

P.Pt

Oleh: Bu Bilqis

Pokok Bahasan

1

2

3

Basis untuk ruang kolom

Basis untuk ruang baris

Basis yang berasal
dari vektor sendiri

Tujuan

- > Beberapa pertemuan yang lalu --> basis untuk matrix A
- > Sekarang :
 - 1.Dapat mencari basis untuk ruang baris A
 - 2.Dapat mencari basis untuk ruang kolom A
 - 3.Dapat mencari basis yang di dapat dari vektor vektor dia sendiri A

Pengertian

④ Kombinasi Linier

$\vec{w} \rightarrow$ kombinasi Linier dr $\vec{v}_1 \vec{v}_2 \dots \vec{v}_n$ jd
 \vec{w} dpt diungkapkan dlm bentuk :

$$\vec{w} = k_1 \vec{v}_1 + k_2 \vec{v}_2 + \dots + k_n \vec{v}_n$$

dimana

$$k_1, k_2, \dots, k_n \rightarrow \text{skalar}$$

ingat!! \vec{w} baris di atas bkn hanya satu baris,
 tp terdiri dari beberapa baris

or kombinasi Linier \rightarrow ada nilai k_1, k_2, \dots, k_n

Merentang = spanning

2. Merentang :

- $\vec{v}_1, \vec{v}_2, \dots, \vec{v}_n$ merentang ruang vektor V jika sembarang vektor pd ruang vektor V dpt dinyatakan sbo kombinasi linier dr $\vec{v}_1, \vec{v}_2, \dots, \vec{v}_n$
- ada banyak nilai $\underline{k_1, k_2, \dots, k_n}$
- $\det \neq 0$ (\det bisa dicari det)

ex:

tent. apakah $\vec{v}_1 = \begin{bmatrix} 2 \\ 1 \end{bmatrix}$ & $\vec{v}_2 = \begin{bmatrix} 3 \\ 2 \end{bmatrix}$ merentang

Jwb: merentang $\det \rightarrow$ sembarang dinyatakan sbo kombinasi

vektor pd R^2 dpt linier \vec{v}_1, \vec{v}_2

4.4 Kebebasan Linier

→ $\bar{v}_1, \bar{v}_2, \dots, \bar{v}_n \rightarrow$ bebas Linier jk hanya ada
satu pemecahan u persamaan :

$$k_1 \bar{v}_1 + k_2 \bar{v}_2 + \dots + k_n \bar{v}_n = \bar{0}$$

yaitu $k_1 = k_2 = \dots = k_n = 0,$

det $\neq 0$ (jk bisa dicaril det)

jk ada sebuh or lebih vektor dpt

dinyatakan sbo k. L vektor lainnya mk
+ bebas linier

ex.

Basis
 $\{\bar{v}_1, \bar{v}_2, \dots, \bar{v}_n\}$

merentang

$$\bar{x} = k_1 \bar{v}_1 + k_2 \bar{v}_2 + \dots + k_n \bar{v}_n$$

\bar{x} = sembarang vektor

$k_1, k_2, \dots, k_n \rightarrow$ ada nilai -
nya

or

$$\text{Det} \neq 0$$

bebas Linier

$$\bar{o} = k_1 \bar{v}_1 + k_2 \bar{v}_2 + \dots + k_n \bar{v}_n$$

$k_1 = k_2 = \dots = k_n = 0 \rightarrow$ hanya satu
jawaban

or

$$\text{Det} \neq 0$$

Tujuan



1. Dapat mencari basis untuk ruang baris A
 - Basis ruang baris A = basis ruang baris R
 - Menghasilkan vektor baru
2. Dapat mencari basis untuk ruang kolom A
 - Basis ruang kolom A \leftrightarrow basis ruang kolom R
 - Tapi berkorespondensi
 - Tidak menghasilkan vektor baru
3. Dapat mencari basis yang di dapat dari vektor
 - Vektor dia sendiri A
 - Tidak menghasilkan vektor baru

Theorem 5.5.3. *Elementary row operations do not change the nullspace of a matrix.*

Theorem 5.5.4. *Elementary row operations do not change the row space of a matrix.*

Theorem 5.5.5. *If A and B are row equivalent matrices, then:*

- (a) *A given set of column vectors of A is linearly independent if and only if the corresponding column vectors of B are linearly independent.*
- (b) *A given set of column vectors of A forms a basis for the column space of A if and only if the corresponding column vectors of B form a basis for the column space of B .*

The following theorem makes it possible to find bases for the row and column spaces of a matrix in row-echelon form by inspection.

