.4705882 0.4705882 ## [8] 0.4705882
```

mpower_table\$`United States`

```
## [1] 0.2352941 0.3529412 0.4705882 0.4705882 0.4705882 0.4705882 0.4705882 ## [8] 0.5294118
```

Turkiye has had a very steep increase

mpower_table\$Türkiye

```
## [1] 0.3529412 0.6470588 0.8823529 1.0000000 1.0000000 1.0000000 1.0000000 ## [8] 1.0000000
```

Frow WHO: "In Turkey, the adoption of MPOWER measures in 2008 led to a significant reduction in smoking. By 2012 data showed that smoking decreased by 13.4% and exposure to second-hand smoke was on the decline too. Turkey became the third country in Europe to go 100% smoke-free indoors and the first country to achieve all six MPOWER measures at the highest level.

The MPOWER measures have been life-changing for Turkey's people, reducing the likelihood of heart disease, lung cancer, and other chronic diseases. Progress is evident, with studies showing a 20% decline in 2012 in the number of citizens admitted to hospital for smoking-related diseases."