

**Problem 1. (2★)**

Find all values of x given that $(x - 2)^{x^2 - 4} = 1$.

Problem 2. (2★)

Given that x and y are integers and $5^{x-y+5} = 7^{x+y+3}$, find the value of $\frac{x-y}{x+y}$.

Problem 3. (3★)

Given that

$$\begin{cases} 4^a \cdot 3^b = 108 \\ 2^b \cdot 9^a = 72 \end{cases}$$

Find $2a + b$.

Problem 4. (5★)

Given that n is an integer that is not equal to 0, and

$$(-2x + 1)^{2n} = (9x^2 + 6x + 1)^n$$

Find the sum of the possible values of x .

Problem 5. (3★)

Given that

$$\begin{cases} (x + y) \cdot 2^{y-x} = 1 \\ (x + y)^{x-y} = 2 \end{cases}$$

Find the sum of possible values of x .

Problem 6. (3★)

x and y are integers such that $2^{x+y} + 2^x = 3^{y+2} - 3^y$. Find x .

Problem 7. (7★)

Assume that a , b , c , and d are positive integers such that $a^5 = b^4$, $c^3 = d^2$, and $c - a = 19$. Determine $d - b$.

Problem 8. (7★)

It is given that $y = x^2 - 5x + 5$, $z = x^2 - 12x + 35$ and $y^z = 1$. Find the sum of all possible values of x .

**Problem 9. (5★)**

Find all possible real values of

$$\frac{\sqrt{x-1} + \sqrt{1-x}}{2x+3}.$$

Problem 10. (3★)

Find the value of

$$\sqrt{|40\sqrt{2} - 57|} - \sqrt{40\sqrt{2} + 57}.$$

Problem 11. (5★)

Find the value of

$$\sqrt{\sqrt{6} + 1} + \sqrt{\sqrt{6} - 1}.$$

In terms of b , where $\sqrt{6} + \sqrt{5} = b^2$.**Problem 12. (5★)**If x, y, k are real numbers not equal to 0, and we know

$$x^{y^k} = k^{x^y}, k = x^y, y = x^{2y}$$

Then find the value of y .**Problem 13. (2★)**If $\sqrt{x+9} + \sqrt{x} = 1$, find the value of $\sqrt{x+9} - \sqrt{x}$.**Problem 14. (3★)**If $x - \sqrt{\frac{2}{x}} = 3$, what is the value of $x - \sqrt{2x}$?**Problem 15. (3★)**

Find the value of

$$\frac{\sqrt[4]{17 + 12\sqrt{2}}}{\sqrt{2} - 1} - 2\sqrt{2}$$

Problem 16. (5★)

Compute

$$\sqrt[3]{5 + 2\sqrt{13}} - \sqrt[3]{5 - 2\sqrt{13}}.$$

**Problem 17. (5★)**

Find the value of

$$\frac{\sqrt{\sqrt{13}-3} + \sqrt{\sqrt{13}+3}}{\sqrt{4+2\sqrt{11+\sqrt{7-\sqrt{9}}}}}.$$

Problem 18. (7★)Find x , if we are given

$$\sqrt{2x + \sqrt{4x-1}} + \sqrt{2x - \sqrt{4x-1}} = 2\sqrt{2}.$$

Problem 19. (7★)

Given that

$$A = \frac{1}{10-3\sqrt{11}} - \frac{1}{3\sqrt{11}-7\sqrt{2}} + \frac{1}{7\sqrt{2}-\sqrt{97}} - \frac{1}{\sqrt{97}-4\sqrt{6}}.$$

Find the value of

$$\frac{A}{5-2\sqrt{6}}.$$

Problem 20. (7★)Find all possible real values of x such that

$$\sqrt{\frac{x-7}{1990}} + \sqrt{\frac{x-6}{1991}} + \sqrt{\frac{x-5}{1992}} = \sqrt{\frac{x-1990}{7}} + \sqrt{\frac{x-1991}{6}} + \sqrt{\frac{x-1992}{5}}.$$

Problem 21. (11★)

Given that

$$A = \sqrt{2 + \sqrt{2}}$$

$$B = \sqrt{2 + \sqrt{2 + \sqrt{2}}}$$

$$C = \sqrt{2 + \sqrt{2 + \sqrt{2 + \sqrt{2}}}}$$

$$D = \sqrt{2 - \sqrt{2 + \sqrt{2 + \sqrt{2}}}}$$

Find the value of $A \cdot B \cdot C \cdot D$.