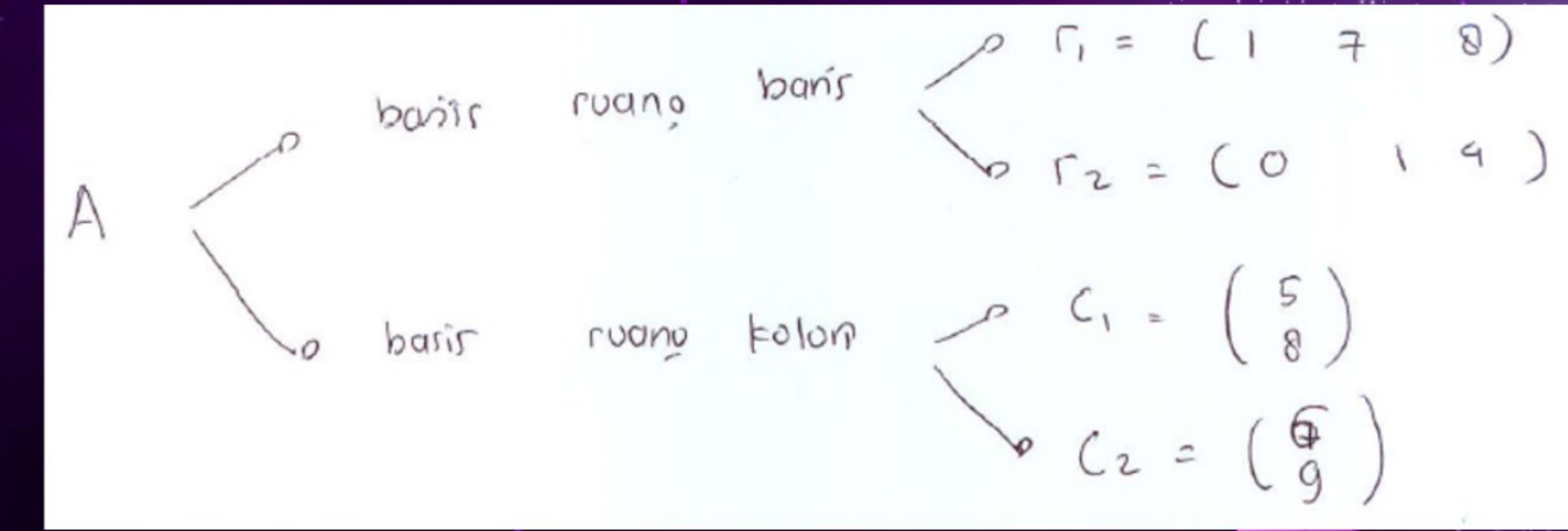
Theorem 5.5.6. *If a matrix R is in row-echelon form, then the row vectors with the leading 1's (i.e., the nonzero row vectors) form a basis for the row space of R , and the column vectors with the leading 1's of the row vectors form a basis for the column space of R .*



