Worksheet 9

Exercise 1 Find the exact value.

 $a) \arcsin(0)$

 $b) \arctan(1)$

 $c) \arccos(1/2)$

d) arccos(-1/2)

Exercise 2 Find the domain and range of the function

$$f(x) = \arcsin(1 - x^2)$$

Exercise 3 Find the limit

 $\mathbf{a.} \quad \lim_{x \to -1^+} \arcsin x$

b. $\lim_{x \to 0^+} \arctan(\ln x)$

Exercise 4 Find the limit. Hint: you can use l'Hôpital's rule

 $\mathbf{a.} \quad \lim_{x \to 0^+} x \, \ln x$

 $\mathbf{b.} \quad \lim_{x \to 0^+} x^x$

Exercise 5 Prove that for all $x \in [0, \frac{\pi}{2}]$

$$\arcsin(x) + \arccos(x) = \frac{\pi}{2}$$

Exercise 6 Find the domain and sketch the graph of

a. $f(x) = \sin(\arcsin x)$

b. $g(x) = \arcsin(\sin x)$