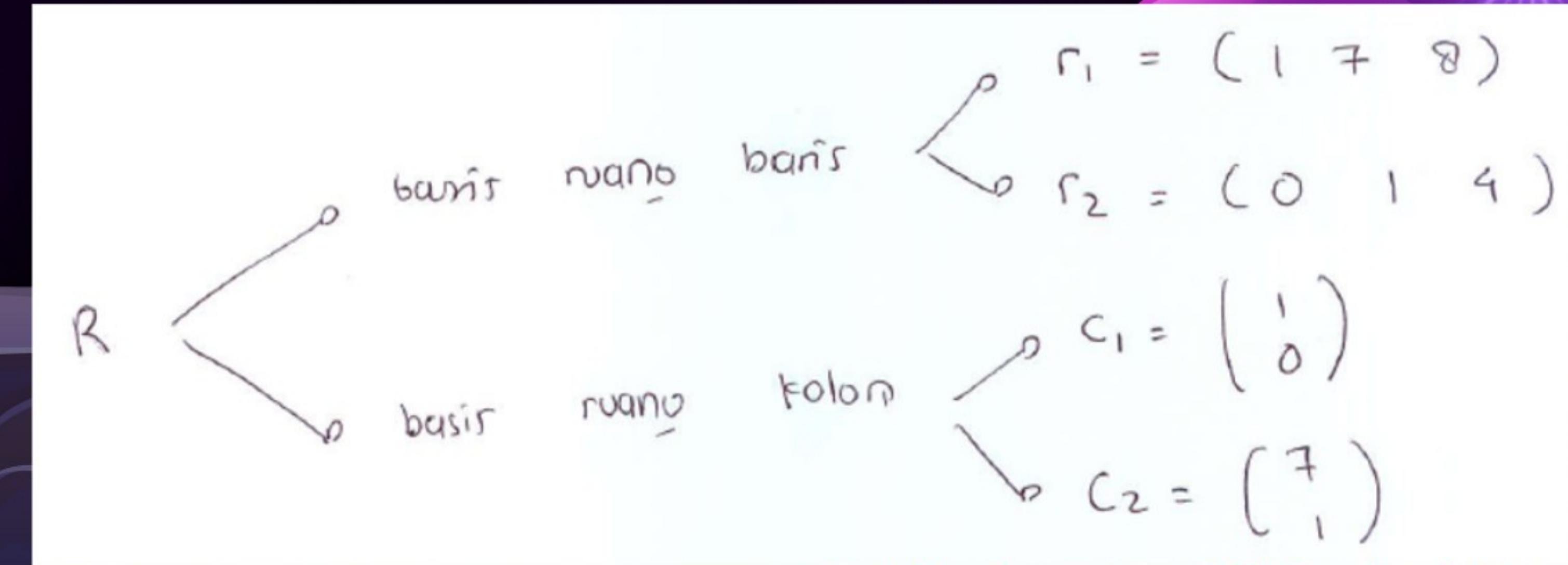
$$A = \begin{bmatrix} 5 & 6 & 7 \\ 8 & 9 & 3 \end{bmatrix}$$

↓ OBE

$$R = \begin{bmatrix} 1 & 7 & 8 \\ 0 & 1 & 4 \end{bmatrix}$$



Catt: bukan hasil sebenarnya



- Matrix A = [...]
- Matrix R = [...]
 - --> Matrix R --> matrix A yang sudah di OBE dan berbentuk eselon baris
- Teori 5.5.4 --> OBE tidak merubah ruang baris dari matrix
- Teori 5.5.6 --> Jika matrix R berbentuk eselon baris, maka vektor baris yang ada 1 utama membentuk basis untuk ruang baris R, dan vektor kolom yang ada 1 utama membentuk basis untuk ruang kolom R
- Gabungan dari 2 teori ini --> basis ruang baris R = basis ruang baris A

- Teori 5.5.5.b --> himpunan vektor kolom yang membentuk basis untuk ruang kolom A berkorespondensi dengan himpunan vektor kolom yang membentuk basis untuk ruang kolom R
- Gabungan teori 5.5.6 dan 5.5.5.b --> basis Ruang kolom R berkorespondensi dengan basis ruang kolom A
- Catt -->
 - Kalau = berarti boleh langsung diambil
 - Kalau berkorespondensi berarti è tidak boleh langsung diambil, tapi disamakan

•Contoh 6 dan 7 --> mencari basis untuk ruang baris dan ruang vektor , dimanahasil basisnya nanti bukan berasal dari baris atau vektor yang ada di A. Tapi vektor baru

Example 6 Find bases for the row and column spaces of

Soal 1

$$A = \begin{bmatrix} 1 & -3 & 4 & -2 & 5 & 4 \\ 2 & -6 & 9 & -1 & 8 & 2 \\ 2 & -6 & 9 & -1 & 9 & 7 \\ -1 & 3 & -4 & 2 & -5 & -4 \end{bmatrix}$$

Solution. Since elementary row operations do not change the row space of a matrix, we can find a basis for the row space of A by finding a basis for the row space of any row-echelon form of A . Reducing A to row-echelon form we obtain (verify)

$$R = \begin{bmatrix} 1 & -3 & 4 & -2 & 5 & 4 \\ 0 & 0 & 1 & 3 & -2 & -6 \\ 0 & 0 & 0 & 0 & 1 & 5 \\ 0 & 0 & 0 & 0 & 0 & 0 \end{bmatrix}$$

By Theorem 5.5.6 the nonzero row vectors of R form a basis for the row space of R , and hence form a basis for the row space of A . These basis vectors are

$$r_1 = [1 \ -3 \ 4 \ -2 \ 5 \ 4]$$

$$r_2 = [0 \ 0 \ 1 \ 3 \ -2 \ -6]$$

$$r_3 = [0 \ 0 \ 0 \ 0 \ 1 \ 5]$$

Keeping in mind that A and R may have different column spaces, we cannot find a basis for the column space of A directly from the column vectors of R . However, it follows from Theorem 5.5.5b that if we can find a set of column vectors of R that forms a basis for the column space of R , then the *corresponding* column vectors of A will form a basis for the column space of A .

The first, third, and fifth columns of R contain the leading 1's of the row vectors, so

$$\mathbf{c}'_1 = \begin{bmatrix} 1 \\ 0 \\ 0 \\ 0 \end{bmatrix}, \quad \mathbf{c}'_3 = \begin{bmatrix} 4 \\ 1 \\ 0 \\ 0 \end{bmatrix}, \quad \mathbf{c}'_5 = \begin{bmatrix} 5 \\ -2 \\ 1 \\ 0 \end{bmatrix}$$

form a basis for the column space of R ; thus the corresponding column vectors of A , namely,

$$\mathbf{c}_1 = \begin{bmatrix} 1 \\ 2 \\ 2 \\ -1 \end{bmatrix}, \quad \mathbf{c}_3 = \begin{bmatrix} 4 \\ 9 \\ 9 \\ -4 \end{bmatrix}, \quad \mathbf{c}_5 = \begin{bmatrix} 5 \\ 8 \\ 9 \\ -5 \end{bmatrix}$$

form a basis for the column space of A .

Contoh 6 : • Rowspace (A) = Rowspace (R) \rightarrow Teorema 5.5.4 .
dimana R adalah matriks A
yang sudah di - O.B.E.
dan berbentuk Eselon Baris
• Terapkan Teorema 5.5.6 , maka akan didapat

Basis Ruang Vektor Baris (A) $= \{\vec{r}_1, \vec{r}_2, \vec{r}_3\}$.
dan Basis Ruang kolom (A) $= \{\vec{c}_1, \vec{c}_2, \vec{c}_3\}$
dengan menerapkan Teorema 5.5.5. (b)
dimana A di soal = A & Teorema 5.5.5.

$$R^{-n-} = B^{-a-} \quad \overline{a} \quad \overline{n} \quad \overline{-}$$

Example 7 Find a basis for the space spanned by the vectors

Soal 2

$$\mathbf{v}_1 = (1, -2, 0, 0, 3), \quad \mathbf{v}_2 = (2, -5, -3, -2, 6), \quad \mathbf{v}_3 = (0, 5, 15, 10, 0), \\ \mathbf{v}_4 = (2, 6, 18, 8, 6)$$

Solution. Except for a variation in notation, the space spanned by these vectors is the row space of the matrix

$$\begin{bmatrix} 1 & -2 & 0 & 0 & 3 \\ 2 & -5 & -3 & -2 & 6 \\ 0 & 5 & 15 & 10 & 0 \\ 2 & 6 & 18 & 8 & 6 \end{bmatrix}$$

Reducing this matrix to row-echelon form we obtain

$$\begin{bmatrix} 1 & -2 & 0 & 0 & 3 \\ 0 & 1 & 3 & 2 & 0 \\ 0 & 0 & 1 & 1 & 0 \\ 0 & 0 & 0 & 0 & 0 \end{bmatrix}$$

The nonzero row vectors in this matrix are

$$\mathbf{w}_1 = (1, -2, 0, 0, 3), \quad \mathbf{w}_2 = (0, 1, 3, 2, 0), \quad \mathbf{w}_3 = (0, 0, 1, 1, 0)$$

These vectors form a basis for the row space and consequently form a basis for the subspace of \mathbb{R}^5 spanned by $\mathbf{v}_1, \mathbf{v}_2, \mathbf{v}_3$, and \mathbf{v}_4 .

Contoh 7: Soal: Basis u/ Ruang yg. direntang $\{\vec{v}_1, \vec{v}_2, \vec{v}_3, \vec{v}_4\}$

↓
"ditransformasi" menjadi

Basis u/ Ruang Baris (A)

- Di mana A dibentuk dari

$$\left(\begin{array}{c} \overline{r}_1 = \vec{v}_1 \\ \overline{r}_2 = \vec{v}_2 \\ \overline{r}_3 = \vec{v}_3 \\ \overline{r}_4 = \vec{v}_4 \end{array} \right)$$

- Gunakan DBE untuk mengubah A ke dalam matriks eselon baris
- Kemudian terapkan Teorema 5.5.6 .

Ex.8 hal 267

- Basis untuk row space yang berasal dari vektor baris yang ada di A

Example 8 Find a basis for the row space of

Soal 3

$$A = \begin{bmatrix} 1 & -2 & 0 & 0 & 3 \\ 2 & -5 & -3 & -2 & 6 \\ 0 & 5 & 15 & 10 & 0 \\ 2 & 6 & 18 & 8 & 6 \end{bmatrix}$$

consisting entirely of row vectors from A.

Solution. We will transpose A, thereby converting the row space of A into the column space of A^T ; then we will use the method of Example 6 to find a basis for the column space of A^T ; and then we will transpose again to convert column vectors back to row vectors. Transposing A yields

Basis dari vektor baris A sendiri, apakah
r₁, r₂, r₃ atau r₄

- R₁ = [1 -2 0 0 3]
- R₂ = [2 -5 -3 -2 6]
- R₃ = [0 5 15 10 0]
- R₄ = [2 6 18 8 6]

$$A^T = \begin{bmatrix} 1 & 2 & 0 & 2 \\ -2 & -5 & 5 & 6 \\ 0 & -3 & 15 & 18 \\ 0 & -2 & 10 & 8 \\ 3 & 6 & 0 & 6 \end{bmatrix}$$

Reducing this matrix to row-echelon form yields

$$\begin{bmatrix} 1 & 2 & 0 & 2 \\ 0 & 1 & -5 & -10 \\ 0 & 0 & 0 & 1 \\ 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 \end{bmatrix}$$

The first, second, and fourth columns contain the leading 1's, so the corresponding column vectors in A^T form a basis for the column space of A^T ; these are

$$c_1 = \begin{bmatrix} 1 \\ -2 \\ 0 \\ 0 \\ 3 \end{bmatrix}, \quad c_2 = \begin{bmatrix} 2 \\ -5 \\ -3 \\ -2 \\ 6 \end{bmatrix}, \quad \text{and} \quad c_4 = \begin{bmatrix} 2 \\ 6 \\ 18 \\ 8 \\ 6 \end{bmatrix}$$

Transposing again and adjusting the notation appropriately yields the basis vectors

$$r_1 = [1 \ -2 \ 0 \ 0 \ 3], \quad r_2 = [2 \ -5 \ -3 \ -2 \ 6],$$

and

$$r_4 = [2 \ 6 \ 18 \ 8 \ 6]$$

for the row space of A . \square

find a basis for the row space of A consisting entirely of row vectors from A (using gauss)

A =	-6	7	-9	7	2
	9	4	-3	-3	5
	-4	7	-4	2	7
	7	-3	7	3	-5

At =	-6	9	-4	7
	7	4	7	-3
	-9	-3	-4	7
	7	-3	2	3
	2	5	7	-5

1 -1.5 0.67 -1.17 iterasi ke 1, berapa isi sel A(1,2) -1.5

7	4	7	-3
-9	-3	-4	7
7	-3	2	3
2	5	7	-5

1 -1.5 0.67 -1.17 iterasi ke 2, berapa isi sel A(2,3) 2.31

0	14.5	2.31	5.19
-9	-3	-4	7
7	-3	2	3
2	5	7	-5

1	-1.5	0.67	-1.17	iterasi ke 3, berapa isi sel A(3,4)	-3.53
0	14.5	2.31	5.19		
0	-16.5	2.03	-3.53		
7	-3	2	3		
2	5	7	-5		
1	-1.5	0.67	-1.17	iterasi ke 4, berapa isi sel A(4,3)	-2.69
0	14.5	2.31	5.19		
0	-16.5	2.03	-3.53		
0	7.5	-2.69	11.19		
2	5	7	-5		
1	-1.5	0.67	-1.17	iterasi ke 5, berapa isi sel A(5,2)	8
0	14.5	2.31	5.19		
0	-16.5	2.03	-3.53		
0	7.5	-2.69	11.19		
0	8	5.66	-2.66		
1	-1.5	0.67	-1.17	iterasi ke 6, berapa isi sel A(2,3)	0.16
0	1	0.16	0.36		
0	-16.5	2.03	-3.53		
0	7.5	-2.69	11.19		
0	8	5.66	-2.66		
1	-1.5	0.67	-1.17	iterasi ke 7, berapa isi sel A(3,4)	2.41
0	1	0.16	0.36		
0	0	4.67	2.41		
0	7.5	-2.69	11.19		
0	8	5.66	-2.66		

1	-1.5	0.67	-1.17	iterasi ke 8, berapa isi sel A(4,3)	-3.89
0	1	0.16	0.36		
0	0	4.67	2.41		
0	0	-3.89	8.49		
0	8	5.66	-2.66		
1	-1.5	0.67	-1.17	iterasi ke 9, berapa isi sel A(5,4)	-5.54
0	1	0.16	0.36		
0	0	4.67	2.41		
0	0	-3.89	8.49		
0	0	4.38	-5.54		
1	-1.5	0.67	-1.17	iterasi ke 10, berapa isi sel A(3,4)	0.52
0	1	0.16	0.36		
0	0	1	0.52		
0	0	-3.89	8.49		
0	0	4.38	-5.54		
1	-1.5	0.67	-1.17	iterasi ke 11, berapa isi sel A(4,4)	10.51
0	1	0.16	0.36		
0	0	1	0.52		
0	0	0	10.51		
0	0	4.38	-5.54		

Contoh 8: • $A \xrightarrow{\text{transpos}} A^T$

$$\begin{aligned} \text{Ruang Baris } (A) &= \text{Ruang kolom } (A^T) \\ \text{Ruang kolom } (A) &= \text{Ruang Baris } (A^T) \end{aligned}$$

- Terapkan Teorema 5.5.6 pada matriks A^T

$$A^T \xrightarrow{\text{O.B.E.}} \text{Matriks eselon-baris } R = \left(\begin{array}{cccc} \vec{c}_1 & \vec{c}_2 & \vec{c}_3 & \vec{c}_4 \\ 1 & 2 & 0 & 2 \\ 0 & 1 & -5 & -10 \\ 0 & 0 & 0 & 1 \\ 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 \end{array} \right) \xrightarrow{\substack{\vec{r}_1 \\ \vec{r}_2 \\ \vec{r}_3}}$$

$$\begin{aligned} \text{Basis Ruang Baris } (A^T) &= \{ \vec{r}_1, \vec{r}_2, \vec{r}_3 \} \\ = \text{Basis Ruang Baris } (R) &= \{ \vec{r}_1, \vec{r}_2, \vec{r}_3 \} \end{aligned} \quad \text{Teorema 5.5.6.}$$

- Basis Ruang kolom $(R) = \{ \vec{c}_1, \vec{c}_2, \vec{c}_4 \} \rightarrow$ Teorema 5.5.6.

$$\hookrightarrow \text{Basis Ruang kolom } (A^T) = \{ \underset{A^T}{\text{kolom-1}}, \underset{A^T}{\text{kolom-2}}, \underset{A^T}{\text{kolom-4}} \}$$

berdasarkan Teorema 5.5.5 (b)

Mencari basis yang direntang oleh vektor itu sendiri

--> **v1 atau v2 atau V3 atau V4 atau V5**

Example 9

- (a) Find a subset of the vectors

$$\mathbf{v}_1 = (1, -2, 0, 3), \quad \mathbf{v}_2 = (2, -5, -3, 6), \\ \mathbf{v}_3 = (0, 1, 3, 0), \quad \mathbf{v}_4 = (2, -1, 4, -7), \quad \mathbf{v}_5 = (5, -8, 1, 2)$$

that forms a basis for the space spanned by these vectors.

- (b) Express the vectors not in the basis as a linear combination of the basis vectors.

find a subset of the vector v_1, v_2, v_3, v_4, v_5 that forms a basis for the space spanned by these vectors (using gauss)

$v_1 =$	6	-2	7	6
$v_2 =$	4	-2	4	-3
$v_3 =$	-5	6	-6	-5
$v_4 =$	5	-7	4	-9
$v_5 =$	-4	5	7	-3

6	4	-5	5	-4
-2	-2	6	-7	5
7	4	-6	4	7
6	-3	-5	-9	-3
1	0.67	-0.83	0.83	-0.67
				iterasi ke 1, berapa isi sel A(1,3)
				-0.83
-2	-2	6	-7	5
7	4	-6	4	7
6	-3	-5	-9	-3
1	0.67	-0.83	0.83	-0.67
0	-0.66	4.34	-5.34	3.66
7	4	-6	4	7
6	-3	-5	-9	-3
1	0.67	-0.83	0.83	-0.67
0	-0.66	4.34	-5.34	3.66
0	-0.69	-0.19	-1.81	11.69
6	-3	-5	-9	-3
1	0.67	-0.83	0.83	-0.67
0	-0.66	4.34	-5.34	3.66
0	-0.69	-0.19	-1.81	11.69
0	-7.02	-0.02	-13.98	1.02
1	0.67	-0.83	0.83	-0.67
0	1	-6.58	8.09	-5.55
0	-0.69	-0.19	-1.81	11.69
0	-7.02	-0.02	-13.98	1.02
1	0.67	-0.83	0.83	-0.67
0	1	-6.58	8.09	-5.55
0	0	-4.73	3.77	7.86
0	-7.02	-0.02	-13.98	1.02

iterasi ke 1, berapa isi sel A(1,3)

-0.83

iterasi ke 2, berapa isi sel A(2,4)

-5.34

iterasi ke 3, berapa isi sel A(3,5)

11.69

iterasi ke 4, berapa isi sel A(4,2)

-7.02

iterasi ke 5, berapa isi sel A(2,3)

-6.58

iterasi ke 6, berapa isi sel A(3,4)

3.77

bilcis

1	0.67	-0.83	0.83	-0.67
0	1	-6.58	8.09	-5.55
0	0	-4.73	3.77	7.86
0	0	-46.21	42.81	-37.94
1	0.67	-0.83	0.83	-0.67
0	1	-6.58	8.09	-5.55
0	0	1	-0.8	-1.66
0	0	-46.21	42.81	-37.94
1	0.67	-0.83	0.83	-0.67
0	1	-6.58	8.09	-5.55
0	0	1	-0.8	-1.66
0	0	0	5.84	-114.65
1	0.67	-0.83	0.83	-0.67
0	1	-6.58	8.09	-5.55
0	0	1	-0.8	-1.66
0	0	0	1	-19.63

iterasi ke 7, berapa isi sel A(4,3)

-46.21

iterasi ke 8, berapa isi sel A(3,5)

-1.66

iterasi ke 9, berapa isi sel A(4,4)

5.84

Iterasi ke 10, berapa isi sel A(4,5) ...

-19.63

Jadi basis nya adalah V1, V2, V3 dan V4

Solution (a). We begin by constructing a matrix that has $\mathbf{v}_1, \mathbf{v}_2, \dots, \mathbf{v}_5$ as its column vectors:

$$\left[\begin{array}{ccccc} 1 & 2 & 0 & 2 & 5 \\ -2 & -5 & 1 & -1 & -8 \\ 0 & -3 & 3 & 4 & 1 \\ 3 & 6 & 0 & -7 & 2 \\ \uparrow & \uparrow & \uparrow & \uparrow & \uparrow \\ \mathbf{v}_1 & \mathbf{v}_2 & \mathbf{v}_3 & \mathbf{v}_4 & \mathbf{v}_5 \end{array} \right] \quad (7)$$

The first part of our problem can be solved by finding a basis for the column space of this matrix. Reducing the matrix to *reduced row-echelon form* and denoting the column vectors of the resulting matrix by $\mathbf{w}_1, \mathbf{w}_2, \mathbf{w}_3, \mathbf{w}_4$, and \mathbf{w}_5 yields

$$\left[\begin{array}{ccccc} 1 & 0 & 2 & 0 & 1 \\ 0 & 1 & -1 & 0 & 1 \\ 0 & 0 & 0 & 1 & 1 \\ 0 & 0 & 0 & 0 & 0 \\ \uparrow & \uparrow & \uparrow & \uparrow & \uparrow \\ \mathbf{w}_1 & \mathbf{w}_2 & \mathbf{w}_3 & \mathbf{w}_4 & \mathbf{w}_5 \end{array} \right] \quad (8)$$

The leading 1's occur in columns 1, 2, and 4, so that by Theorem 5.5.6

$$\{\mathbf{w}_1, \mathbf{w}_2, \mathbf{w}_4\}$$

is a basis for the column space of (8) and consequently

$$\{\mathbf{v}_1, \mathbf{v}_2, \mathbf{v}_4\}$$

is a basis for the column space of (7).

Solution (b). We shall start by expressing w_3 and w_5 as linear combinations of the basis vectors w_1 , w_2 , w_4 . The simplest way of doing this is to express w_3 and w_5 in terms of basis vectors with smaller subscripts. Thus, we shall express w_3 as a linear combination of w_1 and w_2 , and we shall express w_5 as a linear combination of w_1 , w_2 , and w_4 . By inspection of (8), these linear combinations are

$$w_3 = 2w_1 - w_2$$

$$w_5 = w_1 + w_2 + w_4$$

We call these the *dependency equations*. The corresponding relationships in (7) are

$$v_3 = 2v_1 - v_2$$

$$v_5 = v_1 + v_2 + v_4$$

Kombinasi Linier

$$\cdot V_3 = k_1V_1 + k_2V_2 + k_4V_4$$

--> cari k_1, k_2 dan k_4

$$\cdot V_5 = m_1V_1 + m_2V_2 + m_4V_4$$

--> cari m_1, m_2 dan m_4

Contoh g: (a) $A = \begin{pmatrix} 1 & 2 & 0 & 2 & 5 \\ -2 & -5 & 1 & -1 & -8 \\ 0 & -3 & 3 & 4 & 1 \\ 3 & 6 & 0 & -7 & 2 \end{pmatrix}$

↓ di O.B.E.

$$R = \begin{pmatrix} 1 & 0 & 2 & 0 & 1 \\ 0 & 1 & -1 & 0 & 1 \\ 0 & 0 & 0 & 1 & 1 \\ 0 & 0 & 0 & 0 & 0 \\ -\vec{w}_1 & -\vec{w}_2 & -\vec{w}_3 & -\vec{w}_4 & -\vec{w}_5 \end{pmatrix}$$

ada
1 utama

Dengan Teorema 5.5.5. (b)

Basis $\underbrace{(R)}_{\text{ruang kolom}} = \{\vec{w}_1, \vec{w}_2, \vec{w}_4\}$

maka

Basis Ruang kolom (A) = $\{\vec{v}_1, \vec{v}_2, \vec{v}_4\}$

(b): \vec{v}_2 kombinasi linier $\{\vec{v}_1, \vec{v}_2, \vec{v}_4\}$

$$\vec{v}_5 \quad \rightarrow \quad \rightarrow$$

Tugas Kelompok

- cari 2 soal dan jawaban di internet yang berhubungan dengan materi ppt ini
 - Tulis alamat internetnya
 - Di kirim ke elearning, terakhir
--> Minggu depan
- Format --> subject -->
- Alin-B-melati
 - Bentuk --> ppt --> informasi nama kelompok+ anggota

Terima
Kasih

